1	Supplementary materials
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3	An application of upscaled optimal foraging theory using hidden Markov modelling: year-
4	round behavioural variation in a large arctic herbivore
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- 22 Figure S1: Distribution of static covariates across the study area (WGS 84, UTM zone 27): (A)
- 23 'hillshade' (unitless), (B) elevation (meters above sea level), (C) terrain ruggedness (index) and (D)
- 24 distance to coast (km). Dark grey background colour indicates ocean areas.





26 Figure S2: Muskox observations classified as either (A) snow-free summer or (B) snow-covered







35

36 Figure S4: Individual variation in movement variables (kernel density estimates of observed step

lengths and turning angles) during the snow-free summer (A-B) and the snow-covered winter season(C-D).



Figure S5: Individual variation in state-dependent distributions for step length and turning angles,
derived from 3-state HMMs, fitted separately for each animal/season. For each model, 10 sets of

42 random starting values were tested; results are shown for the model with highest log-likelihood

43 values. Models did not include covariates.



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45 Figure S6: Histograms of step length and turning angle between hourly relocations, respectively, for 46 the summer season, overlaid with the state-dependent distributions as estimated by initially explored 47 HMMs including 2 (A-B), 3 (C-D), 4 (E-F) and 5 (G-H) states without covariates. We tested 10 sets of starting values for each model, respectively. The state-dependent distributions were weighted 48 49 according to the proportion of time spent in the different states, as inferred by the Viterbi sequence. 50 Dashed black lines indicate the associated marginal observation distributions. Note that the x- and y-51 axes for step length were truncated at the upper range limit to facilitate visualisation (maximum 52 observed step length was 3486 m). Delta BIC values (differences between the respective model and 53 the best-ranked model) are provided in panel titles for model comparison.







Figure S8: Autocorrelation structure in step length for track bursts classified as (A) summer (snow-free) and (B) winter (snow-covered), as
well as in pseudo-residuals for the movement variable step length included in the three-state bivariate HMMs fitted to the muskox movement
data for the (C) summer and (D) winter season (for the best model according to BIC, respectively).



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Figure S9: Distribution (A, C) and quantile-quantile (B, D) plots of the pseudo-residuals for the movement variable step length included in 69 the three-state bivariate HMMs fitted to the muskox movement data for the summer (snow-free) (A, B) and winter (snow-covered) (C, D) season, for the best models according to BIC. 70



Figure S10: Results of the forward model selection process to determine the influence of a total of 14 covariates considered in the HMMs for the (A) summer and (B) winter season, respectively. Covariate selection was based on the Bayesian Information Criterion (BIC). Point labels

74 correspond to differences in BIC values between the respective model and the best-ranked model (i.e. deltaBIC).



Figure S11: Behavioural time allocation in female muskoxen in northeast Greenland depending on
(A) season, (B) light conditions (i.e. daylight or darkness at time of observation) for the summer and

(A) season, (B) light conditions (i.e. daylight or darkness at time of observation) for the summer and
 winter season, respectively, (C) animal ID and (D) Julian Day (i.e. day of the year).



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Figure S12: Probabilities (mean and 95% CI) of behavioural state occupancy as a function of the 82 environmental covariates included in the BIC-selected bivariate HMMs for the (A) summer and (B-F) winter season. Probabilities were calculated for each covariate and state by fixing the values of the 83 84 remaining continuous environmental covariates at their respective seasonal mean. Continuous temporal covariates were set to Julian Day 213 (i.e. August 1st) and 91 (i.e. April 1st) for summer and 85 winter, respectively, and to12 o'clock for time of day. Landcover type was set to sparse vegetation, 86 87 and the remaining categorical covariates to their corresponding reference categories (i.e. daylight, 88 and winter 2013-2014 for winter model). Monte Carlo simulation from the estimator's approximate 89 multivariate normal distribution was used to obtain pointwise 95% CIs.



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91 Figure S13: Probabilities (mean and 95% CI) of behavioural state occupancy as a function of the 92 environmental covariates included in the BIC-selected bivariate HMMs for the (A) summer and (B-93 F) winter season. Probabilities were calculated for each covariate and state by fixing the values of the 94 remaining continuous environmental covariates at their respective seasonal mean. Continuous 95 temporal covariates were set to Julian Day 213 (i.e. August 1st) and 91 (i.e. April 1st) for summer and winter, respectively, and to12 o'clock for time of day. Landcover type was set to dense vegetation, 96 97 and the remaining categorical covariates to their corresponding reference categories (i.e. daylight, 98 and winter 2013-2014 for winter model). Monte Carlo simulation from the estimator's approximate 99 multivariate normal distribution was used to obtain pointwise 95% CIs.



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Figure S14: Probabilities (mean and 95% CI) of behavioural state occupancy as a function of the 101 environmental covariates included in the BIC-selected bivariate HMMs for the (A) summer and (B-102 103 F) winter season. Probabilities were calculated for each covariate and state by fixing the values of the 104 remaining continuous environmental covariates at their respective seasonal mean. Continuous temporal covariates were set to Julian Day 243 (i.e. August 31st) and 91 (i.e. April 1st) for summer 105 and winter, respectively, and to 0 o'clock for time of day. Light was set to darkness, and the 106 remaining categorical covariates to their corresponding reference categories (i.e. bare ground, and 107 108 winter 2013-2014 for winter model). Monte Carlo simulation from the estimator's approximate 109 multivariate normal distribution was used to obtain pointwise 95% CIs.



summer



В

winter



- 12 Figure S15: Maps showing muskox locations state-decoded based on the Viterbi algorithm during the (A) snow-free summer und (B) snow-
- 113 covered winter season, by animal ID. Note that animals may have been tracked for more than one winter/summer season.

114 Table S1: Number of observations, observation days, number of bursts, tracks and animals per season

115 included in analyses of muskox movement behaviour.

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season	n observations	observation days	n bursts	n tracks	n animals
summer 2014	10368	432	10	10	10
summer 2015	4656	194	4	4	4
summer 2016	10120	422	6	6	6
summer 2017	3021	126	3	3	3
winter 2013/14	87074	3628	14	14	14
winter 2014/15	59459	2477	10	10	10
winter 2015/16	44928	1872	20	8	8
winter 2016/17	22752	948	3	3	3
total	242378	10099	70	19	19

118 Table S2: Coefficients (beta and standard error) of the multinomial logistic regression summer model that were used to predict the probability 119 of muskox state occupancy as a function of the BIC-selected covariates (Figure 4 in main manuscript).

120

	state 1 » 2		state 1 » 3		state 2 » 1		state 2 » 3		state 3 » 1		state 3 » 2	
parameter	beta	se	beta	se								
intercept	-0.48	0.72	-3.93	1.91	-0.86	0.41	-3.98	0.82	-9.91	2.54	-1.84	1.15
light*	0.9	0.11	1.39	0.81	-0.61	0.09	-0.03	0.23	1.13	1.77	-0.95	0.28
landcover type*												
sparse vegetation	0.11	0.1	-1.25	0.36	-0.33	0.06	-0.86	0.13	-1.26	0.27	1.11	0.18
dense vegetation	-0.12	0.15	-2.44	1.45	-0.49	0.09	-1.29	0.23	-6.29	10.51	2.6	0.34
ruggedness	-0.04	0.04	-0.1	0.14	0	0.03	-0.42	0.08	0.06	0.1	0.33	0.09
sin(Julian day)	0.46	0.51	0.48	1.01	-0.43	0.26	-1.17	0.49	-3.38	0.93	-1.32	0.71
cos(Julian day)	-1.36	0.59	-2.69	1.73	0.21	0.36	-1.62	0.73	-6.79	1.65	-0.52	1.01

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* Reference category is daylight [light] and bare ground [landcover type]

Table S3: Coefficients (beta and standard error) of the multinomial logistic regression winter model that were used to predict the probability of muskox state occupancy as a function of the BIC-selected covariates (Figure 4 in main manuscript).

	state 1 » 2		state 1 » 3		state 2 » 1		state 2 » 3		state 3 » 1		state 3 » 2	
parameter	beta	se										
intercept	-1.1	0.03	-1.43	0.07	-1.34	0.03	-3.05	0.09	-1.93	0.08	-1.6	0.07
sin(Julian day)	-0.19	0.02	-0.43	0.06	-0.01	0.02	0.0	0.0	0.23	0.07	0.17	0.06
cos(Julian day)	-0.5	0.03	-1.46	0.09	0.1	0.03	-0.36	0.09	0.03	0.1	-0.45	0.09
sin(time of day)	-0.06	0.01	-0.01	0.04	-0.05	0.01	0.07	0.03	-0.13	0.05	-0.26	0.04
cos(time of day)	-0.28	0.02	-1.3	0.06	0.27	0.02	0.01	0.04	0.36	0.05	0.02	0.04
landcover type*												
sparse vegetation	0.19	0.02	-1.06	0.07	0.3	0.02	-0.83	0.06	0.12	0.07	0.93	0.06
dense vegetation	0.08	0.05	-1.48	0.17	0.38	0.05	-1.51	0.14	-0.19	0.32	1.56	0.14
ruggedness	0.07	0.01	-0.4	0.04	-0.07	0.01	-0.27	0.03	-0.04	0.04	0.23	0.03
snow depth	-0.13	0.02	-0.02	0.05	0.12	0.02	-0.43	0.03	0.02	0.05	-0.09	0.04
year*												
winter 2014/15	0.22	0.03	-0.4	0.07	-0.11	0.03	0.52	0.07	0.17	0.08	0.07	0.07
winter 2015/16	0.21	0.03	-0.96	0.1	0.01	0.03	0.49	0.07	0.3	0.09	0.25	0.07
winter 2016/17	0.4	0.04	-0.76	0.11	0.09	0.04	0.31	0.08	0.17	0.12	0.28	0.09
light*	0.36	0.04	-0.85	0.13	-0.13	0.04	0.82	0.12	-0.35	0.1	-0.17	0.09
temperature	0.2	0.02	-0.19	0.05	-0.08	0.02	0.04	0.05	0.01	0.06	-0.06	0.05
distance to sea	-0.03	0.01	0.25	0.03	0	0.01	0.08	0.03	0.01	0.03	-0.09	0.03
wind speed	-0.08	0.01	-0.11	0.03	0.01	0.01	-0.06	0.03	0.1	0.03	0.01	0.03

* Reference category is bare ground [landcover type], winter 2013/14 [year] and daylight [light]