# **Supplementary Information**

Analysis of microbial compositions: A review of normalization and differential abundance analysis

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## Supplementary Notes

#### Simulation settings

#### Fig. 3

- (a) Nominal level = 0.05
- (b) Number of simulations = 1
- (c) Sample size:  $n_1 = n_2 = n_3 = 30$
- (d) Number of taxa: m = 200
- (e) Proportion of differentially abundant taxa = 25%
- (f) Proportion of structure zeros = 0% out of non-differentially abundant taxa
- (g) Absolute abundance in the ecosystem:  $\log A_{ij} = b_0 + b_i^T x_j + e_i$ .
  - (i)  $b_0 = \log 50$  represents low abundant taxa,  $b_0 = \log 200$  represents medium abundant taxa, and  $b_0 = \log 10,000$  represents high abundant taxa. The proportions of low, median, and high abundant taxa are set to be 60%, 30%, 10%
  - (ii)  $x_j = (x_{j1}, \ldots, x_{jp})^T$  are covariates for the  $j^{th}$  sample;  $b_i = (b_{i1}, \ldots, b_{ip})^T$  are the corresponding coefficients for  $x_j$ .  $b_i$  are set to follow U(0.1, 1)  $\cup$  U(1, 10) for differentially abundant taxa
  - (iii)  $e_i \sim N(0, \frac{1}{exp(b_0)})$
- (h) Observed abundance from a sample:
  - (i) Library sizes across samples:  $O_{j} = p_j \max(A_{j})$ , where  $p_j \sim \frac{1}{U(5,10)}$
  - (ii)  $O_{ij} \sim \text{BIN}(O_{j}, \gamma_{ij} = \frac{A_{ij}}{A_{j}})$

### Fig. 4

Simulation settings are the same as Fig. 3 except that:

- (b) Number of simulations = 100
- (c) Sample size:  $n_1 = n_2 = 30$
- (e) Proportion of differentially abundant taxa = 5%, 15%, 25%
- (f) Proportion of structure zeros = 20% out of non-differentially abundant taxa
- (h) Observed abundance from a sample:
  - (i) Library sizes across samples:  $O_{j} = p_j \max(A_{j})$ , where  $p_j \sim \frac{1}{U(10,50) \cup U(100,500)}$

(ii) 
$$O_{ij} \sim \text{BIN}(O_{j}, \gamma_{ij} = \frac{A_{ij}}{A_{j}})$$