

Supplementary Table 1. Pearson bivariate correlation coefficients between bone volume fraction (V1), gray level co-occurrence matrix (GLCM) texture (V2 – V10) and gray value (GV) histogram (V11 - V15) variables measured from the acetabular region (AR).

| Variables | V1 | V2 | V3 | V4 | V5 | V6 | V7 | V8 | V9 | V10 | V11 | V12 | V13 | V14 |
|-----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|---------|----------|
| V15 | -0.563** | -0.541** | 0.780** | -0.172* | 0.855** | -0.702** | -0.361** | -0.559** | 0.865** | -0.136 | -0.597** | -0.367** | 0.897** | -0.367** |
| V14 | -0.232** | 0.729** | -0.414** | 0.332** | 0.583** | 0.641** | 0.781** | 0.863** | 0.338** | -0.200** | 0.237** | 0.989** | -0.104 | |
| V13 | -0.826** | -0.392** | 0.735** | -0.031 | -0.749** | -0.563** | -0.145** | -0.350** | 0.810** | -0.245** | -0.592** | -0.080 | | |
| V12 | -0.263** | 0.713** | -0.409** | 0.343** | 0.581** | 0.638** | 0.770** | 0.839** | -0.339** | -0.211** | 0.256** | | | |
| V11 | 0.356** | 0.426** | -0.621** | 0.237** | 0.689** | 0.548** | 0.255** | 0.504** | -0.653** | 0.106 | | | | |
| V10 | 0.273** | 0.337** | -0.557** | -0.834** | 0.244** | 0.437** | 0.171* | -0.204** | -0.300** | | | | | |
| V9 | -0.536** | -0.589** | 0.885** | -0.078 | -0.909** | -0.770** | -0.373** | -0.546** | | | | | | |
| V8 | -0.006 | 0.767** | -0.577** | 0.455** | 0.768** | 0.734** | 0.735** | | | | | | | |
| V7 | -0.172* | 0.940** | -0.564** | -0.113 | 0.620** | 0.808** | | | | | | | | |
| V6 | 0.216** | 0.943** | -0.932** | -0.140 | 0.923** | | | | | | | | | |
| V5 | 0.399** | 0.805** | -0.935** | 0.125 | | | | | | | | | | |
| V4 | -0.094 | -0.153* | 0.181* | | | | | | | | | | | |
| V3 | -0.452** | -0.792** | | | | | | | | | | | | |
| V2 | 0.071 | | | | | | | | | | | | | |

* Correlation is significant at the 0.05 level (2-tailed). ** Correlation is significant at the 0.01 level (2-tailed)

V1 = Bone volume fraction (BV/TV)

V2 = Contrast

V3 = Homogeneity

V4 = Correlation

V5 = Entropy

V6 = Difference entropy

V7 = Difference variance

V8 = Sum variance

V9 = Maximum probability

V10 = Information measure of correlation

V11 = GV mean

V12 = GV standard deviation

V13 = GV skewness

V14 = GV variance

V15 = GV kurtosis

Supplementary Table 2. Pearson bivariate correlation coefficients between bone volume fraction (V1), gray level co-occurrence matrix (GLCM) texture (V2 – V10) and gray value (GV) histogram (V11 - V15) variables measured from the femoral head region FHR-1.

| Variables | V1 | V2 | V3 | V4 | V5 | V6 | V7 | V8 | V9 | V10 | V11 | V12 | V13 | V14 |
|-----------|----------|----------|----------|----------|----------|---------|----------|----------|----------|----------|----------|----------|----------|----------|
| V15 | -0.203** | -0.337** | 0.438** | -0.423** | -0.350** | 0.238** | -0.670** | -0.663** | 0.372** | 0.287** | -0.344** | -0.524** | 0.268** | -0.514** |
| V14 | 0.107 | 0.624** | -0.465** | 0.278** | 0.599** | 0.599** | 0.677** | 0.865** | -0.022 | -0.212** | 0.316** | 0.991** | -0.186** | |
| V13 | -0.914** | -0.087 | 0.072 | -0.184** | -0.083 | -0.068 | -0.083 | -0.250** | -0.187** | 0.135 | -0.695** | -0.177 | | |
| V12 | 0.095 | 0.621** | -0.481** | 0.274** | 0.604** | 0.595** | 0.697** | 0.852** | -0.051 | -0.209** | 0.326** | | | |
| V11 | 0.549** | 0.291** | -0.311** | 0.185** | 0.337** | 0.272** | 0.377** | 0.456** | 0.046 | -0.041 | | | | |
| V10 | -0.139* | 0.456** | -0.573** | -0.881** | 0.535** | 0.427** | 0.172* | -0.344** | -0.178* | | | | | |
| V9 | 0.167* | -0.094 | 0.493** | 0.040 | -0.147* | 0.071 | -0.531** | 0.012 | | | | | | |
| V8 | 0.158* | 0.562** | -0.441** | 0.471** | 0.568** | 0.534** | 0.721** | | | | | | | |
| V7 | 0.008 | 0.739** | -0.874** | 0.056 | 0.808** | 0.628** | | | | | | | | |
| V6 | 0.001 | 0.970** | -0.688** | -0.418** | 0.918** | | | | | | | | | |
| V5 | 0.012 | 0.955** | -0.891** | -0.384** | | | | | | | | | | |
| V4 | 0.135 | -0.410** | 0.363** | | | | | | | | | | | |
| V3 | -0.012 | -0.819** | | | | | | | | | | | | |
| V2 | 0.026 | | | | | | | | | | | | | |

* Correlation is significant at the 0.05 level (2-tailed). ** Correlation is significant at the 0.01 level (2-tailed)

V1 = Bone volume fraction (BV/TV)

V2 = Contrast

V3 = Homogeneity

V4 = Correlation

V5 = Entropy

V6 = Difference entropy

V7 = Difference variance

V8 = Sum variance

V9 = Maximum probability

V10 = Information measure of correlation

V11 = GV mean

V12 = GV standard deviation

V13 = GV skewness

V14 = GV variance

V15 = GV kurtosis

Supplementary Table 3. Pearson bivariate correlation coefficients between bone volume fraction (V1), gray level co-occurrence matrix (GLCM) texture (V2 – V10) and gray value (GV) histogram (V11 - V15) variables measured from the femoral head region FHR-2.

| Variables | V1 | V2 | V3 | V4 | V5 | V6 | V7 | V8 | V9 | V10 | V11 | V12 | V13 | V14 |
|-----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| V15 | 0.147* | 0.572** | -0.243** | -0.289** | -0.344** | -0.076 | -0.768** | -0.497** | 0.764** | 0.142* | 0.120 | -0.411** | 0.266** | -0.400** |
| V14 | 0.165* | -0.371** | 0.525** | 0.247** | 0.454** | 0.488** | 0.539** | 0.804** | -0.153* | -0.242** | 0.128 | 0.988** | -0.197** | |
| V13 | -0.908** | -0.194** | -0.045** | -0.208** | -0.005** | -0.150* | 0.139* | -0.278** | -0.433** | 0.178* | -0.676** | -0.197** | | |
| V12 | 0.161* | -0.372** | 0.506** | 0.266** | 0.450** | 0.474** | 0.552** | 0.793** | -0.167* | -0.251** | 0.134 | | | |
| V11 | 0.569** | -0.140* | 0.248** | 0.092 | 0.312** | 0.305** | 0.161* | 0.365** | 0.195** | 0.080 | | | | |
| V10 | -0.214** | -0.583** | 0.501** | -0.844** | 0.619** | 0.466** | 0.217** | -0.291** | -0.145* | | | | | |
| V9 | 0.292** | 0.664** | -0.190** | -0.029 | -0.333** | -0.005** | -0.752** | -0.165** | | | | | | |
| V8 | 0.244** | -0.430** | 0.508** | 0.428** | 0.517** | 0.466** | 0.651** | | | | | | | |
| V7 | -0.099 | -0.892** | 0.646** | 0.032 | 0.774** | 0.500** | | | | | | | | |
| V6 | 0.075 | -0.597** | 0.957** | -0.488** | 0.858** | | | | | | | | | |
| V5 | -0.039 | 0.885** | 0.917** | -0.439** | | | | | | | | | | |
| V4 | 0.221** | 0.358** | -0.489** | | | | | | | | | | | |
| V3 | -0.006 | -0.762** | | | | | | | | | | | | |
| V2 | 0.174* | | | | | | | | | | | | | |

* Correlation is significant at the 0.05 level (2-tailed). ** Correlation is significant at the 0.01 level (2-tailed)

V1 = Bone volume fraction (BV/TV)

V2 = Contrast

V3 = Homogeneity

V4 = Correlation

V5 = Entropy

V6 = Difference entropy

V7 = Difference variance

V8 = Sum variance

V9 = Maximum probability

V10 = Information measure of correlation

V11 = GV mean

V12 = GV standard deviation

V13 = GV skewness

V14 = GV variance

V15 = GV kurtosis

Supplementary Table 4. Correlation of trabecular architectural variables between the two femur head regions, FHR-1 and FHR-2, on femurs the side of the acetabular fractures and the corresponding control side femurs. Pearson correlation coefficients (r) and mean statistical test p-values for all subjects and individual genders are also shown.

| Variables | Fracture side | | | | | | Control side | | | | | |
|------------------------------|---------------|---------|------------|---------|-------------|---------|---------------|---------|------------|---------|-------------|---------|
| | All (n = 196) | | F (n = 44) | | M (n = 152) | | All (n = 214) | | F (n = 50) | | M (n = 164) | |
| | r | p | r | p | r | p | r | p | r | p | r | p |
| BV/TV | 0.404** | 0.123 | 0.528* | 0.221 | 0.367* | 0.239 | 0.577** | 0.001† | 0.441* | 0.103 | 0.566** | 0.002† |
| Contrast | 0.567** | 0.001† | 0.671** | 0.011† | 0.537** | 0.010† | 0.735** | <0.001† | 0.670** | 0.002† | 0.755** | <0.001† |
| Homogeneity | 0.563** | <0.001† | 0.674** | 0.007† | 0.523** | <0.001† | 0.534** | <0.001† | 0.562** | <0.001† | 0.531** | <0.001† |
| Correlation | 0.611** | 0.571 | 0.722** | 0.453 | 0.582** | 0.799 | 0.537** | 0.053 | 0.599** | 0.211 | 0.524** | 0.115 |
| Entropy | 0.599** | 0.004† | 0.664** | 0.023† | 0.579** | 0.034† | 0.643** | <0.001† | 0.661** | 0.003† | 0.638** | <0.001† |
| Difference entropy | 0.569** | 0.051 | 0.650** | 0.044† | 0.550** | 0.279 | 0.750** | 0.001† | 0.733** | 0.032† | 0.765** | 0.006† |
| Difference variance | 0.462** | <0.001† | 0.598** | 0.024† | 0.427** | 0.001† | 0.484** | <0.001† | 0.595** | 0.009† | 0.460** | <0.001† |
| Sum variance | 0.370** | <0.001† | 0.545** | 0.012† | 0.343** | 0.006† | 0.595** | 0.001† | 0.539** | 0.070 | 0.600** | 0.007† |
| Maximum probability | 0.258* | <0.001† | 0.481* | 0.013† | 0.201 | <0.001† | 0.573** | <0.001† | 0.651** | 0.017† | 0.580** | <0.001† |
| IMC | 0.670** | 0.907 | 0.754** | 0.725 | 0.645** | 0.996 | 0.557** | 0.0013† | 0.640** | 0.022† | 0.541** | 0.008† |
| GV mean | 0.856** | 0.001† | 0.906** | 0.274 | 0.837** | 0.001† | 0.869** | <0.001† | 0.923** | 0.452 | 0.821** | <0.001† |
| GV standard deviation | 0.620** | <0.001† | 0.514* | <0.001† | 0.645** | <0.001† | 0.679** | <0.001† | 0.767** | 0.001† | 0.660** | <0.001† |
| GV variance | 0.587** | <0.001† | 0.466* | <0.001† | 0.612** | <0.001† | 0.686** | <0.001† | 0.759** | 0.001† | 0.674** | <0.001† |
| GV skewness | 0.484** | 0.294 | 0.474* | 0.675 | 0.470** | 0.330 | 0.642** | 0.009† | 0.646** | 0.400 | 0.606** | 0.016† |
| GV kurtosis | 0.259** | 0.000† | 0.253 | 0.002† | 0.262* | <0.001† | 0.236** | <0.001† | 0.499* | 0.041† | 0.220* | <0.001† |

* Correlation is significant at the 0.05 level (2-tailed), ** Correlation is significant at the 0.01 level (2-tailed)

† Parametric Independent samples t-test ($p < 0.05$), ‡ Nonparametric Mann-Whitney U-test ($p < 0.05$),

BV/TV = Bone volume fraction, IMC = Information measure of correlation, GV = Gray values, SD = Standard deviation

Supplementary Table 5. Proximal femur geometry variables neck shaft angle (NSA) and femoral neck axis length (FNALa and FNALb). Values given as means, standard deviations (SD) and 95% confidence interval [CI]. Statistical p-values of the differences for all subjects and individual genders are also shown.

| Variables | Fracture side | | | | Control side | | | | p | |
|-------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|---------------------|--------------------|--------------------|--|
| | All (n = 95) | F (n = 20) | M (n = 75) | All (n = 103) | F (n=25) | M (n = 78) | All (n=198) | F (n=45) | M (n = 153) | |
| NSA (°) | 121.71 (5.56) [120.58-122.84] | 118.76 (6.49) [115.72-121.79] | 122.49 (5.05) [121.33-123.66] | 124.60 (5.64) [123.49-125.70] | 124.51 (5.85) [122.09-126.93] | 124.63 (5.61) [123.36-125.89] | <0.001 [‡] | 0.003 [‡] | 0.015 [‡] | |
| FNALb (mm) | 78.36 (0.36) [77.14-79.58] | 71.74 (4.05) [70.04-73.83] | 80.07 (5.24) [78.87-81.28] | 76.03 (0.03) [74.75-77.30] | 70.59 (5.04) [68.51-73.83] | 77.77 (5.98) [76.42-79.12] | 0.010 [‡] | 0.615 | 0.037 [‡] | |
| FNALa (mm) | 103.46 (6.92) [102.06-104.87] | 94.98 (4.34) [92.95-97.01] | 105.73 (5.59) [104.44-107.01] | 101.22 (8.25) [99.61-102.83] | 93.37 (6.20) [90.81-95.93] | 103.74 (7.19) [102.12-105.36] | 0.073 | 0.749 | 0.125 | |

[‡]Parametric Independent samples t-test ($p < 0.05$). [†]Nonparametric Mann-Whitney U-test ($p < 0.05$)

Supplementary Table 6. Coefficient weights of the variables used in the final EN model of trabecular architecture features at the acetabular region (AR). The trabecular architecture features were bone volume fraction (BV/TV), gray level co-occurrence matrix and gray value (GV) histogram variables.

| Model inputs | All subjects | Females | Males |
|----------------------------|---------------------|----------------|--------------|
| Intercept | 0.000 | 0.002 | -0.002 |
| Correlation | - | - | 0.257 |
| Difference variance | - | 0.343 | - |
| GV mean | 0.119 | 0.111 | 0.353 |

Supplementary Table 7. Elastic net (EN) regression hyperparameters (α , λ) used in the acetabular region (AR) and femoral head region (FHR) final models for all subjects, females and males. Models with and without proximal femur geometry (PFG) are shown.

| Model | Without PFG (α, λ) | With PFG (α, λ) |
|------------------|--|---|
| AR | 0.97, 0.116 | - |
| AR-female | 0.94, 0.091 | - |
| AR-male | 0.97, 0.056 | - |
| FHR-1 | 0.01, 0.126 | 0.01, 0.026 |
| FHR-1-female | 0.94, 0.006 | 0.82, 0.146 |
| FHR-1-male | 0.1, 0.146 | 0.01, 0.031 |
| FHR-2 | 0.01, 0.141 | 0.97, 0.011 |
| FHR-2-female | 0.73, 0.056 | 0.01, 0.016 |
| FHR-2-male | 1.00, 0.036 | 0.97, 0.026 |
| FHR-1&2 | 0.88, 0.026 | 0.91, 0.021 |
| FHR-1&2 - female | 0.94, 0.136 | 0.10, 0.001 |
| FHR-1&2 - male | 0.91, 0.031 | 0.13, 0.146 |

Supplementary Figure 1. Receiver operating characteristics curves of the femur head region 1 (FHR-1) and femur head region 2 (FHR-2). Bayesian logistic regression (BLR) and elastic net (EN) models for all subjects and individual genders. FHR was measured from the fracture side. (A) and (B) show FHR-1 curves without and with PFG, while (C) and (D) show FHR-2 curves without and with PFG.

