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Ensemble-Level Organization of Human Kinetochores and Evidence for Distinct Tension and Attachment Sensors

Graphical Abstract

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In Brief

Roscioli et al. use subpixel imaging and computational methods to determine the ensemble-level 3D organization of the human kinetochore. They show how kinetochores undergo distinct rearrangements in response to the loss of attachment and tension.

Highlights

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- 3D mapping of kinetochore architecture in human RPE1 cells
- Outer kinetochore (NDC80, Mad1, and RZZ) has high nematic order
- NDC80 jackknives and KNL1 unravels upon loss of attachment and tension, respectively
- \bullet Recruitment of Mad2 is only coupled to the occupancy sensor (NDC80)

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Ensemble-Level Organization of Human Kinetochores and Evidence for Distinct Tension and Attachment Sensors

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SUMMARY

Kinetochores are multi-protein machines that form dynamic attachments to microtubules and control chromosome segregation. High fidelity is ensured because kinetochores can monitor attachment status and tension, using this information to activate checkpoints and error-correction mechanisms. To explore how kinetochores achieve this, we used two- and three-color subpixel fluorescence localization to define how proteins from six major complexes (CCAN, MIS12, NDC80, KNL1, RZZ, and SKA) and the checkpoint proteins Bub1, Mad1, and Mad2 are organized in the human kinetochore. This reveals how the outer kinetochore has a high nematic order and is largely invariant to the loss of attachment or tension, except for two mechanical sensors. First, Knl1 unravels to relay tension, and second, NDC80 undergoes jackknifing and loss of nematic order under microtubule detachment, with only the latter wired up to the checkpoint signaling system. This provides insight into how kinetochores integrate mechanical signals to promote error-free chromosome segregation.

INTRODUCTION

Human kinetochores are multi-megadalton-sized protein machines that assemble on the centromeres of every sister chromatid and provide an attachment site for the tips of \sim 20 dynamic spindle microtubules (the kinetochore [K]-fiber). Kinetochores must coordinate microtubule dynamics within the K-fiber and maintain attachment during phases of growth and shrinkage, thus coupling the energy release from microtubule depolymerization to do work ([Auckland and McAinsh, 2015; Rago and](#page-14-0) [Cheeseman, 2013\)](#page-14-0). These kinetochore-microtubule attachments are essential for the accurate segregation of chromosomes in all eukaryotes. However, there is limited understanding of how this machinery adapts to changes in microtubule occupancy and/or the imposition of pushing and pulling forces. These are important questions because a substantial body of work indicates that kinetochores must be able to sense changes in tension and occupancy ([Long et al., 2019](#page-15-0)), sensors that underpin decision making and error correction of the kinetochore.

Classic biophysical experiments established how applying tension to a kinetochore stabilized the attachment to microtubules [\(Nicklas and Koch, 1969\)](#page-15-1) and that this was coupled to changes in the chemical (phosphorylation) state of the kinetochore ([Nicklas et al., 1995\)](#page-15-2). Live cell imaging experiments further show that tension between sister kinetochores (as measured by changes in inter-kinetochore [K-K] distance) can explain the oscillatory movements of bi-oriented kinetochores, being a determinant of directional switching [\(Burroughs et al., 2015;](#page-14-1) [Wan et al., 2012\)](#page-14-1). Changes in the K-K distance were also implicated in error-correction processes that destabilize improper kinetochore attachments and stabilize bi-orientation ([Lampson](#page-15-3) [and Cheeseman, 2011; Tanaka et al., 2005\)](#page-15-3). Recent work has, however, shown that low K-K tension kinetochores do not necessarily trigger error correction ([Dudka et al., 2018](#page-15-4)). Furthermore, the imposition of K-K tension does not appear to be required for silencing of the spindle assembly checkpoint (SAC). By correlating the number of kinetochore-bound microtubules with checkpoint protein recruitment, it appears that the crucial transition to SAC silencing occurs at approximately half-maximal occupancy [\(Dudka et al., 2018; Etemad et al.,](#page-15-4) [2015, 2019; Kuhn and Dumont, 2017](#page-15-4)). Kinetochores thus appear to be able to ''count'' the number of bound microtubules.

Intra-kinetochore tension may generate key mechanical signals that are sensitive to changes in microtubule attachment and/or the imposition of force (for review, see [Maresca and Salmon, 2010\)](#page-15-5). Intra-kinetochore tension refers to the measurement of changes in distance between two components of the kinetochore labeled with different fluorophores (denoted by Δ). Initial pioneering experiments showed that increased Δ and not the K-K tension correlates with SAC silencing [\(Maresca and Salmon, 2009; Uchida et al.,](#page-15-6)

2009; Wan et al., 2009). However, there is also evidence that high Δ is not always necessary for SAC silencing ([Etemad et al., 2015;](#page-15-7) [Magidson et al., 2016; Tauchman et al., 2015](#page-15-7)). It thus remains uncertain how the kinetochore monitors change in occupancy and whether it can sense changes in tension at all. One idea is that there are kinetochore conformations or tensile elements that would function as tension and/or attachment sensors.

While X-ray crystallography and electron microscopy are begin-ning to provide a structural view of the kinetochore ([Hamilton et al.,](#page-15-8) [2019; Pesenti et al., 2016; Welburn and Cheeseman, 2008\)](#page-15-8), this approach is limited to subsets of kinetochore components and does not allow the impact of microtubule binding and forces to be easily determined. Furthermore, these approaches are limited to single assemblies, while the human kinetochore in a living cell incorporates multiple microtubule attachment sites (~ 20) populated with multiple copies of each kinetochore complex ([Huis In 't Veld](#page-15-9) [et al., 2016; Johnston et al., 2010; Suzuki et al., 2011](#page-15-9)). Thus, the *in vivo* higher-order, ensemble-level organization of the human kinetochore remains out of reach.

RESULTS

Measurement of 3D Euclidian Distances between Kinetochore Proteins

To obtain insight into the 3-dimensional (3D) nanoscale architecture of the human kinetochore, we deployed an image acquisition and computational pipeline that outputs the 3D Euclidian distances (Δ_{3D}) between differentially labeled kinetochore proteins in near-diploid hTERT-RPE1 cells (referred to hereafter as RPE1; [Smith et al., 2016](#page-16-0)). One limitation of this approach is the overestimation of mean distances ([Suzuki et al., 2018](#page-16-1)). This is because Euclidian distances cannot be negative leading to a positive bias in the Δ_{3D} distribution; in other words, distances are overestimated ([Figure 1A](#page-3-0); [Table S1](#page-14-2); [Methods S1\)](#page-14-2). To correct for this bias, we developed an algorithm to infer the true Euclidian distance (Δ_{FC}) between two fluorophores. This algorithm goes beyond previous methods ([Churchman et al., 2005; Suzuki](#page-14-3) [et al., 2018\)](#page-14-3) by taking into account the anisotropic point spread function in 3D datasets (see [Methods S1](#page-14-2) for details). To test the accuracy of this method, we fixed cells and stained them with an anti-CenpC antibody that recognizes the amino-terminal region of the protein (amino acids [aa] 1–426), binding to a site preceding the region binding CenpA nucleosomes. This primary antibody was then detected using a mixture of 3 different secondary antibodies (conjugated to Alexa Fluor 488, 568, and 647; [Fig](#page-3-0)[ure 1](#page-3-0)A). The Euclidean bias-corrected delta distances were 2.2 \pm 1.5 nm (mean \pm standard deviation; n = 2,302; Alexa Fluor 488–568), 4.3 ± 2.7 nm (n = 1,437; Alexa Fluor 488–647), and 4.5 ± 2.8 nm (n = 1,452; Alexa Fluor 568-647), considerably smaller than the corresponding Δ_{3D} [\(Figure 1A](#page-3-0); [Table S1\)](#page-14-2).

These data confirm that we can measure the 3D nanoscale distances between 3 different fluorophores within the human kinetochore with an accuracy on the scale of 2–4 nm. As a second test, the amino-terminal end of the Ndc80 subunit (of the NDC80 complex) was marked with the 9G3 monoclonal antibody that recognizes the N-terminal globular domain of Hec1 (aa 200–215; [De-](#page-15-10)[Luca et al., 2006;](#page-15-10) hereafter referred to as Ndc80(N)) and the carboxy-terminal end was marked with EGFP (Ndc80(C); [Figures](#page-3-0)

Cell Reports Article

[1](#page-3-0)B and 1C). To label the Ndc80 C-terminal end, we inserted EGFP at the endogenous locus by CRISPR-Cas9 gene editing in RPE1 cells (cell line MC191; see [Methods S1](#page-14-2) and [Figure S2](#page-14-2) for details). The Δ_{EC} distance from Ndc80(C) to Ndc80(N) was 48.7 \pm 1.2 nm $(n = 726;$ [Figure 1](#page-3-0)D; [Table S1\)](#page-14-2). Because there is substantial structural information describing the NDC80 complex *in vitro*, it has been used as a ''molecular ruler'' to validate 2 color fluorescence localization methods ([Suzuki et al., 2018](#page-16-1)). Our Δ_{FC} measurements are close to the 51 nm distance estimated using negative stain electron microscopy (EM) [\(Huis In 't Veld et al., 2016; Wei et al.,](#page-15-9) [2005](#page-15-9); [Figure 1B](#page-3-0)). As expected, the Δ_{3D} measurement is an overestimate (59.50 \pm 20.52 nm, n = 693; [Figure 1](#page-3-0)D; [Table S1](#page-14-2)), while the Δ_{1D} is typically an underestimate (33.37 \pm 14.48 nm, n = 283; [Figure S1A](#page-14-2); [Table S1](#page-14-2); [Smith et al., 2016](#page-16-0)). We next measured the Δ_{FC} distance between the MIS12 complex subunit Nnf1 and Ndc80(N) [\(Figures 1B](#page-3-0) and 1C) and obtained a value of 66.4 \pm 1.5 nm (n = 724; [Figure 1D](#page-3-0); [Table S1\)](#page-14-2). This is similar to the distance measured in parental cells that did not have EGFP knocked in to the *NDC80* locus (Δ_{EC} , 61.5 \pm 0.8 nm, n = 1,748; [Figure S1D](#page-14-2); [Table](#page-14-2) [S1\)](#page-14-2). Again, these distances are very close to the predicted distance $(\sim 65$ nm) that can be estimated from EM studies ([Petrovic](#page-15-11) [et al., 2010; Screpanti et al., 2011](#page-15-11)). Finally, as expected from *in vitro* reconstitution experiments ([Helgeson et al., 2018; Huis In](#page-15-12) ['t Veld et al., 2019](#page-15-12)) the SKA complex (Ska3) was located proximal to the Ndc80 amino terminus [\(Table S1\)](#page-14-2). Overall, these data confirm the accuracy of our method and the importance of correcting intra-kinetochore distance measurements.

The Inner Kinetochore Is Offset from the Outer Kinetochore

Concurrent with measuring the distance between Ndc80(C), Ndc80(N), and Nnf1, we also determined an inner kinetochore position using the CenpC antibody used in [Figure 1A](#page-3-0). We measured the distances from the amino- and carboxy-ends of Ndc80 to CenpC in a 3-fluorophores experiment and obtained a triangle with side lengths of 43.5 ± 2.3 nm (n = 247), 81.9 \pm 2.9 nm (n = 244), and 48.4 ± 3.1 nm (n = 247; [Figures 2](#page-4-0)A, 2B, and [S1B](#page-14-2); [Table S1\)](#page-14-2). These 3 distances are not compatible with collinearity ($p = 0.019$, $z = 2.07$; [Figure 2](#page-4-0)B; [Table S1](#page-14-2)). To further substantiate a lack of collinearity, we also measured the dis-tances from Ndc80(N) and CenpC to Nnf1 in parental cells [\(Fig](#page-14-2)[ure S1C](#page-14-2)). These measurements also indicate a lack of collinearity $(p = 6 \times 10^{-17}, z = 8.28)$ with side lengths of 34.9 \pm 0.6 nm (n = 1,777), 85.8 ± 0.8 nm (n = 1,754), and 61.5 ± 0.8 nm (n = 1,748; [Figures 2](#page-4-0)A, 2B, and [S1](#page-14-2)D; [Table S1\)](#page-14-2). This contrasts with distances between Nnf1-Ndc80(C)-Ndc80(N), which are collinear to our accuracy ($p = 0.07$, $z = 1.47$, distances 48.7 ± 1.2 nm $[n = 726]$, 8.4 \pm 6.0 nm $[n = 727]$, and 66.4 \pm 1.5 nm $[n = 724]$; [Fig](#page-3-0)[ures 1D](#page-3-0), [2](#page-4-0)B, and [S1A](#page-14-2); [Table S1\)](#page-14-2). The CenpC position (inner kinetochore) must therefore be offset (on average) from the axis defined by the Nnf1-Ndc80(C)-Ndc80(N) axis.

Visualization of Kinetochore Ensemble Organization

Each kinetochore contains multiple copies of each protein per microtubule and multiple microtubule binding sites. Our experiments thus measure the ensemble average position of the tagged proteins and not the distance between single molecules. To understand the observed lack of collinearity and interpret our

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Figure 1. Δ_{3D} Measurements Overestimate the True Λ Distance

(A) Kinetochores stained with anti-CenpC primary antibody and a mixture of Alexa488 (A488), Alexa568 (A568), and Alexa647 (A647)-conjugated secondary antibodies. Histograms of Δ_{3D} (black) and inferred Δ_{EC} (red) distances between the indicated fluorophores, mean (dashed line), and SD (horizontal bar for Δ_{EC}) values are indicated at right.

(B) Schematic representation of MIS12 complex (dark blue) and NDC80 complex (light blue) bound to a microtubule protofilament (dark gray). Assembly organization and size are based on electron microscopy (black dotted line) and crys-tallography studies (see [Methods S1](#page-14-2) for details). Approximate antibody binding sites (or EGFP tagging) are indicated with green dots. Distances used for nematic order (*N*) calculation are indicated in pink (see [Table S2](#page-14-2)).

(C) Kinetochores stained with anti-Nnf1 and anti-Hec1(9G3) antibodies and RPE1 Ndc80-EGFP cells.

(D) Histograms of the Ndc80(C) to Ndc80(N), Nnf1 to Ndc80(C), and Nnf1 to Ndc80(N) Δ_{3D} and the Δ_{EC} distances measured in Ndc80-EGFP cells; means and SDs are displayed as in (A). Scale bars, 500 nm.

we fit the NDC80 complex hinge angle and the elevation of the NDC80 complex short arm (Ndc80(N)-to-Ndc80(hinge)) with the microtubule. Best fits are 203.5° and 22.4° , respectively (Figure $2C$; see [Methods S1\)](#page-14-2); hinge angles $>180^\circ$ have been observed [\(Scarborough et al.,](#page-16-2) [2019; Wang et al., 2008\)](#page-16-2), while the latter is compatible with the range determined from EM and crystal structure studies [\(Ci](#page-15-13)[ferri et al., 2008; Wilson-Kubalek et al.,](#page-15-13) [2008\)](#page-15-13). [Figure 2](#page-4-0)D (left and center left panels) shows a simulation of a single kinetochore bound to a K-fiber (gray) with the simulated positions of CenpC (pink), Ndc80(C) (light blue), Ndc80 loop (red), Ndc80(N) (blue), and Nnf1 (orange) at single molecules. The center right panel displays the average of the simulated position of three markers showing the offset of CenpC with respect to the Ndc80 complex. Averaging across multiple simulated kinetochores reveals a multi-layered structure with tight localization and

distances in the context of known structural information, we built a computational simulation. Our simulations incorporate (1) known structural biology on NDC80-MIS12, (2) information from EM data of K-fiber and kinetochore organization, and (3) measurements of kinetochore protein numbers per microtubule. We optimized unknown parameters by fitting the simulations to our measured triangle CenpC-Ndc80(C)-Ndc80(N). Crucially,

sequential ordering of kinetochore components along the K-fiber axis, and an extensive spread transverse to the axis that is suggestive of discs [\(Figure 2D](#page-4-0), right panel). Our simulations indicate that moderate levels of flexibility of the Ndc80 microtubule attachment angle and orientation can produce a lack of collinearity between the average positions of CenpC, Nnf1/ Ndc80(C), and Ndc80(N). In addition, the broad transverse

Ndc80(N) Ndc80 loop Ndc80(C) Nnf1 CenpC Microtubule

Figure 2. Simulations of the Architecture of a Bi-oriented Kinetochore

(A) Histograms of Δ_{3D} and Δ_{EC} distances for CenpC to Ndc80(C) and CenpC to Ndc80(N) (Ndc80-EGFP cells) and for CenpC to Nnf1, mean (dashed line), and SD (horizontal bar) values are indicated at right.

(B) Schematic showing the inferred architecture of CenpC-MIS12-NDC80. Approximate antibody binding sites (or EGFP tagging) are indicated with green dots. Lines indicate A_{EC} mean values (dotted lines show SDs) obtained in 3-fluorophore experiments: CenpC-Ndc80(C)-Ndc80(N) (black), CenpC-Nnf1-Ndc80(N) (orange), and Nnf1-Ndc80(C)-Ndc80(N) (red).

(C) Schematic of CenpC-MIS12-NDC80 showing best-fitted angles (red) from simulations; see [Methods S1](#page-14-2).

dimension allows even small re-distributions of the CenpC population to give rise to an off-axis location. Thus, changes in the distribution of the CenpC marker, potentially due to CenpC's inherent flexibility, are sufficient to explain the lack of collinearity measured *in vivo*.

The simulations also revealed ordered alignment of kinetochore molecules along an internal axis. We sought to quantify the degree of alignment of individual NDC80 complexes. Because these complexes are rod-like with head-tail asymmetry, we can calculate the nematic order (N), which is a measure of the mean degree of filament alignment along a director ([de](#page-15-14) [Gennes and Prost, 1993; Doostmohammadi et al., 2018](#page-15-14)) and related to our distance measurements by $N = \Delta_{EC}/\Delta_{structural}$ (see [Methods S1\)](#page-14-2). Here, $N = \sim 0$ indicates no alignment (low nematic order), and $N = \sim 1$ is perfect parallel alignment of vectors (high nematic order; [Figure 2](#page-4-0)E). At high alignment of the NDC80 complexes within the ensemble (i.e., high nematic order), the structural data and our *in vivo* distance measurements should match, while as nematic order decreases, the measured distance of the ensemble decreases ([Figure 2](#page-4-0)E). We find that for both the Ndc80(C) to Ndc80(N) and Nnf1 to Ndc80(N) linkages, $N = \sim 1$ ([Figure 1](#page-3-0)B; [Table S2](#page-14-2)). This indicates that in the microtubule-attached state, the MIS12-NDC80 complex assemblies are highly ordered and that Δ_{EC} distances reflect the underlying molecular organization as implicitly assumed in using the NDC80 complex as a molecular ruler ([Suzuki et al., 2018](#page-16-1)). We also investigated how increasing the fluctuations in the hinge angle and Ndc80 orientation decreased the nematic order [\(Figure 2F](#page-4-0), left panel) and correspondingly decreased the average Δ_{EC} distance [\(Figure 2](#page-4-0)F, right panel). This further shows how the angular degrees of freedom, such as the NDC80 hinge [\(Methods S1](#page-14-2)) are in effect highly constrained to produce high alignment of the NDC80 complexes. Thus, our simulations and data indicate that at this resolution, the kinetochore is organized along an internal axis with high nematic order in the outer plate ([Table S2](#page-14-2)).

Linking the Inner and Outer Kinetochores: CenpT and CenpC-Mis12 Linkages Both Position NDC80 in the Same Spatial Domain

It is well established that NDC80 complexes are not only targeted to kinetochores through CenpC-Mis12 linkages but also through CenpT ([Gascoigne et al., 2011; Klare et al., 2015\)](#page-15-15); each linker is responsible for recruiting $~50\%$ of the Ndc80 molecules ([Johnston et al., 2010](#page-15-16)). We determined the CenpT position using an antibody, which recognizes the non-histone fold region that extends and interacts with the NDC80 complex. This CenpT epitope was positioned close (5.7 \pm 4.0 nm, n = 894) to the Ndc80 C terminus and 47.9 ± 1.6 nm (n = 882) from CenpC ([Figure 3](#page-6-0)C; [Table S1](#page-14-2)). This suggested that the NDC80

complexes tethered through CenpT or CenpC-MIS12 are not spatially separated within the kinetochore. To further investigate, we depleted each linker by RNAi. Depletion of CenpT resulted in the loss of >93% of the CenpT molecules from kinetochores and an increase in the number of CenpC molecules [\(Figures 3](#page-6-0)A and 3B). However, the distance between the remaining endogenous Ndc80-EGFP $(\sim20\%)$ and CenpC molecules increased by only 10.5 ± 7.0 nm compared to control cells ([Figure 3C](#page-6-0); [Table S1\)](#page-14-2). The reciprocal experiments (CenpC depleted by >96%) resulted in the unbinding of CenpT (by \sim 90%) and Ndc80-EGFP (by \sim 75%; [Figures 3A](#page-6-0) and 3B). The distance between the residual CenpT and Ndc80(C) also increased by 14.5 ± 9.9 nm ([Figure 3C](#page-6-0); [Table S1](#page-14-2)). These data support the idea of a single NDC80 complex population and confirm that the linkers are required for normal kinetochore integrity and composition ([Klare et al.,](#page-15-17) [2015; Suzuki et al., 2014](#page-15-17)).

Jackknifing of NDC80 Complexes Follows Treatment with Nocodazole, but Not Taxol

We next investigated how the structural organization and geometry of the kinetochore respond to a loss of attachment or tension. To do this, we treated the RPE1 cell lines with either (1) 3.3 μ M nocodazole for 2 h and confirmed by tubulin staining that all of the kinetochore-microtubule populations were eliminated and that the 3D K-K distance (CenpC to CenpC) was reduced (0.93 \pm 0.005 µm, n = 2,537, means \pm SEMs), or (2) 1μ M taxol for 15 min, which reduces the K-K distance to nearly rest length (0.96 \pm 0.004 μ m, n = 1,931, means \pm SEMs), but leaves the majority of kinetochores associated with microtubules and aligned on the metaphase plate [\(Figure S3](#page-14-2)A). By measuring microtubule dynamics using photoactivatable PA-EGFP-alphatubulin, we also confirmed that 1 μ M taxol largely eliminated microtubule dynamics [\(Amaro et al., 2010\)](#page-14-4), consistent with the loss of tension ([Figure S3\)](#page-14-2).

We measured the geometry of the CenpC-MIS12-NDC80 assembly; the distances from CenpC to Ndc80(C) and Nnf1 were largely unchanged in nocodazole and taxol ([Figures 4A](#page-7-0), [S4](#page-14-2)A, and S4B; [Table S1](#page-14-2)). This is consistent with previous work reporting that the inner kinetochore does not collapse following microtubule detachment ([Smith et al., 2016; Suzuki et al., 2018\)](#page-16-0). However, the CenpC to Ndc80(N) distance was reduced by 25.3 ± 3.5 nm following treatment with nocodazole (Ndc80-EGFP cells; [Figure 4](#page-7-0)A; similar to the reduction of 30.1 ± 3.3 nm observed in parental cells; [Figure S4B](#page-14-2); [Table S1](#page-14-2)). Consistently, the Ndc80(C) to Ndc80(N) distance decreased by 41.1 \pm 5.5 nm (85%) in unattached kinetochores [\(Figure 4](#page-7-0)A). We also measured the distances between Nnf1, Ndc80(C), and Ndc80(N) [\(Figure 4](#page-7-0)B). This triangulation confirms that there is a substantial reduction of 40.9 ± 5.1 nm (84%) in the Ndc80(C) to

⁽D) Simulated kinetochore organization. Left and center left: 2 perspectives of the same simulated kinetochore; each dot represents a single protein at the specified position (labeled by color). Center right: averages of the simulated position of each marker shown in the plane of the CenpC-Ndc80(N)-Ndc80(C) triangle. Right: an ensemble of 200 simulated kinetochores aligned along their microtubule axis and to the mean of their Ndc80(N) markers. Histogram of the marker density along K-fiber for the above plot.

⁽E) Schematic representation of NDC80 complexes under high (N = ~1) and low (N = ~0) nematic order. Circles represent Ndc80(C) (green), Ndc80 loop (blue), and Ndc80(N) (red).

⁽F) Left: change in the nematic order of the NDC80 complex population with respect to the magnitude of Ndc80 loop stochastic angular fluctuations. Right: average distance between the indicated molecular markers against the nematic order. Simulations based on 200 kinetochores.

(A) Kinetochores stained with anti-CenpT and anti-CenpC antibodies in Ndc80-EGFP cells transfected with small interfering AllStar (siAllStar) (control) and siRNA against CenpC and CenpT. Scale bar, 500 nm.

(B) Box and whiskers plots of CenpC, CenpT, and Ndc80-EGFP kinetochore intensity in the different RNAi conditions; signals are background subtracted. (C) Histograms of CenpC to Ndc80(C) and CenpT to Ndc80(C) Δ_{EC} distances measured in Ndc80-EGFP cells treated as in (A); mean (dashed line) and SD values are indicated at right.

Ndc80(N) linkage under nocodazole treatment ([Figure 4](#page-7-0)C; [Table](#page-14-2) [S1\)](#page-14-2). In taxol, the Δ_{EC} between Ndc80(C) and Ndc80(N) remained the same as in the control [\(Figures 4A](#page-7-0) and 4C; [Table S1\)](#page-14-2). This suggests that the Ndc80 N terminus does not move inward following taxol treatment and the NDC80 complex remains in its straight configuration with a high nematic order, $N = \sim 1$ ([Table](#page-14-2) [S2\)](#page-14-2). These data provide evidence that the kinetochore responds differentially to the loss of attachment and tension.

Next, we sought to investigate the underlying cause of the \sim 85% reduction in the distance between Ndc80 C and N termini observed under nocodazole treatment. Previous studies have suggested that the Ndc80 loop acts as a pivoting point and thus we asked whether the distance reduction can be explained by conformational change in the Ndc80 complex such that the Ndc80 N terminus is brought into close proximity to the C terminus (we call this jackknifing; [Figure 4D](#page-7-0), model 2). Ndc80 structural data suggest that the expected distance between Ndc80 C and N termini upon full closure of the N terminus is \sim 19 nm, and thus is insufficient to explain the measured 7.8 nm distance in nocodazole. Since the measurements reflect

kinetochore ensemble organization, the change could alternatively be explained by the disorganization of the Ndc80 molecules (i.e., loss of nematic order) or a combination of Ndc80 jackknifing and disorganization. Our analysis shows that in the absence of Ndc80 jackknifing (i.e., if Ndc80 maintains its straight conformation as in DMSO), a nematic order decrease from \sim 1 observed in DMSO [\(Figures 4](#page-7-0)D and 4E, model 1) to <0.2 is required to explain the observed 7.8 nm distance be-tween Ndc80 C and N termini [\(Figures 4](#page-7-0)D and 4E, model 3). Alternatively, if Ndc80 undergoes full jackknifing then a loss of order to 0.4 is still required to explain the measured 7.8 nm distance [\(Figures 4](#page-7-0)D and 4E, model 4). We favor this model (see [Discussion](#page-11-0) for details) and hereafter refer to these changes in NDC80 organization as jackknifing.

NDC80 Jackknifing Marks Spindle Checkpoint Active Kinetochores

Does jackknifing within the outer kinetochore plate relate to checkpoint signaling from the kinetochore? For these experiments, we used cells in which Mad2 was labeled at its endogenous locus

Figure 4. Loss of Microtubule Attachment and Stabilization of Microtubule Dynamics Induce Different Organization of Ndc80

(A) Histograms of CenpC to Ndc80(N), CenpC to Ndc80(C), and CenpC to Ndc80(N) Δ_{EC} distances in Ndc80-EGFP cells treated with 3.3 µM nocodazole for 2 h, 1 µM taxol for 15 min, or DMSO; mean (dashed line) and SD values are indicated at right.

(B) Kinetochores stained with anti-Nnf1 and anti-Hec1(9G3) antibodies and in Ndc80-EGFP cells treated as in (A). Scale bar, 500 nm.

(legend continued on next page)

with Venus ([Collin et al., 2013\)](#page-15-18). As expected, nocodazole treatment (unattached kinetochores) led to an increase in Venus-Mad2 and Bub1 kinetochore binding on most kinetochores, while after taxol treatment, the average levels of these proteins were similar [\(Fig](#page-9-0)[ures 5A](#page-9-0), 5B, and [S5](#page-14-2)A). However, in taxol and DMSO, there were multiple outliers [\(Figure 5](#page-9-0)B), suggesting the presence of a Mad2 positive subpopulation, as previously reported [\(Magidson et al.,](#page-15-19) 2016). In addition, we found that treatment with 1 μ M taxol prevents cells in metaphase from exiting mitosis unless 1 μ M reversine (Mps1 inhibitor) is added to the media to override the spindle checkpoint ([Figures 5](#page-9-0)C and [S5B](#page-14-2)). These experiments indicate that the spindle checkpoint is active following treatment with 1 µM taxol and suggest that the few Mad2-signaling kinetochores may be responsible. To understand how the Ndc80 jackknifing relates to Mad2 recruitment, we separated our kinetochore spots into a Venus-Mad2-positive (Mad2⁺) and -negative (Mad2⁻⁻) population, and then determined the distance from CenpC to Ndc80(N) ([Figure 5](#page-9-0)D). The CenpC to Ndc80(N) distances were significantly different in these 2 populations (p = 2.4 \times 10⁻⁵), with the distance in the Mad2⁺ population (66.2 \pm 3.7 nm) nearly identical to that of nocodazole-treated cells (which were all Mad2⁺, $\Delta_{\text{EC}} = 58.3~\pm$ 1.3 nm, $p = 0.044$). Furthermore, the 16.2 \pm 3.8 nm difference in the CenpC to Ndc80(N) between $Mad2^-$ and $Mad2^+$ in DMSO [\(Fig](#page-9-0)[ure 5D](#page-9-0); [Table S1\)](#page-14-2) is consistent with the jackknifing of Ndc80 under the lack of attachment in Mad2⁺ (compare to the Δ_{FC} decrease of 25.3 ± 3.5 nm under nocodazole, $p = 0.039$), suggesting that there is a high correlation between $Mad2^+ / Mad2^-$ and $Ndc80$ being in the jackknife or straight conformations (nocodazole versus DMSO, respectively). Under taxol, we could also detect an inward movement of 11.5 ± 5.1 nm of the Ndc80(N) in the Mad2⁺ versus $Mad2^-$ subpopulations ([Figure 5](#page-9-0)D). These correlations are likely imperfect because the $Mad2^+$ /Mad 2^- populations are also heterogeneous with respect to attachment status and include partial jackknifing states as error correction proceeds.

These data indicate that we can detect the inward movement of Ndc80(N) at Mad2⁺ kinetochores in control metaphase cells, not just under nocodazole treatment. These data clearly demonstrate that checkpoint activation (in terms of Mad2 recruitment) occurs at kinetochores that are in the unattached conformation (Ndc80 jackknifed). Moreover, our data show how most kinetochores in 1 μ M taxol have a low K-K distance without triggering the recruitment of Mad2. We next reasoned that if the Ndc80 jackknifing is downstream of checkpoint activation, then it should not occur when Mps1 kinase activity is inhibited. The treatment of cells with 1 μ M reversine eliminated the Mad1-pT716 substrate signal ([Allan et al., 2020\)](#page-14-5), but had no effect on Ndc80(N) movement in the presence of nocodazole (and MG132 to prevent entry to anaphase; [Figure S5](#page-14-2)C), suggesting that jackknifing is independent from Mps1 activity.

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3D Mapping of the Key Checkpoint Protein Platforms Bub1 and RZZ

We next sought to establish where in the kinetochore the Mad1:- Mad2 complex is recruited. While Bub1 is a bona fide kinetochore receptor for human Mad1:Mad2 complexes ([Zhang](#page-16-3) [et al., 2017](#page-16-3)), the RZZ complex is also implicated [\(Kops et al.,](#page-15-20) [2005\)](#page-15-20) and may even operate as a second receptor (Silió [et al.,](#page-16-4) [2015\)](#page-16-4). To read out the position of Bub1, we used an antibody that recognizes the first 130 aa (referred to as Bub1(N); [Figure 6B](#page-10-0)) and found it positioned 58.9 ± 1.1 nm (n = 2,232) from CenpC and therefore 26.9 ± 1.4 nm to the inside of the Ndc80 head domain [\(Figure 5C](#page-9-0); [Table S1](#page-14-2)). Using antibodies that recognize the carboxy-terminus of Rod (recombinant fragment aa 2,100– 2,209, referred to as $Rod(C)$ and Zwilch (Figures $6A$ and $6B$), we found that while Rod(C) is positioned 14.4 ± 2.1 nm inside Ndc80(N), Zwilch is 10.5 \pm 1.3 nm to the outside [\(Figures 6](#page-10-0)B and 6C; [Table S1\)](#page-14-2). In addition, EGFP-Zw10 was positioned 11.5 \pm 3.6 nm outside Rod(C) and 13.4 \pm 3.3 nm inside Zwlich [\(Figures 6A](#page-10-0) and 6B; [Table S1\)](#page-14-2). This is broadly consistent with the arrangement of these subunits within the cryo-EM structure of the RZZ complex ([Mosalaganti et al., 2017\)](#page-15-21). These results indicate that most of the RZZ complex is located outside the Ndc80 head domain, and thus is spatially separated from Bub1. We can estimate the distance between Zwilch and Rod by subtracting the CenpC to Rod(C) from CenpC to Zwilch distances, giving 24.9 \pm 2.1 nm [\(Figure 6](#page-10-0)C; [Table S1\)](#page-14-2). This distance is similar to that determined from the cryo-EM structure ([Mosalaganti et al.,](#page-15-21) [2017\)](#page-15-21) and indicates high nematic order (N = \sim 0.8; [Table S2](#page-14-2)). The high nematic order further justifies the assumption of the molecular ruler to organize components of the outer kinetochore/corona. These data also suggest that within an end-on attached kinetochore, the RZZ complex is not forming a headto-tail dimer, as suggested by cryo-EM [\(Mosalaganti et al.,](#page-15-21) [2017\)](#page-15-21); this would have resulted in Rod(C) and Zwilch signals being coincident. These data thus provide the first 3D mapping of the key checkpoint protein platforms (Bub1 and RZZ) relative to the major microtubule attachment factor (NDC80 complex) in the human kinetochore.

Mad1:Mad2 Complex Can Occupy Two Distinct Positions within the Kinetochore

We next used the RZZ molecular ruler to map the positions of Mad2 and a phospho-epitope in the carboxy-terminus of Mad1(pT716) following treatment with nocodazole. As the corona/outer kinetochore begins expanding into crescent-shaped structures under these (unattached) conditions, we limited our analysis to non-expanded kinetochores (a ''proto-corona'') to have accurate positional information ([Figure 6](#page-10-0)D). The position of Bub1, Rod, and Zwilch (RZZ complex) remained largely un-changed ([Figure 6](#page-10-0)C), showing that kinetochores do not simply

⁽C) Histograms of Ndc80(C) to Ndc80(N), Nnf1 to Ndc80(C), and Nnf1-to-Ndc80(N) $\Delta_{\rm EC}$ distance in Ndc80-EGFP cells treated as in (A); mean (dashed line) and SD values are indicated at right.

⁽D) Four models of different structural and nematic organizations of NDC80. Circles represent Ndc80(C) (green), Ndc80 loop (blue), and Ndc80(N) (red). For each model, the nematic order (gray), the distance expected from structural information (black), and the expected Δ_{EC} (pink) are indicated.

⁽E) Data-constrained nematic order and hinge angle of the NDC80 complex. For each hinge angle, the nematic order is calculated that is consistent with the observed Δ_{FC} , 48.7 nm (DMSO) and 7.8 nm (nocodazole) for the Ndc80(C) to Ndc80(N) linkage. Dashed lines show 95% confidence intervals. Numbered circles annotate the approximate position of each model on the graph.

 $(n=64)$

(n=558)

 $(n=622)$

Figure 5. Activation of the Spindle Assembly Checkpoint Correlates with NDC80 Conformational Change

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(A) Images of Venus-Mad2 cells stained with anti-CenpC antibody and treated with $3.3 \mu M$ nocodazole for 2 h, 1 μ M taxol for 15 min, or DMSO. White arrows indicate Mad2⁺ kinetochores. Scale bar, $3 \mu m$.

(B) Box and whisker plots of Venus-Mad2 and Bub1 kinetochore intensity in cells treated as in (A). All of the intensities are background subtracted. The Bub1 signal is normalized to the CenpC signal.

(C) Images of cells treated with 1 μ M taxol and DMSO for 15 min and stained with SiR-DNA. Scale bars, $5 \mu m$. Bar chart indicates the fraction of cells exiting mitosis within the indicated imaging time, after DMSO, taxol $(+\text{tax})$, and 1 μ M reversine (+rev) treatment [\(Figure S5](#page-14-2)B; [Method Details](#page-19-0)). Fisher's exact test indicates that the differences are significant with a 99% confidence interval: *p = 7.7 \times 10⁻¹²; **p = 2.3 \times 10⁻⁵; ***p = 1.2 \times 10^{-4} .

(D) Example images of kinetochores stained with anti-CenpC and anti-Hec1(9G3) antibodies in RPE1 Venus-Mad2 cells treated as in (A). Scale bar, 500 nm. [Table](#page-14-2) [S1](#page-14-2) displays the Δ_{EC} (mean \pm SD) between CenpC and Ndc80(N) in Venus-Mad2⁺ (green circle), Venus-Mad2⁻ (pink circles) kinetochores, and pool samples in the 3 conditions. Insets (i–vi) show the distances (yellow dotted lines) between CenpC $(+)$ and Ndc80 $($ \bigcirc) in the indicated kinetochores on the XY plane. Scale bar in insets, 250 nm.

Figure 6. Mad1:Mad2 Binds Different Kinetochore Sites upon Activation of the Spindle Assembly Checkpoint

(A) Scale model of RZZ and approximate positions of anti-Rod(C) and anti-Zwilch antibodies and EGFP-Zw10.

(B) Kinetochore pairs stained with anti-CenpC antibody in combination with anti-Bub1, anti-Rod, or anti-Zwilch antibodies in DMSO-treated cells. Scale bar, 500 nm.

(C) Histograms of Δ_{EC} between CenpC and Ndc80(N), Bub1, Rod, and Zwilch in DMSO- and nocodazole-treated cells. Mad1-pT716 and Mad2 positions are shown for nocodazole only. Mean (dashed line) and SD values are indicated at right.

collapse when unattached. Mad1-pT716 was located 54.4 \pm 2.0 nm (n = 911) from CenpC (close to its binding partner Bub1), while Mad2 was located 16.5 ± 2.7 nm further outward ([Figures](#page-10-0) [6C](#page-10-0) and 6E; [Table S1](#page-14-2)). This distance is consistent the Mad1:Mad2 complex structure [\(Figure 6](#page-10-0)E; [Allan et al., 2020; Kim et al., 2012;](#page-14-5) [Sironi et al., 2002](#page-14-5)). Moreover, the distance from Mad1-pT716 to an antibody that recognizes an epitope (aa 77–115) in the amino terminus, referred to as Mad1(N), was 48.4 ± 13.7 nm (n = 235) [\(Figures 6E](#page-10-0) and [S6](#page-14-2)A), close to the predicted 57 nm from EM structure [\(Allan et al., 2020](#page-14-5)). Thus, Mad1 looks to be extended within the kinetochore and highly ordered [\(Table S2\)](#page-14-2).

Mad1:Mad2 are proposed to bind to both Bub1 and a second RZZ-dependent receptor, recently identified as CyclinB ([Allan](#page-14-5) et al., 2020; Silió et al., 2015). Our measurement of Mad1:Mad2 would thus reflect the average position of these proteins within a kinetochore. To test this idea, we measured the position of Mad1-pT716 and Mad2 in cells carrying a homozygous *bub1 1-23* mutation ([Figures 6](#page-10-0)F, [S7](#page-14-2)A and S7B). In these cells, Bub1 levels are reduced to almost undetectable levels, but Mad1 pT716, Mad2, and Zwilch can still bind kinetochores and generate a checkpoint signal ([Figures S7](#page-14-2)A, S7B, and [S8A](#page-14-2)) [\(Currie et al., 2018; Zhang et al., 2019](#page-15-22)). Here, both Mad1 pT716 and Mad2 signals moved outward by 13.7 \pm 2.3 nm and 13.2 \pm 2.5 nm, respectively ([Figure 6](#page-10-0)G). In contrast, we found that the Zwilch position from CenpC was 92.1 ± 2.9 (n = 296) in parental cells and 97.2 ± 5.8 (n = 133) in *bub1 1-23* cells, suggesting that the RZZ complex was not affected by the loss of Bub1 [\(Figure 6G](#page-10-0)). These data are consistent with the model that there are two spatially distinct kinetochore receptors for Mad1:Mad2.

Kinetochores Adopt a Unique Conformation following the Loss of Tension

The absence of NDC80 jackknifing following taxol treatment raised the question of whether the loss of tension is detected at all. We first checked the position of Bub1 and RZZ subunits in taxoltreated cells and found no changes [\(Figures 7A](#page-12-0) and 7B). We then turned to Knl1, the third component of the KMN network [\(Cheeseman et al., 2006\)](#page-14-6). Knl1 is a largely disordered protein that binds to the MIS12 complex through the carboxy-terminus with the remaining protein comprising multiple MELT sequences that operate as phospho-dependent binding sites for the Bub3- Bub1 checkpoint complexes ([Figure 7C](#page-12-0); [London et al., 2012;](#page-15-23) [Shepperd et al., 2012; Yamagishi et al., 2012\)](#page-15-23). The extreme amino-terminal end of Knl1 contains a microtubule-binding site and a docking site for protein phosphatase 1 (PP1) [\(Figure 7C](#page-12-0)). The amino terminus of Knl1 (marked with a phospho-specific anti-

body that recognizes serine 24, referred to as Knl1-pS24; [Fig](#page-12-0)[ure 7C](#page-12-0)) was positioned 32.8 ± 12.5 nm from Bub1 [\(Figure 7](#page-12-0)B), whereas the second MELT (aa 300–350, referred to as Knl1(MELT2); [Figure 7](#page-12-0)C) was only 6.5 ± 1.5 nm from Bub1, which is consistent with the role of the MELT motifs in recruiting Bub1 to the kinetochores [\(Figures 7B](#page-12-0) and 7E). These data suggest that the unstructured region of Knl1 [\(Figure 7](#page-12-0)C), which has a predicted path length of \sim 380 nm, must be "wrapped up" and occupy the space between the Ndc80 head domain and the CCAN (CenpC here). We next checked the position of the amino terminus of Knl1 (Knl1 pS24) following taxol treatment ([Figure 7D](#page-12-0)) and found that itmoved outward by 93.0 ± 12.8 nm ([Figure 7](#page-12-0)B). There was minimal movement of the second MELT, indicating that the bulk of the MELT array is unchanged ([Figures 7B](#page-12-0) and 7E; [Table S1\)](#page-14-2). This is consistent with our observation that the Bub1 position, which is a proxy for the MELTs, does not change. Because the predicted length of the disordered first 300 aa is \sim 64 nm and the distance from Knl1(MELT2) to Knl1-pS24 in taxol is 50.6 ± 3.3 nm, this region of Knl1 must switch into an almost straight configuration. Compared to the increase in nocodazole treatment, an increase was not detected in the phosphorylation of Knl1-pS24 ([Figure 7D](#page-12-0)), which is a substrate for AuroraB ([Welburn et al., 2010](#page-16-5)). Because nocodazole also causes a loss of tension, we checked the position of Knl1 [\(Figures 7D](#page-12-0) and 7E). Knl1 is again more extended, with the amino-terminal end located 91.7 ± 6.3 nm (n = 472) from CenpC (compared to 26.1 ± 12.5 nm, n = 1,260 in DMSO; [Figure 7D](#page-12-0); [Table](#page-14-2) [S1](#page-14-2)). We also detected an outward movement (17.1 \pm 2.4 nm) of the MELT2 position ([Figure 7E](#page-12-0)). These data provide evidence that the physical re-organization of Knl1 responds to the loss of tension.

DISCUSSION

This work provides an initial architectural map of the human kinetochore by quantifying the relative position (to accuracy 1– 10 nm) and movement of major complexes and subunits (see [Figure 7](#page-12-0)F). Our intra-kinetochore distances are corrected for Euclidean distance inflation and interpreted within the context of a kinetochore ensemble of molecules and available structural data. Using a computational simulation, we generated a 3D visualization of a human kinetochore that produces plate-like structures for the outer (MIS12-NDC80) and inner (CenpC) kinetochores, which is reminiscent of that observed in electron micrographs ([Brinkley et al., 1992](#page-14-7)). These data also demonstrate how the inner and outer plates are shifted relative to each other in the direction perpendicular to the microtubule axis. We propose here that the outer kinetochore is highly ordered with molecules aligned along an outer kinetochore axis, presumably parallel to

⁽D) Examples of spot-like and expanded kinetochores. Kinetochores are stained with anti-Bub1, anti-Rod, and anti-Zwilch antibodies in cells treated with 3.3 mM nocodazole. Scale bars, 250 nm.

⁽E) Top: schematic indicating the Mad1:Mad2 complex size and the approximate binding positions of anti-Mad1-pT716; anti-Mad1 directed against aa 77–115, referred to as Mad1(N); and anti-Mad2 antibodies used in this study. Bottom: histograms of the Δ_{EC} values between CenpC to Mad1-pT716 and CenpC to Mad2 (left), and Mad1(N) to- Mad1-pT716 (right). Mean (dashed line) and SD values are indicated at right. The difference between Δ_{EC} mean values is indicated in black. (F) Kinetochores stained with anti-CenpC, anti-Bub1, and anti-Mad2 antibodies in parental and *bub1 1-23* cells treated with 3.3 mM nocodazole. Scale bars, 500 nm.

⁽G) Histograms of the A_{EC} distances between CenpC and Mad1-pT716, Mad2, and Zwilch in parental and *bub1 1-23* cells treated as in (F). Mean (dashed line) and SD values are indicated at right. The difference between Δ_{EC} mean values is indicated in black.

(legend on next page)

the K-fiber axis. Within the outer plate, the NDC80 complex and the more distal RZZ complex must have a high nematic order, otherwise the ensemble average distances would not be consistent with distances from structural biology. It thus follows that our methods allow structural insights from cryo-EM and X-ray crystallography to be assessed within an *in vivo* context. They also provide a framework for understanding the higher-order ensemble organization of the kinetochore.

We have discovered that there is substantial re-organization of the kinetochore outer plate when microtubules detach (nocodazole). Our analysis shows that this can be explained through a combination of NDC80 jackknifing and loss of nematic order or through a loss of order alone. Two lines of evidence suggest that jackknifing is involved: (1) *in vitro* experiments have directly shown how the NDC80 complex does jackknife in the absence of microtubules around the loop [\(Scarborough et al., 2019\)](#page-16-2), and (2) mutations in the Ndc80 loop that reduce the degree of jackknifing interfere with microtubule-kinetochore attachment ([Zhang](#page-16-6) [et al., 2012\)](#page-16-6). We therefore favor a model in which the loss of attachment triggers NDC80 jackknifing. However, we note that an additional loss of nematic order within the NDC80 complexes is necessary to explain the measured distance changes. This hints at larger-scale reorganization in the outer kinetochore in the absence of microtubule binding. When kinetochores are attached, but no tension is generated, we find that the first 300 aa of Knl1 are unraveled, while NDC80 remains unchanged. What drives cycles of unraveling-raveling in the first 300 aa of Knl1 remains unknown. We also need to consider that taxol and nocodazole do not represent ''physiological'' conditions, and it will be important to develop assays to follow Knl1/Ndc80 re-organization during the prometaphase-to-metaphase transition.

The three kinetochore architectures defined in this work (attached, unattached, and tensionless) can be interpreted in terms of our present understanding of spindle checkpoint and er-

ror-correction mechanisms (see model in [Figure 7F](#page-12-0)). The jackknifed NDC80 state is tightly correlated with the recruitment of Mad2 to kinetochores and activation of the spindle checkpoint, but it is not a downstream consequence, as the state exists when Mps1 is inhibited [\(Figure 7F](#page-12-0), top). The formation of end-on attachment correlates with the NDC80 complexes straightening out and aligning. During this time, the Mps1 kinase is displaced from kinetochores because of the competition with microtubules for binding to the Ndc80 calponin homology domain ([Figure 7](#page-12-0)F, center; [Hiruma et al., 2015; Ji et al., 2015](#page-15-24)). One idea is that the auto-inhibited Ndc80 conformation gates the recruitment of Mad1:Mad2, perhaps by favoring Mps1 binding. This model is different from that presented in budding yeast, which proposes that attachment separates Mps1 from the Knl1 substrate, thus silencing the checkpoint ([Aravamudhan et al., 2015](#page-14-8)). However, at bi-oriented human kinetochores, the Ndc80 head domain (which binds Mps1) and Knl1 MELTs (marked by the average position of Bub1) are only 26.9 ± 1.4 nm apart ([Figure 7](#page-12-0)F, bottom). Nevertheless, conformational changes in Ndc80 appear to be a conserved feature of the mechanisms that monitor microtubule attachment.

Our data also suggest that the loss of tension (taxol) is not sufficient to activate the spindle checkpoint; the tensionless kinetochores do not jackknife NDC80 and have undetectable levels of Mad2 ([Figure 7F](#page-12-0), center). The detected mitotic delays during metaphase are likely due to a sub-population of unattached kinetochores (which do jackknife NDC80), as previously suggested ([Magidson et al., 2016](#page-15-19)), although we cannot yet formally rule out weak checkpoint signals (without detectable Mad2 binding). We also propose that taxol-treated kinetochores reflect a ''transition state'' between the attached (and under tension) and unattached states (see model in [Figure 7](#page-12-0)F for details). While the Aurora B site in the now-unraveled amino terminus of Knl1 is dephosphorylated, fluorescence lifetime imaging microscopy-Förster resonance energy transfer (FLIM/FRET) measurements

Figure 7. Knl1 1–300 Unravels upon the Loss of Kinetochore Tension

(A) Kinetochore pairs stained with anti-Bub1, anti-Rod, and anti-Zwilch antibodies in cells treated with 1 µM taxol for 15 min. Scale bars, 500 nm. (B) Histograms of the A_{EC} distances from CenpC to Bub1, Rod, Zwilch, Knl1-MELT2, and pKnl1(S24) in DMSO and taxol. Mean (dashed line) and SD values are

indicated at right.

(C) Schematic map of Knl1 where the positions of Serine24 (Ser24, orange), MELT repeats (blue), and MIS12-Zwint-binding domain (gray) are shown. Lines indicate the PP1-microtubule binding site (green) and the unstructured region (red). Arrows indicate the binding sites of anti-Knl1-pS24 and anti-Knl1(MELT2) antibodies used in this study.

(D) Top: kinetochores stained with anti-CenpC and anti-Knl1-pS24 antibodies in cells treated with 3.3 uM nocodazole for 2 h, 1 uM taxol for 15 min, or DMSO. Scale bar, 500 nm. Insets show enlargements for the indicated kinetochores. Scale bar, 250 nm. Bottom: histograms of the Δ_{FC} between CenpC and Knl1-pS24 in cells treated as above. Mean (dashed line) and SD values are indicated below. Cumulative frequency plots display the Knl1-pS24 intensity in DMSO-, nocodazole (+noc)-, and taxol-treated cells. The Knl1-pS24 signal is normalized to the CenpC signal. Signals are background subtracted.

(E) Top: kinetochores stained with anti-CenpC and anti-Knl1(MELT2) antibodies and treated as in (D). Scale bars, 500 nm. Bottom: histograms of the Δ_{EC} distances between CenpC and Knl1 in DMSO-, nocodazole (+noc)-, and taxol-treated cells. Mean (dashed line) and SD values are indicated at right.

(F) Schematics representing the ensemble average arrangement of MIS12 complex (dark blue), NDC80 complex (light blue), Bub1 (orange), RZZ complex (green), Mad1:Mad2 (yellow), Knl1 (black), and SKA (purple) in RPE1 cells treated with nocodazole (top), taxol (center), and DMSO (bottom). A single microtubule protofilament is shown in gray and dotted lines represent the position of the indicated complexes in control cells. The arrows indicate the change in position between different conditions. The positions of proteins marked with an asterisk are inferred from known biochemical data. These kinetochore organizational states can be integrated with known checkpoint and error-correction mechanisms as follows: at unattached kinetochores (top), NDC80 is disordered and in an auto-inhibited state, while the first 300 aa of Knl1 are in an extended conformation. Aurora B kinase activity dominates, kinetochore substrates (i.e., Ndc80 and Knl1) are phosphorylated, and Ndc80 is in a low-affinity microtubule-binding state. We note that Mad1 can bridge from the outer kinetochore to the corona, with interactions at either end necessary for stable binding and spindle checkpoint activation. When end-on attachment forms (center), but no tension is generated (e.g., monotelic attachments in which one sister is attached and the other is unattached), the checkpoint is silenced on the attached sister concomitantly with the straightening of Ndc80, which binds to the microtubule lattice. As force from the microtubule depolymerization generates tension (bottom), SKA complexes are recruited and the Knl1 amino terminus ravels. PP1 now fully binds, leading to kinetochore dephosphorylation (counteracting Aurora B) and increased microtubule binding affinity. This model can also explain error correction following the loss of tension at a bi-oriented kinetochore, which would switch the system into the transition (center panel) state (see [Discussion](#page-11-0) for details).

In conclusion, our data suggest that kinetochores are able to distinguish between changes in tension and microtubule occupancy using in-built occupancy (Ndc80) and tension (Knl1) sensors.

STAR+METHODS

Detailed methods are provided in the online version of this paper and include the following:

- **[KEY RESOURCES TABLE](#page-17-0)**
- \bullet **[LEAD CONTACT AND MATERIALS AVAILABILITY](#page-19-1)**
- **.** [EXPERIMENTAL MODEL AND SUBJECT DETAILS](#page-19-2)
- **O** [METHOD DETAILS](#page-19-0)
	- \circ Construction and verification of cell lines
	- \circ Drug treatments and siRNA transfection
	- \circ Immunofluorescence microscopy
	- \circ Delta distance and intensity measurements
	- \circ Assay for spindle assembly checkpoint activity
	- \circ Long term live-cell imaging
	- \circ Photoactivation experiments
- **. [QUANTIFICATION AND STATISTICAL ANALYSIS](#page-21-0)**
- **. [DATA AND CODE AVAILABILITY](#page-21-1)**

SUPPLEMENTAL INFORMATION

Supplemental Information can be found online at [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.celrep.2020.107535) [celrep.2020.107535.](https://doi.org/10.1016/j.celrep.2020.107535)

ACKNOWLEDGMENTS

We thank O. Sen for help validating the cell lines; A. Saurin, A. Musacchio, and I. Cheeseman for the antibodies; J. Pines for the cell lines; G. Chan for the EGFP-Zw10 construct; and V. Silió for construction of the stable EGFP-Zw10 RPE1 line. We also thank the CAMDU (Computing and Advanced Microscopy Unit) for support and J. Harrison for proofreading the manuscript. This work was supported by the Leverhulme Trust (RPG-2017-349 to A.D.M. and N.J.B.). Work in the A.D.M. lab was also supported by a Wellcome Trust Senior Investigator Award (106151/Z/14/Z) and a Royal Society Wolfson Research Merit Award (WM150020). T.E.G. and A.I.T. are funded by the Medical Research Council Doctoral Training Partnership grant MR/J003964/1.

AUTHOR CONTRIBUTIONS

A.D.M. and N.J.B. were responsible for the project conception, planning, and supervision. E.R. carried out the experiments, except for mapping the SKA position (T.E.G.) and the photoactivation experiments (A.I.T.). E.R. carried out the data analysis, with help from T.E.G., and M.E. generated the Ndc80-EGFP knockin cell lines. A.D.M., N.J.B., E.R., and T.E.G. interpreted the data. C.A.S. developed the kinetochore analysis code. N.J.B. developed the

Cell Reports Article

Euclidean distance correction algorithm. P.A.E. built the visualizations of the kinetochore organization. A.D.M. and N.J.B. prepared the manuscript, with input from E.R. and T.E.G.

DECLARATION OF INTERESTS

The authors declare no competing interests.

Received: August 6, 2019 Revised: February 10, 2020 Accepted: March 27, 2020 Published: April 28, 2020

SUPPORTING CITATIONS

The following references appear in the Supplemental Information: [Alushin et al.](#page-14-10) [\(2010\); Booth et al. \(2011\); Churchman et al. \(2006\); Ciferri et al. \(2005\); Jogle](#page-14-10)[kar et al. \(2006\); Ledbetter and Porter \(1963\); Maiolica et al. \(2007\); Musacchio](#page-14-10) [and Desai \(2017\); Petrovic et al. \(2014\); Craiu and Rosenthal, 2014; Nixon et al.,](#page-14-10) [2015](#page-14-10).

REFERENCES

[Allan, L.A., Camacho Reis, M., Ciossani, G., Huis in 't Veld, P.J., Wohlgemuth,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref1) [S., Kops, G.J., Musacchio, A., and Saurin, A.T. \(2020\). Cyclin B1 scaffolds](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref1) [MAD1 at the kinetochore corona to activate the mitotic checkpoint. EMBO](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref1) [J., e103180](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref1).

[Alushin, G.M., Ramey, V.H., Pasqualato, S., Ball, D.A., Grigorieff, N., Musac](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref2)[chio, A., and Nogales, E. \(2010\). The Ndc80 kinetochore complex forms olig](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref2)[omeric arrays along microtubules. Nature](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref2) *467*, 805–810.

[Amaro, A.C., Samora, C.P., Holtackers, R., Wang, E., Kingston, I.J., Alonso,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref3) [M., Lampson, M., McAinsh, A.D., and Meraldi, P. \(2010\). Molecular control](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref3) [of kinetochore-microtubule dynamics and chromosome oscillations. Nat.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref3) Cell Biol. *12*[, 319–329.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref3)

[Aravamudhan, P., Goldfarb, A.A., and Joglekar, A.P. \(2015\). The kinetochore](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref4) [encodes a mechanical switch to disrupt spindle assembly checkpoint signal](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref4)[ling. Nat. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref4) *17*, 868–879.

[Auckland, P., and McAinsh, A.D. \(2015\). Building an integrated model of chro](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref5)[mosome congression. J. Cell Sci.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref5) *128*, 3363–3374.

[Bajaj, R., Bollen, M., Peti, W., and Page, R. \(2018\). KNL1 Binding to PP1 and](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref6) [Microtubules Is Mutually Exclusive. Structure](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref6) *26*, 1327–1336.e4.

[Booth, D.G., Hood, F.E., Prior, I.A., and Royle, S.J. \(2011\). A TACC3/ch-TOG/](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref7) [clathrin complex stabilises kinetochore fibres by inter-microtubule bridging.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref7) EMBO J. *30*[, 906–919](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref7).

[Brinkley, B.R., Ouspenski, I., and Zinkowski, R.P. \(1992\). Structure and molec](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref8)[ular organization of the centromere-kinetochore complex. Trends Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref8) *2*, [15–21.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref8)

[Burroughs, N.J., Harry, E.F., and McAinsh, A.D. \(2015\). Super-resolution kinet](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref9)[ochore tracking reveals the mechanisms of human sister kinetochore direc](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref9)[tional switching. eLife](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref9) *4*, e09500.

[Cheeseman, I.M., Chappie, J.S., Wilson-Kubalek, E.M., and Desai, A. \(2006\).](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref10) [The conserved KMN network constitutes the core microtubule-binding site](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref10) [of the kinetochore. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref10) *127*, 983–997.

[Churchman, L.S., Okten, Z., Rock, R.S., Dawson, J.F., and Spudich, J.A.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref11) [\(2005\). Single molecule high-resolution colocalization of Cy3 and Cy5 attached](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref11) [to macromolecules measures intramolecular distances through time. Proc.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref11) [Natl. Acad. Sci. USA](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref11) *102*, 1419–1423.

[Churchman, L.S., Flyvbjerg, H., and Spudich, J.A. \(2006\). A non-Gaussian dis](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref12)[tribution quantifies distances measured with fluorescence localization tech](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref12)[niques. Biophys. J.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref12) *90*, 668–671.

[Ciferri, C., De Luca, J., Monzani, S., Ferrari, K.J., Ristic, D., Wyman, C., Stark,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref13) [H., Kilmartin, J., Salmon, E.D., and Musacchio, A. \(2005\). Architecture of the](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref13) [human ndc80-hec1 complex, a critical constituent of the outer kinetochore.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref13) J. Biol. Chem. *280*[, 29088–29095](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref13).

[Collin, P., Nashchekina, O., Walker, R., and Pines, J. \(2013\). The spindle as](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref15)[sembly checkpoint works like a rheostat rather than a toggle switch. Nat.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref15) Cell Biol. *15*[, 1378–1385.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref15)

[Craiu, R.V., and Rosenthal, J.S. \(2014\). Bayesian Computation via Markov](http://refhub.elsevier.com/S2211-1247(20)30435-6/optAINSZTuwUU) [Chain Monte Carlo. Annual Review of Statistics and Its Application](http://refhub.elsevier.com/S2211-1247(20)30435-6/optAINSZTuwUU) *1*, 179–201.

[Currie, C.E., Mora-Santos, M., Smith, C.A., McAinsh, A.D., and Millar, J.B.A.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref16) [\(2018\). Bub1 is not essential for the checkpoint response to unattached kinet](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref16)[ochores in diploid human cells. Curr. Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref16) *28*, R929–R930.

[de Gennes, P.G., and Prost, J. \(1993\). The Physics of Liquid Crystals, Second](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref17) [Edition \(Clarendon Press\)](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref17).

[DeLuca, J.G., Gall, W.E., Ciferri, C., Cimini, D., Musacchio, A., and Salmon,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref18) [E.D. \(2006\). Kinetochore microtubule dynamics and attachment stability are](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref18) [regulated by Hec1. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref18) *127*, 969–982.

Doostmohammadi, A., Ignés-Mullol, J., Yeomans, J.M., and Sagués, F. (2018). [Active nematics. Nat. Commun.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref19) *9*, 3246.

[Dudka, D., Noatynska, A., Smith, C.A., Liaudet, N., McAinsh, A.D., and Mer](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref20)[aldi, P. \(2018\). Complete microtubule-kinetochore occupancy favours the](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref20) [segregation of merotelic attachments. Nat. Commun.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref20) *9*, 2042.

[Etemad, B., Kuijt, T.E., and Kops, G.J. \(2015\). Kinetochore-microtubule](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref21) [attachment is sufficient to satisfy the human spindle assembly checkpoint.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref21) [Nat. Commun.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref21) *6*, 8987.

[Etemad, B., Vertesy, A., Kuijt, T.E.F., Sacristan, C., van Oudenaarden, A., and](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref22) [Kops, G. \(2019\). Spindle checkpoint silencing at kinetochores with submaxi](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref22)[mal microtubule occupancy. J. Cell Sci.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref22) *132*, jcs231589.

[Famulski, J.K., and Chan, G.K. \(2007\). Aurora B kinase-dependent recruitment](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref23) [of hZW10 and hROD to tensionless kinetochores. Curr. Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref23) *17*, 2143–2149.

[Gascoigne, K.E., Takeuchi, K., Suzuki, A., Hori, T., Fukagawa, T., and Cheese](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref24)[man, I.M. \(2011\). Induced ectopic kinetochore assembly bypasses the require](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref24)[ment for CENP-A nucleosomes. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref24) *145*, 410–422.

[Hamilton, G., Dimitrova, Y., and Davis, T.N. \(2019\). Seeing is believing: our](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref25) [evolving view of kinetochore structure, composition, and assembly. Curr.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref25) [Opin. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref25) *60*, 44–52.

[Helgeson, L.A., Zelter, A., Riffle, M., MacCoss, M.J., Asbury, C.L., and Davis,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref26) [T.N. \(2018\). Human Ska complex and Ndc80 complex interact to form a load](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref26)[bearing assembly that strengthens kinetochore-microtubule attachments.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref26) [Proc. Natl. Acad. Sci. USA](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref26) *115*, 2740–2745.

[Hiruma, Y., Sacristan, C., Pachis, S.T., Adamopoulos, A., Kuijt, T., Ubbink, M.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref27) [von Castelmur, E., Perrakis, A., and Kops, G.J. \(2015\). Competition between](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref27) [MPS1 and microtubules at kinetochores regulates spindle checkpoint](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref27) [signaling. Science](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref27) *348*, 1264–1267.

[Huis In 't Veld, P.J., Jeganathan, S., Petrovic, A., Singh, P., John, J., Krenn, V.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref28) [Weissmann, F., Bange, T., and Musacchio, A. \(2016\). Molecular basis of outer](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref28) [kinetochore assembly on CENP-T. eLife](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref28) *5*, e21007.

[Huis In 't Veld, P.J., Volkov, V.A., Stender, I.D., Musacchio, A., and Dogterom,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref29) [M. \(2019\). Molecular determinants of the Ska-Ndc80 interaction and their influ](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref29)[ence on microtubule tracking and force-coupling. eLife](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref29) *8*, e49539.

[Ji, Z., Gao, H., and Yu, H. \(2015\). CELL DIVISION CYCLE. Kinetochore attach](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref30)[ment sensed by competitive Mps1 and microtubule binding to Ndc80C. Sci](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref30)ence *348*[, 1260–1264](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref30).

[Joglekar, A.P., Bouck, D.C., Molk, J.N., Bloom, K.S., and Salmon, E.D. \(2006\).](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref31) [Molecular architecture of a kinetochore-microtubule attachment site. Nat. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref31) Biol. *8*[, 581–585](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref31).

[Johnston, K., Joglekar, A., Hori, T., Suzuki, A., Fukagawa, T., and Salmon, E.D.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref32) [\(2010\). Vertebrate kinetochore protein architecture: protein copy number.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref32) [J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref32) *189*, 937–943.

[Kim, S., Sun, H., Tomchick, D.R., Yu, H., and Luo, X. \(2012\). Structure of hu](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref33)[man Mad1 C-terminal domain reveals its involvement in kinetochore targeting.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref33) [Proc. Natl. Acad. Sci. USA](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref33) *109*, 6549–6554.

[Klare, K., Weir, J.R., Basilico, F., Zimniak, T., Massimiliano, L., Ludwigs, N.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref34) [Herzog, F., and Musacchio, A. \(2015\). CENP-C is a blueprint for constitutive](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref34) [centromere-associated network assembly within human kinetochores.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref34) [J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref34) *210*, 11–22.

[Kops, G.J., Kim, Y., Weaver, B.A., Mao, Y., McLeod, I., Yates, J.R., 3rd, Ta](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref35)[gaya, M., and Cleveland, D.W. \(2005\). ZW10 links mitotic checkpoint signaling](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref35) [to the structural kinetochore. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref35) *169*, 49–60.

[Kuhn, J., and Dumont, S. \(2017\). Spindle assembly checkpoint satisfaction oc](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref36)[curs via end-on but not lateral attachments under tension. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref36) *216*, [1533–1542.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref36)

[Lampson, M.A., and Cheeseman, I.M. \(2011\). Sensing centromere tension:](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref37) [Aurora B and the regulation of kinetochore function. Trends Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref37) *21*, [133–140.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref37)

[Ledbetter, M.C., and Porter, K.R. \(1963\). A ''Microtubule'' in Plant Cell Fine](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref38) [Structure. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref38) *19*, 239–250.

[London, N., Ceto, S., Ranish, J.A., and Biggins, S. \(2012\). Phosphoregulation](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref39) [of Spc105 by Mps1 and PP1 regulates Bub1 localization to kinetochores. Curr.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref39) Biol. *22*[, 900–906](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref39).

[Long, A.F., Kuhn, J., and Dumont, S. \(2019\). The mammalian kinetochore](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref40)[microtubule interface: robust mechanics and computation with many microtu](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref40)[bules. Curr. Opin. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref40) *60*, 60–67.

[Magidson, V., He, J., Ault, J.G., O'Connell, C.B., Yang, N., Tikhonenko, I.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref41) [McEwen, B.F., Sui, H., and Khodjakov, A. \(2016\). Unattached kinetochores](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref41) [rather than intrakinetochore tension arrest mitosis in taxol-treated cells.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref41) [J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref41) *212*, 307–319.

[Maiolica, A., Cittaro, D., Borsotti, D., Sennels, L., Ciferri, C., Tarricone, C., Mu](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref42)[sacchio, A., and Rappsilber, J. \(2007\). Structural analysis of multiprotein com](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref42)[plexes by cross-linking, mass spectrometry, and database searching. Mol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref42) [Cell. Proteomics](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref42) *6*, 2200–2211.

[Maresca, T.J., and Salmon, E.D. \(2009\). Intrakinetochore stretch is associated](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref43) [with changes in kinetochore phosphorylation and spindle assembly check](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref43)[point activity. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref43) *184*, 373–381.

[Maresca, T.J., and Salmon, E.D. \(2010\). Welcome to a new kind of tension:](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref44) [translating kinetochore mechanics into a wait-anaphase signal. J. Cell Sci.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref44) *123*[, 825–835](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref44).

[McAinsh, A.D., Meraldi, P., Draviam, V.M., Toso, A., and Sorger, P.K. \(2006\).](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref45) [The human kinetochore proteins Nnf1R and Mcm21R are required for accurate](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref45) [chromosome segregation. EMBO J.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref45) *25*, 4033–4049.

[Mosalaganti, S., Keller, J., Altenfeld, A., Winzker, M., Rombaut, P., Saur, M.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref46) Petrovic, A., Wehenkel, A., Wohlgemuth, S., Müller, F., et al. (2017). Structure [of the RZZ complex and molecular basis of its interaction with Spindly. J. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref46) Biol. *216*[, 961–981](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref46).

[Musacchio, A., and Desai, A. \(2017\). A Molecular View of Kinetochore Assem](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref47)[bly and Function. Biology \(Basel\)](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref47) *6*, E5.

[Nicklas, R.B., and Koch, C.A. \(1969\). Chromosome micromanipulation. 3.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref48) [Spindle fiber tension and the reorientation of mal-oriented chromosomes.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref48) [J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref48) *43*, 40–50.

[Nicklas, R.B., Ward, S.C., and Gorbsky, G.J. \(1995\). Kinetochore chemistry is](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref49) [sensitive to tension and may link mitotic forces to a cell cycle checkpoint.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref49) [J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref49) *130*, 929–939.

Nixon, F.M., Gutiérrez-Caballero, C., Hood, F.E., Booth, D.G., Prior, I.A., and [Royle, S.J. \(2015\). The mesh is a network of microtubule connectors that sta](http://refhub.elsevier.com/S2211-1247(20)30435-6/optgiw7vWvwKJ)[bilizes individual kinetochore fibers of the mitotic spindle. eLife](http://refhub.elsevier.com/S2211-1247(20)30435-6/optgiw7vWvwKJ) *4*, e07635.

Olziersky, A.M., Smith, C.A., Burroughs, N., McAinsh, A.D., and Meraldi, P. (2018). [Mitotic live-cell imaging at different timescales. Methods Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref50) *145*, 1–27.

[Pesenti,M.E.,Weir, J.R., and Musacchio, A. \(2016\). Progress in the structural and](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref51) [functional characterization of kinetochores. Curr. Opin. Struct. Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref51) *37*, 152–163.

[Petrovic, A., Pasqualato, S., Dube, P., Krenn, V., Santaguida, S., Cittaro, D.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref52) [Monzani, S., Massimiliano, L., Keller, J., Tarricone, A., et al. \(2010\). The](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref52) [MIS12 complex is a protein interaction hub for outer kinetochore assembly.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref52) [J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref52) *190*, 835–852.

[Petrovic, A., Mosalaganti, S., Keller, J., Mattiuzzo, M., Overlack, K., Krenn, V.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref53) [De Antoni, A., Wohlgemuth, S., Cecatiello, V., Pasqualato, S., et al. \(2014\).](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref53) [Modular assembly of RWD domains on the Mis12 complex underlies outer](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref53) [kinetochore organization. Mol. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref53) *53*, 591–605.

[Rago, F., and Cheeseman, I.M. \(2013\). Review series: the functions and con](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref54)[sequences of force at kinetochores. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref54) *200*, 557–565.

[Ran, F.A., Hsu, P.D., Wright, J., Agarwala, V., Scott, D.A., and Zhang, F. \(2013\).](http://refhub.elsevier.com/S2211-1247(20)30435-6/optr5WhQp2V9l) [Genome engineering using the CRISPR-Cas9 system. Nat. Protoc.](http://refhub.elsevier.com/S2211-1247(20)30435-6/optr5WhQp2V9l) *8*, 2281– [2308](http://refhub.elsevier.com/S2211-1247(20)30435-6/optr5WhQp2V9l).

[Scarborough, E.A., Davis, T.N., and Asbury, C.L. \(2019\). Tight bending of the](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref55) [Ndc80 complex provides intrinsic regulation of its binding to microtubules. eL](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref55)ife *8*[, e44489.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref55)

[Screpanti, E., De Antoni, A., Alushin, G.M., Petrovic, A., Melis, T., Nogales, E.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref56) [and Musacchio, A. \(2011\). Direct binding of Cenp-C to the Mis12 complex joins](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref56) [the inner and outer kinetochore. Curr. Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref56) *21*, 391–398.

[Shepperd, L.A., Meadows, J.C., Sochaj, A.M., Lancaster, T.C., Zou, J., But](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref57)[trick, G.J., Rappsilber, J., Hardwick, K.G., and Millar, J.B. \(2012\). Phosphode](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref57)[pendent recruitment of Bub1 and Bub3 to Spc7/KNL1 by Mph1 kinase main](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref57)[tains the spindle checkpoint. Curr. Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref57) *22*, 891–899.

Silió[, V., McAinsh, A.D., and Millar, J.B. \(2015\). KNL1-Bubs and RZZ Provide](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref58) [Two Separable Pathways for Checkpoint Activation at Human Kinetochores.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref58) Dev. Cell *35*[, 600–613](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref58).

[Sironi, L., Mapelli, M., Knapp, S., De Antoni, A., Jeang, K.T., and Musacchio, A.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref59) [\(2002\). Crystal structure of the tetrameric Mad1-Mad2 core complex: implica](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref59)[tions of a 'safety belt' binding mechanism for the spindle checkpoint. EMBO J.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref59) *21*[, 2496–2506.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref59)

[Smith, C.A., McAinsh, A.D., and Burroughs, N.J. \(2016\). Human kinetochores](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref60) [are swivel joints that mediate microtubule attachments. eLife](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref60) *5*, e16159.

[Suzuki, A., Hori, T., Nishino, T., Usukura, J., Miyagi, A., Morikawa, K., and Fuka](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref61)[gawa, T. \(2011\). Spindle microtubules generate tension-dependent changes in](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref61) [the distribution of inner kinetochore proteins. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref61) *193*, 125–140.

[Suzuki, A., Badger, B.L., Wan, X., DeLuca, J.G., and Salmon, E.D. \(2014\). The](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref62) [architecture of CCAN proteins creates a structural integrity to resist spindle](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref62) [forces and achieve proper Intrakinetochore stretch. Dev. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref62) *30*, 717–730.

[Suzuki, A., Long, S.K., and Salmon, E.D. \(2018\). An optimized method for 3D](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref63) [fluorescence co-localization applied to human kinetochore protein architec](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref63)[ture. eLife](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref63) *7*, e32418.

[Tanaka, T.U., Stark, M.J., and Tanaka, K. \(2005\). Kinetochore capture and bi](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref64)[orientation on the mitotic spindle. Nat. Rev. Mol. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref64) *6*, 929–942.

[Tauchman, E.C., Boehm, F.J., and DeLuca, J.G. \(2015\). Stable kinetochore](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref65)[microtubule attachment is sufficient to silence the spindle assembly check](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref65)[point in human cells. Nat. Commun.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref65) *6*, 10036.

[Toso, A., Winter, J.R., Garrod, A.J., Amaro, A.C., Meraldi, P., and McAinsh,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref66) [A.D. \(2009\). Kinetochore-generated pushing forces separate centrosomes](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref66) [during bipolar spindle assembly. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref66) *184*, 365–372.

[Uchida, K.S., Takagaki, K., Kumada, K., Hirayama, Y., Noda, T., and Hirota, T.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref67) [\(2009\). Kinetochore stretching inactivates the spindle assembly checkpoint.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref67) [J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref67) *184*, 383–390.

[Wan, X., O'Quinn, R.P., Pierce, H.L., Joglekar, A.P., Gall, W.E., DeLuca, J.G.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref68) [Carroll, C.W., Liu, S.T., Yen, T.J., McEwen, B.F., et al. \(2009\). Protein architec](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref68)[ture of the human kinetochore microtubule attachment site. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref68) *137*, 672–684.

[Wan, X., Cimini, D., Cameron, L.A., and Salmon, E.D. \(2012\). The coupling be](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref69)[tween sister kinetochore directional instability and oscillations in centromere](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref69) [stretch in metaphase PtK1 cells. Mol. Biol. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref69) *23*, 1035–1046.

[Wang, H.W., Long, S., Ciferri, C., Westermann, S., Drubin, D., Barnes, G., and](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref70) [Nogales, E. \(2008\). Architecture and flexibility of the yeast Ndc80 kinetochore](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref70) [complex. J. Mol. Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref70) *383*, 894–903.

[Wei, R.R., Sorger, P.K., and Harrison, S.C. \(2005\). Molecular organization of](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref71) [the Ndc80 complex, an essential kinetochore component. Proc. Natl. Acad.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref71) Sci. USA *102*[, 5363–5367](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref71).

[Welburn, J.P., and Cheeseman, I.M. \(2008\). Toward a molecular structure of](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref72) [the eukaryotic kinetochore. Dev. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref72) *15*, 645–655.

[Welburn, J.P., Vleugel, M., Liu, D., Yates, J.R., 3rd, Lampson, M.A., Fukagawa,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref73) [T., and Cheeseman, I.M. \(2010\). Aurora B phosphorylates spatially distinct tar](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref73)[gets to differentially regulate the kinetochore-microtubule interface. Mol. Cell](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref73) *38*[, 383–392](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref73).

[Wilson-Kubalek, E.M., Cheeseman, I.M., Yoshioka, C., Desai, A., and Milligan,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref74) [R.A. \(2008\). Orientation and structure of the Ndc80 complex on the microtu](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref74)[bule lattice. J. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref74) *182*, 1055–1061.

[Yamagishi, Y., Yang, C.H., Tanno, Y., and Watanabe, Y. \(2012\). MPS1/Mph1](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref75) [phosphorylates the kinetochore protein KNL1/Spc7 to recruit SAC compo](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref75)[nents. Nat. Cell Biol.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref75) *14*, 746–752.

[Yoo, T.Y., Choi, J.M., Conway, W., Yu, C.H., Pappu, R.V., and Needleman,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref76) [D.J. \(2018\). Measuring NDC80 binding reveals the molecular basis of ten](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref76)[sion-dependent kinetochore-microtubule attachments. eLife](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref76) *7*, e36392.

[Zhang, G., Kelstrup, C.D., Hu, X.W., Kaas Hansen, M.J., Singleton, M.R., Ol](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref77)[sen, J.V., and Nilsson, J. \(2012\). The Ndc80 internal loop is required for recruit](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref77)[ment of the Ska complex to establish end-on microtubule attachment to kinet](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref77)[ochores. J. Cell Sci.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref77) *125*, 3243–3253.

Zhang, G., Kruse, T., López-Mé[ndez, B., Sylvestersen, K.B., Garvanska, D.H.,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref78) [Schopper, S., Nielsen, M.L., and Nilsson, J. \(2017\). Bub1 positions Mad1 close](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref78) [to KNL1 MELT repeats to promote checkpoint signalling. Nat. Commun.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref78) *8*, 15822.

Zhang, G., Kruse, T., Guasch Boldú[, C., Garvanska, D.H., Coscia, F., Mann,](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref79) [M., Barisic, M., and Nilsson, J. \(2019\). Efficient mitotic checkpoint signaling](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref79) [depends on integrated activities of Bub1 and the RZZ complex. EMBO J.](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref79) *38*[, e100977](http://refhub.elsevier.com/S2211-1247(20)30435-6/sref79).

KEY RESOURCES TABLE

(*Continued on next page*)

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LEAD CONTACT AND MATERIALS AVAILABILITY

Reagents generated in this study will be made available on request to the Lead Contact, Andrew McAinsh ([A.D.McAinsh@warwick.](mailto:A.D.McAinsh@warwick.ac.uk) [ac.uk\)](mailto:A.D.McAinsh@warwick.ac.uk), but we may require a payment and/or a completed Materials Transfer Agreement if there is potential for commercial application.

EXPERIMENTAL MODEL AND SUBJECT DETAILS

Immortalized (hTERT) diploid human retinal pigment epithelial (RPE1) cells, RPE1 *bub1 1-23* (MC170; [\(Currie et al., 2018\)](#page-15-22)), RPE1 Ndc80-EGFP (MC191), RPE1 Venus-Mad2 (Mad2L1 Venus/+; kind gift from Jonathan Pines), RPE1 HaloTag-CenpA (MC148), RPE1 eGFP-Zw10 (MC156) and RPE1 expressing photoactivatable PA-EGFP-alpha-tubulin (MC021, [Toso et al., 2009\)](#page-16-8) were grown in DMEM/F-12 medium containing 10% fetal bovine serum (FBS), 2 mM L-glutamine, 100 U/ml penicillin and 100 µg/ml streptomycin. 200 mg/ml and 300 mg/ml Geneticin (G418) were added to the media to maintain MC021 and MC148 cells, respectively. All cell cultures were maintained at 37 \degree C with 5% CO₂ in a humidified incubator.

METHOD DETAILS

Construction and verification of cell lines

The RPE1 HaloTag-CenpA (MC148) cell line was generated by transfecting RPE1 cell with the HaloTag-CenpA (pMC442) plasmid. After 24hr cells were plated in selective media containing 300 µg/ml Geneticin (G418). Subsequently, positive clones were visually selected after addition of 2 $µM$ TMR. To generate the RPE1 eGFP-Zw10 (MC156) cell line, RPE1 cells were transfected with EGFP-Zw10 plasmid (pMC453). After 24 hr, EGFP-expressing cells were isolated by FACS sorting and single clones were selected by visual inspection. For CRISPR engineered RPE1 cell lines small guide RNAs (sgRNAs) (5′-caccgATGCATGTCAGAAGATCTCT-3′ and 5'-aaacAGAGATCTTCTGACATGCATc-3') targeting exon 17 of the NDC80 gene were designed using [http://zlab.bio/](http://zlab.bio/guide-design-resources) [guide-design-resources](http://zlab.bio/guide-design-resources) to insert 3xFlagtag-EGFP in frame just prior to the stop codon. sgRNAs were annealed and ligated into pX330 which enables their expression in mammalian cells along with a humanized S. pyogenes Cas9 ([Ran et al., 2013\)](#page-16-9). A homology Directed Repair (HDR) construct was designed with 800bp homology upstream of the Stop codon and 800 bp downstream of the stop codon. 1 µg of sgRNA construct and 1.5 µg of linearized HDR plasmid were transfected into RPE1 cells using Fugene 6. Positive cells were FACS sorted to isolate the Ndc80-EGFP expressing cells and single clones were identified by visual inspection with confocal microscope, with a further round of clonal selection used to eliminate heterogeneity in the population. PCR analysis of clone MC191 confirmed the presence of a wild-type and EGFP-containing allele (primers: Fwd_Ndc80EGFP, 5′-TAAACTGCAGCCATATG TAGTAAC-3'; Rev_Ndc80EGFP, 5'-TTGAAATTAGTAAGAAATGAGAGA-3'). Individual alleles were then analyzed by cloning PCR products and sequencing the products (primers: EGFPNtRev 5'-CCGGACACGCTGAACTTG-3' for the EGFP containing allele band and Rev_Ndc80-EGFP 5'-TTGAAATTAGTAAGAAATGAGAGA-3' for the wild-type allele band). This confirmed that the EGFP was in-frame with the 3' end of NDC80, although a single amino acid change (Threonine 635 to Alanine, T635A) was identified in the unstructured tail distal to the coiled coils that are required for NDC80 complex tetramerisation. We also note that this variant is found in all primates, except *H. sapiens* and H. Neanderthalensis, and that no difference in mitotic timing or multiple delta mea-surements ([Table S1\)](#page-14-2) were detected when compared to parental RPE1 cells ([Figure S2](#page-14-2)). All cell lines were verified by comparing their mitotic timing with parental controls using long term live cell imaging (see below).

Drug treatments and siRNA transfection

For drug treatments, cells were plated on glass coverslips (0.16-0.19 mm) 24 or 48 hr before treatment with 3.3 μ M nocodazole (diluted in DMSO) for 2 hr, 1 μ M taxol (diluted in DMSO) for 15 min or with 0.1% DMSO for 2 hr as a control. In our experimental set-up, we found that treatment with 3.3μ M nocodazole for 15 min tended to leave microtubules stubs in some kinetochores. Thus, we used a 2 hr nocodazole treatment to ensure depolymerization of all microtubules. We note that a 45 min treatment did also eliminated microtubules and produced similar changes in kinetochore organization. Inhibition of Mps1 was performed using 1 μ M reversine in the presence of 3.3 μ M nocodazole and 10 μ M MG132 for 1 hr. As controls, cells were treated with either DMSO and 10 μ M MG132 or 3.3 μ M nocodazole and 10 μ M MG132 for 1hr. To deplete CenpT and CenpC, siRNA oligos targeting their mRNA coding sequences were transfected into RPE1 Ndc80-EGFP (MC191) cells and incubated for 48 hr. For CenpT we used 100 nM of 4 pooled siRNA olgos (25 nM each), whereas for CenpC we transfected 60 nM of a single siRNA oligo. As control, we used 100 nM of the siRNA AllStar oligo. Transfection was performed using oligofectamine following manufacturer's instructions. All depletions were verified by immunofluorescence microscopy (see below).

Immunofluorescence microscopy

Cells were then fixed in 10 mM EGTA, 1 mM MgCl2, 20 mM PIPES pH 6.8, 0.2% Triton X-100, and 4% formaldehyde for 10 min, washed 3 times in PBS before incubation in PBS supplemented with 3% BSA for 30 min to block non-specific antibody binding. Next, cells were incubated with primary antibodies for 1 hr, washed 3 times in PBS and then incubated for 30 min with secondary antibodies and DAPI (1:1000 dilution); all antibodies were diluted in PBS + 3% BSA. Cells were then washed in PBS and mounted

in Vectashield. For experiments that include Ska staining (i.e., CenpC/Ndc80(C)/Ska3 staining), cells were pre-extracted prior to fixation for 1 min with 10 mM EGTA, 1 mM MgCl2, 20 mM PIPES pH 6.8, 0.2% Triton X-100. Image stacks were acquired using a confocal spinning-disk microscope (VOX UltraView; PerkinElmer, UK) equipped with a 100X / 1.4 NA oil-immersion objective and a Hamamatsu ORCA-R2 camera, controlled by Volocity 6.0 (PerkinElmer) running on a Windows 7 64-bit (Microsoft, Redmond, WA) PC (IBM, New Castle, NY). Image stacks were acquired over 61 z-slices separated by 0.2 μ m (for the samples) or over 121 z-slices separated by 0.1μ m (for the chromatic shift slide, see below) using the 488, 561, 640 and 405 nm wavelength lasers. Acquisition settings were set in order that the kinetochore signals were typically larger than 50 units above background.

Delta distance and intensity measurements

Spinning disc images were exported from Volocity 6.0 in OME.TIFF format (The Open Microscopy Environment, UK) and deconvolved using Huygens 4.1, using point spread functions (PSFs) calculated from 100 nm TetraSpeck fluorescent microspheres using the Huygens 4.1 PSF distiller. Where required, images in the 640 nm wavelength were deconvolved within Huygens 4.1 using a theoretical PSF. Deconvolved images were exported from Huygens 4.1 in r3d format and read into MATLAB using the loci-tools java library (The Open Microscopy Environment). Kinetochores spots were first detected using the 561 or 640 nm channel and then (where appropriate) signals from secondary and tertiary markers were identified ([Smith et al., 2016\)](#page-16-0). Initial alignment of all three channels was carried out using images taken from a reference slide (either RPE1 HaloTag-CenpA labeled with Oregon Green, TMR or JF549 and JF646; or anti-CenpA stained with a mix of alexa488, 568 and 647-labeled secondary antibodies) on the day of experiment acqui-sition ([Dudka et al., 2018; Smith et al., 2016\)](#page-15-4). Final outer kinetochore positions were corrected (for chromatic aberrations) per cell so that cell-average intra-kinetochore distance was equal to zero in each the microscope x-, y- and z-coordinates, as is the average orientation previously demonstrated [\(Dudka et al., 2018; Smith et al., 2016\)](#page-15-4). Kinetochore tracking, sister pairing, 3D delta and intensity measurements were made using KiT (Kinetochore Tracking) v2.1.10. Delta 3D (Δ 3D) distances were corrected using an Euclidean correction algorithm (see [Methods S1\)](#page-14-2) that outputs the Euclidian corrected delta parameter (termed ΔEC). For measurement of Bub1, Mad2, Mad1-pT716, Zwilch and Knl1-pS24 signal, intensities were background subtracted and then normalized using the CenpC signal as a reference (also background subtracted). For measurement of endogenous Ndc80-EGFP and Venus-Mad2, and CenpT and CenpC within the RNAi experiments, the background subtracted and non-normalized signal is reported.

Assay for spindle assembly checkpoint activity

Cells were cultured in four compartment CELLview dish (627975, Greiner Bio-One Ltd.). Time-lapse imaging was performed on an Olympus DeltaVision microscope (Applied Precision, LLC) equipped with a Photometrics CoolSNAP HQ camera (Roper Scientific) and a stage-top incubator (TokaiHit) to maintain cells at 37°C and 5% CO2. Temperature was further stabilized using a microscope enclosure (Weather station; Precision Control) held at 37°C. Image stacks (7 \times 2 μ m optical sections) were acquired using the soft-WoRX 6.0 software every 3 min using a 40x / 1.3 NA oil-immersion objective. To visualize the DNA, 1 hr before imaging cells were incubated with DMEM/F-12 media containing 0.5 µM SiR-DNA (Spirochrome). In each experiment, only fields (1024 x 1024 pixels) containing at least one metaphase cells were imaged using the point visit function in softWoRX 6.0. Imaging started after the addition of DMSO or 1 µM taxol-containing media. Cells were imaged for 15 min to reproduce the same conditions used for the fixed cell experiments. For experiments with RPE1 bub1 1-23 cells imaging was extended to 24 min because the timing to anaphase onset was slightly delayed with respect to the parental cell line. To inactivate the Spindle Assembly Checkpoint, cells were treated with either DMSO or 1 μ M taxol-containing media for 15 min and then 1 μ M reversine-containing media was added for 120 min (total imaging time was 135 min) to inhibit Mps1. As control, cells were treated with 1 μ M taxol and imaged for 135 min. Images were acquired at 32% solid source illumination with Cy5 and neutral density filters, exposure time 0.05 s. Timing of exit from mitosis was scored by eye.

Long term live-cell imaging

Parental RPE1 and RPE1 stably expressing Ndc80-EGFP were cultured in glass bottom FluoroDish (FD35-100, World Precision Instrument, Inc.). Time-lapse imaging was performed on Olympus DeltaVision microscopes (Applied Precision, LLC) equipped either with Photometrics CoolSNAP HQ (Roper Scientific) or Photometrics CoolSNAP HQ2 cameras (Roper Scientific) and temperature held at 37°C as described above. Image stacks ($7 \times 2 \mu$ m optical sections) were acquired using the SoftWoRX 6.0 software every 3 min using a 40x/1.3 NA oil-immersion objective. To visualize the DNA, 1 hr before imaging RPE1 cells were incubated with DMEM/F-12 media containing 0.5 μ M SiR-DNA (Spirochrome). In each experiment, 30 to 40 fields (1024 \times 1024 pixels) were imaged using the point visit function in softWoRX 6.0. Images were acquired for 15 hr at 10% solid source illumination with neutral density and Cy5 filter, exposure time 0.05 s. The timing of nuclear envelope breakdown and anaphase onset were scored by eye.

Photoactivation experiments

RPE1 cells stably expressing photoactivatable-(PA)-GFP-alpha-tubulin ([Toso et al., 2009](#page-16-8)) were cultured in Fluorodishes (FD35-100, World Precision Instrument, Inc.) and DNA was visualized by incubation for 30 min with CO2 independent L15 media (Invitrogen, UK) containing 0.5 µM SiR-DNA (Spirochrome, CH). DMSO or 1µM taxol was added 15 min prior to imaging. Photoactivation was carried out using a confocal spinning disk microscope (Marianas SDC, 3i, UK) equipped with a Vector module for photoactivation, a 100x / 1.46 NA immersion oil objective and a Photometrics 95B Prime sCMOS camera controlled by Slidebook 6.0 (3i, UK). Cells were maintained at 37°C using a stage top incubator (both Okolab, Italy). PA-GFP-tubulin was activated in an ROI (100x5 pixels, parallel to the

metaphase plate) with 4 x 2 ms pulses of a 405 nm laser. Images were then acquired (excitation 488 nm) every 15 s for 2 min (150 ms exposure, 3 planes 1 µm z-step centered on the photoactivated plane). Images of the DNA staining were acquired (excitation 640nm) at frame 1, 5 and 9. Poleward flux was calculated by measuring the displacement of photoactivated marks over the first 5 frames. To determine the turnover of PA-GFP-alpha-Tubulin the background-subtracted pixel intensity of the photo-activated EGFP-alphatubulin over time was measured in ImageJ (averaging the mean intensity of two 7x7 pixels square boxes placed on the photo-activated region). In DMSO, intensity was measured at every time point, whereas, in taxol, intensity was analyzed at time points 0 min, 1 min and 2 min.

QUANTIFICATION AND STATISTICAL ANALYSIS

For all intrakinetochore Δ analysis, expanded kinetochores and kinetochores where the software failed to correctly identify the spot center (as assessed by visual inspection), were excluded to prevent compromising accuracy. All significance tests were done using z-test, except for the microtubule flux rate measurements where we used a t test. Fisher exact test was used to compare the fraction of cells exiting mitosis in live cell imaging experiments. The calculation of Nematic order is defined in [Methods S1](#page-14-2). In all figures, fluorophores imaged in different experimental conditions are displayed using the same dynamic range for comparison purposes. Effective cell number is calculated as 1/SI where SI is the Simpson Index Σ_i p_i² where p_i is the fraction of KTs in cell i.

DATA AND CODE AVAILABILITY

Kinetochore Tracking (KiT) 2.1.10 and the Bayesian Euclidean distance correction algorithm (BEDCA) codes are available on our github site: <https://github.com/cmcb-warwick>

Cell Reports, Volume 31

Supplemental Information

Ensemble-Level Organization of Human Kinetochores

and Evidence for Distinct Tension

and Attachment Sensors

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Supplemental figures

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2020

Supplemental Figure 1 related to Figure 1. Comparison of Δ_{1D} , Δ_{3D} and Δ_{EC} measurements. (A) Histograms showing the $Ndc80(C)$ -to- $Ndc80(N)$, Nnf1-to- $Ndc80(C)$ and Nnf1-to-Ndc80(N) Δ_{1D} , Δ_{3D} and Δ_{EC} distances in Ndc80-EGFP cells. (B) Histograms showing the CenpCto-Ndc80(C), CenpC-to-Ndc80(N) and the Ndc80(C)-to-Ndc80(N) Δ_{1D} , Δ_{3D} and the Δ_{EC} distances in Ndc80-EGFP cells. (C) Kinetochore pair stained with anti-CenpC, anti-Nnf1 and anti-Hec1(9G3) antibodies. Scale bar 500 nm. (D) Histograms show the Nnf1-to-Ndc80(N), CenpC-to-Ndc80(N) and CenpC-to-Nnf1 Δ_{1D} , Δ_{3D} and Δ_{EC} distances in cells. Mean (dashed line) and sd (horizontal bar) values are indicated on the right.

Supplemental Figure 2 related to Figure 1. Parental and Ndc80-EGFP expressing RPE1 cells display the same mitotic timing. Image shows mitotic RPE1 cells expressing Ndc80-EGFP. Scale bar20 μ m. Cumulative frequency plot displaying the timing between nuclear envelope breakdown (NEB) and anaphase onset in parental RPE1 and RPE1 Ndc80-EGFP cells (MC191). Mean and sd values are indicated on the right.

Supplemental Figure 3 related to Figure 4. Nocodazole and taxol reduce inter-sister kinetochore distance and the taxol-dependent loss of inter-sister kinetochore tension is associated with reduced microtubule poleward flux. (A) Example images of RPE1 cells treated with 3.3 μ M nocodazole for 2 hr and DMSO as control. Scale bars 3 μ m. In control cells, bi-orientated kinetochore pairs (red) are attached to microtubules (blue) and are under tension (white arrowheads in insets i. and ii.; these images were enhanced to better show kinetochores and microtubules). Nocodazole induces full depolymerization of microtubules and reduces the interkinetochore distance (white arrowheads in inset iii. and iv.). In this condition, only centrosomes (*) and few rare microtubule stubs (white arrow in inset iv.) remain intact. Scale bar in insets is 500 nm. Bar charts (right) show the 3D K-K distance from CenpC to CenpC in cells treated with 3.3 μ M nocodazole for 2 hr, 1 μ M taxol for 15 min and DMSO as control. Mean and SEM values are indicated above the chart. (B) Effect of 1 μ M taxol treatment on microtubule dynamics was determined by photoactivating PA-EGFP-alpha-tubulin adjacent to the metaphase plate and then measuring its movement to the pole (poleward microtubule flux) and the dissipation of the signal over time (plus-end turnover). Example images of RPE1 expressing photoactivatable PA-EGFPalpha-tubulin (green) stained with SiR-DNA to visualize the chromosomes (red). Photo-activation was carried out at T=0 and cells were imaged every 15 s for 2 min. White dotted lines indicate the centre of the metaphase plate used as reference to measure the position of the PA-EGFP-alphatubulin (green). Scale bar 5 μ m. 1 μ M taxol abolishes plus-end turnover as the tubulin signal is

stable for 120 s, while the signal in DMSO treated cells exponentially decays as previously reported (Amaro et al., 2010) (C) Left: Box and whiskers plot showing the measured microtubule poleward flux whitin the first 60 s in cells treated with 1 μ M taxol or DMSO (see Materials and Methods for details). T-test indicates the difference is significant: (*) p=3.5x10-8. Mean and sd values are indicated below the chart. Right: Intensity of PA-EGFP-alpha-tubulin at the indicated times in 1 μ M taxol or DMSO-treated cells (see Materials and Methods for details). Black solid line indicates the double exponential fitting for the DMSO intensities.

Supplemental Figure 4 related to Figure 4. The Ndc80 N-terminus moves close to Nnf1 in unattached kinetochores. (A) Kinetochores in RPE1 cells stained with anti-CenpC, anti-Nnf1 and anti-Hec1(9G3) antibodies and treated with 3.3 μ M nocodazole for 2 hr, 1 μ M taxol for 15 min and DMSO as control. Scale bar 500 nm. (B) Distribution of the Nnf1-to-Ndc80(N), CenpC-to-Nnf1 and CenpC-to-Ndc80(N) Δ_{EC} distances in DMSO, nocodazole (+noc) and taxol treated cells. Mean (dashed line) and sd values are indicated on the right.

Supplemental Figure 5 related to Figure 5. Taxol-induced mitotic delay is dependent on the activation of the Spindle Assembly Checkpoint. (A) Images of RPE1 Venus-Mad2 cells stained with anti-CenpC antibody and treated with 3.3 μ M nocodazole for 2 hr, 1 μ M taxol for 15 min and DMSO as control. Scale bars 3µm. (B) Images of RPE1 cells treated with 1 μ M taxol (+tax) or DMSO for 15min and then with 1 μ M reversine for 2h. Bottom row shows a cell treated with 1 μ M taxol (+tax) only, as negative control. Time frame images at 39, 42 and 45 min in the DMSO sample were enhanced to better display the cell exiting mitosis. To visualize DNA, cells were previously treated with SiR-DNA. Scale bars 5 µm. (C) Kinetochore pair in RPE1 Ndc80-EGFP cells stained with anti-Hec1(9G3) antibodies and treated with 3.3 μ M nocodazole + 10 μ M MG132 for 1 hr, 3.3 μ M nocodazole + 10 μ M MG132 + 1 μ M reversine for 1 hr and DMSO as control. Scale bar 500 nm. Histograms show the distribution of the Ndc80(C)-to-Ndc80(N) Δ_{EC} in cells treated as above. Mean (dashed line) and sd values are indicated on the right.

Supplemental Figure 6 related to Figure 6. Mad1(N) to Mad1-pT716 Δ_{EC} distance reflects EM structural data. Kinetochore pair stained with antibodies against Mad1 (aa Kinetochore pair stained with antibodies against Mad1 (aa 77-115), here referred as Mad1(N), and Mad1-pT716. Scale bar 500 nm.

Supplemental Figure 7 related to Figure 6. bub1 1-23 cells can recruit Mad1:Mad2 at kinetochores and are delayed in metaphase upon taxol treatment. (A) Images of parental and RPE1 bub1 1-23 cells stained with anti-CenpC, anti-Bub1 and anti-Mad2 antibodies and treated with 3.3 μ M nocodazole for 2 hr. Scale bars 500 nm. Box and whiskers plots on the right show Bub1 and Mad2 intensities in parental and RPE1 bub1 1-23 cells. Bub1 and Mad2 signals were background-subtracted and normalised to CenpC signal (also background corrected). (B) Kinetochore pair stained with anti-CenpC, anti-Zwilch and anti-Bub1(N) antibodies (top) and with anti-CenpC, anti-Mad1-pT716 and anti-Bub1(N) antibodies (bottom) in parental and RPE1 bub1 1-23 cells treated with 3.3 μ M nocodazole for 2 hr. Scale bars 500 nm. Box and whiskers plots on the right show Zwilch and Mad1-pT716 intensities in parental and RPE1 bub1 1-23 cells. Zwilch and Mad1-pT716 signals were background-subtracted and normalised to CenpC signal (also background corrected).

Supplemental Figure 8 related to Figure 6. bub1 1-23 cells activate Spindle Assembly Checkpoint in taxol. Images of RPE1 bub1 1-23 cells treated with $1 \mu M$ taxol (+tax) and DMSO as control, for 24 min. To visualize DNA, cells were previously treated with SiR-DNA. Scale bars 3 μ m. Bar chart shows the fraction of cells exiting mitosis within 24 min. Fisher's exact test indicates the differences are significant with 99% confidence interval: (*) p=7x10-7.

Methods S1: Δ_{EC} algorithm, Simulation and Nematic order calculations, related to STAR Methods.

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2020

1 A Bayesian Euclidean distance correction algorithm: paired fluorophores

1.1 Introduction

Errors in the measurement of distances causes an over estimation of those distances which is nonnegligible when measurement noise is of a similar order to the true distance, see Figure 1. Thus, distances below the resolution of light will be subject to overestimation/inflation under super resolution methods, the degree of inflation being determined by the spatial accuracy of the measurement. Inflation affects measurements in all dimensions, 1D, 2D and 3D, Churchman et al. (2006). Inflation occurs because measurement error can exceed the actual distance, which could then reverse the orientation along a given axis corresponding to a negative displacement (Figure below, black). Since orientation is however not known, eg kinetochores can twist beyond 90^o, Smith et al. (2016), the euclidean distance is used which is always positive. This is subject to the same effect, i.e. there is a shift of the measurements upwards because of noise (Figure below, blue).

Schematic showing inflation under measurement noise of the displacement between 2 fluorophores in 1D. Histograms of displacement measurements under Gaussian noise assuming known orientation (black), and distance distribution under the modulus (absolute value) operation, $|x|$ when orientation unknown (blue). The measurements where noise exceeds the true distance switching the orientation of the fluorophores (turquoise shaded) - are measured as positive distances causing inflation, e.g. the mean of the distribution (dashed line) is increased.

From multiple samples of intra-kinetochore distance measurements between two fluorophores we present a Bayesian algorithm to infer the true 3D distance. Noise in the measurement means that the measured distance is an over-estimate, e.g. see (Churchman et al., 2005, 2006), a bias that needs to be corrected. Measurement noise comes from both the microscope point spread function (PSF) and the number of emitted photons, which is determined by the brightness of the flourophores. Thus, measurement noise is both wavelength dependent and protein density dependent. Isotropic measurement errors have been analysed before with published formulae/maximum likelihood correction algorithms in 1-3D (Churchman et al., 2006). However, non-isotropic measurement errors have not been analysed.

In section 1.2 we introduce a 3D model of paired fluorophore measurements. In section 1.3 we derive the associated likelihood. In section 1.4 we present a Markov chain Monte carlo (MCMC) algorithm to sample the posterior distribution of the model parameters. In section 1.5 we demonstrate the algorithm's accuracy on simulated data.

1.2 Euclidean distance model

Let \vec{X} be the observed vector from flourophore 1 to fluorophore 2. For N measurements, we have samples \vec{X}_i , $i = 1, 2...N$. Assume that the measurement noise is Gaussian, and if the true displacement is $\mu \vec{n}_i$, with true direction \vec{n}_i (unit vector) and true distance μ , we have

$$
\vec{n} \sim \mathcal{P}, \ \vec{X}_i \sim \mu \vec{n} + N(0, 2\Sigma^{-1})
$$

where Σ is the 3D precision matrix (inverse of covariance) for the spot centre accuracy, and direction vector \vec{n}_i is chosen according to a direction distribution P , e.g. uniform over a sphere. The task is to determine the mean distance $\mu \geq 0$ and the measurement error covariance matrix $2\Sigma^{-1}$. The factor of 2 comes from the fact that both fluorophores have measurement error, so we could write this as the sum of the two measurement errors $2\Sigma^{-1} = \Sigma_1^{-1} + \Sigma_2^{-1}$; however we don't estimate these separately. For isotropic measurements Σ is diagonal; $\Sigma^{-1} = \frac{1}{2}\sigma^2 I$, I is the diagonal matrix and σ is the intradistance error standard deviation. Thus, if spot accuracies are identical, individual spot centres would have variance $\sigma^2/2$. Note that the measurement noise can reverse the orientation, i.e. $\vec{X}_i \cdot \vec{n}_i$ can be negative (see introduction section 1.1).

To quantify distances, it is natural to consider the distribution of $r = |\vec{X}|$; this involves integrating over the orientation distribution $\mathcal P$ and the angular components of $\vec X$ (i.e. angular measurements are ignored). For the case of isotropic errors we take advantage of the rotational invariance, i.e. choose axes relative to \vec{n} ; thus, the only coordinate is r - the distance between the fluorophores. Then, for isotropic measurement error in 3D we obtain the probability density (Churchman et al., 2006),

$$
\pi_{3D}(r) = \frac{1}{\sqrt{2\pi}} \frac{r}{\mu \sigma} \left(e^{-\frac{(r-\mu)^2}{2\sigma^2}} - e^{-\frac{(r+\mu)^2}{2\sigma^2}} \right) \tag{1}
$$

This gives for the mean and variance,

$$
E[r] = \sqrt{\frac{2}{\pi}}\sigma e^{-\frac{\mu^2}{2\sigma^2}} + \frac{\sigma^2 + \mu^2}{\mu} erf\left(\frac{\mu}{\sqrt{2}\sigma}\right), \ var(r) = 3\sigma^2 + \mu^2 - E[r]^2,
$$

which can, for instance, be fitted to data and μ , σ thereby inferred.

1.3 The model likelihood

For N 3D measurements the likelihood of this model is given by,

$$
L = \prod_{i=1}^{N} \left(\frac{1}{(2\pi)^{\frac{3}{2}} \sigma_x^2 \sigma_z} \right) \exp - \left(\vec{X}_i - \mu \vec{n}_i \right)^T \Sigma \left(\vec{X}_i - \mu \vec{n}_i \right),
$$

where $2^{-1}\Sigma$ is the 3D precision matrix for the spot centre accuracy (averaged over the two flourophores), and in microscope coordinates is given by $\Sigma^{-1} = diag(\frac{1}{2}\sigma_x^2, \frac{1}{2}\sigma_x^2, \frac{1}{2}\sigma_z^2)$.

We use spherical coordinates to specify the relative position of the two vectors \vec{X}_i, \vec{n}_i ; ϕ_i is the relative angle in the x, y plane between \vec{X}_i, \vec{r}_i , and θ_i, θ_{Xi} are the angles of \vec{n}_i, \vec{X}_i with the z-axis:

$$
\vec{n}_i = (\sin \theta_i, 0, \cos \theta_i), \ \vec{X}_i = r_i (\sin \theta_{Xi} \cos \phi_i, \sin \theta_{Xi} \sin \phi_i, \cos \theta_{Xi})
$$

Then the likelihood reads,

$$
L = \prod_{i=1}^{N} \left(\frac{1}{(2\pi)^{\frac{3}{2}} \sigma_x^2 \sigma_z} \right) \exp \left(-\frac{1}{2\sigma_x^2} \left(\mu^2 \sin^2 \theta_i + r_i^2 \sin^2 \theta_{Xi} - 2\mu r_i \sin \theta_i \sin \theta_{Xi} \cos \phi_i\right) - \frac{1}{2\sigma_z^2} \left(\mu \cos \theta_i - r_i \cos \theta_{Xi}\right)^2.
$$
\n(2)

This has global parameters μ, σ_x, σ_z and kinetochore specific hidden (unmeasured) variables θ_i, ϕ_i , $i = 1, 2...N$ to determine (recall r_i, θ_{Xi} are measured).

1.4 Markov chain Monte carlo methods for Bayesian parameter inference

The objective of Bayesian inference is to determine the probability distribution of the model parameters given the data, specifically the posterior density:

$$
\pi(\mu, \sigma_x, \sigma_z, \{\vec{n}_i\}|\{\vec{X}_i\}) = \pi(\{\vec{X}_i\}|\mu, \sigma_x, \sigma_z, \{\vec{n}_i\})\pi(\mu, \sigma_x, \sigma_z, \{\vec{n}_i\})/\pi(\{\vec{X}_i\})
$$

from Bayes theorem, where the first term is the likelihood L above and $\pi(\mu, \sigma_x, \sigma_z, \{\vec{n_i}\})$ are the priors on the parameters. Here we are inferring the model using all the kinetochore data, indicated by the set $\{\vec{X}_i\}$, $i = 1, ..., n$, i.e. the model assumes all kinetochores are in the same state. This could correspond to all attached, or all detached for example. Using the spherically symmetric measure (solid angle) $d\Omega = \sin\theta d\theta d\phi$, the posterior distribution is thus given up to proportionality,

$$
\pi(\mu, \sigma_x, \sigma_z, \vec{n}_i | \vec{X}) \propto \pi(\mu) \pi(\sigma_x, \sigma_z) \prod_{i=1}^N \pi(\theta_i, \phi_i) r_i^2 \sin \theta_i \left(\frac{1}{(2\pi)^{\frac{3}{2}} \sigma_x^2 \sigma_z} \right)
$$

\n
$$
\exp -\frac{1}{2\sigma_x^2} \left(\mu^2 \sin^2 \theta_i + r_i^2 \sin^2 \theta_{Xi} - 2\mu r_i \sin \theta_i \sin \theta_{Xi} \cos \phi_i \right) - \frac{1}{2\sigma_z^2} \left(\mu \cos \theta_i - r_i \cos \theta_{Xi} \right)^2,
$$
\n(3)

where $\pi(\mu), \pi(\sigma_x, \sigma_z)$ and $\pi(\theta_i, \phi_i)$ are appropriate priors. If $\mathcal{P}(\vec{n}_i)$ is uniform over the surface of the sphere, the prior on $\cos \theta_i$ is $U([1, -1])$. This distribution has 3 global variables $\mu, \sigma_{x,z}$, and 2N hidden variables ϕ_i, θ_i .

However, the posterior can be marginalised in ϕ_i (integrating out ϕ_i using a uniform prior) to give the alternative form with only N hidden variables θ_i ,

$$
\pi(\mu, \sigma_x, \sigma_z, \theta | \vec{X}) \propto \pi(\mu) \pi(\sigma_x, \sigma_z) \prod_{i=1}^N \pi(\theta_i) \sin \theta_i \left(\frac{1}{(2\pi)^{\frac{1}{2}} \sigma_x^2 \sigma_z} \right) I_0 \left(\frac{\mu r_i \sin \theta_i \sin \theta_{Xi}}{\sigma_x^2} \right)
$$

$$
\exp -\frac{1}{2\sigma_x^2} \left(\mu^2 \sin^2 \theta_i + r_i^2 \sin^2 \theta_{Xi} \right) - \frac{1}{2\sigma_z^2} \left(\mu \cos \theta_i - r_i \cos \theta_{Xi} \right)^2, \quad (4)
$$

where I_0 is the modified Bessel function. If the measurement error is isotropic we can also integrate out the angular variables θ_i to obtain the posterior corresponding to (1).

Neither of these posterior distributions are tractable analytically as far as we are aware, and thus numerical methods are required to generate samples. We use a Markov chain Monte Carlo (MCMC) methodology to sample from these posteriors. The marginalised posterior (4) is computationally more expensive per step but has superior mixing than (3) so convergence is achieved with fewer steps. We thus focus on (4) in the following.

There are a vast number of MCMC algorithms, Craiu and Rosenthal (2014). The fundamental idea of MCMC is that parameters are updated either individually, or in groups, using a proposal and these proposals are accepted or rejected such that the distribution is corrected to conform to the conditional posterior. Specifically, consider sampling from the distribution $\pi(\theta)$ (which could be

our posterior above where θ are our model parameters). If the current state of the markov chain is θ, then propose a new $\theta' \sim q(\theta'|\theta)$, where typically a subset of the θ are changed. Then accept the proposal with probability (the Metropolis-Hastings ratio),

$$
\alpha(\theta \to \theta') = \min\left(1, \frac{\pi(\theta')}{\pi(\theta)} \frac{q(\theta | \theta')}{q(\theta' | \theta)}\right)
$$

and remain at θ if the proposal is rejected. This is called the update. A number of proposals are needed so that all parameters are updated. Then under fairly weak conditions the resulting Markov chain converges in probability to the target distribution $\pi(\theta)$, Craiu and Rosenthal (2014). Key to the Metropolis-Hastings ratio is that $\pi(\theta)$ only needs to be known up to normalisation. Special cases include the Gibbs update.

1.5 MCMC sampling algorithm

We use a Metropolis-Hastings within Gibbs algorithm, i.e. we have a mix of Metropolis-Hastings and Gibbs proposals. We use an algorithm that updates variables separately except for μ , σ_x that are highly correlated. We switch to precisions $\tau_{x/z} = \sigma_{x/z}^{-1}$ as is typical for models with Gaussian noise since precisions are (conditionally) Gamma distributed under the choice of a conjugate Gamma prior. We use short hand $s_i = \sin \theta_i$, $c_i = \cos \theta_i$, $s_{Xi} = \sin \theta_{Xi}$, $s_{Xi} = \sin \theta_{Xi}$. We use weak conjugate priors, imposing any positivity conditions by truncation. Updates are as follows:

Joint μ , τ_x proposal. We find that μ and τ_x are often highly correlated. Here we describe a twisted random walk along the eigendirections of the covariance matrix. For an estimated covariance matrix C , determined during burnin (computed sequentially 5 times), define the orthonormal eigenvectors η_j , $C\eta_j = \lambda_j \eta_j$. Then propose a move in the two directions separately, $j = 1, 2$,

$$
\left(\frac{\mu}{\tau_x}\right)' = \left(\frac{\mu}{\tau_x}\right) + N(0, \lambda_j)\eta_j
$$

which has an acceptance probability,

$$
\alpha \left(\left(\frac{\mu}{\tau_x} \right) \rightarrow \left(\frac{\mu}{\tau_x} \right)' \right) = \max \left(1, \frac{\pi(\mu') \pi(\tau'_x)}{\pi(\mu) \pi(\tau_x)} \left(\frac{\tau'_x}{\tau_x} \right)^N \prod_i \frac{I_0 \left(\mu' \tau'_x r_i s_i s_{Xi} \right)}{I_0 \left(\mu \tau_x r_i s_i s_{Xi} \right)} \right)
$$

\n
$$
\exp -\frac{1}{2} \tau'_x \sum_i \left((\mu' s_i)^2 + (r_i s_{Xi})^2 \right) + \frac{1}{2} \tau_x \sum_i \left((\mu s_i)^2 + (r_i s_{Xi})^2 \right)
$$

\n
$$
\exp -\frac{1}{2} \tau_z \left(\mu' - \mu \right) \sum_i c_i \left((\mu' + \mu) c_i - 2 c_{Xi} r_i \right) \right).
$$
 (5)

The priors enforce rejection of proposals that violate the positivity requirements, $\mu > 0, \tau_x > 0$.

Precision $\tau_z = \sigma_z^{-2}$. Using a conjugate Gamma prior $\Gamma(a_z, k_z)$ we have the Gamma distributed update

$$
\tau_z | \sim \Gamma \left(a_z + \frac{N}{2} - \frac{3}{2}, k_z + \frac{1}{2} \sum_i (\mu c_i - r_i c_{Xi})^2 \right). \tag{6}
$$

Hidden variable θ_i . We use a random walk proposal. We used proposal $\theta'_i \sim \theta_i + N(0, w^2)$, with step size $w = 0.75$ giving reasonable acceptance rates. The acceptance probability is,

$$
\alpha(\theta_i \to \theta'_i) = \min\left(1, \frac{\pi(\theta')\sin\theta'_i}{\pi(\theta)\sin\theta_i} \frac{I_0(\mu\tau_x r_i s'_i s_{Xi})}{I_0(\mu\tau_x r_i s_i s_{Xi})} \exp\left(-\frac{\tau_x \mu^2}{2}\left((s'_i)^2 - (s_i)^2\right) - \frac{\tau_z}{2}\left((\mu c'_i - r_i c_{Xi})^2 - (\mu c_i - r_i c_{Xi})^2\right)\right)\right)
$$

Since this is a symmetric random walk, the proposal cancels.

Priors. The prior in μ is a truncated Gaussian ($\mu > 0$) with large standard deviation, $\mu \sim$ $N(60, 100^2)$ (all distances in nm). Priors for τ_x, τ_z are weakly informative Gamma distributions, $\tau_{x/z} \sim \Gamma(a, a s_{x/z}^2)$ (shape and rate), with $a = 10$. This has mean precision s^{-2} and a relative standard deviation $a^{-\frac{1}{2}} = 0.32$. Weaker priors with wider distributions (smaller a, e.g. $a = 1$) worked on some data sets and gave similar results, but $a = 10$ gave good performance on all our data, see convergence discussion below. For τ_x, τ_z we used $s_x = 20, s_z = 40$ nm respectively when both flourophores are antibodies, and $s_x = 25$, $s_z = 75$ nm if one of them is a fluorescent protein. Our posteriors are always tighter than these priors and typically have posterior means 20-30 nm for σ_x , and 40-55 nm for σ_z .

1.6 MCMC algorithm performance on simulated data

We tested the algorithm on simulated data (see Figure below). Convergence was determined using the Gelman-Rubin diagnostic for multiple chains and determined converged if the corrected Gelman-Rubin statistic was below 1.1. We used 4 chains with chains initialized from the priors. The true parameters are accurately reconstructed, as seen in the following Figure.

Performance on simulated data. Markov chains (4) and posterior distributions shown for distance μ , precision $\tau_x = \sigma_x^{-2}$, precision $\tau_z = \sigma_z^{-2}$. The four chains are shown in different colors. Corrected Gelman Rubin statistic (GRc) for each variable are indicated on top of panel. True values are indicated by red asterisk on the x-axis, *i.e.* $\mu = 40$ nm, $\sigma_x = 25, \sigma_z = 45$ nm. MCMC runs of length 100000 including 50000 burnin. Priors for $\tau_{x,z}$ had $a = 3$. Data set consists of 1000 simulated kinetochores.

1.7 Running the MCMC algorithm on experimental data

We initially filtered the data with the constraint $|X| < \Delta_{max}$ since extremely large measured distances are clearly in error. For most data we used a threshold $\Delta_{max} = 200$ nm; however for KNL1-pS24 the measured 3D distances still had a significant tail population at 200nm. Thus, we used $\Delta_{max} = 250$ nm for pKNL1 data sets. We reduced the threshold to 180 nm for the Ndc80(C) to Ska distance (7 kinetochores were rejected out of 273) because these outliers caused the precision to be abnormally high.

On all runs we used priors with $a = 10$. We used the Gelman-Rubin diagnostic for 4 multiple chains to assess convergence, requiring that the corrected Gelman-Rubin statistic was below 1.1 on all three parameters μ, τ_x, τ_z (typically below 1.02). Burn-in was 50% of the run in all cases. Most data sets converged within 100,000 steps; for datasets that failed to converge within 100,000 the run length was increased until convergenced attained. The maximum run length (including burn-in) was 2,000,000 for the CenpC-to-Ndc80(C) distance in MC191 cell line under nocodazole treatment. All histograms are based on a single run with $50,000$ samples (using subsampling at appropriate rates).

2 Kinetochore architecture simulations

2.1 Structural data

We used kinetochore architectural information and structural data (crystalographic and EM), see Table below, to build a kinetochore simulation. The orientation of the Ndc80/Nuf2 calponin homogy (CH) domains with respect to the microtubule lattice, and the extending coiled coils were from Wilson-Kubalek et al. (2008). The Ndc80 hinge (also called loop or kink) was positioned 16 nm from the CH domains and allowed to bend and rotate given the intrinsic flexibility of the hinge and the coiled coil that connects to the Spc24/Spc25 subunits (Maiolica et al., 2007; Huis in 't Veld et al., 2016; Scarborough et al., 2019; Wang et al., 2008). The Ndc80 hinge angle and the elevation angle of the NDC80 complex short arm (the coiled coil between Ndc80 hinge and Ndc80/Nuf2 CH domains) with respect to the microtubule lattice have been measured using purified complexes but not within the context of the intact kinetochore in vivo. So this information was not imposed.

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Nnf1 ^{**} to $Ndc80(C)$	14 nm	estimated from (Huis in 't Veld et al., 2016;
		Petrovic et al., 2010; Ciferri et al., 2005)
Nnf1 ^{**} to Ndc80(N) [*]	64 nm	estimated from (Petrovic et al., 2014; Screpanti
		et al., 2011; Musacchio and Desai, 2017; Huis in 't
		Veld et al., 2016)

^{*} Ndc80(N) denotes the anti-Hec1 (9G3) antibody binding site (Ndc80 amino acids 200-215; DeLuca et al., 2006)

** The anti-Nnf1 antibody is assumed to bind in the middle of the MIS12 complex

2.2 Simulation

The simulation proceeds as follows. For parameters that are fixed from structural data, the values are described in Section 2.1. Parameters that are fitted to the Ndc80(N)-Ndc80(C)-CenpC triangle distances are indicated below (indicated as 'fitted' in text, and in red color in schematic) and the fitting is described in Section 2.3. Note that variability in angles is set to 10° in absence of constraining data. See schematics below for graphical representation of the incorporated flexibility and annotations.

- 1. Microtubule Bundle (K-fibre). The K-fibre is defined as a disc of diameter 360 nm, centred on the x-axis. Next, 20 microtubules (MT), radius 13 nm, are uniformly distributed within the K-fibre cross-section. Here, the microtubules lie parallel to the x-axis. If there are overlapping microtubules, all positions are rejected and the process is repeated.
- 2. NDC80 complex. The true mean of the Ndc80 attachment points is labelled x along the central axis of the K-fibre. Next, 8 NDC80 complexes are placed on each microtubule as follows:

First, we determine a binding site along the MT (Gaussian, mean x , sd 25 nm) and rotate around the MT axis by angle φ_0 (uniform in [0, 360^o]). Next, the Ndc80(N) is positioned at 4.25 nm offset from the microtubule surface, considering the 9G3 antibody binding site. This results in 17.25 nm offset from the MT axis (13 nm MT radius). The NDC80 complex short arm is simulated by elevation at angle φ_1 (Gaussian, fitted mean, sd 10^o) relative to the microtubule axis, with the Ndc80 hinge oriented towards the inner kinetochore plate. The NDC80 complex short arm can tilt around the axis parallel to the x-axis going through Ndc80(N), angle φ_2 (Gaussian, mean 0° , sd 10°), i.e. the NDC80 complex short arm and the microtubule axes would no longer lie in the same plane for non-zero tilt. The Ndc80 hinge is positioned at a fixed distance of 16 nm from $Ndc80(N)$. The hinge angle between the NDC80 complex short arm and long arm (NDC80 complex coiled coil region between Spc24/Spc25 Head domains and Ndc80 hinge) is defined as φ_3 (Gaussian, fitted mean, sd 10^o). We also incorporate rotation of the long arm around the NDC80 complex short arm axis, angle φ_4 (Gaussian, mean 0° , sd 10°). Ndc80(C) is positioned 35 nm from the Ndc80 hinge along the NDC80 complex long arm. Nnf1 is positioned a further 14 nm from Ndc80(C) along the NDC80 complex long arm axis towards the inner kinetochore. Finally, CenpC is positioned as described bellow.

3. CenpC-Ndc80(N) axis. Here, we use a model where the inner kinetochore (detected by the CenpC marker in this study) is off axis relative to the K-fibre. The inner-outer kinetochore axis is defined by elevating a line from the x-axis (pinned at x) at angle φ_5 (Gaussian, fitted mean, sd) and rotating around the K-fibre axis by a random angle φ_6 (uniformly distributed). The focus point y is positioned at a fixed distance (fitted) from x along this inner-outer kinetochore axis. CenpC is placed at a distance u (fitted) along the line joining Nnf1 to the focus point y; the focus will act to concentrate CenpC molecules relative to Nnf1. If y is at infinity there is no focusing, i.e. the spread of CenpC and Nnf1 will be identical.

Geometrical setup for simulations of the CenpC-MIS12-NDC80 ensembles. Green and red dots represent the positions of the indicated kinetochore proteins. A representative microtubule is shown in grey and its axis (black dotted line) lies on plane A. The purple dotted line indicates the K-fibre axis (x-axis). The NDC80 complex short arm lies on plane B and tilts (φ_2) around the axis (light blue dotted line) that is parallel to the x-axis and goes through Ndc80(N). Fixed angle parameters used in the simulations are shown in black. Fitted parameters obtained from the simulations are displayed in red. For illustration only, the NDC80 MT attachment is shown vertically above the microtubule ($\varphi_0 = 0$).

2.3 Fitting of parameters. Optimisation.

The measured Δ_{EC} distances in DMSO (cell line MC191) of 1. Ndc80(C)-to-Ndc80(N), 2. CenpCto-Ndc80(N), and 3. CenpC-to-Ndc80(C), were used to fit six parameters: the focus point y (fitting distance from x, and mean and sd of angle φ_5), the distance u from CenpC-to-Nnf1, the means of the short arm elevation angle and the Ndc80 hinge angle. We use a least-squares fitting method to minimise the difference between simulated distances in the triangle Ndc80(N)-Ndc80(C)-CenpC, and those observed. Specifically we minimise:

$$
V := (\Delta_{sim} (\text{Ndc80(N)} - \text{Ndc80(C)}) - \Delta_{EC} (\text{Ndc80(N)} - \text{Ndc80(C)}))^2 + (\Delta_{sim} (\text{Ndc80(C)} - \text{CenpC}) - \Delta_{EC} (\text{Ndc80(C)} - \text{CenpC}))^2 + (\Delta_{sim} (\text{CenpC} - \text{Ndc80(N)}) - \Delta_{EC} (\text{CenpC} - \text{Ndc80(N)}))^2,
$$

where the Δ_{sim} are the simulated distances, averaged over 20000 independently simulated kinetochores using the algorithm above.

The optimisation procedure is as follows: Starting from the current values of the 6 parameters a new set of these parameters is proposed based on a random walk (Gaussian) around the current values. The random walk has a drift term \vec{v} so that the algorithm continues to move in profitable directions, where the new drift vector is calculated for each jump and given by,

$$
\vec{v}' = \frac{1}{2} \left(\vec{v} + \vec{J} \right)
$$

where \vec{v} is the previous drift and \vec{J} is the just accepted jump, if the proposal was accepted, and zero otherwise. The random walk has the following standard deviations: i) 50 nm for the $|x-y|$ distance, ii) 2.5° for all angles except the mean of φ_5 , which was 5°. Larger step sizes were used early on to explore a larger part of the parameter space. A proposal is accepted if the cost function V is reduced. Otherwise, the proposal is rejected and a new proposal is attempted. As the simulations have many stochastic degrees of freedom, the Δ_{sim} are prone to fluctuations (despite the 20000 kinetochore sample size). To remove any bias, we re-evaluate V for a new, independent sample of 20000 kinetochores every time after an acceptance and every second time after a rejection. The process is completed if the results are considered close enough to the minimum of V , or if there is no improvement.

This method gives the following fit, reproducing the observed mean distances in the Ndc80(N)- Ndc80(C)-CenpC triangle to within 3 nm:

- angle φ_1 : mean 22.4^o. This is within the range 20-60^o given by Wilson-Kubalek et al. 2008.
- angle φ_3 : mean 203.5^o (where 180^o represents straight NDC80 complex conformation and angles $>180^\circ$ denote clockwise bending).
- distance $|x-y|$: 490 nm
- \bullet distance u: 37.9 nm
- angle φ_5 : mean 64.2^o, sd 18.1^o.

Here it needs to be noted that if additional constraints are imposed, a solution can still be found that fits the observed distances. For instance, imposing the elevation of the NDC80 complex short arm relative to the microtubule axis (φ_1) to be 10^o , sd 10^o (restricted to be positive) gives a solution with Ndc80 hinge angle (φ_3) mean of 177.3^o. Therefore, there are nearby solutions that do not require the hinge angle to be above 180^o .

3 Nematic order

Nematic order refers to the alignment of the molecules, alignment relative to an orientation axis (the director of Ericksen-Leslie theory). If the alignment distribution is $f(\cos(\theta))$, where θ is the angle between a molecule and the director, alignment order can be quantified in a number of ways. Typically, the distribution $f(\cos(\theta))$ is expanded in Legendre polynomials as follows,

$$
f(\cos(\theta)) = \sum_{l=0}^{\infty} \frac{2l+1}{2} N_l P_l(\cos(\theta)).
$$

This is analogous to a moment expansion; Legendre polynomials are used because they are orthogonal and $\cos(\theta)$ is valued in $[-1, 1]$. The most common measure of order for uniaxial materials is the second order Legendre polynomial, $N_2 = \mathbf{E}[P_2(\cos(\theta))],$ which can be used for materials with both aligned orientated molecules, eg ferromagnetic, and those with alignment but orientation can be random (no distinguishable head versus tail). For the latter, $f(\cos(\theta))$ is symmetric about zero, so the odd polynomials are zero, including N_1 , limiting their general use. The order parameter N_2 is related to the alignment tensor Q. The first Legendre polynomial order parameter, $N_1 = \mathbf{E}[P_1(\cos(\theta))] =$ $\mathbf{E}[\cos(\theta)]$, can also be used for aligned orientated molecules, with $N_1 = 1$ full alignment, $N_1 = 0$ no alignment. We use this measure because of its easy relationship to the *structural distance fraction*,

$$
SDF = \frac{\Delta_{EC}}{\Delta_{structural}}
$$

the ratio of the observed (mean) distance between two fluorophores and the expected structural distance $\Delta_{structural}$. Then $N_1 = SDF$. For Ndc80(N)-Ndc80(C) distance the hinge angle needs to be specified. Because each kinetochore is an ensemble, Δ_{EC} is the (average) distance of the average vector over the ensemble. Thus, N_1 is the proportion of the structural distance recovered by the ensemble average. We cannot use our data to compute N_2 since we only have the average ensemble distance Δ_{EC} .

In the simulations nematic order N is defined as $(|\cdot|)$ denotes Euclidean distance, $\langle \cdot \rangle$ denotes average over sample),

$$
N = \frac{|<\vec{x}>|}{<|\vec{x}|>}
$$

i.e. the length of the average vector to the average length of those vectors. If all molecules (vectors) have the same length then these formulae are identical, i.e. $N = N_1$. They differ when molecule length is not constant, eg for Ndc80 and a variable hinge degree of freedom. If molecule length variation is substantial the SDF and its relation to the order parameter need to be reconsidered as the true structural distance is an ensemble average over these conformations and not known.