

Supporting information to "A modified interaction-strength interpolation method as an important step towards self-consistent calculations."

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TABLE S4: Atomization energies (in kcal/mol) of small radicals set corresponding to various methods. The last lines report the mean absolute error (MAE) and mean absolute relative error (MARE) calculated with respect CCSD(T) data. All calculation have been performed with fully uncontracted cc-pVTZ basis set. <sup>a)</sup> with TPSS-GL2

	@OEPx							
	CCSD(T)	MP2	OEP2-sc	GL2	ISI	mISI	mISI <sup>a</sup>	ACSC
BH <sub>2</sub>	-167.4	-167.9	-168.0	-169.2	-163.6	-162.8	-177.9	-174.5
BH <sup>+</sup>	218.0	217.2	136.5	148.4	144.9	144.7	134.5	135.0
BO	-189.7	-204.1	-209.5	-240.0	-211.8	-206.3	-167.5	-164.4
C <sub>2</sub> <sup>-</sup>	-210.3	-222.3	-229.8	-317.3	-250.0	-238.6	-184.6	-175.9
CF	-129.6	-134.8	-140.2	-165.3	-143.5	-139.0	-110.2	-107.9
CH	-82.0	-78.4	-78.8	-91.1	-82.0	-80.7	-80.1	-77.7
CN	-174.0	-161.0	-194.4	-206.4	-175.3	-169.5	-135.3	-132.3
CO <sup>+</sup>	66.2	62.1	45.2	17.9	48.2	53.9	103.0	107.3
F <sub>2</sub> <sup>+</sup>	321.0	310.8	298.7	214.7	270.3	281.2	390.1	395.4
FH <sup>+</sup>	227.4	228.7	228.3	225.9	228.1	228.7	231.0	232.8
H <sub>2</sub> O <sup>+</sup>	60.1	61.0	60.5	44.7	57.8	60.2	65.4	70.5
HCO	-272.6	-282.2	-288.0	-340.0	-296.6	-288.3	-250.8	-242.4
HNF	-151.4	-152.5	-159.5	-202.1	-167.2	-160.1	-124.2	-119.3
HOO	-169.0	-170.8	-183.1	-234.4	-190.3	-181.4	-134.8	-125.8
N <sub>2</sub> <sup>+</sup>	136.3	121.4	109.0	-17.7	76.7	92.4	208.6	213.6
NH <sub>2</sub>	-176.4	-173.1	-174.1	-200.6	-179.6	-176.2	-170.4	-166.9
NH <sup>+</sup>	228.4	235.3	234.8	221.3	228.8	229.9	241.5	241.0
NO	-146.0	-152.7	-162.4	-225.0	-175.9	-166.4	-105.3	-100.6
O <sub>2</sub> <sup>+</sup>	158.6	141.4	132.9	38.7	106.2	118.8	217.9	226.3
OF	-49.9	-50.5	-63.0	-99.5	-68.6	-62.2	-12.6	-7.9
OH	-103.5	-103.6	-104.3	-121.2	-108.1	-105.7	-97.0	-93.5
MAE	6.1	15.7	52.98	21.69	16.59	30.23	34.23	
MARE[%]	3.89	12.05	89.10	16.97	12.18	32.10	46.35	

TABLE S5: Energies (in kcal/mol) of K9 set corresponding to various methods. The last lines report the mean absolute error (MAE) and mean absolute relative error (MARE) calculated with respect CCSD(T) data. All calculation have been performed with fully uncontracted cc-pVTZ basis set. <sup>a</sup>) with TPSS-GL2

		@OEPx						
	CCSD(T)	MP2	OEP2-sc	GL2	ISI	mISI	mISI <sup>a</sup>	ACSC
OH + CH <sub>4</sub> → TS	7.1	8.52	2.07	-7.04	2.95	5.69	18.48	20.25
TS → CH <sub>3</sub> + H <sub>2</sub> O	18.25	23.74	17.3	14.05	18.97	20.49	24.78	25.79
H + OH → TS	50.1	55.43	13.35	13.9	13.93	13.65	13.59	15.06
TS → O + H <sub>2</sub>	55.19	55.63	12.93	6.27	11.12	14.03	23.15	24.71
H + H <sub>2</sub> S → TS	4.1	6.77	5.66	3.09	4.06	4.16	5.94	6.5
TS → H <sub>2</sub> + SH	18.93	17.37	16.15	9.92	8.03	10.15	11.73	18.62
MAE		2.82	14.89	18.91	16.01	15.01	15.92	14.82
MARE[%]		22.46	46.45	75.88	45.52	37.87	68.32	68.63





TABLE S9: Open-shell reaction energies (in kcal/mol) corresponding to various methods. The last lines report the mean absolute error (MAE) and mean absolute relative error (MARE) calculated with respect CCSD(T) data. All calculation have been performed with fully uncontracted cc-pVTZ basis set. <sup>a)</sup> with TPSS-GL2

	CCSD(T)	MP2	OEP2-sc	GL2	ISI	mISI	mISI <sup>a</sup>	@OEPx	ACSC
HCl+H→Cl+H <sub>2</sub>	4.13	-1.17	-1.17	-6.1	-8.82	-6.75	-5.26	1.46	
H <sub>2</sub> O+F <sub>2</sub> →2HF+O	13.37	12.48	6.48	-42.22	-8.27	-1.4	49.25	54.13	
CH <sub>4</sub> +OH→CH <sub>3</sub> +H <sub>2</sub> O	11.19	15.28	15.31	21.27	16.1	14.86	6.26	5.5	
CH <sub>3</sub> +Cl <sub>2</sub> →CH <sub>3</sub> Cl+Cl	31.32	31.85	30.75	23.28	31.5	31.39	39.76	37.69	
S+2HCl→H <sub>2</sub> S+Cl <sub>2</sub>	22.54	23.43	26.05	49.22	42.3	40.84	24.01	13.42	
N+O <sub>2</sub> →NO+O	29.8	25.71	26.91	29.66	25.75	25.33	26.05	28.42	
4HCl+O <sub>2</sub> →2H <sub>2</sub> O+2Cl <sub>2</sub>	25.73	28.07	25.25	32.55	24.54	24.47	15.28	19.12	
2NO→N <sub>2</sub> +O <sub>2</sub>	44.03	52.59	46.4	62.47	54.29	52.99	46.39	43.05	
2H <sub>2</sub> O <sub>2</sub> →2H <sub>2</sub> O+O <sub>2</sub>	48.36	51.74	52.44	36.69	49.01	52.47	62.86	65.6	
Cl <sub>2</sub> +H→HCl+Cl	51.36	47.33	45.3	32.29	35.7	36.57	56.1	59.07	
2SO <sub>2</sub> +O <sub>2</sub> →2SO <sub>3</sub>	35.68	44.58	42.25	26.62	31.9	31.95	65.02	59.18	
H <sub>2</sub> S+F <sub>2</sub> →S+2HF	61.25	66.52	60.81	22.48	36.75	40.55	72.44	86.28	
NO+N→O+N <sub>2</sub>	73.83	78.29	73.31	92.13	80.04	78.31	72.45	71.48	
2SiH <sub>3</sub> →Si <sub>2</sub> H <sub>6</sub>	76.97	77.02	77.61	90.38	86.03	85.11	87.9	77.18	
CH <sub>3</sub> +SH→CH <sub>3</sub> SH	76.72	81.14	82.15	101.73	100.37	98.36	87.69	73.49	
CS+O→CO+S	89.4	94.62	92.98	84.05	61.57	58.08	73.08	81.7	
CH <sub>3</sub> +Cl→CH <sub>3</sub> Cl	84.47	89.49	90.46	110.72	110.61	108.73	95.53	80.34	
NH+H→NH <sub>2</sub>	96.59	96.37	96.62	111.34	99.71	98.01	94.5	91.13	
Si+2H <sub>2</sub> →SiH <sub>4</sub>	101.49	102.58	103.41	105.31	112.11	108.57	119.99	111.48	
2C <sub>2</sub> H <sub>4</sub> +O <sub>2</sub> →2CH <sub>3</sub> CHO	104.35	110.31	109.71	105.1	102.52	100.69	116.47	111.97	
NH <sub>2</sub> +H→NH <sub>3</sub>	113.4	115.24	115.22	129.55	116.75	114.87	113.58	108.54	
2H <sub>2</sub> +O <sub>2</sub> →2H <sub>2</sub> O	120.18	125.07	118.19	109.32	113.58	111.1	138	134.33	
CO <sub>2</sub> +C→2CO	128.17	129.06	128.34	156.12	138.46	135.88	108	107.2	
N <sub>2</sub> H <sub>4</sub> +O <sub>2</sub> →N <sub>2</sub> +2H <sub>2</sub> O	132.86	139.43	134.48	151.22	139.48	138.47	119.64	116.77	
4NH <sub>3</sub> +5O <sub>2</sub> →4NO+6H <sub>2</sub> O	203.1	201.58	199.16	196.92	189.65	188.46	182	180.15	
2NH <sub>3</sub> +2NO+O→2N <sub>2</sub> +3H <sub>2</sub> O	247.16	269.4	260.13	321.04	278.44	270.76	223.35	212.2	
MAE	4.33	3.43	18.29	11.52	10.38	12.16	11.61		
MARE [%]	12.28	12.65	51.53	34.64	29.47	35.61	30.20		

## 4 Vertical ionization potentials

TABLE S10: Vertical ionization potential (in eV) corresponding to various methods calculated as an energy difference between the neutral and the ionic species ( $VIP = E(N) - E(N-1)$ ) . The last lines report the mean absolute error (MAE) and mean absolute relative error (MARE) calculated with respect CCSD(T) data. The computational setup, namely basis sets and geometries in case of molecules, is identical as in J. Comput. Chem. 37 (2016), 2081. <sup>a</sup>) with TPSS-GL2

				@OEPx				
	CCSD(T)	MP2	OEP2-sc	GL2	ISI	mISI	mISI <sup>a</sup>	ACSC
Ar	-15.63	-15.77	-15.75	-16.31	-16.01	-15.94	-16.06	-15.76
Be	-9.31	-8.88	-8.88	-10.01	-9.51	-9.49	-9.14	-8.82
C <sub>2</sub> H <sub>2</sub>	-11.43	-11.6	-11.64	-12.94	-11.94	-11.77	-11.08	-10.91
C <sub>2</sub> H <sub>4</sub>	-10.63	-10.65	-10.7	-11.94	-11.01	-10.85	-10.11	-9.95
C <sub>2</sub> H <sub>6</sub>	-13.01	-13.11	-12.67	-12.74	-12.69	-12.68	-13.23	-13.19
CH <sub>2</sub> CF <sub>2</sub>	-10.61	-10.67	-10.5	-11.3	-10.83	-10.74	-10.77	-10.58
CH <sub>3</sub> CN	-10.75	-11.33	-10.76	-12.47	-11.53	-11.36	-10.94	-10.72
CH <sub>4</sub>	-14.37	-14.4	-14.41	-14.82	-14.46	-14.4	-14.52	-14.41
CHF <sub>3</sub>	-14.59	-14.61	-14.23	-15.87	-15.93	-15.94	-16.95	-16.85
Cl <sub>2</sub>	-11.45	-11.5	-11.37	-11.06	-11.09	-11.1	-12.54	-12.29
CO <sub>2</sub>	-13.7	-14.63	-13.85	-15.51	-14.63	-14.46	-14.03	-13.79
CO	-13.94	-14.31	-13.71	-14.88	-14.35	-14.24	-14.32	-14.21
CS	-11.27	-11.63	-11.19	-14.52	-13.73	-13.58	-11.64	-11.23
FCN	-13.65	-13.85	-13.72	-16.33	-15.32	-15.13	-14.45	-14.29
H <sub>2</sub> CO	-10.83	-11.26	-10.84	-12.2	-11.41	-11.27	-10.75	-10.59
H <sub>2</sub> CS	-9.29	-9.57	-9.28	-10.73	-10.27	-10.19	-9.48	-9.16
H <sub>2</sub> O	-12.5	-12.69	-12.7	-13.6	-12.86	-12.73	-12.16	-12
HCCF	-11.5	-11.54	-11.44	-12.49	-11.8	-11.67	-11.41	-11.2
HCl	-12.59	-12.67	-12.66	-13.27	-13.07	-13.03	-12.97	-12.65
HCN	-13.9	-14.72	-14.09	-16.44	-15.1	-14.86	-13.81	-13.66
He	-24.48	-24.54	-24.41	-24.74	-24.51	-24.54	-24.49	-24.34
He <sub>2</sub>	-24.48	-24.54	-24.52	-24.7	-24.52	-24.54	-24.74	-24.8
HF	-15.96	-16.18	-16.2	-17.05	-16.38	-16.26	-15.57	-15.41
Mg	-7.57	-7.32	-7.33	-8.11	-7.97	-7.94	-7.44	-7.22
N <sub>2</sub>	-15.51	-15.34	-15.06	-13.41	-14.59	-14.76	-16.66	-16.64
NCCN	-13.51	-14.85	-13.77	-12.62	-13.89	-14.08	-16.52	-16.49
Ne <sub>2</sub>	-21.34	-21.42	-20.72	-22.37	-21.79	-21.67	-21.01	-20.86
Ne	-21.47	-21.67	-21.69	-22.39	-21.83	-21.72	-21.04	-20.88
NH <sub>3</sub>	-10.78	-10.86	-10.88	-11.69	-11.01	-10.9	-10.52	-10.39
OCS	-11.18	-11.75	-11.27	-12.6	-12.1	-12	-11.69	-11.36
P <sub>2</sub>	-10.66	-10.68	-10.55	-10.43	-10.4	-10.39	-11.41	-11.06
SiH <sub>4</sub>	-12.78	-12.82	-12.72	-13.13	-13	-12.98	-12.99	-12.88
	MAE	0.24	0.17	1.17	0.61	0.52	0.42	0.39
	MARE [%]	2.37	1.21	9.03	4.90	4.26	3.83	3.55



## 6 GL2 correlation energies

TABLE S12: The GL2 correlation energies obtained from exact and various semi-local energy expression (in mHa) calculated on top of self-consistent OEPx orbitalas and orbital energies in fully uncontacted cc-pVTZ basis set. The last lines report the mean absolute error (MAE) and mean absolute relative error (MARE) calculated with respect exact GL2 data.

	GL2	PBE-GL2	TPSS-GL2	revTPSS-GL2
He	-44.363	-46.337	-47.903	-51.808
Li	-39.994	-57.796	-56.165	-60.445
Be	-113.802	-113.424	-112.781	-122.476
B	-134.885	-140.928	-137.370	-147.979
C	-161.406	-176.444	-174.906	-186.062
N	-191.277	-217.471	-219.668	-231.197
O	-254.493	-281.078	-275.198	-288.047
F	-326.869	-346.140	-341.461	-355.356
Ne	-405.145	-412.358	-414.265	-429.077
BeH	-97.580	-124.940	-119.303	-129.022
OH	-340.946	-349.456	-342.201	-357.811
NH <sub>2</sub>	-327.428	-357.601	-347.322	-364.718
NH	-254.288	-286.955	-277.722	-292.113
NO	-723.276	-627.878	-619.234	-645.573
PH <sub>2</sub>	-422.856	-746.632	-735.950	-764.970
O <sub>2</sub>	-770.850	-666.881	-657.954	-684.674
S <sub>2</sub>	-918.035	-1515.626	-1501.791	-1552.064
SiH <sub>2</sub>	-347.422	-654.585	-643.779	-670.087
C <sub>2</sub> H <sub>5</sub>	-601.636	-738.081	-717.140	-753.425
CH <sub>2</sub>	-226.830	-289.601	-277.095	-292.735
CH <sub>3</sub>	-287.709	-359.285	-346.147	-365.085
CN	-541.471	-511.417	-500.899	-524.626
COH	-670.735	-619.500	-610.582	-638.332
CH <sub>4</sub>	-348.835	-424.613	-417.151	-439.289
LiF	-487.876	-451.807	-453.721	-473.896
Li <sub>2</sub>	-137.012	-164.787	-162.619	-177.591
F <sub>2</sub>	-875.886	-744.616	-744.887	-773.967
CO	-659.650	-571.305	-568.931	-594.734
CH <sub>2</sub>	-278.421	-300.300	-296.480	-313.730
H <sub>2</sub>	-47.537	-57.984	-53.775	-58.555
CS	-781.015	-1000.806	-995.643	-1033.483
LiH	-86.328	-100.313	-100.918	-109.990
N <sub>2</sub>	-708.486	-595.291	-592.501	-618.479
P <sub>2</sub>	-910.610	-1403.130	-1396.442	-1445.947
NaCl	-729.401	-1265.590	-1264.610	-1307.531
H <sub>2</sub> O	-433.049	-418.419	-416.233	-434.688
MAE	105.03	101.89	110.28	
MARE [%]	21.99	15.45	18.87	

## 7 Binding energies on top of HF orbitals

TABLE S13: Binding energies (in kcal/mol) from MP2, ISI and mISI methods calculated on top of HF orbitals. The last lines report the mean absolute error (MAE) and mean absolute relative error (MARE) calculated with respect CCSD(T) data. All calculation have been performed with fully uncontracted cc-pVTZ basis set.

	MP2	ISI	mISI
WI			
He-Ne	-0.03	-0.05	-0.02
He-Ar	-0.06	-0.05	-0.04
Ne-Ne	-0.06	-0.08	-0.04
Ne-Ar	-0.12	-0.11	-0.09
CH <sub>4</sub> -Ne	-0.18	-0.19	-0.12
C <sub>6</sub> H <sub>6</sub> -Ne	-0.61	-0.54	-0.34
CH <sub>4</sub> -CH <sub>4</sub>	-0.56	-0.49	-0.28
MAE	0.04	0.04	0.09
HB6			
NH <sub>3</sub> -NH <sub>3</sub>	-3.25	-3.13	-2.87
HF-HF	-4.59	-4.68	-4.51
H <sub>2</sub> O-H <sub>2</sub> O	-5.10	-5.10	-4.85
NH <sub>3</sub> -H <sub>2</sub> O	-6.66	-6.54	-6.24
HF-HCN	-7.86	-7.83	-7.54
(HCONH <sub>2</sub> ) <sub>2</sub>	-15.83	-15.80	-15.27
(HCOOH) <sub>2</sub>	-18.18	-18.35	-17.84
MAE	0.17	0.14	0.23
DI6			
H <sub>2</sub> S-H <sub>2</sub> S	-2.15	-1.98	-1.92
Hcl-Hcl	-2.56	-2.39	-2.33
H <sub>2</sub> S-Hcl	-4.19	-3.94	-3.86
CH <sub>3</sub> Cl-Hcl	-4.49	-4.13	-4.01
CH <sub>3</sub> SH-HCN	-4.25	-3.98	-3.81
CH <sub>3</sub> SH-Hcl	-6.13	-5.67	-5.52
MAE	0.45	0.17	0.11
DHB			
AlH-HCl	-5.26	-4.92	-4.83
AlH-HF	-6.85	-6.54	-6.41
LiH-HCl	-13.28	-12.78	-12.65
LiH-HF	-14.74	-14.44	-14.16
MgH <sub>2</sub> -HCl	-5.72	-5.4	-5.31
MgH <sub>2</sub> -HF	-7.66	-7.38	-7.24
BeH <sub>2</sub> -HCl	-2.7	-2.49	-2.42
BeH <sub>2</sub> -HF	-3.72	-3.59	-3.39
MAE	0.54	0.27	0.25
CT7			
NF <sub>3</sub> -HCN	-1.24	-1.2	-1.00
C <sub>2</sub> H <sub>4</sub> -F <sub>2</sub>	-1.6	-1.29	-1.03
NF <sub>3</sub> -HNC	-1.99	-1.68	-1.44
C <sub>2</sub> H <sub>4</sub> -Cl <sub>2</sub>	-4.14	-3.43	-3.22
NH <sub>3</sub> -F <sub>2</sub>	-2.06	-1.77	-1.51
NF <sub>3</sub> -ClF	-2.44	-2.11	-1.88
NF <sub>3</sub> -HF	-2.33	-2.04	-1.80
C <sub>2</sub> H <sub>2</sub> -ClF	-5.04	-4.47	-4.21
HCN-ClF	-5.8	-5.39	-5.16
NH <sub>3</sub> -Cl <sub>2</sub>	-5.87	-5.44	-5.29
H <sub>2</sub> O-ClF	-5.69	-5.45	-5.27
NH <sub>3</sub> -ClF	-2.44	-4.65	-5.68
MAE	0.55	0.48	0.57
MAE	0.38	0.25	0.29
MARE[%]	12.58	10.26	17.11