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# Supplementary Materials for

# **Reducing the aerosol forcing uncertainty using observational constraints on warm rain processes**

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#### <span id="page-1-1"></span>Text S1: Positive and negative adjustments

Processes that lead to enhanced evaporation of smaller droplets in polluted conditions involve mixing of drier ambient air into clouds at cloud top (*8*, *9*, *75*, *76*) and cloud sides (*10*, *77*), as well as responses in cloud-scale and cloud-field-scale dynamics (*27*, *78*, *79*). These cloud responses are difficult to parameterize in GCMs because they occur at length scales typical of turbulent processes (centimeters through kilometers) through mesocale processes (kilometers to tens of kilometers), with abundant feedbacks across scales that are implicitly represented, at best, by GCM parameterizations. Processes that lead to precipitation suppression by increased droplet number concentration in polluted clouds, on the other hand, can be parameterized entirely at the cloud droplet scale within the microphysical warm-phase precipitation processes (see Methods). These cloud responses are explicitly, albeit crudely, represented in many GCMs (*80*–*83*).

#### Text S2: Caveats

We are not suggesting that the tuning strategies explored here are optimal; they are not able to reduce the warm-rain bias to zero, nor are they free from compensating biases elsewhere in the model – as shown by the need for scale factors smaller than unity, opposite to the enhancement factors needed to correct for subgrid variability in liquid water content (*61*, *84*). Rather, we have chosen these strategies to explore the parameter space of possible model behavior if the far more involved task of addressing base precipitation process behavior biases were undertaken. These simple experiments suffice to document the likely rewards in reduced base-process-induced ERF<sub>aci</sub> uncertainty and reduced equifinality-induced parameter degeneracy and to elicit the improvements in modeling, observations, and model–observation intercomparison techniques required to realize said rewards.

We also acknowledge that  $f_{\text{warm}}$  would ideally be superseded by a diagnostic that does not mix warm and cold rain processes, such as the warm-rain probability conditioned on the presence of cloud  $p_{\text{warm}}$ . We have chosen  $f_{\text{warm}}$  to simplify future comparison of ECHAM–HAMMOZ with other models that do not implement radar simulators. In these models, a threshold surface rain rate must be chosen below which the grid box is considered nonprecipitating. The uncertainty associated with the choice of threshold largely cancels in the ratio  $p_{\text{warm}}/(p_{\text{warm}} + p_{\text{cold}}) = f_{\text{warm}}$ ; if the intensity spectra of warm and cold rain matched, the cancellation would be exact. However, observations indicate so little warm rain in the extratropics compared to the model that the magnitude of the denominator in *f*warm is relatively unimportant to the constraint mechanism there; the constraint is simply that warm rain should not occur in those regions. Fortuitously, the adjustments in the model also predominantly occur in the polluted northern-hemisphere extratropics (*41*). Nonetheless, we advocate rapid adoption of satellite simulators by all models, a cobenefit of which is that this analysis can be refined using  $p_{\text{warm}}$ .

Finally, we acknowledge that large TOA imbalances, while a necessary evil in these sensitivity studies (see Text [S3\)](#page-1-0), are unacceptable in a production model. Thus, reducing the large model bias in autoconversion will require a similarly large retuning elsewhere, which will have to be accomplished without introducing or worsening biases in other state variables. We surmise that revisions that enhance the accretion of cloud water to rain droplets may be a promising avenue, simultaneously acting as a sink for the excess  $\mathcal L$  resulting from reduced autoconversion, strengthening the intensity and reducing the frequency of precipitation, and bringing the autoconversion–accretion partitioning into better agreement with observations (*14*, *85*, *86*).

#### <span id="page-1-0"></span>Text S3: Rapid-adjustment metrics

It is inherently difficult to quantify the change in ERFaci components in a GCM when parameterized processes are changed. There are two reasons for this. The first reason is that, for many applications, it is desirable for the model to reproduce the PD state of the atmosphere as closely as possible; this is especially true in coupled atmosphere–ocean climate runs, where an energy imbalance in the model will result in a drift of heat content of the climate system over time. Changing one process in isolation, even if it happens to make that process more realistic, is likely to bring the atmospheric state, including the energy balance, into worse overall agreement than what had been achieved previously by careful tuning. Thus, the model is often retuned after implementing the process change, so that the overall quality of the model is not degraded. However, even apparently unrelated parameter changes used for retuning can impact the  $ERF_{\text{aci}}$  and its components, masking the effect of the

intentional process change (*[19](#page-1-1)*). To avoid this problem, we choose not to retune the model for these experiments. In fixed-SST, nudged simulations, the model climate cannot diverge far from its control climate.

However, we still run into a second reason why quantifying  $ERF_{\text{aci}}$  components is difficult; namely, that the  $ERF_{\text{aci}}$  components depend on the model base state, and changing the process formulations changes the base state. Assume that the model can be described by a vector of processes  $p$  and a vector of state variables  $x$ . The processes map the state variables onto rates of change of the state variables. In general, the state variables will depend on the processes through an unknown functional ξ:

$$
x = \xi(p); \tag{S3.1}
$$

reformulating the processes so that  $p \rightarrow p'$  will therefore change the state vector as well.

<span id="page-2-0"></span>Further assume that  $F_L$  can be decomposed into a factor  $S$  that explicitly depends only on the state variables and a factor  $\mathcal{F}_{\mathcal{L}}$  that depends only on processes:

$$
F_{\mathcal{L}}(\mathbf{p}, \mathbf{x}) = \mathcal{F}_{\mathcal{L}}(\mathbf{p}) \times \mathcal{S}(\mathbf{x}).
$$
\n<sup>(S3.2)</sup>

Our aim is to find another variable  $\Phi$  that does not depend explicitly on p and depends on x in the same way as  $F_L$ , i.e.,  $\Phi(x) \propto$  $S(x)$ . If we can identify such a variable, the ratio  $F_L/\Phi \propto \mathcal{F}_L(p)$  can be used to diagnose the response of the adjustments to the change in process formulation, free from the confounding effect of unrelated state variable changes  $x \to x'$ .

The assumption that a factorization of the form [\(S3.2\)](#page-2-0) is possible can be rationalized for changes in model formulation that result in small changes in  $x$  by the following argument. Suppose we artificially made clouds more reflective while keeping the processes affecting  $\mathcal{F}_L$  the same, e.g., by introducing a perturbation in  $N_d$  that is visible only to the radiation scheme; this would leave  $\mathcal{F}_L$  unchanged by construction but still change  $F_L$  due to the increased cloud albedo encapsulated in a change in S.

A more difficult step is identifying candidates for Φ. The preceding proportionality argument suggests that a desirable property of  $\Phi$  is covariability with cloud albedo change. An initial set of candidates might therefore include  $\mathcal{L}$ , which strongly controls cloud albedo; and the shortwave cloud radiative effect  $S_c = S<sup>all</sup> - S<sup>clr</sup>$ , i.e., the difference in solar-spectrum radiative flux at the model top of atmosphere between all-sky and clear-sky conditions, which converts the change in cloud albedo into a radiative flux perturbation. While there is indeed a very tight relationship between  $\mathcal L$  and albedo across all our model configurations, the albedo saturates at high  $\mathcal{L}$ , which reduces its utility as a normalization for radiative quantities.

We consider a further candidate for  $\Phi$ : the radiative forcing  $F_{N_d}$ . The process changes we have made do not affect  $F_{N_d}$ explicitly, satisfying one of our above criteria for  $\Phi$ . The state variable changes induced by the process changes do affect  $F_{N_d}$ , however, in that the cloud albedo response to a given  $N_d$  perturbation is a nonlinear function of  $\mathcal L$  and  $N_d$ . We surmise that the dependence of  $F_{N_d}$  and  $F_{\mathcal{L}}$  on x are better analogs than the dependence of  $S_c$ . The reason is that both components of ERF<sub>aci</sub> are sensitive to the spatial covariability of cloud changes and anthropogenic aerosol perturbations ([41](#page-1-1)), whereas  $S_c$  is not; both components are affected by the greater anthropogenic  $N_d$  perturbation per unit emissions that results from reduced wet scavenging when precipitation probability is reduced; and the sensitivity of both components to changes in  $\mathcal L$  and  $N_d$ saturates in a higher- $\mathcal{L}$ , higher- $N_d$  state. Evidence for proportionality between  $F_{N_d}$  and  $F_{\mathcal{L}}$  in GCMs is presented based on spatial correlations in Mülmenstädt *et al.* (*[41](#page-1-1)*) and on intermodel correlation in Gryspeerdt *et al.* (*[42](#page-1-1)*).

Based on these arguments, we use the normalized adjustment  $F_{\mathcal{L}}/F_{N_d}$  in this paper. To test the robustness of our conclusions this choice. Fig. S a reproduces Fig. 3 for the other normalization choices we have cons to this choice, Fig. [S8](#page-12-0) reproduces Fig. [3](#page-10-0) for the other normalization choices we have considered,  $\Phi \in \{\mathcal{L}, \mathcal{S}_{c}\}\$ ; Tables [S1–](#page-14-0)S3 list the global-mean  $ERF_{\text{aci}}$  components and state variables. For all three metrics, there is a bifurcation in the adjustment response to reduced  $f_{\text{warm}}$  bias; the  $Q_{\text{aut}}$  scaling reduces the adjustment strength according to all three metrics, while the  $r_e$  threshold tuning increases the adjustment strength according to the  $F_L/F_{N_d}$  and  $F_L/S_c$  metrics and causes little change according to the *F<sub>C</sub>*/*F* metric. Thus the conclusion that an observational constraint on the rapid adjustm the  $F_L/L$  metric. Thus, the conclusion that an observational constraint on the rapid adjustment depends on knowing whether to address the drizzle bias or the rain bias appears robust to the choice of Φ. For all three metrics, increasing  $β$  (i.e., tuning in the direction of stronger susceptibility) results in adjustment changes that are comparable to the experiments modifying parameters that control base process behavior  $(\alpha, \gamma, r_c)$ ; for all three metrics, large increases in  $\beta$ , which should correspond to greater process susceptibility, results in weaker adjustment (see also Text [S5\)](#page-3-0). Thus, the conclusion that the base precipitation process behavior and the process susceptibility are both important contributors to the projected adjustment also appears robust to the choice of Φ.

#### Text S4: Geographic patterns of adjustment changes

Figure [S4](#page-8-0) shows the geographic distribution of the changes in normalized adjustment when the scale factor is reduced and when the  $r_e$  threshold is increased; the most drastic retuning is chosen in each case to produce clear patterns in the presence of statistical noise.

In the scale factor experiment, the change in normalized adjustment is robustly negative in the northern-hemisphere extratropics. Given the decrease in warm rain in these regions, this change is consistent with our hypothesis that base process behavior leading to reduced warm rain reduces  $F<sub>f</sub>$ . In the Sc regions, where cold rain is exceedingly rare, warm rain is still the dominant form of precipitation even with a reduced scale factor; here, the sign is reversed, presumably because the Golaz *et al.* (*[19](#page-1-1)*) applies; see below.

In the  $r_e$  threshold experiment, there is a robust increase in  $F_{\mathcal{L}}/F_{N_d}$  over oceans. This is in accordance with the Golaz *et al.*<br>2) aroument. To summarize the aroument, we first note that effective radius and l (*[19](#page-1-1)*) argument. To summarize the argument, we first note that effective radius and liquid-water mixing ratio are related:

$$
q_l = \frac{4}{3}\pi \frac{\rho_l}{\rho} r_e^3 N_d,\tag{S4.1}
$$

where  $\rho_l$  is the density of water and  $\rho$  is the density of air; strictly, the relationship holds for the volumetric-mean radius (by definition) but the ratio between r and volumetric radius is close to unity. Next, we definition), but the ratio between  $r_e$  and volumetric radius is close to unity. Next, we note that precipitation is a sufficiently important sink of  $q_l$  in the model that reducing the ability of clouds to precipitate below a threshold  $r_e$  (or equivalently  $q_l$ ) causes cloud water to build up until the new, higher threshold is reached. The mean  $q_l$  is thus strongly controlled by the threshold  $r_e$ :

$$
q_l \sim \frac{4}{3}\pi \frac{\rho_l}{\rho} r_c^3 N_d. \tag{S4.2}
$$

An anthropogenic  $N_d$  perturbation  $\Delta N_d$  thus leads to a  $q_l$  response that is proportional to  $r_c^3$ .

$$
\Delta q_l \sim \frac{4}{3} \pi \frac{\rho_l}{\rho} r_c^3 \Delta N_d,\tag{S4.3}
$$

so that models with higher *r*<sup>c</sup> will have a stronger *q*<sup>l</sup> response to a give anthropogenic aerosol perturbation than models with lower  $r_c$ .

For this argument to work, the moisture must not be limited by source processes, such as limits on surface evaporation, or other sink processes, such as consumption by parameterized convection. Over oceans, where Fig. [S4](#page-8-0) shows an increase in  $F_{\mathcal{L}}/F_{N_d}$ , we expect the moisture supply to be unrestricted. Figure [S4](#page-8-0) also shows a reduction in  $F_{\mathcal{L}}/F_{N_d}$  over parts of the continents, which may be explained by a lower exporative flux or a more convect continents, which may be explained by a lower evaporative flux or a more convective atmosphere that limits the applicability of the Golaz *et al.* (*[19](#page-1-1)*) argument.

#### <span id="page-3-0"></span>Text S5: Susceptibility versus base process behavior

The thinking underlying Wang *et al.* (*[27](#page-1-1)*) is that the susceptibility of precipitation to aerosol (*[87](#page-1-1)*) controls the model estimate of  $F_L$ . Accordingly, some modeling studies find that varying  $\beta$ , which changes the susceptibility of precipitation to aerosol, is the main control on  $ERF_{\text{aci}}$  ([88](#page-1-1), [89](#page-1-1)). The difficulty of diagnosing  $F_L$  separately from other components of  $ERF_{\text{aci}}$ , as well as the retuning process after perturbing a parameter of the model ( $90$ ), complicates the assessment to what extent  $F_L$  responds to changes in  $\beta$  in such studies (see also Text [S3\)](#page-1-0).

A more detailed calculation of the process susceptibility ([91](#page-1-1), [92](#page-1-1)) shows that  $\beta$  is not the only contribution to the autoconversion rate susceptibility to  $N_d$ ; rather, the susceptibility receives contributions both from exponents in [\(2\)](#page-1-1):

<span id="page-3-1"></span>
$$
\frac{d\ln Q_{\text{aut}}}{d\ln N_d} = -\beta + \alpha \frac{d\ln q_l}{d\ln N_d},\tag{S5.1}
$$

i.e., the susceptibility both influences and depends on rapid adjustments  $(d \ln q_l/d \ln N_d)$ , in a global-mean sense, controlling  $F_c$ ). In light of the model diversity in  $F_c$  estimates (42), we can assume that the relative c *F<sub>L</sub>*). In light of the model diversity in *F<sub>L</sub>* estimates (*[42](#page-1-1)*), we can assume that the relative contribution of  $\beta$  to the process superibility will also be diverse. These considerations notwithstanding  $F_c/F_M$  decre susceptibility will also be diverse. These considerations notwithstanding,  $F_L/F_{N_d}$  decreases at large β, when the process<br>susceptibility should be maximal, indicating that the presence of multiple terms in (S5.1) is not susceptibility should be maximal, indicating that the presence of multiple terms in [\(S5.1\)](#page-3-1) is not the dominant source of the insensitivity of the rapid adjustments to  $\beta$  in this model. A more likely explanation is that the components of  $ERF_{\text{aci}}$  are emergent properties of a complex system ([83](#page-1-1)), so we should not expect a straightforward correspondence between  $F_L$  and process rates or susceptibility (*[93](#page-1-1)*).



#### Figure S1. Distributions of cloud properties in different experiments.

Distributions of *C*,  $\langle N_d \rangle / C$ , and  $\mathcal{L}/C$ } are shown, where *C* is the two-dimensional projected liquid-cloud fraction, and  $\langle N_d \rangle$  is the vertical average of  $N_d$  over the liquid cloud column; the normalization by *C* is chosen to approximate an "in-cloud" liquid water path and "in-cloud" droplet number concentration, although the concept is not well defined in clouds spanning multiple model levels. Frequencies are normalized to the mode of the frequency distribution.



Figure S2. Warm-rain fraction from satellite and model in various scaling configurations. The reference configuration is *Q*aut ×4. As the scale factor is reduced, warm rain decreases rapidly, but warm drizzle is relatively unaffected.



Figure S3. Warm-rain fraction from satellite and model in various  $r_e$  threshold configurations. The reference configuration is  $r_e > 0$ . As the threshold is increased, warm drizzle decreases rapidly, but warm rain is relatively unaffected.

<span id="page-8-0"></span>

Figure S4. Geographic distribution of the change in normalized adjustment.  $F_{\perp}/F_{N_d}$  in the  $Q_{\text{aut}} \times 0.04$  and  $r_e > 17$  µm experiments is shown relative to the reference configuration.

<span id="page-9-0"></span>

**Figure S5. The relationship between** *f*warm bias and  $F_{\mathcal{L}}/F_{N_d}$  when varying  $\alpha$ .<br>This figure reprises Fig. 3 but varies  $\alpha$  instead of  $r_a$  and  $\alpha$ This figure reprises Fig. [3](#page-10-0) but varies  $\alpha$  instead of  $r_c$  and  $\gamma$ .

<span id="page-10-0"></span>

**Figure S6. The relationship between** *f*warm bias and  $F_{\mathcal{L}}/F_{N_d}$  when varying  $\beta$ .<br>This figure reprises Fig. 3 but varies  $\beta$  instead of  $r$ , and  $\gamma$ This figure reprises Fig. [3](#page-10-0) but varies  $\beta$  instead of  $r_c$  and  $\gamma$ .



**Figure S7. The relationship between**  $f_{\text{warm}}$  bias and  $F_{\mathcal{L}}/F_{N_d}$  over land and ocean.<br>This figure reprises Fig. 3 but separates the  $F_{\mathcal{L}}/F_{N_d}$  responses over land and ocean. This figure reprises Fig. [3](#page-10-0) but separates the  $F_{\mathcal{L}}/F_{N_d}$  responses over land and ocean.

<span id="page-12-0"></span>

### Figure S8. The relationship between  $f_{\rm warm}$  bias and multiple adjustment metrics.

This figure reprises Figs. [3,](#page-10-0) [S5,](#page-9-0) and [S6,](#page-10-0) but for alternate adjustment metrics  $-F_L/L$  (the negative prefactor is chosen so that a larger value<br>of the metric indicates a stronger adjustment, in common with the other metrics of the metric indicates a stronger adjustment, in common with the other metrics) and  $F_L/S_c$ . (Note that the  $\alpha \in \{1.75, 2\}$  data points are off scale in the  $-F_c/F$  panel.) scale in the  $-F_L/L$  panel.)



#### Figure S9. Correspondence between simulated radar reflectivity and surface precipitation rate.

Cumulative distribution functions (CDFs) of surface precipitation rate *P* by radar-simulator reflectivity-based classification of the column as cloudy, drizzling, or rainy show that reflectivity-based intensity classifications correspond closely with surface precipitation rate. The gray dashed lines correspond to 0.01, 0.1, and 1 mm  $h^{-1}$ .

#### <span id="page-14-0"></span>Table S1. Rapid adjustments and cloud state (global mean) across experiments.

Compared to the reference model, the reduced scaling factor configurations estimate a weaker normalized adjustment  $F_{\mathcal{L}}/F_{N_d}$ , while the increased threshold  $r_s$  configurations estimate a stronger normalized adjustm increased threshold *r*e configurations estimate a stronger normalized adjustment. The large TOA radiative imbalance *R*TOA in the reference run is a result of nudging; the non-nudged version of the reference run for the same time period has a more plausible  $R_{\text{TOA}} = 0.34 \text{ W m}^{-2}$ . Despite large changes in warm cloud properties, the ice water path  $I$  changes are within approximately 1%.

	ERF contributions (W $m^{-2}$ )			State variables					
Case	$F_{N_d}$	$F_{\mathcal{L}}$	$F_{\mathcal{L}}/F_{N_d}$	$R_{\rm TOA}$ (W m <sup>-2</sup> )	$S_c$ (W m <sup>-2</sup> )	$I (g m^{-2})$	$\mathcal{L}$ (g m <sup>-2</sup> )		
$Q_{\text{aut}} \times 0.04$	$-0.66$	$-0.57$	0.87	$-9.98$	$-58.97$	10.56	214		
$Q_{\text{aut}} \times 0.1$	$-0.65$	$-0.59$	0.91	$-8.23$	$-57.10$	10.55	184		
$Q_{\text{aut}} \times 0.4$	$-0.62$	$-0.64$	1.02	$-4.76$	$-53.33$	10.53	139		
$Q_{\text{aut}} \times 1$	$-0.59$	$-0.64$	1.07	$-1.93$	$-50.24$	10.50	110		
Reference	$-0.52$	$-0.57$	1.08	2.89	$-44.95$	10.45	73		
$r_e > 10 \mu m$	$-0.51$	$-0.59$	1.15	2.82	$-45.04$	10.45	73		
$r_e > 12 \mu m$	$-0.52$	$-0.61$	1.17	2.41	$-45.46$	10.46	76		
$r_e > 15 \text{ }\mu\text{m}$	$-0.59$	$-0.73$	1.24	0.26	$-47.84$	10.50	92		
$r_e > 17 \,\mathrm{\upmu m}$	$-0.65$	$-0.81$	1.25	$-2.31$	$-50.60$	10.52	114		



Table S2. Rapid adjustments and cloud state (global mean) across experiments scanning  $\alpha$ .<br>This table reprises Table S1 but varies  $\alpha$ This table reprises Table [S1](#page-14-0) but varies  $\alpha$ .

	ERF contributions (W m <sup>-2</sup> )			State variables		
Case	$F_{N_A}$	$F_{\mathcal{L}}$	$F_{\mathcal{L}}/F_{N_d}$	$R_{\rm TOA}$ (W m <sup>-2</sup> )	$S_c$ (W m <sup>-2</sup> )	$\mathcal{L}$ (g m <sup>-2</sup> )
$\beta = 1$	$-0.23$	$-0.24$	1.06	14.59	$-32.23$	21
$\beta = 1.2$	$-0.29$	$-0.31$	1.07	11.79	$-35.28$	30
$\beta = 1.4$	$-0.36$	$-0.38$	1.08	8.80	$-38.51$	41
$\beta = 1.6$	$-0.42$	$-0.46$	1.09	5.82	$-41.78$	56
$\beta$ = 1.79 (reference)	$-0.52$	$-0.57$	1.08	2.89	$-44.95$	73
$\beta = 2$	$-0.58$	$-0.67$	1.17	$-0.23$	$-48.35$	95
$\beta = 2.4$	$-0.65$	$-0.75$	1.15	$-5.50$	$-54.07$	147
$\beta = 2.8$	$-0.68$	$-0.75$	1.10	$-9.31$	$-58.20$	202
$\beta = 3.2$	$-0.67$	$-0.68$	1.01	$-11.72$	$-60.85$	252
$\beta = 3.6$	$-0.64$	$-0.47$	0.75	$-13.11$	$-62.36$	291

<span id="page-16-0"></span>Table S3. Rapid adjustments and cloud state (global mean) across experiments scanning  $\beta$ .<br>This table reprises Table S1 but varies  $\beta$ This table reprises Table [S1](#page-14-0) but varies  $\beta$ .

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