

## SUPPLEMENTAL MATERIALS

**Supplemental Table 1. Model parameters**

Parameter name	Variable	Value*	Unit	Source
<b>Physical characteristics</b>				
Female reference BMI	$BMI_{Fem}^{Ref}$	(0.0417,14.2),(0.125,14.9),(0.208,15.5),(0.292,16),(0.375,16.5),(0.458,16.8),(0.542,17.1),(0.625,17.2),(0.708,17.4),(0.792,17.4),(0.875,17.5),(0.958,17.5),(1.04,17.5),(1.13,17.4),(1.21,17.4),(1.29,17.3),(1.38,17.2),(1.46,17.1),(1.54,17),(1.63,16.9),(1.71,16.8),(1.79,16.7),(1.88,16.5),(1.96,16.4),(2,16.4),(2.29,16.2),(2.79,15.8),(3.29,15.6),(3.79,15.4),(4.29,15.2),(4.79,15.2),(5.29,15.2),(5.79,15.2),(6.29,15.3),(6.79,15.4),(7.29,15.5),(7.79,15.7),(8.29,15.9),(8.79,16.2),(9.29,16.4),(9.79,16.7),(10.3,17),(10.8,17.3),(11.3,17.6),(11.8,17.9),(12.3,18.3),(12.8,18.6),(13.3,18.9),(13.8,19.2),(14.3,19.5),(14.8,19.8),(15.3,20.1),(15.8,20.3),(16.3,20.6),(16.8,20.8),(17.3,21),(17.8,21.2),(18.3,21.4),(18.8,21.5),(19.3,21.6),(19.8,21.7),(20,21.7)	Age in Year, Kg/M <sup>2</sup> (Age, BMI)	(1)
Male reference BMI	$BMI_{Mal}^{Ref}$	(0.0417,14.4),(0.125,15.2),(0.208,16),(0.292,16.6),(0.375,17.1),(0.458,17.5),(0.542,17.7),(0.625,17.9),(0.708,18),(0.792,18.1),(0.875,18.1),(0.958,18.1),(1.04,18.1),(1.13,18),(1.21,17.9),(1.29,17.8),(1.38,17.6),(1.46,17.5),(1.54,17.4),(1.63,17.2),(1.71,17.1),(1.79,17),(1.88,16.8),(1.96,16.7),(2,16.6),(2.29,16.4),(2.79,16.1),(3.29,15.9),(3.79,15.7),(4.29,15.6),(4.79,15.5),(5.29,15.4),(5.79,15.4),(6.29,15.4),(6.79,15.5),(7.29,15.6),(7.79,15.7),(8.29,15.9),(8.79,16.1),(9.29,16.3),(9.79,16.5),(10.3,16.8),(10.8,17.1),(11.3,17.3),(11.8,17.7),(12.3,18),(12.8,18.3),(13.3,18.6),(13.8,19),(14.3,19.3),(14.8,19.7),(15.3,20),(15.8,20.4),(16.3,20.7),(16.8,21.1),(17.3,21.4),(17.8,21.7),(18.3,22.1),(18.8,22.4),(19.3,22.6),(19.8,22.9),(20,23)	Age in Year, Kg/M <sup>2</sup> (Age, BMI)	(1)
Female reference height	$H_{Fem}^{Ref}$	(0.0417,51.7),(0.125,55.3),(0.208,58.1),(0.292,60.5),(0.375,62.5),(0.458,.64.4),(0.542,66.1),(0.625,67.7),(0.708,69.2),(0.792,70.6),(0.875,71.9),(0.958,73.2),(1.04,74.4),(1.13,75.6),(1.21,76.7),(1.29,77.8),(1.38,78.8),(1.46,79.8),(1.54,80.8),(1.63,81.8),(1.71,82.7),(1.79,83.6),(1.88,84.5),(1.96,85.3),(2,85),(2.29,88),(2.79,92.4),(3.29,95.9),(3.79,99.3),(4.29,103),(4.79,106),(5.29,110),(5.79,113),(6.29,117),(6.79,120),(7.29,123),(7.79,126),(8.29,129),(8.79,132),(9.29,134),(9.79,137),(10.3,140),(10.8,143),(11.3,146),(11.8,150),(12.3,153),(12.8,156),(13.3,158),(13.8,160),(14.3,161),(14.8,162),(15.3,162),(15.8,162),(16.3,163),(16.8,163),(17.3,163),(17.8,163),(18.3,163),(18.8,163),(19.3,163),(19.8,163)	Age in Year, cm (Age, height)	(1)
Male reference height	$H_{Mal}^{Ref}$	(0.0417,52.7),(0.125,56.6),(0.208,59.6),(0.292,62.1),(0.375,64.2),(0.458,.66.1),(0.542,67.9),(0.625,69.5),(0.708,70.9),(0.792,72.3),(0.875,73.7),(0.958,74.9),(1.04,76.1),(1.13,77.3),(1.21,78.4),(1.29,79.4),(1.38,80.5),(1.46,81.4),(1.54,82.4),(1.63,83.3),(1.71,84.2),(1.79,85.1),(1.88,86),(1.96,86.8),(2,86.5),(2.29,89.2),(2.79,93.4),(3.29,97.2),(3.79,101),(4.29,104),(4.79,108),(5.29,111),(5.79,114),(6.29,117),(6.79,120),(7.29,124),(7.79,127),(8.29,130),(8.79,132),(9.29,135),(9.79,138),(10.3,140),(10.8,142),(11.3,145),(11.8,148),(12.3,151),(12.8,154),(13.3,158),(13.8,162),(14.3,166),(14.8,169),(15.3,171),(15.8,173),(16.3,174),(16.8,175),(17.3,176),(17.8,176),(18.3,176),(18.8,177),(19.3,177),(19.8,177)	Age in Year, cm (Age, height)	(1)
Female reference fat mass index	$FMI_{Fem}^{Ref}$	(0,1.92),(0.25,5.16),(0.5,5.52),(0.75,4.9),(1,4.62),(1.5,4.27),(2,3.97),(3,3.66),(4,3.38),(5,3.3),(6,3.54),(7,3.77),(8,4.01),(9,4.24),(10,4.46),(11,4.68),(12,4.9),(13,5.11),(14,5.32),(15,5.51),(16,5.7),(17,5.88),(18,6.05),(19,6.21),(20,6.37),(80,6.55)	Age in Year, Kg/M <sup>2</sup> (Age, FMI)	(2-4)
Male reference fat mass index	$FMI_{Mal}^{Ref}$	(0,1.6),(0.25,5.1),(0.5,5.03),(0.75,4.49),(1,4.42),(1.5,4.15),(2,4.04),(3,3.54),(4,3.21),(5,2.84),(6,2.65),(7,2.45),(8,2.54),(9,2.98),(10,3.37),(11,3.52),(12,3.4),(13,3.18),(14,3.02),(15,2.9),(16,2.84),(17,2.9),(18,3.14),(19,3.55),(20,4.01),(80,5.31)	Age in Year, Reference FMI in Kg/M <sup>2</sup> (Age, FMI)	(2-4)
Female reference fractional cellularity	$CL_{Fem}^{Ref}$	(0,0.85),(1,0.894),(2,0.928),(3,0.947),(4,0.958),(5,0.966),(6,0.974),(7,0.98),(8,0.988),(9,0.997),(10,1),(20,1),(80,0.895)	Age in Year, Reference Fractional Cellularity	(5)
Male reference fractional cellularity	$CL_{Mal}^{Ref}$	(0,0.8),(1,0.83),(2,0.871),(3,0.897),(4,0.918),(5,0.934),(6,0.946),(7,0.957),(8,0.968),(9,0.979),(10,0.99),(11,1),(20,1),(80,0.825)	Age in Year, Reference Fractional Cellularity	(5)
Fractional weight of the four active organs	$\sum_{i=1}^4 \frac{M_i^{Ref}}{BW^{Ref}}$	(0,0.152),(1,0.145),(2,0.132),(3,0.124),(4,0.119),(5,0.106),(6,0.0984),(7,0.0917),(8,0.0833),(9,0.0803),(10,0.077),(11,0.0732),(12,0.0707),(13,0.0663),(14,0.062),(15,0.0592),(16,0.0578),(17,0.0566),(18,0.0573),(20,0.0543)	kg	(6)

Female reference physical activity level	$PAL_{Fem}^{Ref}$	(0,1.3),(1.5,1.42),(2.5,1.42),(3.5,1.44),(4.5,1.49),(5.5,1.53),(6.5,1.56),(7.5,1.6),(8.5,1.63),(9.5,1.66),(10.5,1.71),(11.5,1.74),(12.5,1.76),(13.5,1.76),(14.5,1.75),(15.5,1.73),(16.5,1.73),(17.5,1.72),(20,1.62),(30,1.48),(40,1.41),(50,1.36),(60,1.32),(70,1.28),(80,1.25)	Age in Year, Reference physical activity level (dimensionless)	(4, 7)
Male reference physical activity level	$PAL_{Mal}^{Ref}$	(0,1.3),(1.5,1.43),(2.5,1.45),(3.5,1.44),(4.5,1.49),(5.5,1.53),(6.5,1.57),(7.5,1.6),(8.5,1.63),(9.5,1.66),(10.5,1.71),(11.5,1.75),(12.5,1.79),(13.5,1.82),(14.5,1.84),(15.5,1.84),(16.5,1.84),(17.5,1.83),(20,1.75),(30,1.55),(40,1.45),(50,1.38),(60,1.33),(70,1.3),(80,1.27)	Age in Year, Reference physical activity level (dimensionless)	(4, 7)
<b>Energy needs and densities</b>				
BMR contribution of Brain, Kidneys, Liver, Heart based on organ specific weights	$\sum_{i=1}^4 \frac{M_i^{Ref}}{\gamma_i \cdot BW^{Ref}}$	$Max(31.4 + 189.9e^{-0.107 \cdot age}, 59.05)$	KJ/Kg/day	(5)
Maximum energy density of lean mass	$\rho_L^{Adult}$	5000	KJ/Kg	(8)
Minimum energy density of lean mass	$\rho_L^{Base}$	3514	KJ/Kg	(8)
Slope of lean mass energy density with respect to lean mass	$\alpha_\rho$	18	KJ/Kg <sup>2</sup>	(8)
Energy density of fat mass	$\rho_F$	39500	KJ/Kg	(9)
Energy need for turnover of lean mass	$\eta_L$	960	KJ/Kg	(9)
Energy need for turnover of fat mass	$\eta_F$	750	KJ/Kg	(9)
Energy requirements of active organs	$\gamma_{\Delta L}$	92	KJ/Kg/Day	(9)
Energy requirement of structural muscle and other residual lean tissue	$\gamma_5$	54	KJ/Kg/Day	(5, 10)
Energy requirements for unit fat mass	$\gamma_F$	13	KJ/Kg/Day	(9)
<b>Other Factors</b>				
Growth projection horizon	$d$	0.02	Year	
Time to consume or adjust body mass reserves	$\tau$	30	Days	
Slope of height growth rate reaction to relative BMI	$s_H$	8	Dimensionless	
Maximum catch up growth rate relative to normal height growth for age	$v_H$	4	Dimensionless	(11)
Energy partitioning factor	$c$	10.4	Kg	Based on Forbes partitioning equation (12)

Fat mass fraction of active metabolic organs	$f_{FM}$	0.1	Dimensionless	(5)
Thermic cost of eating	$\beta$	0.1	Dimensionless	(9)
Weight of WHO based projection on desired weight	$sb$	0.5	Dimensionless	
Adaptive thermogenesis effect	$\beta_T$	0.14	Dimensionless	(9)

\*Simulations use linear interpolation between data-points reported in the table.

## References

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