Multimedia Appendix 2

Federated queries of clinical data repositories: balancing accuracy and privacy

Yun William Yu, PhD Computer and Mathematical Sciences University of Toronto at Scarborough Toronto, ON M5S 1J7 ywyu@math.toronto.edu

Griffin M Weber, MD, PhD
Department of Biomedical Informatics
Harvard Medical School
Boston, MA 02115
weber@hms.harvard.edu

Table A1. Detailed benchmark results

We measure the accuracy, wait time (in seconds), and privacy risk of running the query using raw counts, HyperLogLog sketches of various sizes, and sending full Hashed patient IDs.

Table A1a. 1 patient query

| Table A | a. i patiei | | - | - · · | | | |
|------------|-------------|-----------------|---------------|-------|-------|-------|-------------------|
| | | Estimated num | | | t (s) | Risk: | Risk: Hub+Site |
| Method | | Range of Counts | | Mean | Max | | |
| Count | None | [1.000, 3.525] | [0%, 252%] | 0 | 0 | 1.91 | 1.91 |
| | Mask | [10.000, 35.25] | [900%, 3425%] | 0 | 0 | 0 | 0 |
| | MPC | [1.000, 3.525] | [0%, 252%] | 0.099 | 0.099 | 0 | 0 |
| HLL0 | None | [0.694, 22.20] | [-31%, 2120%] | 0 | 0 | 0 | 0 |
| | Shuffle | [0.694, 22.20] | [-31%, 2120%] | 0 | 0 | 0 | 0 |
| | Rehash | [0.694, 22.20] | [-31%, 2120%] | 0 | 0 | 0 | 0 |
| | Mask | [0.694, 22.20] | [-31%, 2120%] | 0 | 0 | 0 | 0 |
| | MPC | [0.694, 22.20] | [-31%, 2120%] | 0.385 | 0.385 | 0 | 0 |
| | Shuffle+MPC | [0.694, 22.20] | [-31%, 2120%] | 0.385 | 0.385 | 0 | 0 |
| HLL1 | None | [1.386, 1.386] | [39%, 39%] | 0 | 0 | 0 | 0 |
| | Shuffle | [1.386, 1.386] | [39%, 39%] | 0 | 0 | 0 | 0 |
| | Rehash | [1.386, 1.386] | [39%, 39%] | 0 | 0 | 0 | 0 |
| | Mask | [1.386, 1.386] | [39%, 39%] | 0 | 0 | 0 | 0 |
| | MPC | [1.386, 1.386] | [39%, 39%] | | 0.675 | 0 | 0 |
| | Shuffle+MPC | [1.386, 1.386] | [39%, 39%] | 0.675 | 0.675 | 0 | 0 |
| HLL4 | None | [1.033, 1.033] | [3%, 3%] | 0.001 | 0.001 | 0 | 0 |
| | Shuffle | [1.033, 1.033] | [3%, 3%] | 0.001 | 0.001 | 0 | 0 |
| | Rehash | [1.033, 1.033] | [3%, 3%] | 0.001 | 0.001 | 0 | 0 |
| | Mask | [1.033, 1.033] | [3%, 3%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [1.033, 1.033] | [3%, 3%] | 4.781 | 4.781 | 0 | 0 |
| | Shuffle+MPC | [1.033, 1.033] | [3%, 3%] | 4.781 | 4.781 | 0 | 0 |
| HLL7 | None | [1.004, 1.004] | [0%, 0%] | 0.006 | 0.006 | 0 | 0 |
| | Shuffle | [1.004, 1.004] | [0%, 0%] | 0.006 | 0.006 | 0 | 0 |
| | Rehash | [1.004, 1.004] | [0%, 0%] | 0.007 | 0.007 | 0 | 0 |
| | Mask | [1.004, 1.004] | [0%, 0%] | 0.007 | 0.007 | 0 | 0 |
| | MPC | [1.004, 1.004] | [0%, 0%] | 37.73 | 37.73 | 0 | 0 |
| | Shuffle+MPC | [1.004, 1.004] | [0%, 0%] | 37.73 | 37.73 | 0 | 0 |
| HLL15 | None | [1.000, 1.000] | [0%, 0%] | 1.463 | 1.463 | 0.31 | 0.31 |
| | Shuffle | [1.000, 1.000] | [0%, 0%] | 1.463 | 1.463 | 0 | 0.31 |
| | Rehash | [1.000, 1.000] | [0%, 0%] | 1.623 | 1.647 | 0 | 0.31 |
| | Mask | [1.000, 21.00] | [0%, 2000%] | 1.632 | 1.632 | 0 | 0 |
| Hashed IDs | None | [1.000, 1.000] | [0%, 0%] | 0.001 | 0.001 | 1.91 | 1.91 |
| | Rehash | [1.000, 1.000] | [0%, 0%] | 0.001 | 0.001 | 0 | 1.91 |
| | | | | | | | |

 Table A1b.
 10 patient query.

| | | Estimated numb | er of patients | Wait (s) | | Risk: | Risk: |
|------------|-------------|------------------|----------------|----------|-------|-------|----------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [1.475, 24.00] | [-85%, 140%] | 0 | 0 | 15.72 | 15.72 |
| | Mask | [10.000, 205.2] | [0%, 1952%] | 0 | 0 | 0 | 0 |
| | MPC | [15.47, 24.00] | [55%, 140%] | 0.099 | 0.099 | 0 | 0 |
| HLL0 | None | [2.776, 88.82] | [-72%, 788%] | 0 | 0 | 0 | 0 |
| | Shuffle | [2.776, 88.82] | [-72%, 788%] | 0 | 0 | 0 | 0 |
| | Rehash | [2.776, 88.82] | [-72%, 788%] | 0 | 0 | 0 | 0 |
| | Mask | [2.776, 88.82] | [-72%, 788%] | 0 | 0 | 0 | 0 |
| | MPC | [2.776, 88.82] | [-72%, 788%] | 0.385 | 0.385 | 0 | 0 |
| | Shuffle+MPC | [2.776, 88.82] | [-72%, 788%] | 0.385 | 0.385 | 0 | 0 |
| HLL1 | None | [3.332, 35.23] | [-67%, 252%] | 0 | 0 | 0 | 0 |
| | Shuffle | [3.332, 35.23] | [-67%, 252%] | 0 | 0 | 0 | 0 |
| | Rehash | [3.332, 35.23] | [-67%, 252%] | 0 | 0 | 0 | 0 |
| | Mask | [3.332, 35.23] | [-67%, 252%] | 0 | 0 | 0 | 0 |
| | MPC | [3.332, 35.23] | [-67%, 252%] | 0.675 | 0.675 | 0 | 0 |
| | Shuffle+MPC | [3.332, 35.23] | [-67%, 252%] | 0.675 | 0.675 | 0 | 0 |
| HLL4 | None | [5.995, 15.69] | [-40%, 57%] | 0.001 | 0.001 | 0 | 0 |
| | Shuffle | [5.995, 15.69] | [-40%, 57%] | 0.001 | 0.001 | 0 | 0 |
| | Rehash | [5.995, 15.69] | [-40%, 57%] | 0.001 | 0.001 | 0 | 0 |
| | Mask | [5.995, 15.69] | [-40%, 57%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [5.995, 15.69] | [-40%, 57%] | 4.778 | 4.778 | 0 | 0 |
| | Shuffle+MPC | [5.995, 15.69] | [-40%, 57%] | 4.778 | 4.778 | 0 | 0 |
| HLL7 | None | [8.261, 10.41] | [-17%, 4%] | 0.006 | 0.006 | 0.01 | 0.01 |
| | Shuffle | [8.261, 10.41] | [-17%, 4%] | 0.006 | 0.006 | 0 | 0.01 |
| | Rehash | [8.261, 10.41] | [-17%, 4%] | 0.007 | 0.007 | 0 | 0 |
| | Mask | [8.261, 10.41] | [-17%, 4%] | 0.007 | 0.007 | 0 | 0 |
| | MPC | [8.261, 10.41] | [-17%, 4%] | 37.72 | 37.72 | 0 | 0 |
| | Shuffle+MPC | [8.261, 10.41] | [-17%, 4%] | 37.72 | 37.72 | 0 | 0 |
| HLL15 | None | [10.00, 10.00] | [0%, 0%] | 1.477 | 1.477 | 4 | 4 |
| | Shuffle | [10.00, 10.00] | [0%, 0%] | 1.477 | 1.477 | 0 | 4 |
| | Rehash | [10.00, 10.00] | [0%, 0%] | 1.636 | 1.659 | 0 | 3.8 |
| | Mask | [10.000, 87.53] | [0%, 775%] | 1.578 | 1.578 | 0 | 0 |
| Hashed IDs | None | [10.000, 10.000] | [0%, 0%] | 0.002 | 0.002 | 19 | 19 |
| | Rehash | [10.000, 10.000] | [0%, 0%] | 0.002 | 0.002 | 0 | 19 |

Table A1c. 100 patient query.

| | | Estimated number of patients | | Wait (s) | | Risk: | Risk: |
|------------|-------------|------------------------------|----------------|----------|-------|-------|----------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [9.000, 205.6] | [-91%, 106%] | 0 | 0 | 59.78 | 59.78 |
| | Mask | [10.000, 734.1] | [-90%, 634%] | 0 | 0 | 0 | 0 |
| | MPC | [176.9, 205.6] | [77%, 106%] | 0.099 | 0.099 | 0 | 0 |
| HLL0 | None | [11.10, 541.8] | [-89%, 442%] | 0 | 0 | 0 | 0 |
| | Shuffle | [11.10, 541.8] | [-89%, 442%] | 0 | 0 | 0 | 0 |
| | Rehash | [11.10, 541.8] | [-89%, 442%] | 0 | 0 | 0 | 0 |
| | Mask | [11.10, 541.8] | [-89%, 442%] | 0 | 0 | 0 | 0 |
| | MPC | [11.10, 541.8] | [-89%, 442%] | 0.384 | 0.384 | 0 | 0 |
| | Shuffle+MPC | [11.10, 541.8] | [-89%, 442%] | 0.384 | 0.384 | 0 | 0 |
| HLL1 | None | [19.99, 807.6] | [-80%, 708%] | 0 | 0 | 0 | 0 |
| | Shuffle | [19.99, 807.6] | [-80%, 708%] | 0 | 0 | 0 | 0 |
| | Rehash | [19.99, 807.6] | [-80%, 708%] | 0 | 0 | 0 | 0 |
| | Mask | [19.99, 807.6] | [-80%, 708%] | 0 | 0 | 0 | 0 |
| | MPC | [19.99, 807.6] | [-80%, 708%] | 0.676 | 0.676 | 0 | 0 |
| | Shuffle+MPC | [19.99, 807.6] | [-80%, 708%] | 0.676 | 0.676 | 0 | 0 |
| HLL4 | None | [58.08, 158.6] | [-42%, 59%] | 0.001 | 0.001 | 0 | 0 |
| | Shuffle | [58.08, 158.6] | [-42%, 59%] | 0.001 | 0.001 | 0 | 0 |
| | Rehash | [58.08, 158.6] | [-42%, 59%] | 0.001 | 0.001 | 0 | 0 |
| | Mask | [58.08, 158.6] | [-42%, 59%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [58.08, 158.6] | [-42%, 59%] | 4.782 | 4.782 | 0 | 0 |
| | Shuffle+MPC | [58.08, 158.6] | [-42%, 59%] | 4.782 | 4.782 | 0 | 0 |
| HLL7 | None | [87.68, 115.3] | [-12%, 15%] | 0.006 | 0.006 | 0.07 | 0.07 |
| | Shuffle | [87.68, 115.3] | [-12%, 15%] | 0.006 | 0.006 | 0 | 0.07 |
| | Rehash | [87.68, 115.3] | [-12%, 15%] | 0.007 | 0.007 | 0 | 0.07 |
| | Mask | [87.68, 118.0] | [-12%, 18%] | 0.007 | 0.007 | 0 | 0 |
| | MPC | [87.68, 115.3] | [-12%, 15%] | 37.65 | 37.65 | 0 | 0 |
| | Shuffle+MPC | [87.68, 115.3] | [-12%, 15%] | 37.65 | 37.65 | 0 | 0 |
| HLL15 | None | [99.15, 100.2] | [-1%, 0%] | 1.44 | 1.44 | 36.12 | 36.12 |
| | Shuffle | [99.15, 100.2] | [-1%, 0%] | 1.44 | 1.44 | 0 | 36.12 |
| | Rehash | [99.15, 100.2] | [-1%, 0%] | 1.6 | 1.625 | 0 | 36.12 |
| | Mask | [48.41, 464.9] | [-52%, 365%] | 1.207 | 1.207 | 0 | 0 |
| Hashed IDs | None | [100.00, 100.00] | [0%, 0%] | 0.002 | 0.002 | 190.6 | 190.6 |
| | Rehash | [100.00, 100.00] | [0%, 0%] | 0.002 | 0.002 | 0 | 190.6 |

Table A1d. 1,000 patient query.

| | | Estimated num | ber of patients | Wait (s) | | Risk: | Risk: |
|------------|-------------|------------------|-----------------|----------|-------|-------|----------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [93.47, 1,973] | [-91%, 97%] | 0 | 0 | 43.84 | 44 |
| | Mask | [93.47, 2,236] | [-91%, 124%] | 0 | 0 | 0 | 0 |
| | MPC | [1,863, 1,973] | [86%, 97%] | 0.099 | 0.099 | 0 | 0 |
| HLL0 | None | [177.6, 22,737] | [-82%, 2174%] | 0 | 0 | 0 | 0 |
| | Shuffle | [177.6, 22,737] | [-82%, 2174%] | 0 | 0 | 0 | 0 |
| | Rehash | [177.6, 22,737] | [-82%, 2174%] | 0 | 0.001 | 0 | 0 |
| | Mask | [177.6, 22,737] | [-82%, 2174%] | 0 | 0 | 0 | 0 |
| | MPC | [177.6, 22,737] | [-82%, 2174%] | 0.385 | 0.385 | 0 | 0 |
| | Shuffle+MPC | [177.6, 22,737] | [-82%, 2174%] | 0.385 | 0.385 | 0 | 0 |
| HLL1 | None | [277.9, 5,118] | [-72%, 412%] | 0 | 0 | 0.04 | 0 |
| | Shuffle | [277.9, 5,118] | [-72%, 412%] | 0 | 0 | 0.03 | 0 |
| | Rehash | [277.9, 5,118] | [-72%, 412%] | 0 | 0.001 | 0 | 0.04 |
| | Mask | [237.9, 5,118] | [-76%, 412%] | 0 | 0 | 0 | 0 |
| | MPC | [277.9, 5,118] | [-72%, 412%] | 0.676 | 0.676 | 0 | 0 |
| | Shuffle+MPC | [277.9, 5,118] | [-72%, 412%] | 0.676 | 0.676 | 0 | 0 |
| HLL4 | None | [594.1, 1,498] | [-41%, 50%] | 0.001 | 0.001 | 0.19 | 0 |
| | Shuffle | [594.1, 1,498] | [-41%, 50%] | 0.001 | 0.001 | 0 | 0 |
| | Rehash | [594.1, 1,498] | [-41%, 50%] | 0.001 | 0.002 | 0 | 0 |
| | Mask | [594.1, 1,498] | [-41%, 50%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [594.1, 1,498] | [-41%, 50%] | 4.764 | 4.764 | 0 | 0 |
| | Shuffle+MPC | [594.1, 1,498] | [-41%, 50%] | 4.764 | 4.764 | 0 | 0 |
| HLL7 | None | [839.9, 1,180] | [-16%, 18%] | 0.006 | 0.006 | 1.67 | 2 |
| | Shuffle | [839.9, 1,180] | [-16%, 18%] | 0.006 | 0.006 | 0 | 2 |
| | Rehash | [839.9, 1,180] | [-16%, 18%] | 0.006 | 0.007 | 0 | 2 |
| | Mask | [832.6, 1,251] | [-17%, 25%] | 0.006 | 0.006 | 0 | 0 |
| | MPC | [839.9, 1,180] | [-16%, 18%] | 37.61 | 37.61 | 0 | 0 |
| | Shuffle+MPC | [839.9, 1,180] | [-16%, 18%] | 37.61 | 37.61 | 0 | 0 |
| HLL15 | None | [992.4, 1,008] | [-1%, 1%] | 1.44 | 1.44 | 375 | 375 |
| | Shuffle | [992.4, 1,008] | [-1%, 1%] | 1.44 | 1.44 | 0 | 375 |
| | Rehash | [992.4, 1,008] | [-1%, 1%] | 1.601 | 1.621 | 0 | 375 |
| | Mask | [93.02, 2,231] | [-91%, 123%] | 0.267 | 0.267 | 0 | 0 |
| Hashed IDs | None | [1000.0, 1000.0] | [0%, 0%] | 0.002 | 0.002 | 1,919 | 1,919 |
| | Rehash | [1000.0, 1000.0] | [0%, 0%] | 0.002 | 0.002 | 0 | 1,919 |

 Table A1e.
 10,000 patient query.

| | | Estimated num | ber of patients | Wait (s) | | Risk: | Risk: |
|------------|-------------|------------------|-----------------|----------|-------|--------|----------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [899.9, 19,470] | [-91%, 95%] | 0 | 0 | 2.65 | 2.65 |
| | Mask | [899.9, 19,477] | [-91%, 95%] | 0 | 0 | 0 | 0 |
| | MPC | [18,886, 19,470] | [89%, 95%] | 0.099 | 0.099 | 0 | 0 |
| HLL0 | None | [1,421, 363,799] | [-86%, 3538%] | 0 | 0 | 0.23 | 0.23 |
| | Shuffle | [1,421, 363,799] | [-86%, 3538%] | 0 | 0 | 0.23 | 0.23 |
| | Rehash | [1,421, 363,799] | [-86%, 3538%] | 0.001 | 0.01 | 0 | 0.23 |
| | Mask | [1,421, 182,085] | [-86%, 1721%] | 0 | 0 | 0 | 0 |
| | MPC | [1,421, 363,799] | [-86%, 3538%] | 0.384 | 0.384 | 0 | 0 |
| | Shuffle+MPC | [1,421, 363,799] | [-86%, 3538%] | 0.384 | 0.384 | 0 | 0 |
| HLL1 | None | [2,802, 56,273] | [-72%, 463%] | 0 | 0 | 0.31 | 0.31 |
| | Shuffle | [2,802, 56,273] | [-72%, 463%] | 0 | 0 | 0.23 | 0.31 |
| | Rehash | [2,802, 56,273] | [-72%, 463%] | 0.001 | 0.01 | 0 | 0.31 |
| | Mask | [2,559, 41,028] | [-74%, 310%] | 0 | 0 | 0 | 0 |
| | MPC | [2,802, 56,273] | [-72%, 463%] | 0.676 | 0.676 | 0 | 0 |
| | Shuffle+MPC | [2,802, 56,273] | [-72%, 463%] | 0.676 | 0.676 | 0 | 0 |
| HLL4 | None | [6,243, 16,850] | [-38%, 68%] | 0.001 | 0.001 | 1.84 | 1.84 |
| | Shuffle | [6,243, 16,850] | [-38%, 68%] | 0.001 | 0.001 | 0.23 | 1.84 |
| | Rehash | [6,243, 16,850] | [-38%, 68%] | 0.002 | 0.011 | 0 | 1.84 |
| | Mask | [5,704, 16,369] | [-43%, 64%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [6,243, 16,850] | [-38%, 68%] | 4.787 | 4.787 | 0.05 | 0.05 |
| | Shuffle+MPC | [6,243, 16,850] | [-38%, 68%] | 4.787 | 4.787 | 0 | 0.05 |
| HLL7 | None | [8,310, 11,347] | [-17%, 13%] | 0.006 | 0.006 | 15.73 | 15.73 |
| | Shuffle | [8,310, 11,347] | [-17%, 13%] | 0.006 | 0.006 | 0.23 | 15.73 |
| | Rehash | [8,310, 11,347] | [-17%, 13%] | 0.007 | 0.016 | 0 | 15.73 |
| | Mask | [7,167, 14,123] | [-28%, 41%] | 0.005 | 0.005 | 0 | 0 |
| | MPC | [8,310, 11,347] | [-17%, 13%] | 37.83 | 37.83 | 0.3 | 0.3 |
| | Shuffle+MPC | [8,310, 11,347] | [-17%, 13%] | 37.83 | 37.83 | 0 | 0.3 |
| HLL15 | None | [9,928, 10,075] | [-1%, 1%] | 1.462 | 1.462 | 3,707 | 3,707 |
| | Shuffle | [9,928, 10,075] | [-1%, 1%] | 1.462 | 1.462 | 0.23 | 3,707 |
| | Rehash | [9,928, 10,075] | [-1%, 1%] | 1.625 | 1.668 | 0 | 3,707 |
| | Mask | [899.9, 19,477] | [-91%, 95%] | 0.012 | 0.012 | 0 | 0 |
| Hashed IDs | None | [10,000, 10,000] | [0%, 0%] | 0.002 | 0.002 | 19,174 | 19,174 |
| | Rehash | [10,000, 10,000] | [0%, 0%] | 0.002 | 0.004 | 0 | 19,174 |

Table A1f. 100,000 patient query.

| | | Estimated number | er of patients | Wait (s) | | Risk: | Risk: |
|------------|-------------|--------------------|--|----------|--|---------|----------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [9,057, 194,126] | [-91%, 94%] | 0 | 0 | 0.02 | 0.02 |
| | Mask | [9,057, 194,126] | [-91%, 94%] | 0 | 0 | 0 | 0 |
| | MPC | [188,850, 194,126] | [89%, 94%] | 0.099 | 0.099 | 0 | 0 |
| HLL0 | None | [11,369, 727,598] | [-89%, 628%] | 0 | 0 | 1.32 | 1.32 |
| | Shuffle | [11,369, 727,598] | [-89%, 628%] | 0 | 0 | 1.32 | 1.32 |
| | Rehash | [11,369, 727,598] | [-89%, 628%] | 0.011 | 0.096 | 0 | 1.32 |
| | Mask | [11,369, 369,142] | [-89%, 269%] | 0 | 0 | 0 | 0 |
| | MPC | [11,369, 727,598] | [-89%, 628%] | 0.385 | 0.385 | 0 | 0 |
| | Shuffle+MPC | [11,369, 727,598] | [-89%, 628%] | 0.385 | 0.385 | 0 | 0 |
| HLL1 | None | [20,470, 393,030] | [-80%, 293%] | 0 | 0 | 2.71 | 2.71 |
| | Shuffle | [20,470, 393,030] | [-80%, 293%] | 0 | 0 | 1.32 | 2.71 |
| | Rehash | [20,470, 393,030] | [-80%, 293%] | 0.011 | 0.115 | 0 | 2.71 |
| | Mask | [20,470, 226,929] | Ints Relative Error Mean Max Hub Hub 6] [-91%, 94%] 0 0 0.02 6] [-91%, 94%] 0 0 0 126] [89%, 94%] 0.099 0.099 0 98] [-89%, 628%] 0 0 1.32 98] [-89%, 628%] 0.011 0.096 0 42] [-89%, 628%] 0.011 0.096 0 42] [-89%, 628%] 0.385 0.385 0 98] [-89%, 628%] 0.385 0.385 0 98] [-89%, 628%] 0.385 0.385 0 30] [-80%, 293%] 0 0 2.71 30] [-80%, 293%] 0.011 0.115 0 29] [-80%, 127%] 0 0 0 30] [-80%, 293%] 0.677 0.677 0 30] [-80%, 293%] 0.677 0.677 0 75] | 0 | | | |
| | MPC | [20,470, 393,030] | 98] [-89%, 628%] 0.385 0.385 0 30] [-80%, 293%] 0 0 2.71 30] [-80%, 293%] 0 0 1.32 30] [-80%, 293%] 0.011 0.115 0 29] [-80%, 127%] 0 0 0 30] [-80%, 293%] 0.677 0.677 0 30] [-80%, 293%] 0.677 0.677 0 75] [-42%, 70%] 0.001 0.001 19.51 75] [-42%, 70%] 0.001 0.001 1.32 75] [-42%, 70%] 0.012 0.123 0 79] [-55%, 38%] 0.001 0.001 0 75] [-42%, 70%] 4.771 4.771 0 75] [-42%, 70%] 4.771 4.771 0 | 0 | | | |
| | Shuffle+MPC | [20,470, 393,030] | [-80%, 293%] | 0.677 | 0.677 | 0 | 0 |
| HLL4 | None | [58,024, 169,675] | [-42%, 70%] | 0.001 | 0.001 | 19.51 | 20 |
| | Shuffle | [58,024, 169,675] | [-42%, 70%] | 0.001 | 0.001 | 1.32 | 19.51 |
| | Rehash | [58,024, 169,675] | [-42%, 70%] | 0.012 | 0.123 | 0 | 19.51 |
| | Mask | [45,325, 138,479] | [-55%, 38%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [58,024, 169,675] | [-42%, 70%] | 4.771 | Max Hub 0 0 0.02 0 0 0 0 0 0.099 0 0 1.32 0 0 0 0 0 | 0 | |
| | Shuffle+MPC | [58,024, 169,675] | [-42%, 70%] | 4.771 | 4.771 | 0 | 0 |
| HLL7 | None | [79,547, 117,654] | [-20%, 18%] | 0.006 | 0.006 | 158 | 158 |
| | Shuffle | [79,547, 117,654] | [-20%, 18%] | 0.006 | 0.006 | 1.32 | 158.3 |
| | Rehash | [79,547, 117,654] | [-20%, 18%] | 0.017 | 0.103 | 0 | 158 |
| | Mask | [15,973, 190,297] | [89%, 94%] 0.099 0.099 0 [-89%, 628%] 0 0 1.32 [-89%, 628%] 0 0 1.32 [-89%, 628%] 0.011 0.096 0 [-89%, 628%] 0.385 0.385 0 [-89%, 628%] 0.385 0.385 0 [-80%, 293%] 0 0 2.71 [-80%, 293%] 0 0 1.32 [-80%, 293%] 0.011 0.115 0 [-80%, 293%] 0.011 0.115 0 [-80%, 293%] 0.677 0.677 0 [-80%, 293%] 0.677 0.677 0 [-80%, 293%] 0.0677 0.677 0 [-42%, 70%] 0.001 0.001 19.51 [-42%, 70%] 0.001 0.001 1.32 [-42%, 70%] 0.012 0.123 0 [-55%, 38%] 0.001 0.001 0 [-42%, 70%] 4.771 4.771 0 | 0 | | | |
| | MPC | [79,547, 117,654] | [-20%, 18%] | 37.63 | 37.63 | 1.64 | 1.64 |
| | Shuffle+MPC | [79,547, 117,654] | [-20%, 18%] | 37.63 | 37.63 | 0 | 1.64 |
| HLL15 | None | [99,893, 101,691] | [-0%, 2%] | 1.363 | 1.363 | 36,876 | 36,876 |
| | Shuffle | [99,893, 101,691] | [-0%, 2%] | 1.363 | 1.363 | 1 | 36,876 |
| | Rehash | [99,893, 101,691] | [-0%, 2%] | 1.537 | 1.637 | 0 | 36,876 |
| | Mask | [9,057, 194,126] | [-91%, 94%] | 0.001 | 0.001 | 0 | 0 |
| Hashed IDs | None | [100,000, 100,000] | [0%, 0%] | 0.008 | 0.008 | 191,759 | 191,759 |
| | Rehash | [100,000, 100,000] | [0%, 0%] | 0.011 | 0.032 | 0 | 191,759 |

Table A1g. 1,000,000 patient query.

| | | Estimated number | of patients | Wai | t (s) | Risk: | Risk: |
|------------|-------------|------------------------|----------------|-------|-------|-----------|-----------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [90,222, 1,940,247] | [-91%, 94%] | 0 | 0 | 0 | 0 |
| | Mask | [90,222, 1,940,247] | [-91%, 94%] | 0 | 0 | 0 | 0 |
| | MPC | [1,888,932, 1,940,247] | [89%, 94%] | 0.1 | 0.1 | 0 | 0 |
| HLL0 | None | [181,899, 17,753,385] | [-82%, 1675%] | 0 | 0 | 11.71 | 11.71 |
| | Shuffle | [181,899, 17,753,385] | [-82%, 1675%] | 0 | 0 | 11.71 | 11.71 |
| | Rehash | [181,899, 17,753,385] | [-82%, 1675%] | 0.104 | 0.947 | 0 | 11.71 |
| | Mask | [90,950, 932,550] | [-91%, -7%] | 0 | 0 | 0 | 0 |
| | MPC | [181,899, 17,753,385] | [-82%, 1675%] | 0.385 | 0.385 | 0.2 | 0.2 |
| | Shuffle+MPC | [181,899, 17,753,385] | [-82%, 1675%] | 0.385 | 0.385 | 0.2 | 0.2 |
| HLL1 | None | [206,887, 11,581,296] | [-79%, 1058%] | 0 | 0 | 23.06 | 23.06 |
| | Shuffle | [206,887, 11,581,296] | [-79%, 1058%] | 0 | 0 | 12.15 | 23.06 |
| | Rehash | [206,887, 11,581,296] | [-79%, 1058%] | 0.105 | 0.947 | 0 | 23.06 |
| | Mask | [109,175, 1,273,729] | [-89%, 27%] | 0 | 0 | 0 | 0 |
| | MPC | [206,887, 11,581,296] | [-79%, 1058%] | 0.679 | 0.679 | 0.39 | 0.39 |
| | Shuffle+MPC | [206,887, 11,581,296] | [-79%, 1058%] | 0.679 | 0.679 | 0.2 | 0.39 |
| HLL4 | None | [538,869, 1,713,823] | [-46%, 71%] | 0.001 | 0.001 | 186.3 | 186.3 |
| | Shuffle | [538,869, 1,713,823] | [-46%, 71%] | 0.001 | 0.001 | 12.41 | 186.3 |
| | Rehash | [538,869, 1,713,823] | [-46%, 71%] | 0.105 | 0.943 | 0 | 186.3 |
| | Mask | [90,644, 1,892,176] | [-91%, 89%] | 0 | 0 | 0 | 0 |
| | MPC | [538,869, 1,713,823] | [-46%, 71%] | 4.754 | 4.754 | 1.91 | 1.91 |
| | Shuffle+MPC | [538,869, 1,713,823] | [-46%, 71%] | 4.754 | 4.754 | 0.2 | 1.91 |
| HLL7 | None | [837,269, 1,158,432] | [-16%, 16%] | 0.006 | 0.006 | 1,508 | 1,508 |
| | Shuffle | [837,269, 1,158,432] | [-16%, 16%] | 0.006 | 0.006 | 12.48 | 1,508 |
| | Rehash | [837,269, 1,158,432] | [-16%, 16%] | 0.111 | 0.955 | 0 | 1,508 |
| | Mask | [90,222, 1,940,247] | [-91%, 94%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [837,269, 1,158,432] | [-16%, 16%] | 37.39 | 37.39 | 14.71 | 14.71 |
| | Shuffle+MPC | [837,269, 1,158,432] | [-16%, 16%] | 37.39 | 37.39 | 0.2 | 14.71 |
| HLL15 | None | [987,401, 1,011,968] | [-1%, 1%] | 1.379 | 1.379 | 348,258 | 348,258 |
| | Shuffle | [987,401, 1,011,968] | [-1%, 1%] | 1.379 | 1.379 | 12.5 | 348,258 |
| | Rehash | [987,401, 1,011,968] | [-1%, 1%] | 1.652 | 2.537 | 0 | 348,258 |
| | Mask | [90,222, 1,940,247] | [-91%, 94%] | 0.001 | 0.001 | 0 | 0 |
| Hashed IDs | None | [1,000,000, 1,000,000] | [0%, 0%] | 0.071 | 0.071 | 1,917,817 | 1,917,817 |
| | Rehash | [1,000,000, 1,000,000] | [0%, 0%] | 0.097 | 0.302 | 0 | 1,917,817 |

Table A1h. 10,000,000 patient query.

| | | Estimated number of | f patients | Wai | t (s) | Risk: | Risk: |
|------------|-------------|--------------------------|----------------|-------|-------|---|------------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [902,793, 19,402,938] | [-91%, 94%] | 0 | 0 | 0 | 0 |
| | Mask | [902,793, 19,402,938] | [-91%, 94%] | 0 | 0 | 0 | 0 |
| | MPC | [18,884,586, 19,402,938] | [89%, 94%] | 0.105 | 0.105 | 0 | 0 |
| HLL0 | None | [1,455,196, 71,013,541] | [-85%, 610%] | 0 | 0 | 70.06 | 70 |
| | Shuffle | [1,455,196, 71,013,541] | [-85%, 610%] | 0 | 0 | 70 | 70 |
| | Rehash | [1,455,196, 71,013,541] | [-85%, 610%] | 1.032 | 9.685 | 0 | 70 |
| | Mask | [734,987, 17,239,998] | [-93%, 72%] | 0 | 0 | 0 | 0 |
| | MPC | [1,455,196, 71,013,541] | [-85%, 610%] | 0.383 | 0.383 | 1 | 1 |
| | Shuffle+MPC | [1,455,196, 71,013,541] | [-85%, 610%] | 0.383 | 0.383 | 1 | 1 |
| HLL1 | None | [2,215,613, 41,923,242] | [-78%, 319%] | 0 | 0 | 140.8 | 141 |
| | Shuffle | [2,215,613, 41,923,242] | [-78%, 319%] | 0 | 0 | 92.64 | 140.8 |
| | Rehash | [2,215,613, 41,923,242] | [-78%, 319%] | 1.033 | 9.483 | 0 | 141 |
| | Mask | [887,447, 18,931,827] | [-91%, 89%] | 0 | 0 | 0 | 0 |
| | MPC | [2,215,613, 41,923,242] | [-78%, 319%] | 0.675 | 0.675 | 2 | 2 |
| | Shuffle+MPC | [2,215,613, 41,923,242] | [-78%, 319%] | 0.675 | 0.675 | 1.17 | 2 |
| HLL4 | None | [6,171,672, 16,428,565] | [-38%, 64%] | 0.001 | 0.001 | 1,123 | 1,123 |
| | Shuffle | [6,171,672, 16,428,565] | [-38%, 64%] | 0.001 | 0.001 | 122 | 1,123 |
| | Rehash | [6,171,672, 16,428,565] | [-38%, 64%] | 1.035 | 9.495 | 0 | 1,123 |
| | Mask | [902,793, 19,402,938] | [-91%, 94%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [6,171,672, 16,428,565] | [-38%, 64%] | 4.755 | 4.755 | 18 | 18 |
| | Shuffle+MPC | [6,171,672, 16,428,565] | [-38%, 64%] | 4.755 | 4.755 | 1.18 | 18 |
| HLL7 | None | [8,352,290, 12,307,282] | [-16%, 23%] | 0.006 | 0.006 | 8,947 | 8,947 |
| | Shuffle | [8,352,290, 12,307,282] | [-16%, 23%] | 0.006 | 0.006 | 126 | 8,947 |
| | Rehash | [8,352,290, 12,307,282] | [-16%, 23%] | 1.043 | 9.496 | 0 | 8,947 |
| | Mask | [902,793, 19,402,938] | [-91%, 94%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [8,352,290, 12,307,282] | [-16%, 23%] | 37.41 | 37.41 | 144 | 144 |
| | Shuffle+MPC | [8,352,290, 12,307,282] | [-16%, 23%] | 37.41 | 37.41 | 1.18 | 144 |
| HLL15 | None | [9,887,923, 10,123,720] | [-1%, 1%] | 1.392 | 1.392 | 2,127,583 | 2,127,583 |
| | Shuffle | [9,887,923, 10,123,720] | [-1%, 1%] | 1.392 | 1.392 | 127 | 2,127,583 |
| | Rehash | [9,887,923, 10,123,720] | [-1%, 1%] | 2.641 | 11.55 | 0 70.06 70 0 0 0 1 1 140.8 92.64 0 0 2 1.17 1,123 122 0 0 18 1.18 8,947 126 0 0 144 1.18 2,127,583 127 | 2,127,583 |
| | Mask | [902,793, 19,402,938] | [-91%, 94%] | 0.001 | 0.001 | 0 | 0 |
| Hashed IDs | None | [10,000,000, 10,000,000] | [0%, 0%] | 0.794 | 0.794 | 19,178,114 | 19,178,114 |
| | Rehash | [10,000,000, 10,000,000] | [0%, 0%] | 1.045 | 3.09 | 0 | 19,178,114 |

Table A1i. 100,000,000 patient query.

| | | Estimated number of | patients | Wai | t (s) | Risk: | Risk: |
|------------|-------------|----------------------------|----------------|-------|-------|-------------|-------------|
| Method | Obfuscation | Range of Counts | Relative Error | Mean | Max | Hub | Hub+Site |
| Count | None | [9,431,902, 200,018,431] | [-91%, 100%] | 0 | 0 | 0 | 0 |
| | Mask | [9,431,902, 200,018,431] | [-91%, 100%] | 0 | 0 | 0 | 0 |
| | MPC | [199,984,637, 200,018,431] | [100%, 100%] | 0.171 | 0.171 | 0 | 0 |
| HLL0 | None | [11,641,564, 818,287,824] | [-88%, 718%] | 0 | 0 | 99.97 | 99.97 |
| | Shuffle | [11,641,564, 818,287,824] | [-88%, 718%] | 0 | 0 | 99.97 | 99.97 |
| | Rehash | [11,641,564, 818,287,824] | [-88%, 718%] | 9.42 | 84.36 | 0 | 99.97 |
| | Mask | [9,431,902, 200,018,431] | [-91%, 100%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [11,641,564, 818,287,824] | [-88%, 718%] | 0.387 | 0.387 | 9.91 | 9.91 |
| | Shuffle+MPC | [11,641,564, 818,287,824] | [-88%, 718%] | 0.387 | 0.387 | 9.91 | 9.91 |
| HLL1 | None | [22,952,975, 448,641,535] | [-77%, 349%] | 0 | 0 | 199.9 | 199.9 |
| | Shuffle | [22,952,975, 448,641,535] | [-77%, 349%] | 0 | 0 | 198.5 | 199.9 |
| | Rehash | [22,952,975, 448,641,535] | [-77%, 349%] | 9.42 | 84.36 | 0 | 199.9 |
| | Mask | [9,431,902, 200,018,431] | [-91%, 100%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [22,952,975, 448,641,535] | [-77%, 349%] | 0.681 | 0.681 | 19.82 | 19.82 |
| | Shuffle+MPC | [22,952,975, 448,641,535] | [-77%, 349%] | 0.681 | 0.681 | 10.75 | 19.82 |
| HLL4 | None | [57,717,266, 167,663,627] | [-42%, 68%] | 0.001 | 0.001 | 1,599 | 1,599 |
| | Shuffle | [57,717,266, 167,663,627] | [-42%, 68%] | 0.001 | 0.001 | 854.1 | 1,599 |
| | Rehash | [57,717,266, 167,663,627] | [-42%, 68%] | 9.422 | 84.36 | 0 | 1,599 |
| | Mask | [9,431,902, 200,018,431] | [-91%, 100%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [57,717,266, 167,663,627] | [-42%, 68%] | 4.768 | 4.768 | 153.8 | 153.8 |
| | Shuffle+MPC | [57,717,266, 167,663,627] | [-42%, 68%] | 4.768 | 4.768 | 11.69 | 153.8 |
| HLL7 | None | [84,484,568, 117,231,365] | [-16%, 17%] | 0.006 | 0.006 | 12,795 | 12,795 |
| | Shuffle | [84,484,568, 117,231,365] | [-16%, 17%] | 0.006 | 0.006 | 1,199 | 12,795 |
| | Rehash | [84,484,568, 117,231,365] | [-16%, 17%] | 9.426 | 84.36 | 0 | 12,795 |
| | Mask | [9,431,902, 200,018,431] | [-91%, 100%] | 0.001 | 0.001 | 0 | 0 |
| | MPC | [84,484,568, 117,231,365] | [-16%, 17%] | 37.43 | 37.43 | 1,246 | 1,246 |
| | Shuffle+MPC | [84,484,568, 117,231,365] | [-16%, 17%] | 37.43 | 37.43 | 11.83 | 1,246 |
| HLL15 | None | [99,097,598, 101,037,154] | [-1%, 1%] | 1.362 | 1.362 | 3,259,256 | 3,259,256 |
| | Shuffle | [99,097,598, 101,037,154] | [-1%, 1%] | 1.362 | 1.362 | 1,265 | 3,259,256 |
| | Rehash | [99,097,598, 101,037,154] | [-1%, 1%] | 10.96 | 85.89 | 0 | 3,259,256 |
| | Mask | [9,431,902, 200,018,431] | [-91%, 100%] | 0.001 | 0.001 | 0 | 0 |
| Hashed IDs | None | [100,000,000, 100,000,000] | [0%, 0%] | 10.12 | 10.12 | 199,999,801 | 199,999,801 |
| | Rehash | [100,000,000, 100,000,000] | [0%, 0%] | 11.56 | 23.31 | 0 | 199,999,801 |