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Supplementary Materials for

Plasma-derived extracellular vesicle analysis and deconvolution enable prediction and tracking of melanoma checkpoint blockade outcome

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The PDF file includes:

Figs. S1 to S10 Legends for tables S1 to S5 Supplementary Note

Other Supplementary Material for this manuscript includes the following:

(available at advances.sciencemag.org/cgi/content/full/6/46/eabb3461/DC1)

Tables S1 to S5

Supplementary figure legends

Supplementary figure 1: (a) Outline of both the discovery and validation study cohort. The complete cohort metadata is available in Supplementary Table 1. (b) Outline of the processing and analysis steps undertaken to generate the major results in the paper.

Supplementary figure 2: *In vitro* EV characterization. (a) Electron microscope images of representative cellline and patient-derived EVs. (b) Nanosight analysis of a representative cell line sample (RPMI) and patient sample. (c) Western blot of 5 cell line/paired EV proteins with no calnexin within EV, but high levels of CD9 within EV as compared to paired cells.

Supplementary figure 3: Characterization of transcriptomic similarities between cell-line derived melanoma samples and their matched EV. (a) Scatter plot visualizing differences between tissue and plasma-derived EV in patient samples. (b) Histogram visualizing the log fold changes between melanoma cell-lines and their EV counterparts. The profiles were compiled using the average of four expression profiles. (c) Concordance analysis across our 4 cell-line samples. Concordance was calculated by using a low expression cutoff as a cut-off for expressed vs. non-expressed status. Genes that were either expressed or not expressed in both tissue and EV compartments are considered concordant. (d) Correlation plot between all 4 cell-lines and their EV counterparts.

Supplementary figure 4: Box-plots and associated p-values for validated MSigDB canonical pathways that differ between responders (green) and non-responders (purple). The visualized points are individual GSVA scores inferred for each pathway. The p-values were generated by comparing responder vs. non-responder GSVA scores via a Mann-Whitney U-test.

Supplementary figure 5: (a-e) Un-normalized time-series plots showing time dynamics for pathways and genes discussed in **Fig. 2b** and **Fig. 2d**. Individual GSVA scores were used to plot the TCR KEGG pathway, while platform-normalized log2 expression values were used to plot the individual gene expression levels. **Supplementary figure 6:** (a-d) Normalized and unnormalized time-series plots showing time dynamics for selected pathways. The plotting was performed per methodology previously discussed in captions for **Fig. 2b**,

Fig. 2d and SFig 5.

Supplementary figure 7: Kaplan-Meier progression-free and overall survival curves for selected genes that showed significant or near-significant differences between high-expressed and low-expressed patients. **Supplementary figure 8:** Kaplan-Meier progression-free and overall survival curves for selected genes that showed significant or near-significant differences between high-expressed and low-expressed patients. **Supplementary figure 9:** Example of per-patient imputed tumor-EV expression from our Bayesian deconvolution model. (a-b) Posterior estimates for two illustrative genes for high immune fraction (CD8A) and high tumor fraction (MIR47888). (c-d) Predicted tumor-derived EV expression from our deconvolution model for CD8A and MIR4788 for a subset of patients.

Supplementary figure 10: Kaplan-Meier progression-free survival (PFS) plots for COSMIC mutational fraction in the validation evRNA-seq cohort. High and low expression classifications were determined for each patient based on whether a particular patient's COSMIC mutational fraction was in the top half (teal) or bottom half (yellow) of the validation cohort's COSMIC mutational fraction distribution.

Supplementary Tables Legends

Supplementary Table 1: Worksheet 1: Anonymized metadata of patient cohort from discovery cohort. Worksheet 2: anonymized metadata of patient cohort from validation cohort. Additional columns in worksheet 2 denote driver mutations detected by SNaPShot tumor sequencing and the specific mutations validated in our evRNA-seq mutational analysis.

Supplementary Table 2: GO pathways enriched in patient EV-unique or tumor-unique samples.

Supplementary Table 3: Worksheet 1: Validated DEGs and associated statistics from limma from our ontreatment DEG analysis. Worksheet 2: All DEGs from on-treatment discovery cohort and associated limma statistics. Worksheet 3: All DEGs from on-treatment validation cohort and associated limma statistics.

Supplementary Table 4: Worksheet 1: Validated DEGs and associated statistics from limma from our pretreatment DEG analysis. Worksheet 2: All DEGs from pre-treatment discovery cohort and associated limma statistics. Worksheet 3: All DEGs from pre-treatment validation cohort and associated limma statistics.

Supplementary Table 5: Estimated mixing fractions from our EV deconvolution model running in multi-gene mode for all genes. Full details regarding the model are available in the supplemental note.



SFig. 1

samples Fig. 2b, 2d)

A) Electron Microscopy B) NANOSIGHT



SFig. 2





Histogram of average expression change in cell lines



d.



On-treatment v differential pat

alidated	Discovery Cohort	Validation Cohort
hwavs	KEGG_TGF_BETA_SIGNALING_PATHWAY (p=0.02761)	KEGG_TGF_BETA_SIGNALING_PATHWAY (p=0.00167)
innayo		
	KEGG_T_CELL_RECEPTOR_SIGNALING_PATHWAY (p=0.06232)	KEGG_T_CELL_RECEPTOR_SIGNALING_PATHWAY (p=0.05553)
	BIOCARTA_P53HYPOXIA_PATHWAY (p=0.04407)	BIOCARTA_P53HYPOXIA_PATHWAY (p=0.08143)
	BIOCARTA_TCRA_PATHWAY (p=0.06771)	BIOCARTA_TCRA_PATHWAY (p=0.09753)
	BIOCARTA_MTOR_PATHWAY (p=0.09304)	BIOCARTA_MTOR_PATHWAY (p=0.0675)
	-0.4 -0.2 0.0 0.2 0.4	-0.25 0.00 0.25 0.50
	BIOCARTA_CTLA4_PATHWAY (p=0.00458)	BIOCARTA_CTLA4_PATHWAY (p=0.08143)
	-0.6 -0.3 0.0 0.3	-0.6 -0.3 0.0 0.3 0.6
	BIOCARTA_TNFR2_PATHWAY (p=0.05728)	BIOCARTA_TNFR2_PATHWAY (p=0.0235)
	-0.6 -0.3 0.0 0.3	-0.2 0.0 0.2 0.4
	PID_SMAD2_3NUCLEAR_PATHWAY (p=0.02264)	PID_SMAD2_3NUCLEAR_PATHWAY (p=0.03672)
	-0.4 -0.2 0.0 0.2	-0.2 -0.1 0.0 0.1 0.2
	PID_NOTCH_PATHWAY (p=0.04407)	PID_NOTCH_PATHWAY (p=0.0295)
	-0.2 0.0 0.2	-0.1 0.0 0.1 0.2 0.3
	PID_ECADHERIN_KERATINOCYTE_PATHWAY (p=0.05728)	PID_ECADHERIN_KERATINOCYTE_PATHWAY (p=0.03672)
		•• ••
	-0.50 -0.25 0.00 0.25 0.50	
	PID_ALK1_PAIHWAY (p=0.0/347)	PID_ALK1_PAI HWAY (p=0.04084)
	-0.4 -0.2 0.0 0.2 PID ERA GENOMIC PATHWAY (p=0.00151)	-0.2 0.0 0.2 0.4 PID ERA GENOMIC PATHWAY (n=0.02635)
		4 - 61161111111111111
	-0.25 0.00 0.25 PID_VEGFR1_PATHWAY (p=0.00308)	-0.2 0.0 0.2 PID_VEGFR1_PATHWAY (p=0.0675)
	REACTOME_SIGNALING_BY_NOTCH2 (p=0.07347)	REACTOME_SIGNALING_BY_NOTCH2 (p=0.00657)
	-0.4 -0.2 0.0 0.2	-0.2 0.0 0.2
	REACTOME_SIGNALING_BY_NOTCH1 (p=0.02502)	REACTOME_SIGNALING_BY_NOTCH1 (p=0.0675)
	-0.4 -0.2 0.0 0.2	-0.2 -0.1 0.0 0.1 0.2 0.3
	REACTOME_CD28_CO_STIMULATION (p=0.09304)	REACTOME_CD28_CO_STIMULATION (p=0.09753)
	-0.50 -0.25 0.00 0.25	-0.25 0.00 0.25 0.50
	REACTOME_COSTIMULATION_BY_THE_CD28_FAMILY (p=0.04407)	REACTOME_COSTIMULATION_BY_THE_CD28_FAMILY (p=0.04084)
	-0.4 -0.2 0.0 0.2 0.4	-0.2 0.0 0.2 0.4
	REACTOME_KINESINS (p=0.03673)	REACTOME_KINESINS (p=0.0065/)
	-0.4 -0.2 0.0 0.2 0.4 BIOCARTA BANBP2 PATHWAY (p=0.06232)	-0.2 0.0 0.2 BIOCARTA RANB22 PATHWAY (n=0.00754)
		• • • • • • • • • • • • • • • • • • •
	-0.6 -0.3 0.0 0.3 REACTOME MISCELLANEOUS SUBSTRATES (p=0.02045)	-0.3 0.0 0.3 0.6 REACTOME_MISCELLANEOUS_SUBSTRATES (p=0.0675)
RE	ACTOME_SUMOYLATION_OF_INTRACELLULAR_RECEPTORS (p=0.02502)	REACTOME_SUMOYLATION_OF_INTRACELLULAR_RECEPTORS (p=0.0742)
	-0.25 0.00 0.25	-0.2 0.0 0.2
	REACTOME_MITOCHONDRIAL_TRANSLATION (p=0.04407)	REACTOME_MITOCHONDRIAL_TRANSLATION (p=0.0675)
	-0.6 -0.3 0.0 0.3	-0.25 0.00 0.25 0.50
REACTO	DME_REGULATION_OF_TP53_ACTIVITY_THROUGH_ACETYLATION (p=0.02761)	REACTOME_REGULATION_OF_TP53_ACTIVITY_THROUGH_ACETYLATION (p=0.08919)
	-0.50 -0.25 0.00 0.25	-0.2 0.0 0.2 0.4
REACTO	DME_COPI_DEPENDENT_GOLGI_TO_ER_RETROGRADE_TRAFFIC (p=0.04817)	REACTOME_COPI_DEPENDENT_GOLGI_TO_ER_RETROGRADE_TRAFFIC (p=0.08919)
F	IEAC IUME_SIGNALING_BY_IGF_BEIA_FAMILY_MEMBERS (p=0.06771)	
	-0.50 -0.25 0.00 0.25	-0.4 -0.2 0.0 0.2 0.4

GSVA level in responder GSVA level in non-responder Γ

SFig. 4





C.







d.











Time-series for BIOCARTA_CTLA4_PATHWAY







SFig. 6





Strata - Low Expression - High Expression

Strata - Low Expression - High Expression



a.

b. Posterior distributions of mixing and scaling coefficients for CD8A Posterior distributions of mixing and scaling coefficients for MIR4788 Posterior density for mixing coefficient Posterior density for mixing coefficient Posterior density for s Posterior density for s 0.08 0.10 н ÷ Γ 0.07 T n Г 0.08 0.06 1 n Probability 90°0 П П 0.05 П Probability Probability Probabilit Γ 0.04 П Г 0.04 H 0.03 Ľ Г 0.02 ï Ľ 0.02 Ľ 0.01 0.00 0.00 0.2 0.4 0.6 0.8 1.0 0.4 0.2 0.0 0.2 0.4 0.6 0.8 0.0 0.2 0.4 0.6 0.8 1.0 0.2 0.2 0.4 0.6 0.8 1.0

C.

Posterior imputed tumor EV distributions for CD8A





SFig. 9

1.0

EV COSMIC Mutational Fraction PFS Kaplan-Meier



SFig. 10

Supplemental Note: Plasma-derived EV deconvolution model

In this supplemental note, we provide the mathematical background underlying our deconvolution model, as described in Figure 4a of "Plasma-derived extracellular vesicles analysis and deconvolution enables prediction and tracking of melanoma checkpoint blockade outcome". The rationale for the model is introduced in the main text. References in the Supplemental Note will also reference the main text. To summarize, we want to infer the contribution of the tumor-derived EV component and non-tumor derived (interchangeably referred to as "immune" and "non-tumor") component to the observed plasma-derived EV transcriptomic profile. In contrast to existing deconvolution models designed for bulk deconvolution (e.g., CIBERSORT[12]), our model explicitly models the changes in transcript abundance as a result of export/packaging from the transcript abundance in the tumor to the transcript abundance. All of the data shown both here and in the main-figures related to deconvolution utilized only non-platformcorrected discovery cohort microarray data, since the discovery cohort exoRNA-seq included only plasmaderived EV samples and thus were not suitable inputs for our deconvolution model (see Supplementary Figure 1b for more detailed information regarding our analysis methodology). We created two versions of the deconvolution probabilistic model. In single-gene mode, the probabilistic model is fully fitted using the No-U-Turn Sampler (NUTS) Hamiltonian Monte Carlo (HMC) algorithm[46] and full posterior estimates for all the relevant parameters are returned. This model is fitted using the probabilistic programming language Stan [45]. This mode is designed for in-depth analysis of a single gene (or few genes), or situations where inferred parameters (e.g., scaling parameter, patient inferred tumor-EV expression) of interest requires a full posterior estimate. Due to the time and resource intensive nature of the fitting process, it is impractical to perform full MCMC inference when we want to analyze the deconvolution profiles for tens of thousands of genes. Thus, we included a second mode, a **multi-gene mode**, in which we fit a simplified version of the single-gene model using Scipy's implementation sequential least squares programming (SLSQP) to return a point estimate of the mixing coefficient. The single-gene model not only returns posterior distribution mixing fraction, but also the full posterior distribution of the scaling coefficient, which allows per-patient imputation of the tumor-derived EV fractions (Supplemental Figure 9); however, the multi-gene model only returns a single maximum a posterori (MAP) estimate of the mixing fraction. We envision the usage of the single-gene model in cases when a specific gene needs to carefully dissected and more robust inference is required, whereas the multi-gene model can be used on large-scale transcriptomic datasets to infer population-wide mixing fractions.

1 Single-gene Bayesian probabilistic model

- N: number of patient derived tumor profiles and tumor EV profiles
- M: number of cell-line tumor and tumor EV profiles
- x_i : the *i*th patient's observed tumor expression for the current gene
- y_i : the *i*th patient's observed peripheral-blood derived expression for the current gene
- w_j : the *j*th cell-line's
- α : mixing fraction between tumor-component and immune-component
- σ_T^2 : variance component
- μ_I : Immune component mean (fixed parameter)
- σ_I^2 : Immune variance component (fixed parameter)



Prior specification

$$s \sim \mathcal{N}(0, 2)$$

$$\sigma_T^2 \sim \mathcal{IG}(1, 1)$$

$$\alpha \sim \mathcal{B}(2, 2)$$

Where $\mathcal B$ denotes the Beta distribution and $\mathcal I\mathcal G$ denotes the Inverse-Gamma distribution.

Data likelihood

$$p(y_i|\alpha, \sigma_T^2; \mu_I, \sigma_I^2) = \underbrace{\alpha \mathcal{N}(y_i|x_i + s, \sigma_T^2)}_{\text{Tumor EV component}} + \underbrace{(1 - \alpha)\mathcal{N}(y_i|\mu_I, \sigma_I^2)}_{\text{Immune/background EV component}}$$
(1)

$$p(w_j|s, v_j, \sigma_T^2) = \mathcal{N}(w_j|s + v_j, \sigma_T^2)$$
⁽²⁾

$$p(\mathbf{y}, \mathbf{w} | \mathbf{x}, \mathbf{v}, s, \alpha, \sigma_T^2; \mu_I, \sigma_I^2) = \prod_{i=1}^N \left[\alpha \mathcal{N}(y_i | x_i + s, \sigma_T^2) + (1 - \alpha) \mathcal{N}(y_i | \mu_I, \sigma_I^2) \right] \prod_{j=1}^M \mathcal{N}(w_j | s + v_j, \sigma_T^2)$$
(3)

Full Posterior

$$p(\mathbf{y}, \mathbf{w} | \mathbf{x}, \mathbf{v}, s, \alpha, \sigma_T^2; \mu_I, \sigma_I^2) \propto p(\mathbf{y}, \mathbf{w}, \mathbf{x}, \mathbf{v}, s, \alpha, \sigma_T^2; \mu_I, \sigma_I^2) p(s, \sigma_T^2, \alpha)$$
(4)
$$p(\mathbf{y}, \mathbf{w} | \mathbf{x}, \mathbf{v}, s, \alpha, \sigma_T^2; \mu_I, \sigma_I^2) \propto \prod_{i=1}^N \left[\alpha \mathcal{N}(y_i | x_i + s, \sigma_T^2) + (1 - \alpha) \mathcal{N}(y_i | \mu_I, \sigma_I^2) \right] \prod_{j=1}^M \mathcal{N}(w_j | s + v_j, \sigma_T^2)$$
(5)

$$p(s,\alpha,\sigma_T^2|\mathbf{x},\mathbf{v},\mathbf{y},\mathbf{w};\mu_I,\sigma_I^2) \propto \prod_{i=1}^N \left[\alpha \mathcal{N}(y_i|x_i+s,\sigma_T^2) + (1-\alpha)\mathcal{N}(y_i|\mu_I,\sigma_I^2) \right] \prod_{j=1}^M \mathcal{N}(w_j|s+v_j,\sigma_T^2) p(s,\alpha,\sigma_T^2)$$
(6)

2 Multi-gene probabilistic model

For the multi-gene model, we utilize a simplified version of the model from the single gene model to reduce the time and computational intensiveness of the model. The multi-gene model only returns the mixing fraction α for the gene-of-interest, and as a result, it runs significantly faster and is able to process transcriptome-wide datasets on the order of hours instead of days on a single computer, unlike the more computationally intensive single-gene model.

The multi-gene model differs from the single gene model in several key respects:

- The inference of the scaling coefficient s is not done jointly with the inference of α and other parameters of interest. Instead, it is precomputed for each gene. To compute s, we take the mean difference between v_j and w_j for each gene and use this as a fixed constant.
- Thus, the inference of α is simplified into a much simpler problem that only depends on the right plate in the graph model depicted in section 1. Since we are interested in only in α , we optimize the log posterior formula using Sequential Least Squares Programming (SLSQP) from the python SciPy library with the appropriate constraints for α . The $\mathcal{B}(2, 2)$ prior for α is retained.

3 Validation of our deconvolution model using CIBERSORTx



Figure 1: Scatterplot with line-of-best-fit and correlation between inferred CIBERSORTx and our deconvolution model inferred tumor fraction estimates on discovery cohort data

In order to provide evidence that our model is correctly partitioning genes into tumor and non-tumor components, we utilized CIBERSORTx[13]- a recently published bulk deconvolution program from Newman et al. that attempts to separate bulk transcriptomic profiles into component cell-type-specific profiles. In order to run the program, we utilized first inputted our discovery cohort (non-cross-platform corrected) microarray data matrix into the online CIBERSORTx web portal and utilized the melanoma reference profiles from Tirosh et al.'s Science 2016 single-cell dissection of metastatic melanoma that is provided by CIBERSORT's default online profiles [12,13]. Since the algorithm generates estimates for all component cell-types instead of tumor-only profiles, we averaged the non-tumor cell-types in order to make it comparable to our non-tumor component estimation. A direct comparison of our values can be found in Supplemental Note Figure 1. We see that there's a slight but significant correlation between CIBER-SORTx inferred-tumor fraction and tumor fraction inferred from our deconvolution model; however, it is clear from the CIBERSORTx density plot (y-axis) that the inferred tumor fraction is roughly normally distributed, an assumption that our model does not make (see density plot on x-axis). This continuous coding of tumor fractions hinders direct comparison of model predictions between CIBERSORTx and our model; thus, in order to better compare our cell-type predictions, we binarized model predictions for each gene as either tumor-derived or non-tumor derived using a cut-off of 0.5 as the threshold between tumor and non-tumor (same threshold used in the main manuscript). Using this cutoff, we can generate the confusion matrix found in Supplementary Note Table 1.

	CIBERSORTx tumor	CIBERSORTx non-tumor
EV deconvolution tumor	12984	2319
EV deconvolution non-tumor	3719	1244

Table 1: Confusion matrix between CIBERSORTx and our deconvolution model using 0.5 tumor fraction as a cutoff between tumor and non-tumor binary classification of genes

We can assess the concordance between binary predictions generated by CIBERSORTx and our model using values from the confusion matrix. This corresponded to the following binary classification statistics shown in Supplementary Note Table 2, using CIBERSORTx tumor predictions as "ground" truth and our deconvolution model estimates as predictions. We see that overall accuracy (0.70), sensitivity (0.78), precision (0.85), and F1-score (0.81) all support the ability of our deconvolution model to properly classify CIBERSORTx predicted tumor-derived genes. However, the two models' predictions diverge significantly in terms of specificity (0.35) and negative predictive value (0.25), suggesting that the two models differ significantly in the overall prediction of non-tumor derived genes, with our model predicting a higher fraction of tumor-derived genes relative to CIBERSORTx. This is likely a result of the different distributional assumptions regarding tumor vs. non-tumor distributions between the two models (see Supplementary Note Figure 1). We reason that our model is likely to approximate reality more closely, based on known literature regarding significant increases in both overall and tumor-derived EV load in plasma during progression[10]. Furthermore, as mentioned in the main text, our model explicitly accounts for EV-specific characteristics - such as the differential EV packaging process - that bulk deconvolution techniques like CIBERSORTx does not account for. Additionally, our the underlying reference profiles is trained directly or inferred utilizing EV data, which is likely a far better approximation of the underlying mixture profiles in the context of cell-type deconvolution than bulk references. Though in silico independent validation via CIBERSORTx provides evidence for the validity of our deconvolution model predictions, particularly the prediction of tumor-derived genes, in vivo experimental evidence gathered via tumor vs. non-tumor derived EV selection/enrichment remains the gold standard to validate our model.

Metrics	Value
Accuracy	0.70
Sensitivity	0.78
Specificity	0.35
Precision	0.85
Negative Predictive Value	0.25
False Positive Rate	0.65
F1 Score	0.81

Table 2: Binary classification performance metrics generated from the confusion matrix in Table 1

4 Source Code

4.1 Stan code for the single-gene model:

```
data {
          int<lower = 0> N; // number of patient samples
int<lower = 0> M; // number of cell line samples/controls
real<lower = 0> L; //lower bound on truncated normal
           real<lower = 0> mu_i; // non-tumor observed mean
           real<lower = 0> sigmaSq_i; // non-tumor observed variance
           vector[N] y; // observed EV mixture
           vector[N] x; // observed tumor
          vector[M] ct; // observed cell line cancer
vector[M] ce; // observed cell line EV
}
parameters {
           real s; // tumor to EV
           //real<lower = 0> sigmaSq_e; // variance of tumor EV
          real<lower = 0> sigmaSq_t; // variance of tumor
          real<lower = 0, upper=1> alpha; //mixing coefficient
// real<lower = 0> sigma_common;
           // real<lower = 0> sigmaSq_immune;
}
transformed parameters{
          vector[N] z;
```

```
//real<lower = 0> sigma_immune;
        real<lower = 0> sigma_t;
        real<lower = 0> sigma_i;
        real<lower = 0> sigma_e;
        for (n in 1:N)
        z[n] = s+x[n];
        // sigma_immune = sqrt(sigmaSq_immune);
        sigma_t = sqrt(sigmaSq_t);
        //sigma_e = sqrt(sigmaSq_e);
        sigma_i = sqrt(sigmaSq_i);
}
model {
        s \sim normal(0,1);
        sigma_t ~ inv_gamma(1,1);
        //sigma_e \sim inv_gamma(1,1);
        alpha ~ beta(2,2);
        for (m in 1:M)
        target += normal_lpdf(ce[m] | s+ct[m], sigma_t);
        for (n in 1:N)
        target += log_mix(alpha, normal_lpdf(y[n] | z[n], sigma_t),
        normal_lpdf(y[n] | mu_i, sigma_i));
}
```

Inference was performed using pystan's MCMC module with 10000 iterations and 4 chains, and all other parameters at default. The default pystan inference algorithm is the No-U-Turn Hamiltonian Monte Carlo (NUTS-HMC) sampler.

4.2 Python inference code for the simplified multi-gene model MAP inference procedure.

```
from scipy.optimize import minimize
from scipy.stats import beta, norm
import numpy as np
import math
def log_loss(theta,x,y,s,mu_i,sigmasq_i,N):
        alpha = theta[0]
        sigmasq = theta[1]
        log_loss = 0
        for i in range(N):
                log_loss += np.log(alpha*norm.pdf(y[i], x[i]+s, sigmasq)
                          + (1-alpha)*norm.pdf(y[i], mu_i,sigmasq_i))
        log_loss += beta.logpdf(alpha, 2,2)
        return -1*log_loss
def SimpleInferenceSLSQP(gene):
        N = tumor_shared_df.shape[1]
        M = cell_line_exp_mat.shape[1]
        mu_i = healthy_exp_mean.loc[gene]
        sigmasq_i = healthy_exp_var.loc[gene]
        y = exosome_shared_df.loc[gene,:]
        x = tumor_shared_df.loc[gene,:]
        ct = cell_line_exp_df.loc[gene,:]
        ce = exosome_exp_df.loc[gene,:]
        exosome_shared_mean = np.mean(y) # h e a l t h y
```

```
cell_line_exosome = np.mean(ce)
cell_line_tissue = np.mean(ct)
cell_line_diff = cell_line_tissue - cell_line_exosome
imputed_tumor = x + cell_line_diff
imputed_immune = np.repeat(mu_i, N)
design_matrix = np.vstack([imputed_tumor, imputed_immune]).T
alpha0 = [0.5, 1]
xargs = (x, y, cell_line_diff,mu_i, sigmasq_i, N)
bounds = [(0,1), (None, None)]
SLSQP = minimize(log_loss_two, alpha0,args=xargs,
method='SLSQP', bounds=bounds, tol = 1e-9)
return SLSQP.x[0]
```

MAP inference was performed using the SLSQP package from the Python scipy.optimize library using default parameters. Note that the MAP estimates for α can and often differ from the single-gene probabilistic model - this is primarily due to the (1) the simplification of the probabilistic model for computational ease and (2) less robust/advanced inference algorithm relative to the NUTS-HMC used in the single-gene model.