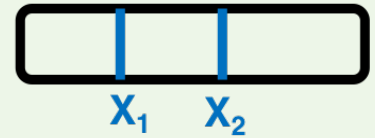♣ Simulation of phenotypic values (**100** iterations)

$$\mathbf{y} = \mathbf{X}_1\beta_1 + \mathbf{X}_2\beta_2 + \mathbf{X}_3\beta_3 + \mathbf{Zu} + \mathbf{e}, (\mathrm{Eq.}\,1)$$

$\mathbf{y}$: phenotypic values	$\mathbf{X}_1\beta_1, \mathbf{X}_2\beta_2, \mathbf{X}_3\beta_3$: fixed effects (marker effects)
$\mathbf{Zu}$: random effects (polygene effects)	$\mathbf{e}$: residuals

· $\mathbf{X}_1$ and $\mathbf{X}_2$ belong to the same haplotype block.

one haplotype block

$\mathbf{X}_1$ $\mathbf{X}_2$

♣ We assumed 2 scenarios.

① **Coupling** : $\mathrm{cor}(\mathbf{X}_1, \mathbf{X}_2) > 0 \;\text{->}\; \beta_1 = \beta_2$, $\mathrm{cor}(\mathbf{X}_1, \mathbf{X}_2) < 0 \;\text{->}\; \beta_1 = -\beta_2$

② **Repulsion** : $\mathrm{cor}(\mathbf{X}_1, \mathbf{X}_2) > 0 \;\text{->}\; \beta_1 = -\beta_2$, $\mathrm{cor}(\mathbf{X}_1, \mathbf{X}_2) < 0 \;\text{->}\; \beta_1 = \beta_2$

⬇

♣ Perform GWAS with 4 methods.

① Our proposed method, **RAINBOW** (R package RAINBOWR)

② The **single-SNP** method (R package rrBLUP)

③ **Haplotype-based** method introduced by Yano *et al.*, 2016

④ **SNP-set** method, SKAT (R package SKAT)

⬇

♣ Evaluate the results with the following summary statistics

① $-\log_{10}(p)$ and $-\log_{10}(p_a)$, correspond to the **detection power**

② **Recall**, **Precision**, and **F-measure**

③ **AUC** (area under the curve) for **regions around causals**