

Supporting Information

# An Insight into the Excitation States of Small Molecular Semiconductor Y6

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## **1. Computational details**

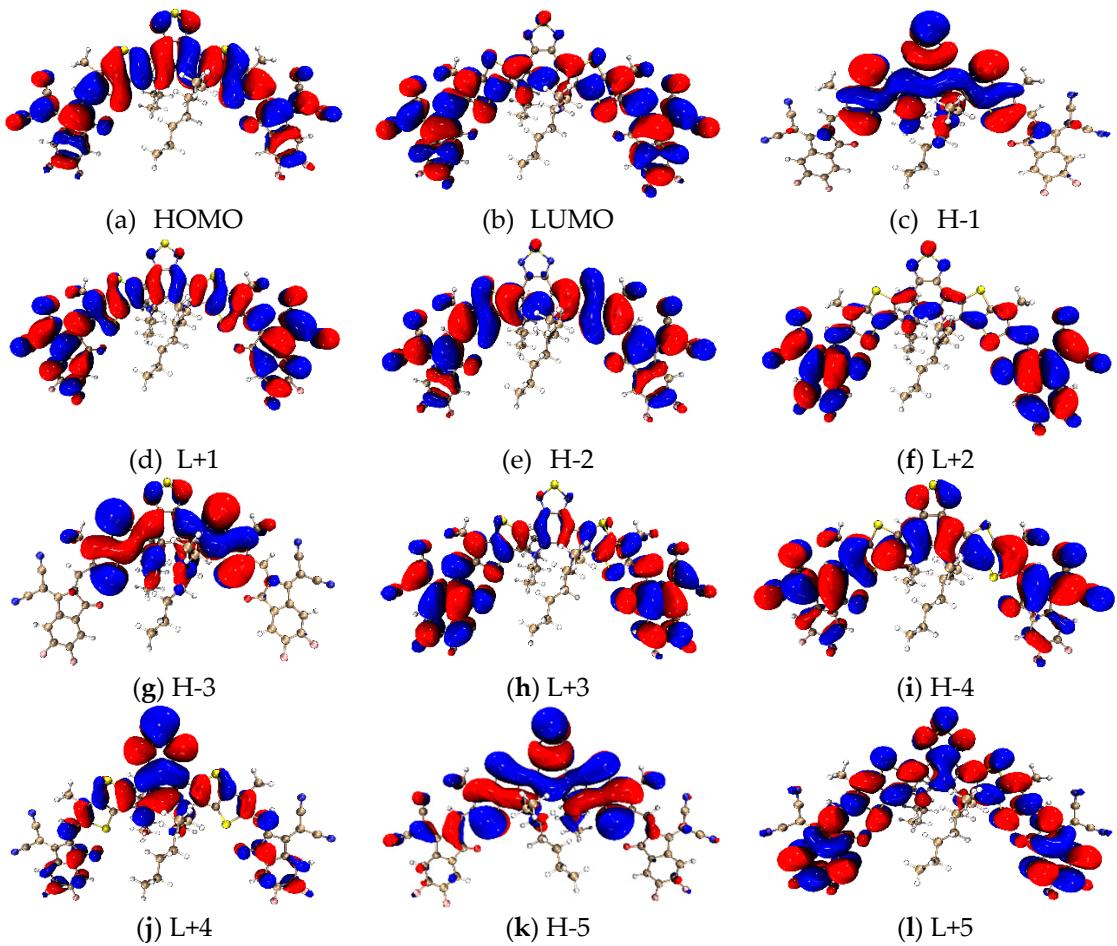
The original 3-dimensional chemical structure of Y6 was drawn in the open-source molecular editor software package ChemBio3D Ultra 12.0 (Cambridge Inc.). In order to reduce the computational costs, the long alkyl chains of the central unit are replaced by methyl groups. The geometry structure optimization of the ground state of Y6 was performed using density functional theory (DFT) with the hybrid Becke 3-parameter Lee-Yang-Parr (B3LYP) functional [1] and the Pople-style double zeta and one polarization function basis set (6-31G\*) [2]. After that time-dependent density functional theory (TD-DFT) calculations were carried out to optimize the geometry of excited state with B3LYP/6-31G\*. All the DFT and TD-DFT calculations were carried out employing Gaussian 16 Revision B.01 [3]. Moreover, the single point energy of the ten lowest energy of excited states was calculated by TD-DFT using the polarizable continuum model (PCM) with the dielectric constant of 4.7113 at the level of B3LYP functional with 6-31G\* basis set and a balanced basis set of triple zeta valence quality with two sets of polarization function (Def2-TZVPP) [4]. The dominant particle-hole pair contributions and the associated weights were calculated through the natural transition orbitals (NTOs) [5] so as to evaluate the properties of electronic transitions from ground state to excited states. Finally, based on the output files of TD-DFT method, multifunctional wavefunction analyzer (Multiwfn) version 3.7 [6] and VMD version 1.9.3 [7] were used to get more transition information such as the theoretical UV-vis absorption and fluorescence spectrum, the electron density of frontier molecular orbitals (FMOs), major molecular orbital (MO) transitions in all excited states, natural transition orbitals (NTOs), the overlap of electron-hole distribution of excited states [8] and the presentation of the electron density difference between excited and ground state.

## 2. TD-DFT with B3LYP/Def2-TZVPP

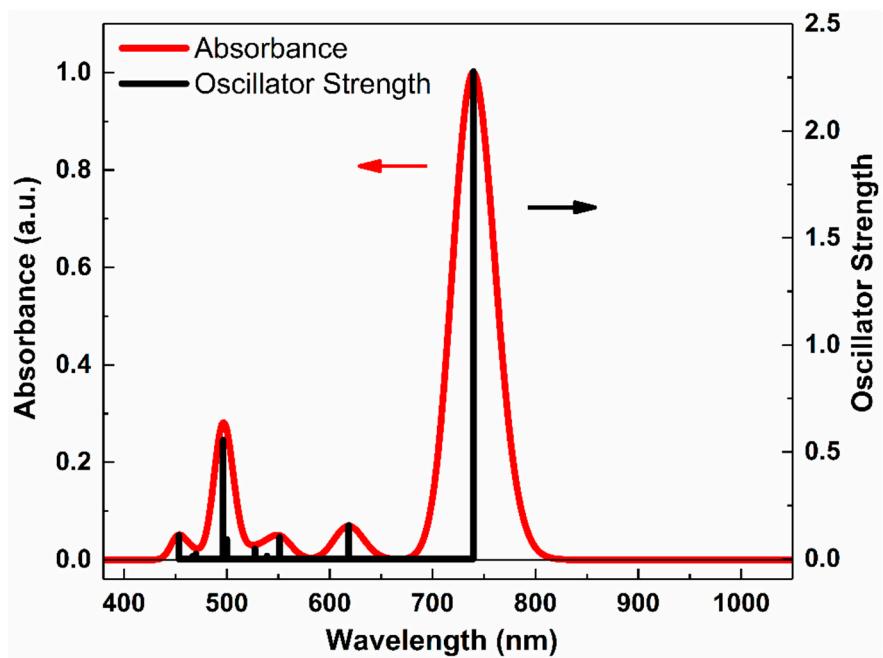
**Table S1.** Computed positions and oscillator strength ( $f$ ) of the 10 lowest-energy electronic transitions of Y6 solution by TD-DFT at B3LYP/Def2-TZVPP level of theory.

State	$\lambda_{\text{cal}}$ (eV, nm)	$f^{\text{a}}$	Excitation contribution <sup>b</sup> (%)
S <sub>1</sub>	1.68 (739)	2.2771	H→L (98.5)
S <sub>2</sub>	2.00 (618)	0.1572	H→L+1 (96.5)
S <sub>3</sub>	2.25 (539)	0.1024	H→L+2 (96.1)
S <sub>4</sub>	2.30 (539)	0.0137	H-1→L (92.6)
S <sub>5</sub>	2.35 (527)	0.0471	H→L+3 (79.8), H-2→L (15.0)
S <sub>6</sub>	2.48 (500)	0.0916	H-3→L (50.1), H-1→L+1 (43.8)
S <sub>7</sub>	2.50 (496)	0.5543	H-2→L (76.6), H→L+3 (15.1)
S <sub>8</sub>	2.64 (470)	0.0229	H-1→L+1 (47.9), H-3→L (36.6), H→L+4 (8.8)
S <sub>9</sub>	2.66 (467)	0.0127	H→L+4 (74.8), H-2→L+1 (9.5), H-3→L (9.2)
S <sub>10</sub>	2.74 (453)	0.1106	H-2→L+1 (80.3), H→L+4 (13.6)

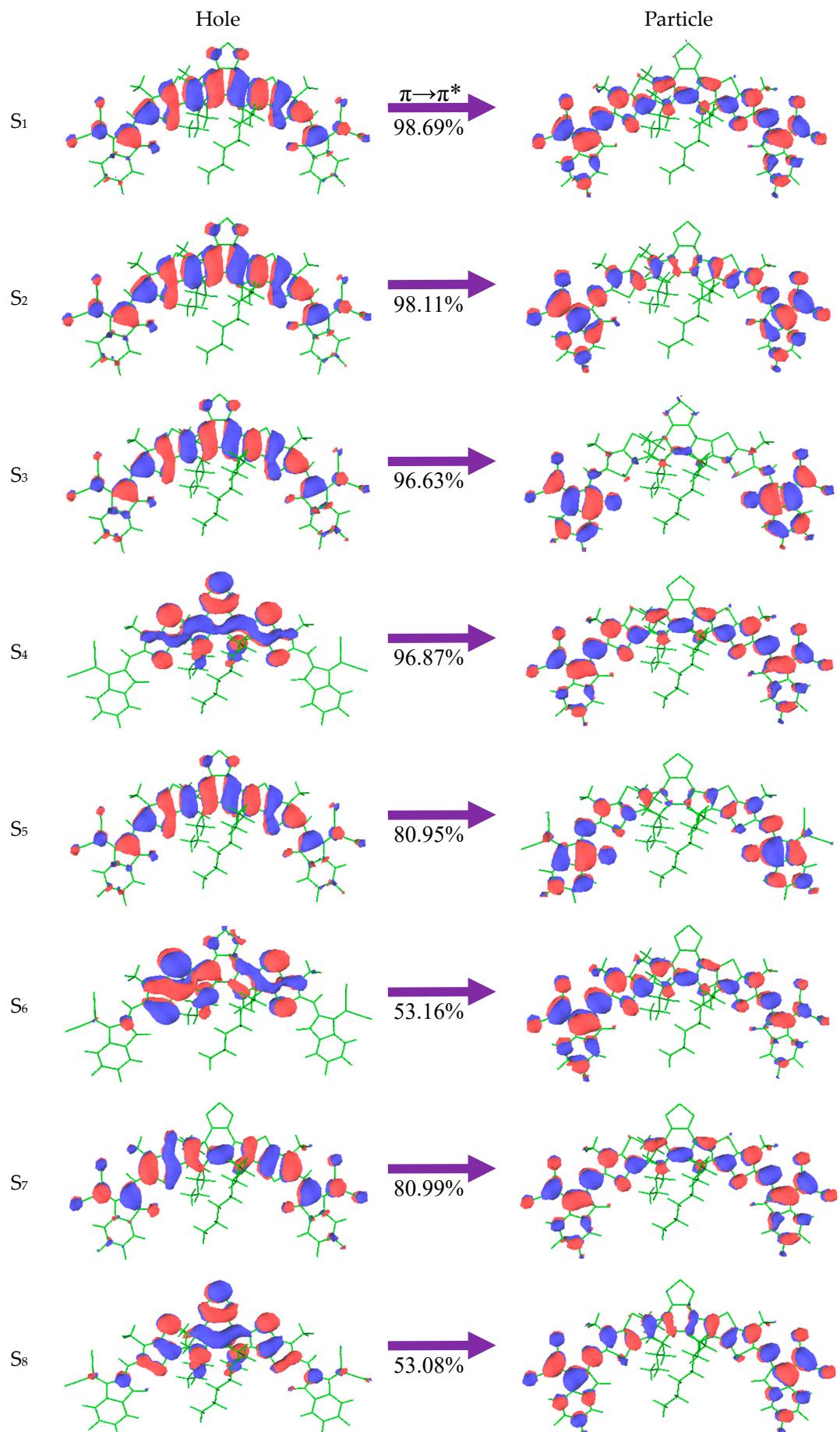
<sup>a</sup>Oscillator strengths. <sup>b</sup>H=HOMO, L=LUMO, H-1=HOMO-1, L+1=LUMO+1.



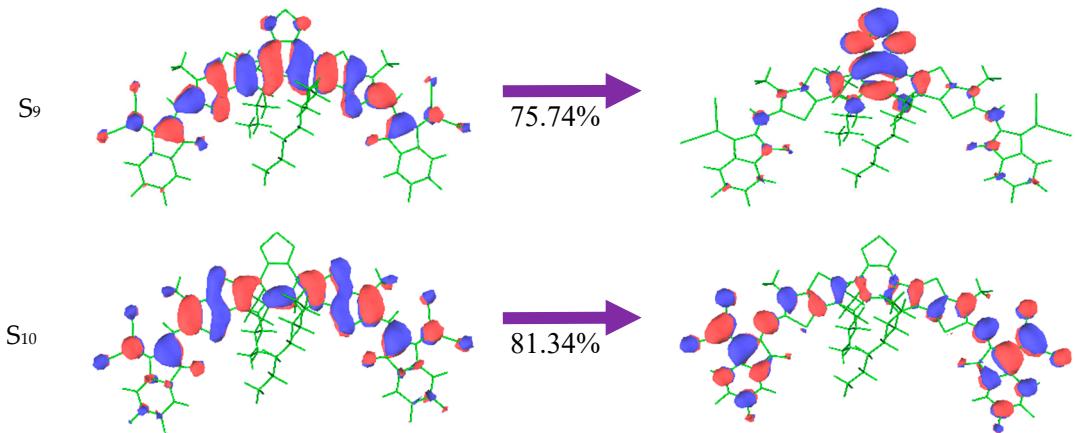
**Figure S1.** Electron density contours of (a) HOMO, (b) LUMO, (c) HOMO-1, (d) LUMO+1, (e) HOMO-2, (f) LUMO+2, (g) HOMO-3, (h) LUMO+3, (i) HOMO-4, (j) LUMO+4, (k) HOMO-5, (l) LUMO+5 of Y6 solution by TD-DFT at B3LYP/Def2-TZVPP level of theory. The isosurface value was set at 0.01 a.u..



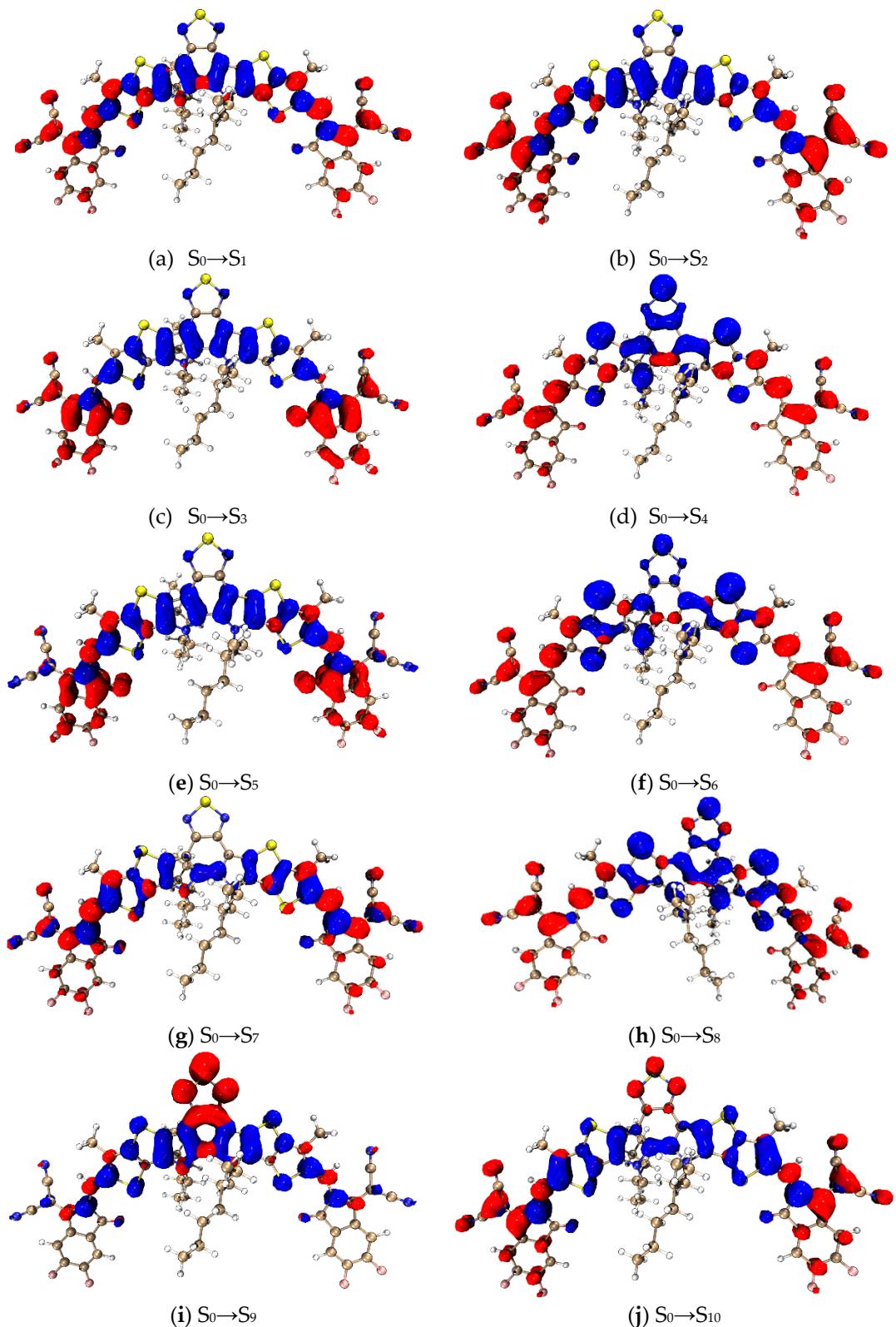
**Figure S2.** Simulated UV-vis absorption spectrum (red curve) and oscillator strength (black spikes) of the Y6 solution by TD-DFT at B3LYP/Def2-TZVPP level of theory. A Gaussian function with a full width at half-maximum (FWHM) of 0.11 eV was employed.



**S5**



**Figure S3.** Computed natural transition orbital pairs for S<sub>1</sub>-S<sub>10</sub> of Y6 by TD-DFT at the level of B3LYP/Def2-TZVPP. The isosurface value was set at 0.018 a.u..



**Figure S4.** The overlap of electron-hole isosurface density maps between (a)  $S_0$  and  $S_1$ , (b)  $S_0$  and  $S_2$ , (c)  $S_0$  and  $S_3$ , (d)  $S_0$  and  $S_4$ , (e)  $S_0$  and  $S_5$ , (f)  $S_0$  and  $S_6$ , (g)  $S_0$  and  $S_7$ , (h)  $S_0$  and  $S_8$ , (i)  $S_0$  and  $S_9$ , (j)  $S_0$  and  $S_{10}$  of Y6 solution by TD-DFT at B3LYP/Def2-TZVPP level of theory. The isosurface value was set at 0.0009 a.u..

**Table S2.**  $S_r$ ,  $D$ ,  $t$ ,  $H$ ,  $E_{\text{coul}}$ ,  $HDI$  and  $EDI$  of the transitions between  $S_0$  and 10 lowest-energy states in Y6 solution by TD-DFT at the level of B3LYP/Def2-TZVPP.

Transition	$D^a$ (Å)	$S_r^b$	$H^c$ (Å)	$t^d$ (Å)	$E_{\text{coul}}^e$ (eV)	$HDI^f$	$EDI^g$	Transition Character
$S_0 \rightarrow S_1$	1.34	0.67	7.50	-2.74	1.94	4.56	4.23	LE
$S_0 \rightarrow S_2$	2.00	0.64	8.02	-2.83	1.82	4.52	4.66	LE
$S_0 \rightarrow S_3$	3.34	0.56	7.72	-0.87	1.75	4.48	5.54	CT
$S_0 \rightarrow S_4$	3.14	0.50	6.31	-0.54	2.07	5.31	4.23	CT
$S_0 \rightarrow S_5$	2.36	0.69	7.59	-2.16	1.88	4.33	4.92	CT
$S_0 \rightarrow S_6$	2.66	0.55	6.72	-1.44	2.02	4.89	4.30	CT
$S_0 \rightarrow S_7$	0.95	0.77	7.99	-3.19	1.84	4.31	4.02	LE
$S_0 \rightarrow S_8$	2.13	0.67	6.84	-1.98	2.04	4.47	4.03	CT
$S_0 \rightarrow S_9$	1.68	0.72	6.09	-2.03	2.35	4.11	6.73	LE
$S_0 \rightarrow S_{10}$	0.68	0.71	8.16	-4.45	1.82	4.14	4.24	LE

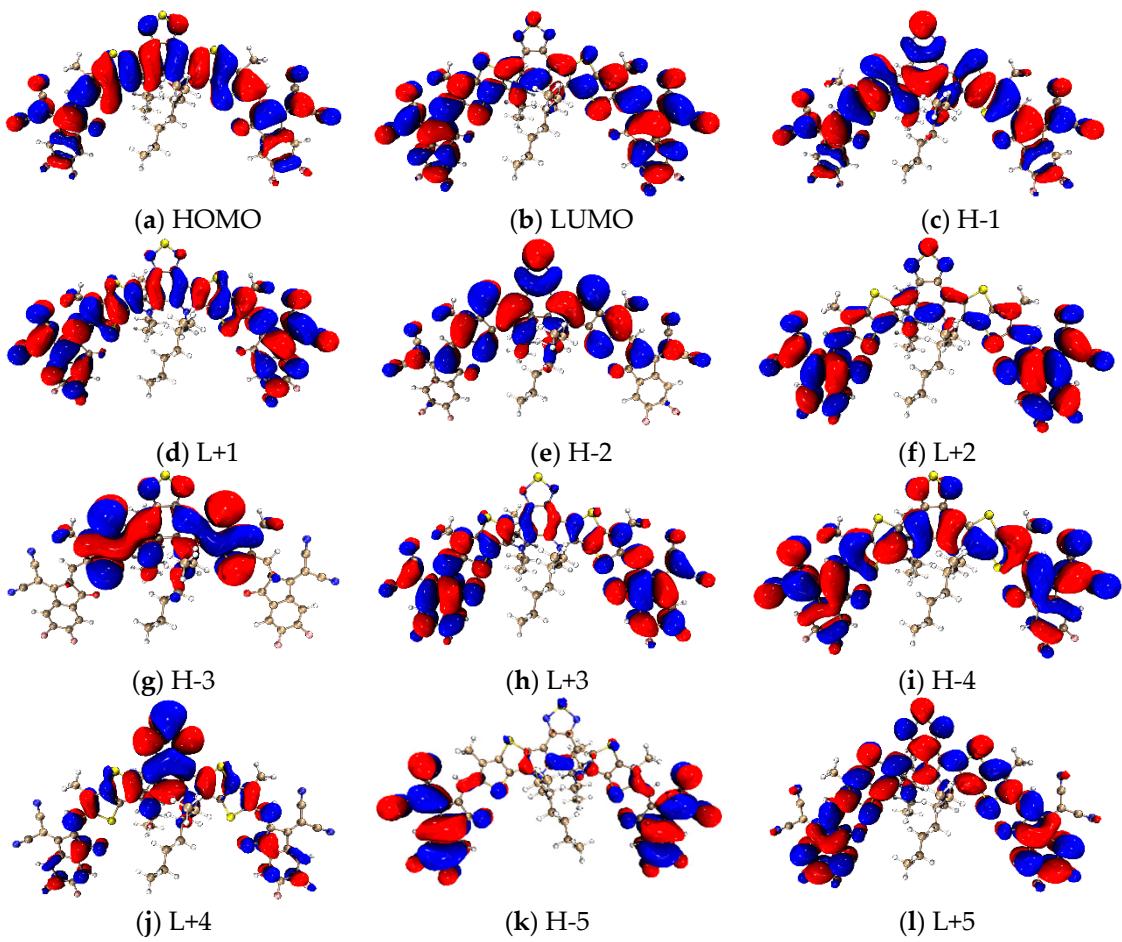
<sup>a</sup>the distance between centroid of hole and electron in corresponding directions; <sup>b</sup>the overlap function between hole and electron distribution; <sup>c</sup>the average degree of spatial extension of hole and electron distribution in X/Y/Z direction; <sup>d</sup>the degree of hole and electron in charge transfer direction; <sup>e</sup>exciton binding energy; <sup>f</sup>the hole delocalization index; <sup>g</sup>the electron delocalization index.

### 3. TD-DFT with B3LYP/6-31G\*

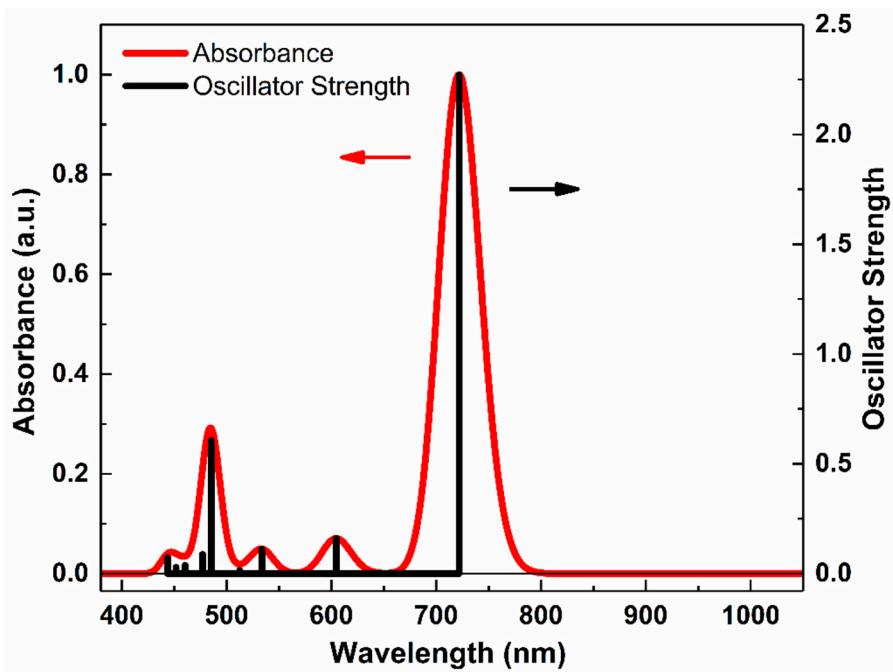
**Table S3.** Computed positions and oscillator strength ( $f$ ) of the 10 lowest-energy electronic transitions of Y6 solution by TD-DFT at B3LYP/6-31G\* level of theory.

State	$\lambda_{\text{cal}}$ (eV, nm)	$f^a$	Excitation contribution <sup>b</sup> (%)
$S_1$	1.72 (722)	2.2709	$H \rightarrow L$ (98.7)
$S_2$	2.05 (605)	0.1601	$H \rightarrow L+1$ (96.6)
$S_3$	2.32 (534)	0.1104	$H \rightarrow L+2$ (96.0)
$S_4$	2.42 (513)	0.0060	$H-2 \rightarrow L$ (69.2), $H-1 \rightarrow L$ (22.8)
$S_5$	2.42 (513)	0.0141	$H \rightarrow L+3$ (65.9), $H-1 \rightarrow L$ (29.5)
$S_6$	2.55 (485)	0.6055	$H-1 \rightarrow L$ (45.2), $H-2 \rightarrow L$ (26.9), $H \rightarrow L+3$ (24.6)
$S_7$	2.60 (477)	0.0867	$H-3 \rightarrow L$ (45.0), $H-1 \rightarrow L+1$ (25.7), $H-2 \rightarrow L+1$ (25.6)
$S_8$	2.69 (460)	0.0381	$H \rightarrow L+4$ (69.1), $H-1 \rightarrow L+1$ (24.6)
$S_9$	2.74 (452)	0.0287	$H-3 \rightarrow L$ (42.6), $H-1 \rightarrow L+1$ (34.5), $H \rightarrow L+4$ (17.7)
$S_{10}$	2.79 (444)	0.0721	$H-2 \rightarrow L+1$ (65.7), $H-1 \rightarrow L+1$ (11.3), $H \rightarrow L+4$ (9.6)

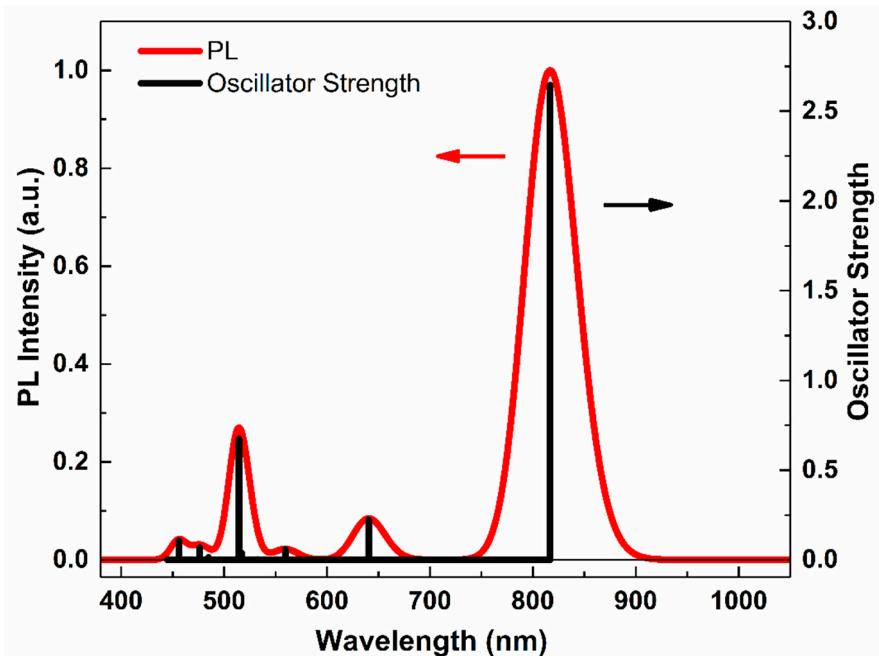
<sup>a</sup>Oscillator strengths. <sup>b</sup>H=HOMO, L=LUMO, H-1=HOMO-1, L+1=LUMO+1.



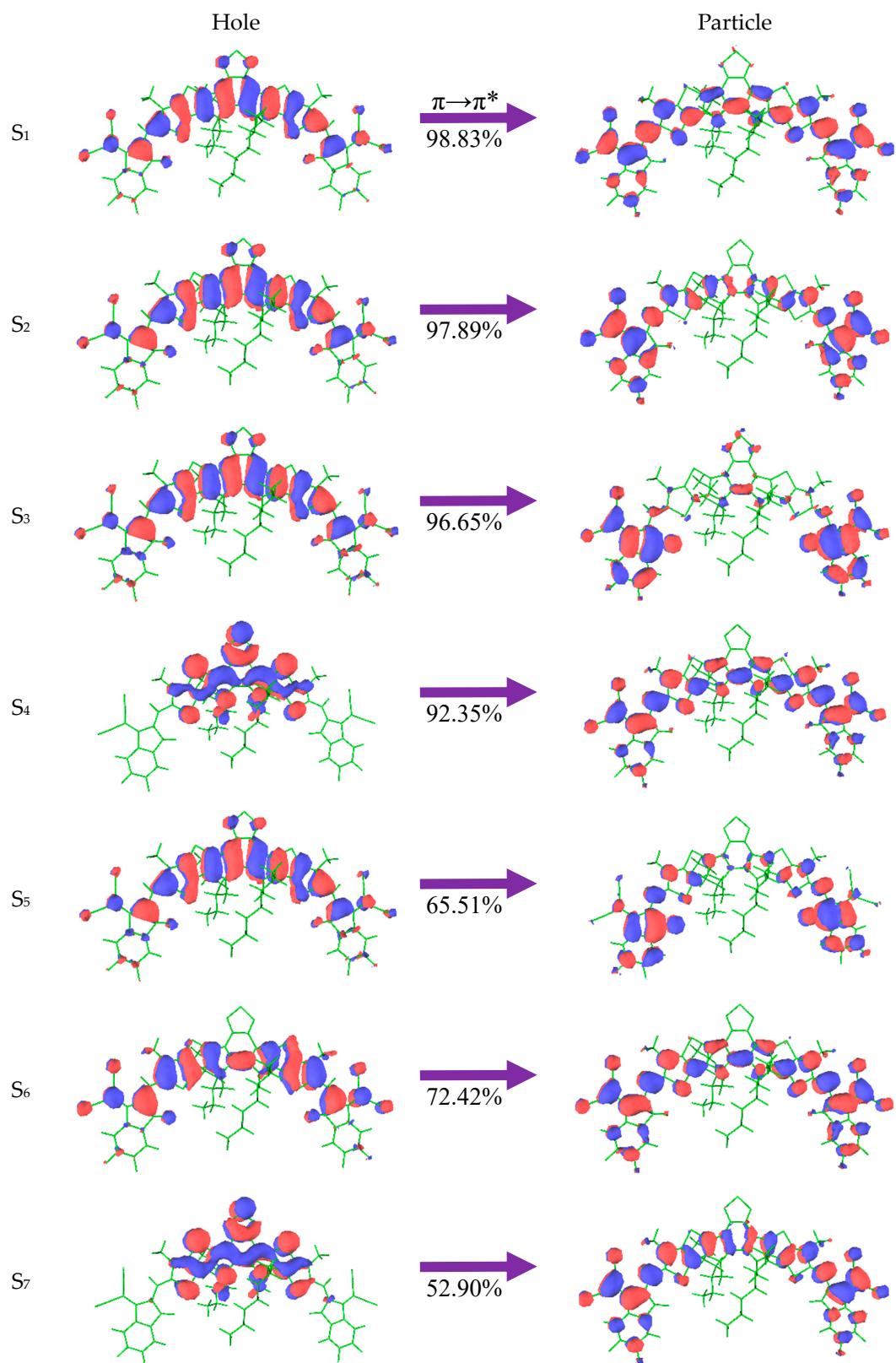
**Figure S5.** Electron density contours of (a) HOMO, (b) LUMO, (c) HOMO-1, (d) LUMO+1, (e) HOMO-2, (f) LUMO+2, (g) HOMO-3, (h) LUMO+3, (i) HOMO-4, (j) LUMO+4, (k) HOMO-5, (l) LUMO+5 of Y6 solution by TD-DFT at B3LYP/6-31G\* level of theory. The isosurface value was set at 0.01 a.u..

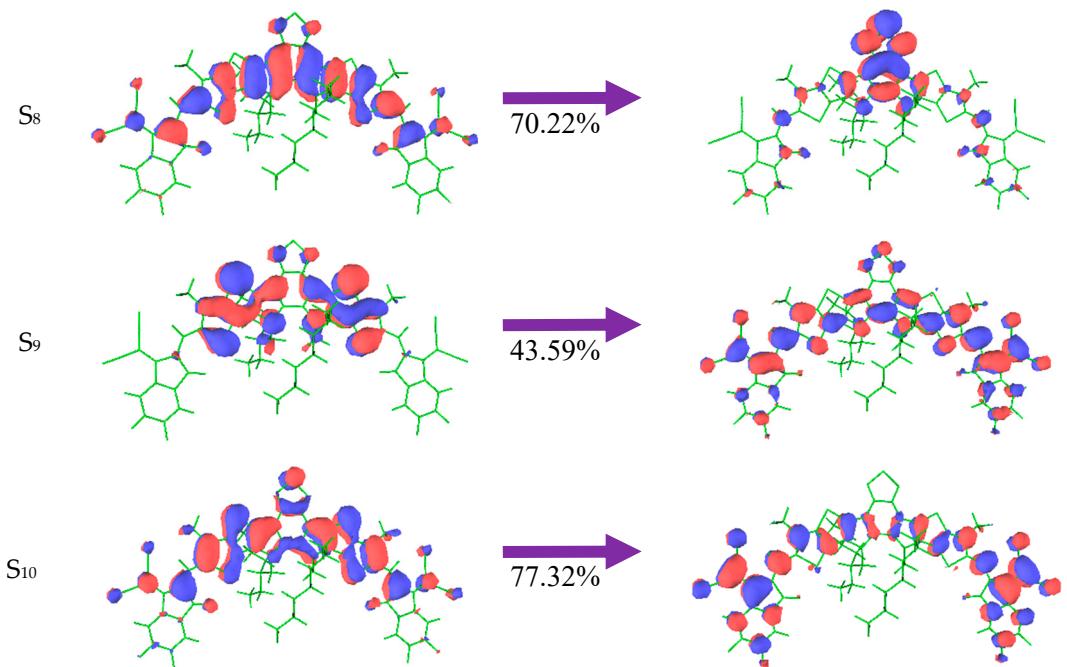


**Figure S6.** Simulated UV-vis absorption spectrum (red curve) and oscillator strength (black spikes) of the Y6 solution by TD-DFT at B3LYP/6-31G\* level of theory. A Gaussian function with a full width at half-maximum (FWHM) of 0.11 eV was employed.

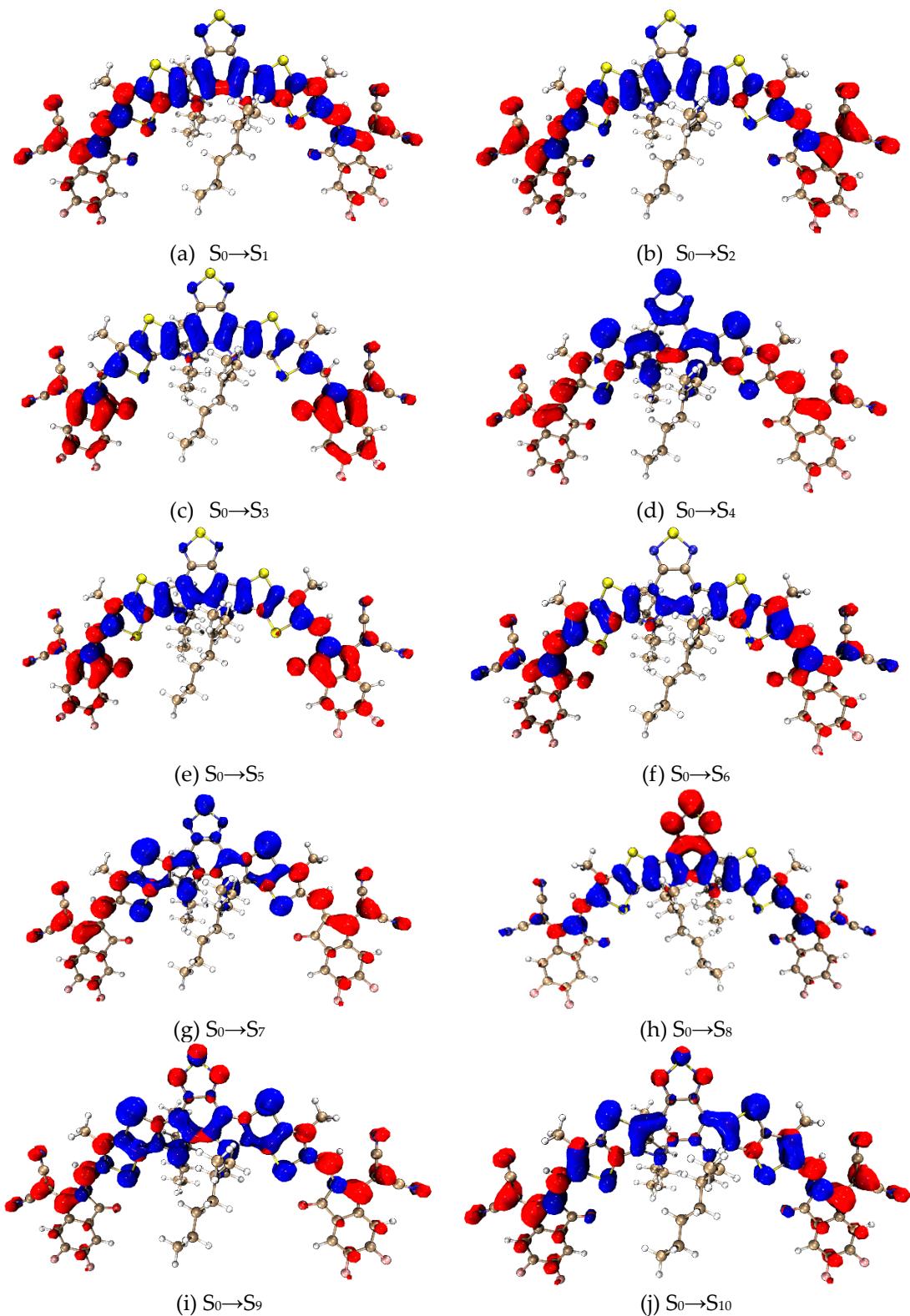


**Figure S7.** Simulated PL spectrum (red curve) and oscillator strength (black spikes) of the Y6 solution by TD-DFT at level of B3LYP/6-31G\*.A Gaussian function with a full width at half-maximum (FWHM) of 0.11 eV was employed.





**Figure S8.** Computed natural transition orbital pairs for  $S_1$ - $S_{10}$  of Y6 solution by TD-DFT at B3LYP/6-31G\* level of theory. The isosurface value was set at 0.018 a.u.,

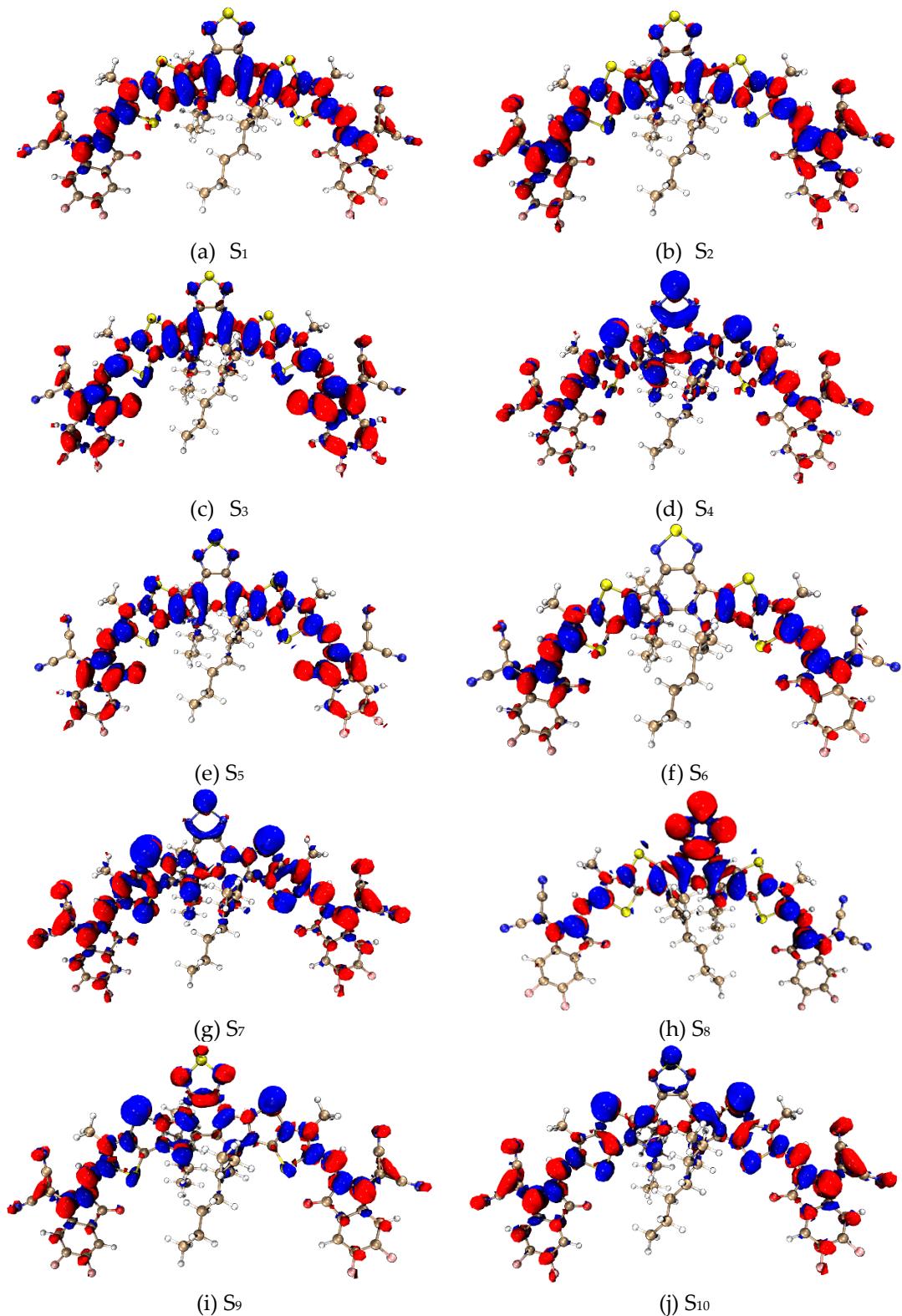


**Figure S9.** The overlap of electron-hole isosurface density maps between (a)  $S_0$  and  $S_1$ , (b)  $S_0$  and  $S_2$ , (c)  $S_0$  and  $S_3$ , (d)  $S_0$  and  $S_4$ , (e)  $S_0$  and  $S_5$ , (f)  $S_0$  and  $S_6$ , (g)  $S_0$  and  $S_7$ , (h)  $S_0$  and  $S_8$ , (i)  $S_0$  and  $S_9$ , (j)  $S_0$  and  $S_{10}$  of Y6 solution by TD-DFT at B3LYP/6-31G\* level of theory. The isosurface value was set at 0.0009 a.u..

**Table S4.**  $S_r$ ,  $D$ ,  $t$ ,  $H$ ,  $E_{\text{coul}}$ ,  $HDI$  and  $EDI$  for the transitions between  $S_0$  and 10 lowest-energy excited states in Y6 solution by TD-DFT at the level of B3LYP/6-31G\*.

Transition	$D^{\text{a}}$ (Å)	$S_r^{\text{b}}$	$H^{\text{c}}$ (Å)	$t^{\text{d}}$ (Å)	$E_{\text{coul}}^{\text{e}}$ (eV)	$HDI^{\text{f}}$	$EDI^{\text{g}}$	Transition Character
$S_0 \rightarrow S_1$	1.29	0.67	7.45	-2.75	1.95	4.64	4.24	LE
$S_0 \rightarrow S_2$	1.95	0.64	7.96	-2.84	1.83	4.61	4.67	LE
$S_0 \rightarrow S_3$	2.98	0.60	7.80	-1.42	1.81	4.54	5.57	CT
$S_0 \rightarrow S_4$	3.09	0.57	6.35	-0.62	2.07	5.12	4.16	CT
$S_0 \rightarrow S_5$	2.18	0.71	7.65	-2.56	1.88	4.23	4.58	CT
$S_0 \rightarrow S_6$	1.06	0.78	7.92	-3.62	1.86	4.33	4.03	LE
$S_0 \rightarrow S_7$	2.63	0.55	6.70	-1.32	2.02	4.95	4.35	CT
$S_0 \rightarrow S_8$	1.60	0.71	6.61	-2.36	2.18	4.29	6.33	LE
$S_0 \rightarrow S_9$	1.34	0.73	6.87	-2.78	2.07	4.11	3.98	LE
$S_0 \rightarrow S_{10}$	1.48	0.72	7.84	-3.21	1.86	3.84	4.21	LE

<sup>a</sup>the distance between centroid of hole and electron in corresponding directions; <sup>b</sup>the overlap function between hole and electron distribution; <sup>c</sup>the average degree of spatial extension of hole and electron distribution in X/Y/Z direction; <sup>d</sup>the degree of hole and electron in charge transfer direction; <sup>e</sup>exciton binding energy; <sup>f</sup>the hole delocalization index; <sup>g</sup>the electron delocalization index.



**Figure S10.** The electron density difference between (a)  $S_0$  and  $S_1$ , (b)  $S_0$  and  $S_2$ , (c)  $S_0$  and  $S_3$ , (d)  $S_0$  and  $S_4$ , (e)  $S_0$  and  $S_5$ , (f)  $S_0$  and  $S_6$ , (g)  $S_0$  and  $S_7$ , (h)  $S_0$  and  $S_8$ , (i)  $S_0$  and  $S_9$ , (j)  $S_0$  and  $S_{10}$  of Y6 solution by TD-DFT at B3LYP/6-31G\* level of theory. The isosurface value was set at 0.0005 a.u. (blue, electron density decreases upon transition; red, electron density increases upon transition).

**Table S5.** Geometrically optimized atomic X/Y/Z coordinates of the ground state structure of Y6.

N	3.334	-1.423	-6.840
N	4.17	-2.722	-4.838
C	2.203	0.914	-4.155
C	3.477	-0.987	-3.226
C	3.595	-1.567	-4.530
C	2.879	0.293	-3.054
C	3.115	-0.823	-5.677
C	2.401	0.402	-5.469
C	4.396	1.124	6.548
H	-2.067	1.302	-4.117
H	9.715	2.247	-2.467
C	-4.505	8.431	-10.889
S	4.703	-2.765	-1.212
C	-2.715	6.63	-7.968
N	3.038	0.702	-1.730
S	1.361	1.391	-8.049
O	-2.366	6.578	-5.561
H	-2.804	-0.508	-2.507
F	-5.514	10.828	-4.765
H	6.386	3.927	0.772
H	5.625	-0.389	9.368
C	-5.449	10.348	-7.071
H	-2.363	1.919	1.131
H	5.684	5.541	0.591
H	-1.951	5.41	-9.477
C	0.312	2.776	-7.697
C	0.234	3.082	-6.325
C	5.045	-2.293	1.633
C	-1.943	5.568	-8.405
C	-4.205	8.992	-5.496
C	4.058	-0.643	0.264
F	4.845	1.762	10.546
S	3.982	0.139	1.809
S	0.784	4.453	-6.022
C	5.006	0.123	7.323
N	-2.599	5.775	-11.787
C	3.939	2.322	7.083
C	3.658	-0.345	-1.056
C	-3.773	8.242	-6.583
H	-5.361	9.878	-9.142
C	6.916	2.094	-2.098

H	-0.371	2.499	2.583
C	9.180	1.626	-3.195
C	4.608	2.578	-1.010
C	3.160	2.100	-1.272
H	9.742	1.655	-4.135
C	-5.016	9.596	-8.156
H	5.458	3.562	-2.753
C	-1.119	4.610	-7.77
C	5.168	0.328	8.700
H	2.551	2.218	-0.369
C	6.35	-3.261	6.018
C	-2.872	7.069	-6.565
C	1.682	1.242	-6.339
C	4.513	3.973	-0.350
C	-1.024	3.271	2.159
C	4.643	-1.921	0.346
H	-0.404	4.153	1.954
C	5.996	-2.171	6.870
H	6.908	1.072	-1.692
H	7.243	1.496	-4.15
H	6.505	4.782	-0.776
C	4.948	-0.656	5.078
H	-2.528	-1.171	-4.118
C	1.025	2.200	-5.557
C	4.762	-1.273	2.579
H	-3.892	8.758	-4.484
C	5.37	-1.014	6.435
C	7.741	2.116	-3.391
H	-0.119	4.374	-10.528
S	4.105	-2.851	-6.492
H	6.682	-3.483	2.408
C	5.091	-1.436	3.944
N	1.324	2.002	-4.213
H	-1.526	3.331	-10.375
F	-6.269	11.387	-7.266
C	-2.036	-0.691	-3.265
C	0.367	2.427	-3.166
H	9.199	0.593	-2.827
O	3.861	1.340	4.212
C	-1.719	2.775	0.887
H	-1.320	-1.410	-2.848
C	-1.330	0.596	-3.708
H	0.095	2.628	-10.355

H	3.472	3.079	6.462
F	3.691	3.640	9.038
C	-3.517	7.524	-8.808
C	4.336	0.688	5.136
H	5.814	-4.216	1.0540
C	-3.079	6.539	-11.049
C	5.692	-3.612	1.958
C	4.711	1.526	9.236
C	-3.688	7.496	-10.182
C	5.465	2.560	-2.300
H	0.904	2.927	-2.362
C	-5.054	10.057	-5.757
C	-0.735	2.364	-0.217
C	-0.501	3.481	-10.02
H	-0.081	3.22	-0.436
C	4.105	2.514	8.446
C	-4.158	8.518	-7.906
C	-0.437	3.619	-8.523
C	5.850	4.586	0.079
H	3.864	3.898	0.533
C	3.934	-1.385	-1.954
H	-1.753	3.55	2.927
N	6.654	-4.17	5.355
H	5.062	1.897	-0.278
H	5.095	-4.194	2.669
H	4.009	4.66	-1.045
H	2.731	2.73	-2.050
H	5.005	1.897	-3.044
H	7.413	2.716	-1.342
H	7.754	3.139	-3.795
H	-0.266	3.189	-3.63
H	-0.657	0.345	-4.536
H	-0.08	1.565	0.163
H	-2.386	3.559	0.502
H	5.559	-2.399	4.109
C	-0.523	1.300	-2.597
C	-1.439	1.877	-1.494
H	0.138	0.554	-2.131
H	-2.039	2.697	-1.918
H	-2.158	1.101	-1.206
N	-5.161	9.175	-11.499
C	6.360	-2.401	8.232
N	6.671	-2.624	9.333

#### 4. Fitting parameters in Figure 5

**Table S6.** Fitting parameters of the TRPL decay shown in Figure 5a.

Excitation Fluence (photons/(pluse×cm <sup>2</sup> ))	Amplitude <i>A</i> <sub>1</sub>	Lifetime $\tau_1$ (ps)
$4.8 \times 10^{12}$	1.053	$822 \pm 17$
$1.0 \times 10^{13}$	1.084	$794 \pm 18$
$1.6 \times 10^{13}$	1.081	$884 \pm 16$

**Table S7.** Fitting parameters of the TA decay shown in Figure 5b.

Excitation Fluence (photons/(pluse×cm <sup>2</sup> ))	Amplitude <i>A</i> <sub>1</sub>	Lifetime $\tau_1$ (ps)	Amplitude <i>A</i> <sub>2</sub>	Lifetime $\tau_2$ (ps)	Amplitude <i>A</i> <sub>3</sub>	Lifetime $\tau_3$ (ps)
$2 \times 10^{14}$	4.7	$1.6 \pm 0.2$	2.8	$31 \pm 2$	0.58	$3929 \pm 1155$

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