Supporting Information:



Supporting Information Figure S1: Relationship of the Vencs in triple-Venc encoding. As the high-Venc to low-Venc ratio increases, the iVenc approaches the low-Venc. As the Vencs get closer together, iVenc approaches infinity. The blue dots indicate ratios used in this study.



Supporting Information Figure S2: Evaluation of dual-Venc and triple-Venc unwrapping algorithms. I, 50/75/150 representative phase-difference images. All phase-difference images are shown for the same slice location and time point. Both low-Venc (LV) and high-Venc (HV) data show significant velocity aliasing throughout the phantom. The unwrapped dual-Venc (UDV) dataset (B) shows more residual aliasing than the unwrapped triple-Venc (UTV) dataset, which shows successful unwrapping of most voxels, but some residual ones near the vessel wall (red arrows).



Supporting Information Figure S3: Rotation phantom consisting of a rotating cylinder and a static ring. Compressed air from an external source and the centrifugal impeller drive the rotation of the inner cylinder. A static ring of Gd-doped gel is used for background phase correction. An optical counter with a display screen provides real-time updates on the rotational speed in rotations per minute.

$$\begin{split} & \text{low} - \text{Venc} = \frac{\pi}{\gamma(\Delta M_1^{\text{low}-\text{Venc}})}, \text{ where} \\ & \Delta M_1^{(\text{low}-\text{Venc})} = \frac{\Delta M_1^{(\text{low}-\text{Venc})}}{2} - \Delta M_1^{(\text{TR1})}, \\ & \text{and } \Delta M_1^{(\text{TR1})} = \Delta M_1^{(\text{ref})} = -\frac{\Delta M_1^{(\text{low}-\text{Venc})}}{2} \\ & \text{high} - \text{Venc} = \frac{\pi}{\gamma(\Delta M_1^{\text{high}-\text{Venc}})} = \frac{\pi}{\gamma(M_1^{\text{high}-\text{Venc}}-M_1^{\text{ref}})} [2], \\ & \text{Since the high-Venc is inversely proportional to the required gradient moment,} \\ & \text{with high-Venc>2*low-Venc, where } \Delta M_1^{\text{high}-\text{Venc}} < \frac{\Delta M_1^{(\text{low}-\text{Venc})}}{2} \text{ in maintaining the same} \\ & \text{low-Venc gradients as for a conventional 4-point acquisition, the sign of } M_1^{\text{high}-\text{Venc}}, \text{ i.e.} \\ & \text{gradient polarity, needs to be flipped such that } M_1^{\text{high}-\text{Venc}} + \frac{\Delta M_1^{(\text{low}-\text{Venc})}}{2} < \frac{\Delta M_1^{(\text{low}-\text{Venc})}}{2}. \\ & \text{This results in TRs 5-7 (high-Venc) having the opposite first moment polarity of 2-4 (low-Venc).} \end{split}$$

Supporting Information Figure S4: Brief explanation of gradient polarity flipping for high-Venc > 2*low-Venc. Refer to Figure 1 in the main manuscript for corresponding pulse sequence diagram.



Supporting Information Figure S5: Pulsatile flow phantom background phase/eddy-current effects. I, magnitude image of a central slice in the pulsatile phantom (A) with corresponding manually segmented static tissue mask (yellow, B). II, Histograms of pulsatile phantom background phase quantified over a manually segmented static tissue mask. II and III depict histograms without additional offline second-order background phase correction (BC, left) and the right histograms represent the velocity distribution in the static tissue after background phase correction. Note that after background phase correction¹ more velocities are corrected towards static 0 m/s velocity, however, the dual-Venc acquisition histogram is wider with less velocities in the most central bins (red arrows). Note, correction for Maxwell terms was performed on the scanner.²

- 1. Walker PG, Cranney GB, Scheidegger MB, Waseleski G, Pohost GM, Yoganathan AP. Semiautomated method for noise reduction and background phase error correction in MR phase velocity data. *Journal of Magnetic Resonance Imaging*. 1993;3(3):521-530.
- 2. Bernstein MA, Zhou XJ, Polzin JA, et al. Concomitant gradient terms in phase contrast MR: analysis and correction. *Magnetic resonance in medicine*. 1998;39(2):300-308.