1	Electronic Supplementary Materials
2	Testing predictions of inclusive fitness theory in inbreeding relatives with biparental care
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$r_{iWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2}f_i$	$r_{\scriptscriptstyle iEPO}=k_{\scriptscriptstyle ij}\!+\!k_{\scriptscriptstyle iq}$
$r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2}f_j$	$r_{jEPO} = \frac{l_2}{2} + k_{jq} + \frac{l_2}{2} f_j$

Figure S1. Schematic illustration of calculation of relatedness between a parent and its genetic offspring (i.e., a male's within-pair offspring (WPO) giving r_{iWPO} , or a female's WPO or extra-pair offspring (EPO) giving r_{jWPO} and r_{jEPO} , respectively), and the relatedness between a male and an EPO that it did not sire but could rear (r_{iEPO}). The parameters *i*, *j*, and *q* denote the identities of the focal male, its socially-paired female, and the female's extra-pair mate (i.e., the sire of the EPO). k_{ij} is the coefficient of kinship between male *i* and his socially-paired female *j*, and is identical to the coefficient of kinship between female *j* and male *i*. k_{iq} is the coefficient of

- 43 kinship between *i* and *j*'s extra-pair mate *q*, and k_{jq} is the coefficient of kinship between *j* and *q*. f_i and f_j are *i* and *j*'s own coefficients of
- 44 inbreeding respectively. The grey oval highlights the social pairing, involving *i* and *j*. Dotted lines indicate mating, solid lines indicate
- 45 parentage, and dashed lines indicate links between other potentially related individuals.

WPO \clubsuit EPO \clubsuit WPO $\int TAV_i = (r_{iWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_i) | (r_{iEPO} = k_{ij} + k_{iq}) | (r_{iWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_i) | (r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_j) | (r_{jEPO} = \frac{1}{2} + k_{jq} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + k_{ij} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} f_j) | (r_{jWPO} = \frac{1}{2} +$

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49 Figure S2. Example calculation of total allelic value (TAV) for a socially-paired male and female 50 rearing a hypothetical brood comprising two within-pair offspring (WPO) and one extra-pair offspring (EPO), and hence total brood size (BS) of three nestlings. TAV is calculated by 51 52 summing appropriate values of relatedness for each nestling in the brood, calculated with 53 respect to each focal parent using the formulae specified (see also Figure S1). Note that this can 54 generate different values of TAV with respect to a focal male *i* (TAV_i) and his socially-paired 55 female *j* (TAV_i). In general, TAV increases with BS and, conditional on BS, is larger when the 56 parents have higher coefficients of inbreeding (f_i or f_i) and/or higher coefficients of kinship (k_{ij} 57 and/or k_{iq} and/or k_{iq}). All terminology is defined in figure S1.

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WPO WPO WPO WPO WPO EPO WPO $(\frac{1}{2} + k_{ij} + \frac{1}{2} f_{j}) + (\frac{1}{2} + k_{ij} + \frac{1}{2} f_{j})$ Lost allelic value (LAV) PAV to focal male



63 Figure S3. Example calculation of lost allelic value (LAV) as the decrease in total allelic value of 64 a brood to a focal male (TAV_i) resulting from extra-pair paternity (EPP) in offspring produced by the male's socially-paired female. LAV is calculated as PAV-TAV_i, where PAV is the brood's 65 66 potential allelic value to the focal male, which equals the brood's TAV to the male calculated as 67 if he had sired the entire brood. WPO and EPO denote within-pair and extra-pair offspring 68 respectively. The indices *i*, *j*, and *q* denote the identities of the focal male, its socially-paired 69 female, and the female's extra-pair mate (i.e., the sire of the EPO). k_{ii} is the coefficient of kinship 70 between male *i* and its socially-paired female *j*, and k_{iq} is the coefficient of kinship between *i* and 71 i's extra-pair mate q. LAV can therefore take values between 0 (given zero paternity loss) and 72 $\frac{1}{2}BS(1+f_i)$ (given complete paternity loss and $k_{iq}=0$).

Appendix S2: Further details of paternity and pedigree analyses, and observation of 75 feeding rates

76 Pedigree construction and analysis

77 All nestlings and adults ringed since 1993 were genotyped at 160 microsatellite loci [1]. The 78 identities of the genetic parents of each nestling were identified with >99% individual-level 79 statistical confidence [2,3]. Overall, 28% of nestlings were assigned as EPO and 72% as WPO 80 [4]. The social pedigree (i.e., constructed from observed social parentage) was corrected for 81 EPP from 1993 onwards [1,3,5]. Coefficients of kinship (k) between any two individuals, and 82 each individual's own coefficient of inbreeding (f) were calculated from the corrected pedigree 83 using standard algorithms and are relative to a 1975 baseline [2,5,6]. Since the focal individuals 84 have multiple generations of genetically verified ancestors there is very little error in k and f85 relative to the defined baseline [5]. For reference, values of k of 0, 0.0625, 0.125, 0.25 indicate 86 pairings between unrelated individuals and outbred third-order, second-order, and first-order 87 relatives, respectively. The same values of f refer to offspring of such pairings. Both f and k are 88 expectations, and realized parent-offspring relatedness will deviate from these expectations due 89 to Mendelian sampling variance. However, such variance is reduced by inbreeding, and also 90 reduced across groups of individuals. This implies that deviations between expected and 91 realized relatedness will commonly be relatively small in our system, especially for TAV for 92 broods that contain multiple offspring.

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94 Parental feeding rates

95 On Mandarte Island, song sparrows construct open cup nests in grass/scrub margins. Individual 96 parents are typically consistent in the route they approach their nest, as determined by the 97 orientation of open vegetation and foraging locations. For each focal nest, typical parental 98 approach routes were determined during extensive observations during incubation (for females)

and early stages of chick feeding (both parents). These observations also served to accustombreeding sparrows to observer presence.

101 For each feeding rate observation session a single observer approached the territory 102 along established trails, and positioned themselves 15-20m from the focal nest in the best 103 possible position (often on a free-standing ladder or high rock) to retain a clear line of sight of 104 incoming parents while minimizing disturbance. A 10–15 min habituation period was then 105 imposed, during which observers checked for signs of disturbance (e.g. parental alarm calls), 106 and allowed parental behaviour to return to normal after any initial disturbance. If any signs of 107 disturbance were evident, the observer changed position and the habituation period was 108 repeated; however, in most cases no such impacts occurred. The 1-hour session then 109 commenced, and the observer noted the time of arrival of each parent (as identified from their 110 colour-rings). It is unlikely that any visits were missed, due to the close proximity to the nest and 111 consistency in the routes parents took to the nest. However, in three sessions the visiting 112 parent's identity was uncertain during at least one nest visit. These sessions were excluded from 113 analyses. The total of 338 retained sessions spanned the 12-day nestling period (2-5 days, 114 N=112; 6–7 days; N=117; 8–11 days; N=109).

115 Some nests initiated in the population during the focal periods were excluded from field 116 observations, either because their locations prevented reliable observations without causing 117 disturbance, or because they failed during incubation or early in the chick-rearing period. 118 Observers also attempted to visually score food loads as small, medium or large, but such 119 scoring was not always possible and could not be easily validated. The number of feeding visits 120 per hour was consequently used as the focal metric, and is taken to capture one aspect of 121 parental care. There were no observations of parents visiting nests without food, providing no 122 obvious evidence of 'cheating'. Observations also suggested that parents typically brought 123 relatively equal amounts of food each visit (e.g. either one or two large items or several small 124 items), suggesting that feeding rate likely predicts the amount of food provided to offspring.

- Feeding rate data were collected blind to key predictor variables; indeed, the molecular genetic
 paternity analyses required to calculate TAV, P_{EPO} and LAV were not undertaken until after each
 breeding season had finished. Extra-pair sires were never observed to visit nests where they
 had sired extra-pair offspring.

131 Appendix S3: Null model variables, and focal and null and variable distributions

- 132 Over half of the observation sessions were at monogamous nests (N=192), while the rest were
- split between primary polygynous and secondary polygynous nests (N= 74 and 71, respectively;
- 134 Fig S4a). Across all 138 observed nests, mean brood size was 2.9±1.0 nestlings (median: 3,
- 135 range 1-4, Fig. S4b). Mean TAV values were 1.411±0.682 (range 0.063–2.946) for males and
- 136 1.785±0.584 (range 0.538–2.998) for females (Fig S4c, d). Mean P_{EPO} was 0.27±0.35 (median 0,
- 137 range 0–1, 52% zeros; Fig S4e). Mean LAV was 0.208 ± 0.373 (median 0.000, range 0.000–
- 138 1.913, 50% zeros; Fig S4f). Across all 75 observed female-male pairs, mean k_{ij} was 0.085±0.054
- 139 (range 0.000–0.300, Fig S4g). Mean f_i was 0.056 ± 0.038 (range 0.000–0.181) across 55
- 140 individual males (Fig S4h) and mean f_i was 0.055 ± 0.035 (range 0.000–0.164) across 65
- 141 individual females (Fig S4i).













(h)



143	Figure S4. Frequency histograms (number of individuals) of null and focal variables. Social statuses (a) are defined as monogamous
144	(M), only one female per male; primary polygynous (PP), two females per male territory but the first nest to hatch; secondary
145	polygynous (SP), two or three females per male territory but the second or third nest to hatch. TAV _i (c) and TAV _j (d) are the "total
146	allelic values" for males and females respectively. PEPO is the proportion of extra-pair offspring in a brood (e) and LAV is the "lost
147	allelic value" (f). k_{ij} is the coefficient of kinship between socially-paired mates (g) and male f_i and female f_j (h, i) are the coefficients of
148	inbreeding of the focal male and female.
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159 Null model variables

- 160 Both sexes' feeding rates increased with increasing nestling age, but male feeding rates decreased as the breeding season
- 161 progressed (Fig S5). Models that contained brood size as a linear covariate were slightly better supported than the null model that
- 162 excluded brood size for males (ΔAIC_c:-0.7) and much more strongly supported for females (ΔAIC_c:-11.1). Models that contained
- 163 brood size as a continuous variable were better supported than models that contained brood size as a factor for males (ΔAIC_c:+3.6)
- 164 and females (ΔAIC_c:+7.1; Table S2). Male and female feeding rates increased with brood size (Fig S6). Feeding rates varied with
- social status, with females feeding more at secondary polygynous than monogamous and primary nests, in contrast males fed less at
- 166 secondary polygynous nests (Fig S7).



Figure S5. Relationships between male and female feeding rates and time of season (first egg date; a, b) and nestling age (c, d). Points denote individual observation sessions and lines denote linear regressions. Time of season is in Julian dates, with 1 representing January 1. β are the estimates from the null model and BS (as a continuous covariate) ±SE. Statistics are in Appendix S6.



Figure S6. Relationships between female (a) and male (b) feeding rates and brood size. Points denote individual observation sessions and lines denote linear regressions. β are the estimates ±SE from the null model and BS (as a continuous variable). $β_{1/2BS}$ indicates the β estimate for a

- 178 null model and ½ BS. Slopes of ½ BS were included as they can be compared to those from
- 179 TAV.
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Figure S7. (a) Female and male feeding rates across 'monogamous', 'primary polygynous' and 'secondary polygynous' nests. Boxplots represent the median, upper and lower quartiles, and minimum and maximum values, with outliers depicted by dots. (b) Relationship between male and female feeding rates across nests of different social status. Social statuses are

monogamous (M), primary polygynous (PP), and secondary polygynous (SP). Points represent individual observation sessions, across monogamous (squares, solid line), primary polygynous (circles, dashed line) and secondary polygynous nests (triangles, dotted line). Lines are linear predictions for each social status, and grey-shaded areas are confidence intervals around the line. Numbers on plots represent estimates ± standard errors from the null model and BS (as a continuous variable) for female feeding rates at monogamous, primary and secondary polygynous nests.

199 Figure S8. Male (a) and female (b) total allelic values $(TAV_i \text{ and } TAV_j)$ of a focal brood in relation

200 to brood size. Points denote broods (total N=138), and lines denote linear regressions. r

²⁰¹ indicates the Pearson correlation coefficient.

Figure S9. Total allelic values of a focal brood for males (TAV_i) and females (TAV_j) within a pair.
Points denote broods (total N=138) and the dashed line indicates equal TAV values for each pair
member. See [8] for more detailed consideration of this relationship.

Appendix S5: Relationships between P_{EPO} and other variables

209 Traditionally, most studies considering socially monogamous systems with extra-pair paternity 210 use the proportion of a brood that comprises extra-pair offspring (P_{EPO}) as a metric to quantify a male's relatedness to a brood. Instead, we define "lost allelic value" (LAV) as a more appropriate 211 212 metric in systems with reproductive interactions among relatives (Appendix S1). However, to 213 facilitate comparison with existing studies, we also assessed relationships among P_{EPO}, feeding 214 rates, social status, and TAV. 215 P_{EPO} varied with social status (Fig S10). P_{EPO} was of course strongly positively correlated 216 with LAV (r_p=0.89), but not all values of P_{EPO} and LAV aligned (Fig S11). P_{EPO} was not correlated 217 with TAV_i (i.e., female TAV, r_p =-0.14) but was negatively correlated with TAV_i (i.e., male TAV, 218 r_p =-0.62). Models explaining variation in feeding rates that included P_{EPO} were similarly 219 supported as the null model that also included BS (as a continuous variable) for males 220 ($\Delta AIC_c = +0.4$) but less well supported for females ($\Delta AIC_c = +1.8$); feeding rate decreased with 221 increasing P_{EPO} in males but not females (Fig S12). Models that additionally included P_{EPO} by 222 social status interactions were similarly well supported as the null model for males ($\Delta AIC_c = +0.4$) 223 and less supported for females ($\Delta AIC_c = +2.3$).

Figure S10. The relationship between the proportion of extra-pair offspring (P_{EPO}) in a brood and social status, defined as monogamous (one female per male territory); primary polygynous (two females per male territory but the first nest to hatch); secondary polygynous (two females per male territory but the second or third nest to hatch). Points indicate the mean across observed broods, and bars indicate the 95% CIs.

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Figure S12. Relationships between (a) female and (b) male song sparrow parental feeding rates
(trips/hr) and the proportion of EPO in the brood (P_{EPO}). Colours indicate nest social status
(monogamous: blue; primary polygynous: purple; secondary polygynous: yellow). Points

represent observation sessions. Lines show predicted regression of feedings rate on P_{EPO}
overall (black), and across each social status. Numbers are the estimates ± SE from the P_{EPO} by
social status interaction model, where "M", "PP" and "SP" are monogamous, primary and
secondary polygynous nests, respectively. Y-axes are on different scales for males and females.

250 Appendix S6: Supplementary results

251 Table S1: Null model variables and results from the null model.

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- 253 Table S2: Results from sets of models that contain additive or interactive effects of total allelic
- 254 value (TAV), TAV standardized within brood size (TAV_z) and brood size (BS) on male and

255 female feeding rates (trips/hr).

256

- 257 Table S3: Results from each models examining the effects of lost allelic value (LAV), the
- proportion of extra-pair offspring in a brood (P_{EPO}), kinship (k_{ij}), male and female coefficients of
- inbreeding (f_i and f_j) in comparison to the null model.

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