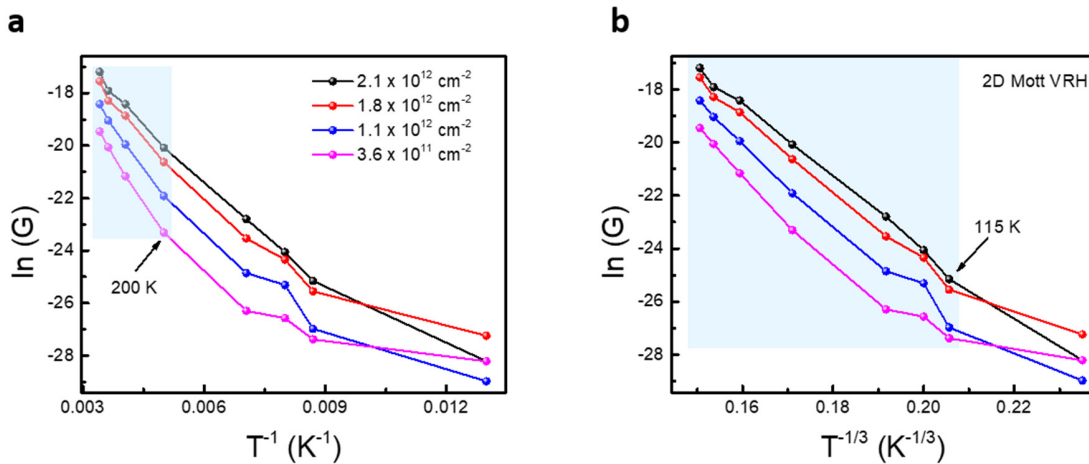


Supplementary Information for
“Probing magnetism in atomically thin semiconducting PtSe₂”

Avsar et al.

Supplementary Note 1. Observation of variable range hopping in PtSe₂ monolayer up to room temperature

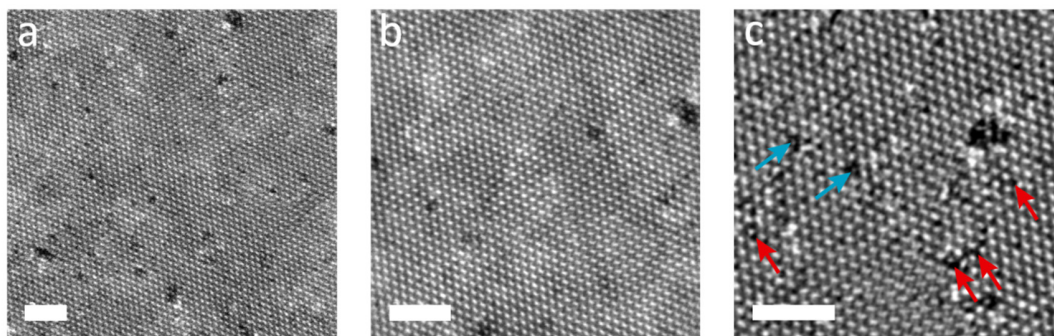
To shed light on the mechanism of charge transport in monolayer PtSe₂, we study the temperature dependence of conductivity. Supplementary Figure 1a shows the Arrhenius plot of the recorded conductivity as a function of carrier concentration. Strong deviation of the data from linearity indicates that the electron transport cannot be fully explained by thermally activated transport. Our device is extremely insulating below 115 K as shown in Fig. 1d. Above this temperature range, it starts to be more conductive and $\ln(G)$ has a linear dependence on $T^{-1/3}$ up to room temperature which is the indication of 2D variable range hopping (VRH) conduction (Supplementary Figure 1b).¹⁻⁴ Similar transport characteristics have been previously observed for several 2D crystals including MoS₂^{1,3,4} and disordered graphene nanoribbons⁵ and this indicates the presence of high concentration of defects which were directly imaged in our crystals by TEM as shown in Supplementary Figure 2 & 4.



Supplementary Figure 1. **a**, $\ln(G)$ plotted against inverse of temperature for the monolayer PtSe₂ device. **b**, $\ln(G)$ plotted against $T^{-1/3}$ for the same device. Shaded areas represent the linear regimes.

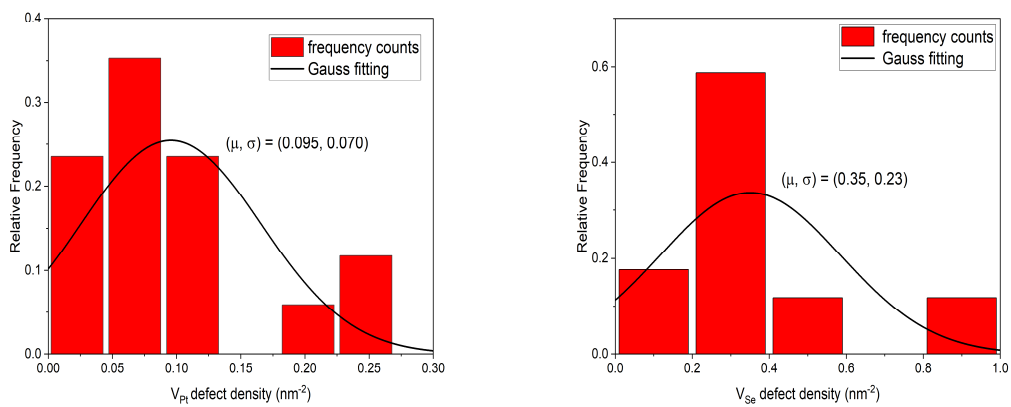
Supplementary Note 2. Estimation of defect concentration in bilayer PtSe₂

Due to the ADF-STEM contrast dependency, the intensity of the atomic columns is proportional to the atomic number. Thus, the position of Pt (brighter) and Se (slightly darker) atoms can be directly interpreted by their intensities. Supplementary Figure 2a shows the clean large area of bilayer PtSe₂ lattice. To avoid the e-beam induced damage, a low beam current (18 pA) was used. Total e-beam doses for Supplementary Figure 2 a-c are 0.7×10^7 , 0.33×10^7 and 0.17×10^7 e per nm², respectively. However, it varies to 2.8×10^7 e per nm² for the Fig. 1b in main manuscript. The magnified images from the same regions shows the atomic defect structures in the lattice.



Supplementary Figure 2. STEM image acquired in a bilayer PtSe₂. Scanned area magnifies as it goes from a-to-c. Some of Pt (Se) point defects are highlighted with blue (red) colored arrows in c. Scale bars in a-c are 2 μ m.

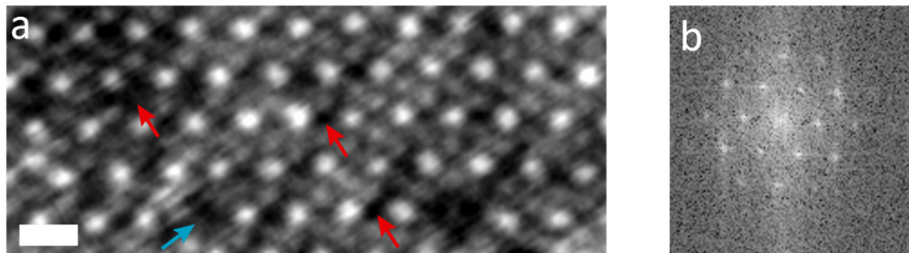
To measure the defect concentration, total number of missing Pt and Se atoms were counted directly using ImageJ. Total number of missing Pt and Se atoms in bilayer PtSe₂ were 79 and 278, respectively. Total measured area was 1095.81 nm². This corresponds to the Pt defect density $(0.9 \pm 0.06) \times 10^{13}$ cm⁻², whereas the Se defect concentration is $(3.5 \pm 0.2) \times 10^{13}$ cm⁻². Frequency distribution histograms for both Pt and Se are shown in Supplementary Figure 3. Here, we would like to also note that we have not observed any intercalates or crystalline phases other than the 1T phase.



Supplementary Figure 3. Frequency distribution histograms for both Pt and Se vacancies.

Supplementary Note 3. TEM investigation of monolayer PtSe₂

Supplementary Figure 4 shows the STEM image of monolayer PtSe₂. As in the bilayer PtSe₂ case (Fig. 1b and Supplementary Figure 2), both Pt and Se point defects exist in monolayer PtSe₂. Total e-beam dose for Supplementary Figure 4 is 2.7×10^7 e per nm²

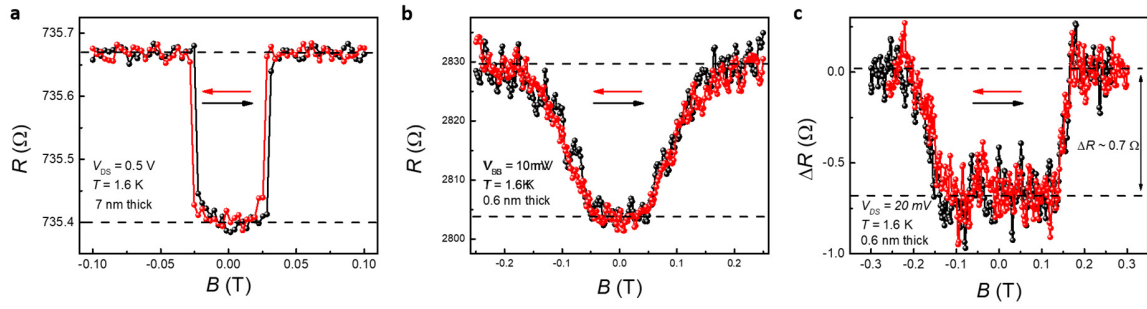


Supplementary Figure 4. (a) STEM image acquired in a monolayer PtSe₂. Some of Pt (Se) point defects are highlighted with blue (red) colored arrows. Scale bar is 1 μ m. (b) Corresponding fast Fourier transform shows its crystalline structure.

Supplementary Note 4. Hysteresis in monolayer PtSe₂-based devices

We performed the direction dependent magneto-transport measurements on monolayer PtSe₂ (see Supplementary Figure 5b). Unlike metallic devices where we observe a small hysteresis as shown in Supplementary Figure 5a, we do not observe hysteresis in this semiconducting device, most likely due to higher noise to signal ratio compared to metallic devices. To double check this, we have fabricated and characterized an additional monolayer PtSe₂-based tunneling device in which the magnetic response was probed measuring the adjacent graphene layer as in Fig. 3c (Supplementary Figure 5c). While we observe a similar magneto-transport response with two clear plateaus, this device also shows little to no hysteresis. This could be related to the absence of net perpendicular anisotropy as our ribbon-type crystals have an in-plane spin orientation due to its shape anisotropy which could be compensating the magneto-crystalline anisotropy of the crystal that normally favors an out-of-plane spin orientation.⁶

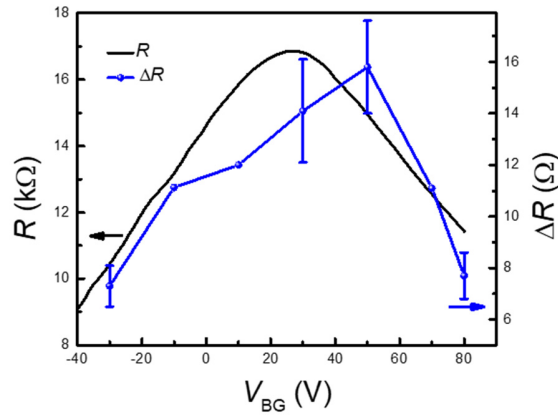
We would like to note that hysteresis in bilayer CrI₃ which has similarly antiferromagnetic ground state ordering is also challenging to observe below the Neel temperature, e.g. it was absent in previous magneto-optical Kerr effect microscopy measurements conducted at 15 K, much below its Curie temperature of ~ 61 K.^{6,7} Detailed temperature dependent tunneling experiments also confirm that hysteresis can only be probed at low temperatures [see Supplementary Figure 4 of Ref. 8]. The origin of this remains poorly understood. Here, we would like to note that the Curie temperature of PtSe₂ (typically ~ 5 K⁹) is much smaller than CrI₃ (~ 61 K) and probing the hysteresis is therefore even more challenging.



Supplementary Figure 5. Magnetic field dependence of the device resistances measured at $T = 1.6$ K, obtained from (a) a 7 nm thick PtSe₂-based lateral device, (b) a 0.6 nm thick PtSe₂-based tunneling device and (c) another 0.6 nm thick PtSe₂-based device. While lateral metallic device is contacted using Pd, tunneling devices utilize graphene (Pd) as a bottom (top) contact. Red and black arrows represent the magnetic field sweep directions.

Supplementary Note 5. Gate dependence of induced magnetization in graphene

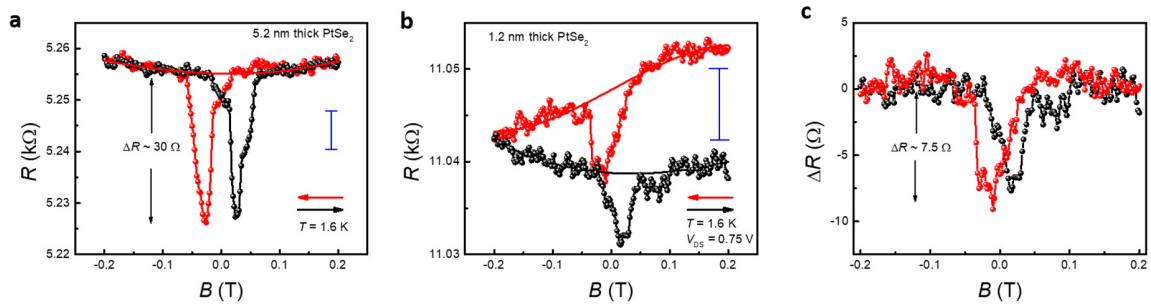
Supplementary Figure 6 shows the back-gate voltage dependences of the device resistance and the change in the device resistance, ΔR , under magnetic field, measured in a monolayer graphene utilizing bilayer PtSe₂ as the substrate. Similarly to the device resistance, ΔR also shows the maximum value near the Dirac point of graphene. MR percentage is found to be $\sim 0.1\%$ and is almost back-gate voltage independent.



Supplementary Figure 6. Dependence of the change in device resistance and device resistance on the back-gate voltage at fixed bias of $V_{SD} = 1$ V. Measurements were taken at $T = 1.6$ K.

Supplementary Note 6. Background signal

For the device characterized in Fig. 3d, the background signal in these MR sweeps are direction dependent in contrast to our previous metallic devices (Supplementary Figure 7a-b).⁹ While the origin of this is not clear at this point, this makes the successful demonstration of minor loop sweeps as in our previous work with metallic devices⁹ nearly impossible as the amplitude of signal is comparable to the background level. This is also partly because the magnitude of the maximum change in device resistance in bilayer PtSe₂-based device is significantly smaller (by nearly a factor of 50) than what we observed in metallic samples.



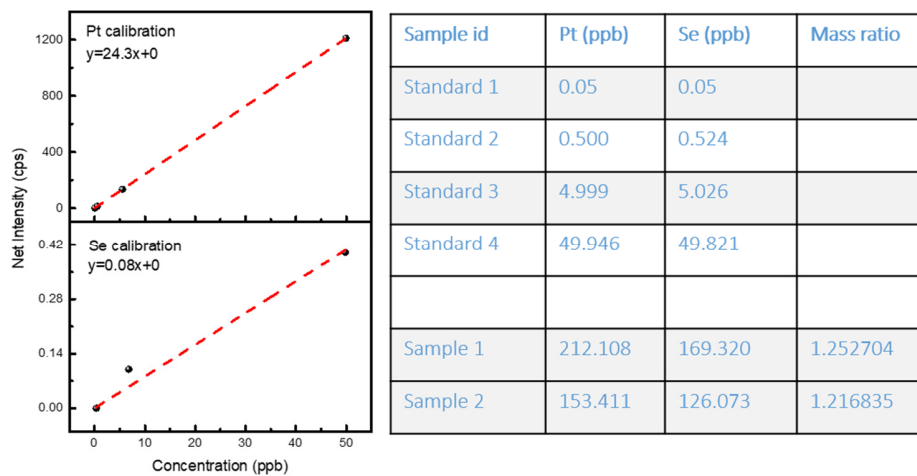
Supplementary Figure 7. Magnetic field dependence of the device resistances measured at $T = 1.6 \text{ K}$, obtained from (a) a 5.2 nm thick PtSe₂-based lateral device, (b) a 1.2 nm thick PtSe₂-based tunneling device. Scale bars shown in these plots are 7.5 Ω . (c) The same with (b), after removing the background signal. Red and black arrows represent the field sweep direction.

Supplementary Note 7. Trace elemental analysis of PtSe₂

We studied the Inductively coupled plasma mass spectroscopy (ICP-MS) (NexIon 350 D instrument, Perkin Elmer) response of our CVT grown crystals for trace elemental analysis of PtSe₂. Two samples that were grown under different runs by the manufacturer (HQ graphene) were investigated (Supplementary Figure 8).

We first performed a quantitative assessment of our samples, which did not show the presence of any chemical elements except for Pt and Se. This unambiguously proves that our crystals are not contaminated with foreign elements, in line with our previous EDX⁹ and TEM measurements. Furthermore, we would like to remark that the powder X-ray diffraction (XRD) provided by the manufacturer do not show any contamination by foreign atoms either. A copy of the XRD certificate from the manufacturer can be accessed at the Ref. 10. XRD 2 theta peak of (001) crystal plane of PtSe₂ is at 17.5degree, which matches well with the reported XRD analysis from other similarly grown PtSe₂.¹¹

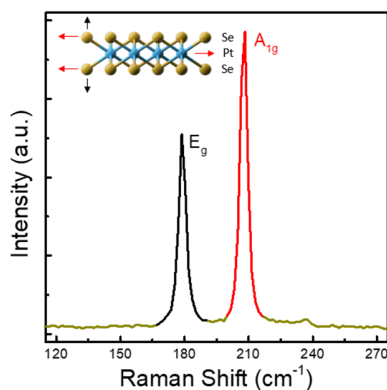
Next, we carried out a precise analysis to determine the mass ratios between Pt and Se atoms. To this end, calibration curves of platinum based on its isotope 195, and selenium based on its isotope 82 were obtained (See Supplementary Figure 8). The calculated mass (weight) Pt-to-Se ratio for sample 1 and 2 are 1.253 and 1.217, respectively which are closely matching the theoretical mass ratio of 1.235-to-1 for PtSe₂. To determine the errors of the measurement, we performed 5 repetitions on the same digested sample. Also note that each measurement by the instrument is already composed of triplicates, i.e. three individual passes. Calculated average mass ratio is 1.246 with a relative standard deviation of 1.4 %. Therefore, the difference between theory and experiment in percentage is only 0.84 %.



Supplementary Figure 8. Bottom and top insets show the calibration curves for Selenium (Se) and Platinum (Pt). Table represents the concentration of Se and Pt that were measured in the solutions resulted from digestion. Calculated mass ratios for both samples are also provided in the table.

Supplementary Note 8. Raman spectroscopy measurements of ultra-thin PtSe₂

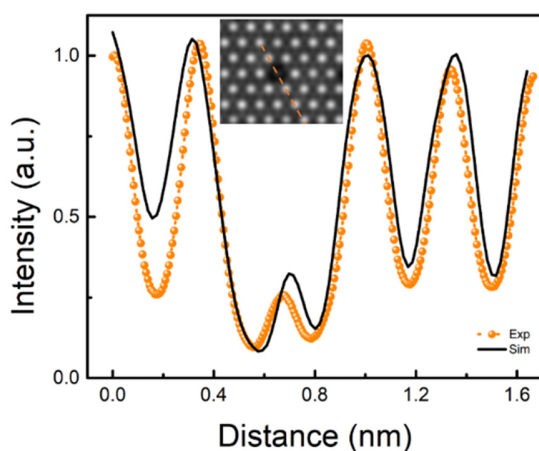
In order to determine the crystalline phase of our crystal, we have performed Raman spectroscopy measurements. Raman spectra show two different vibrational modes of comparable intensities at ~ 178 and 208 cm^{-1} (Supplementary Figure 9). These characteristic Raman peaks are assigned to E_g and A_{1g} modes respectively, with vibration modes illustrated in the inset of Supplementary Figure 9. The Raman response of our crystal is thus consistent with the one obtained from similar CVT-grown PtSe₂ which was later demonstrated to be 1T phase on the basis of direct TEM imaging measurements.^{11,12} Our TEM studies also show the presence of 1T phase in our crystals, therefore consistent with the literature.



Supplementary Figure 9. Raman spectra of PtSe₂. Inset shows the crystal structure of monolayer PtSe₂. Red (black) arrows represent the oscillation direction of A_{1g} (E_g) phonons.

Supplementary Note 9. TEM simulation of bilayer PtSe₂

Prior to TEM scans, we perform AFM to determine the thickness of the investigated flakes. As mentioned in the Methods section, we use < 1% KOH solution to avoid or minimize any structural modification or degradation during sample transfer. To minimize the effect of electron-beam induced knock-on damage, a low acceleration voltage (80 kV) and a very short exposure time is used for all the experiments. To compare with the measured intensities across the dotted line shown in Fig. 1b, we performed STEM image simulations for a bilayer PtSe₂ by using the Dr. Probe software package.¹³ The simulation parameters were chosen similar to the experimental conditions and details are given in the Methods section. As can be seen in Supplementary Figure 10, the line profile depicted in Fig. 1b with a single Pt vacancy can be fitted to this theoretical profile of electron transmission for bilayer PtSe₂.



Supplementary Figure 10: Distance dependence of the intensity measured from a bilayer PtSe₂ and its simulated intensity. Inset shows the STEM image simulation for bilayer PtSe₂. Following the dashed orange line, we extract the simulated intensity.

Supplementary Note 10. Additional first-principles calculations

Density Functional	$E_{AFM} - E_{FM}$ (meV) (w/o SOC)	$E_{AFM} - E_{FM}$ (meV) (w SOC)
LDA	-42	-32
PBE	-29	-35
PBEsol	-3	-7
PW91	-63	-65
revPBE	-34	-44

Supplementary Table 1. Difference in energy between the antiferromagnetic (AFM) and ferromagnetic (FM) configurations for a 4×4 supercell of monolayer PtSe₂ hosting a Pt vacancy defect, as calculated using different local (LDA¹⁴) and semi-local (PBE,¹⁵ PBEsol,¹⁶ PW91,¹⁷ revPBE¹⁸) exchange-correlation density functionals, either without and with spin-orbit coupling (SOC). Irrespective of the adopted functional, the AFM configuration is found to be the stable solution. In addition, the metastable FM configuration exhibits a local magnetic moment of 4.00 μ_B , in contrast to the findings of Ref. [19].

Density Functional	$E_{AFM} - E_{NM}$ (meV)
LDA	-8
PBE	-89
PBEsol	-64
PW91	-27
revPBE	-94

Supplementary Table 2. Difference in energy between the antiferromagnetic (AFM) and non-magnetic (NM) configurations for a 4×4 supercell of monolayer PtSe₂ hosting a Pt vacancy defect, as calculated using different local (LDA¹⁴) and semi-local (PBE,¹⁵ PBEsol,¹⁶ PW91,¹⁷ revPBE¹⁸) exchange-correlation density functionals. Irrespective of the adopted functional, the AFM configuration is found to be lower in energy as compared to the NM configuration.

Supercell Size	$E_{\text{AFM}} - E_{\text{FM}}$ (meV) (w/o SOC)	$E_{\text{AFM}} - E_{\text{FM}}$ (meV) (w SOC)
3×3	-8	-14
4×4	-29	-35
5×5	-43	-47
6×6	-44	-50

Supplementary Table 3. Difference in energy between the antiferromagnetic (AFM) and ferromagnetic (FM) configurations for monolayer PtSe₂ hosting a Pt vacancy defect for different supercell sizes, as calculated using the PBE exchange-correlation functional,¹⁵ either without and with spin-orbit coupling (SOC). Irrespective of the supercell size, the AFM configuration is found to be the stable solution.

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