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Intrinsic Disorder in the T Cell Receptor Creates Cooperativity and Controls ZAP70 Binding

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ABSTRACT Many immunoreceptors have cytoplasmic domains that are intrinsically disordered (i.e., have high configurational entropy), have multiple sites of posttranslational modification (e.g., tyrosine phosphorylation), and participate in nonlinear signaling pathways (e.g., exhibiting switch-like behavior). Several hypotheses to explain the origin of these nonlinearities fall under the broad hypothesis that modification at one site changes the immunoreceptor's entropy, which in turn changes further modification dynamics. Here, we use coarse-grain simulation to study three scenarios, all related to the chains that constitute the T cell receptor (TCR). We find that first, if phosphorylation induces local changes in the flexibility of the TCR ζ-chain, this naturally leads to rate enhancements and cooperativity. Second, we find that TCR CD3ε can provide a switch by modulating its residence in the plasma membrane. By constraining our model to be consistent with the previous observation that both basic residues and phosphorylation control membrane residence, we find that there is only a moderate rate enhancement of 10% between first and subsequent phosphorylation events. Third, we find that volume constraints do not limit the number of ZAP70s that can bind the TCR but that entropic penalties lead to a 200-fold decrease in binding rate by the seventh ZAP70, potentially explaining the observation that each TCR has around six ZAP70 molecules bound after receptor triggering. In all three scenarios, our results demonstrate that phenomena that change an immunoreceptor chain's entropy (stiffening, confinement to a membrane, and multiple simultaneous binding) can lead to nonlinearities (rate enhancement, switching, and negative cooperativity) in how the receptor participates in signaling. These polymer-entropy-driven nonlinearities may augment the nonlinearities that arise from, e.g., kinetic proofreading and cluster formation. They also suggest different design strategies for engineered receptors, e.g., whether or not to put signaling modules on one chain or multiple clustered chains.

SIGNIFICANCE Many of the proteins involved in signal processing are both mechanically flexible and have multiple sites of interaction, leading to a combinatorial complexity making them challenging to study. One example is the T cell receptor, a key player in immunological decision making. It consists of six flexible chains with 20 interaction sites, and exhibits nonlinear responses to signal inputs, although the mechanisms are elusive. By using polymer physics to simulate the T cell receptor's chains, this work demonstrates that several of the nonlinear responses observed experimentally emerge naturally because of constraints on the chains that change their entropy. This work points to new avenues to modulate signaling proteins for therapeutics by modulating their mechanical flexibility and spatial extent.

INTRODUCTION

Challenging the tenet that "structure determines function," more than 40% of human proteins contain intrinsically disordered regions longer than 30 amino acids (1,2). Intrinsically disordered regions appear as linkers between globular domains (3), associated with the cytoskeleton (4,5),

Submitted May 21, 2020, and accepted for publication November 19, 2020.

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Editor: Michael Grabe.

https://doi.org/10.1016/j.bpj.2020.11.2266

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or in signaling networks (6,7). These regions often include sites for binding and posttranslational modification, suggestions they serve a purpose beyond as passive tethers (3,8,9). Additionally, the length of the domains themselves influences their interactions, affecting binding kinetics and catalytic performance (10–13).

One example is offered by the T cell receptor (TCR) (14–16). The TCR has eight subunits, six of which contain intrinsically disordered cytoplasmic tails: ζ (two per TCR), ε (two per TCR), δ , and γ . The tyrosines on these tails are organized in pairs called ITAMs (immunoreceptor tyrosine-based activation motifs) and become phosphorylated by a kinase (LCK) upon extracellular ligand binding to the TCR. Phosphorylation of the ITAMs allows a cytosolic signaling molecule, ZAP70, to bind to the phosphotyrosines (17) and propagate the activation signal (18). Despite lacking structure in the intracellular cytoplasmic tails, the TCR itself endows the signaling pathway with what we term nonlinearities, raising specific questions:

- 1) The ζ chains exhibit cooperative phosphorylation (19,20), which can endow systems with ultrasensitivity (21). A hypothesis for this nonlinearity is in local changes in flexibility upon phosphorylation, as shown in Fig. 1 Bii and as observed for other intrinsically disordered proteins (8,22). Would this local structuring be sufficient to explain the cooperativity? If so, this may explain why many immune receptors have disordered cytoplasmic tails containing multiple phosphorylation sites (10,23).
- 2) The ε -chain is known to associate with the inner leaflet of the membrane (24,25), as are many other immune receptor chains including ζ (26), CD28 (27), and BCR (28). This has been hypothesized to sequester the tyrosines to guard against phosphorylation (Fig. 1 Biii) before a signal is initiated by an antigen. But, given that tyrosine phosphorylation is one of the first steps of T cell activation, how do the first tyrosines become phosphorylated to induce membrane dissociation?
- 3) Finally, although the full TCR complex has 10 ITAMs, only six ZAP70 molecules associate with the receptor at one time (29). What property sets the limits of simultaneous occupation (Fig. 1 Biv)?

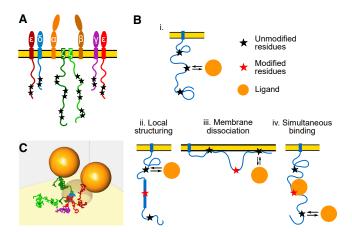


FIGURE 1 Possible consequences of membrane-bound disordered protein interacting with ligand. (A) A cartoon of the T cell receptor complex is given. (Bi) Interaction of ligand (orange circle) with membrane-bound disordered protein with multiple binding sites (black stars) is shown, where (Bii) binding causes local stiffening near posttranslational modification (e.g., phosphorylation; red stars), (Biii) phosphorylation reduces membrane association of the polymer, or (Biv) the ligand remains bound while more ligands attempt to bind simultaneously. (C) A snapshot of the residue-scale computational model of T cell receptor is given. To see this figure in color, go online.

Computational study of the TCR is challenging not only because it is large and membrane bound, but the intrinsic disorder introduces a large configuration space that is explored on microsecond timescales, making atomistic molecular dynamics methods computationally expensive. An alternative modeling approach is to use coarse-grain models from polymer physics in which the disordered regions are represented as ideal chains, with each residue represented by a particle. Despite the simplicity of the approach, "residue-scale" models have proven valuable (11,30,31), including for formins (12,32) and kinesins (33). Here, we use coarse-grain, residue-scale models to simulate the intrinsically disordered regions of the T cell receptor, exploring the consequences of posttranslational modification to answer the above questions.

We find that first, in agreement with previous theoretical calculations (19), if phosphorylation induces local changes in the flexibility of the chain, this naturally leads to rate enhancements and cooperativity. We find the rate enhancement for a single chain with properties of ζ is around twofold, with a Hill coefficient around 1.8. However, the ultrasensitivity seen is only strong if the kinase is large in molecular size compared with the phosphatase.

Second, we find that CD3 ε can exhibit a switch-like response to phosphorylation by modulating its residence in the membrane. The observation that both tyrosine phosphorylation and basic residue deletion change membrane residency under the assumptions of our model sets a requirement that there be a rate enhancement of at least 10% between first and second phosphorylation events.

Third, we ask how many ZAP70 molecules can simultaneously bind the 10 ITAMs on the six chains of a TCR. We find that volume constraints do not limit the number (i.e., there exists a configuration in which 10 can fit) but that the entropic penalty needed to bind subsequent ZAP70s leads to a 200-fold decrease in binding rate by the seventh ZAP70, potentially explaining the observation that each TCR has around six ZAP70 molecules bound after receptor triggering. We also explore how binding rates are affected if the 10 ITAMs are distributed on different numbers of chains, a question that may be relevant for artificially engineered receptors. We find that for parameters similar to the TCR, neighbor-chain interference dominates self-chain interference, so receptors with signaling modules on the same chain would allow faster simultaneous binding.

In all three scenarios, our results demonstrate that phenomena that change an immunoreceptor chain's entropy (stiffening, confinement to a membrane, and multiple simultaneous binding) can lead to emergent behavior with consequences for how the receptor participates in signaling. These polymer-entropy-driven nonlinearities may augment the nonlinearities that arise from, for example, kinetic proofreading and cluster formation. They also suggest different design strategies for engineered receptors, e.g., whether or not to have one chain or multiple clustered chains.

METHODS

Polymer model of disordered protein and globular binding partner

We represent the TCR cytoplasmic tails as ideal disordered proteins using a θ -solvent freely jointed chain model in which each particle represents a single residue (31). The Kuhn length is $\delta = 0.3$ nm (25,30). The number of segments N is therefore the number of residues in the tail, i.e., 113, 55, 47, and 45 for ζ , ε , δ , and γ , respectively.

The chains interact with LCK and ZAP70, which for generality we refer to as the ligand. This is modeled as an idealized sphere that interacts with the chain. For each ligand, we estimate the volume of the domain of interest and calculate the radius for a sphere with the specified volume. Volume estimates are made using the molecular mass of the domains and an estimated protein density of 1.41 g/cm³ (34). For comparison, we also estimate volumes from measurements of crystal structures of the domains (LCK, Protein Data Bank, PDB: 3LCK; ZAP70, PDB: 2OQ1; CD45, PDB: 1YGR) in PyMol (35-37). For LCK, we represent the kinase domain as a sphere with radius 2.1 nm (7 Kuhn lengths). For ZAP70, we represent the tandem SH2 domains as a sphere with radius 2.7 nm (9 Kuhn lengths). For CD45, we represent the tandem phosphatase domains as a sphere with radius 3.4 nm (11 Kuhn lengths) For simulations of the full TCR, the relative location of the membrane-anchor for each cytoplasmic domain is estimated from (38) (PDB: 6JXR).

We compute quasiequilibrium statistics of the chain and its ligands using the Metropolis-Hastings algorithm, a form of Monte Carlo simulation (39,40) that generates a distribution of configurations from the canonical ensemble. At each proposed configuration, the Metropolis algorithm computes the energy of the system and accepts or rejects based on energetic preference (specifically, interactions in Eqs. 5 and 6 below) and hard constraints (the polymer cannot pass through the membrane or ligands, and ligands cannot pass through each other). The Metropolis algorithm proposes configurations using a perturbation size that is adaptive and increases or decreases until the acceptance rate is 0.44 (41). We repeat configuration proposals until the sequence of samples has reached a stationary distribution, which we define when the third quarter and fourth quarter of the sequence have the same distribution according to the Kolmogorov-Smirnov statistics.

Polymer simulation code and analysis routines are available at https:// github.com/allardjun/IntrinsicDisorderTCRModel (https://doi.org/10.5281/ zenodo.4117255).

Calculation of ligand binding rates from occlusion statistics

The dissociation constant of a binding reaction $K_D \equiv k_{\text{off}}/k_{\text{on}}$ is influenced by changes in entropy. If a binding reaction limits the configurational freedom of the binding partners, the entropy, and thus the free energy, is reduced. We can compute the change in K_D between two states (e.g., fully phosphorylated compared to dephosphorylated) as (22,42)

$$\frac{K_{D_1}}{K_{D_2}} = \exp\left(\frac{\Delta G_1 - \Delta G_2}{k_B T}\right),\tag{1}$$

$$= \exp\left(\frac{(E_1 - TS_1) - (E_2 - TS_2)}{k_B T}\right),\tag{2}$$

$$= \exp\left(\frac{\left(k_B \ln\left(\frac{\Omega_2 P_2}{\Omega_2}\right)\right) - \left(k_B \ln\left(\frac{\Omega_1 P_1}{\Omega_1}\right)\right)}{k_B}\right), \tag{3}$$

and

$$= P_2/P_1, (4)$$

where $G_i = E_i - TS_i$ is the free energy of binding in a given state, $S_i = k_B \ln \Omega_i$ is the entropy of binding, Ω_i is the number of microstates, and P_i is the probability in the canonical ensemble that the configuration allows for binding. We assume $\Delta E_1 = \Delta E_2$, i.e., the change in energy due to ligand binding is the same, regardless of conformation. Define P_{occ} as the probability that the region of space needed by the ligand is occupied by some of the polymer or another steric barrier. Then, $P_{\text{occ}_1} = 1 - P_j$, and $K_{D_1}/K_{D_2} = (1 - P_j)$ $P_{\text{occ}_2})/(1-P_{\text{occ}_1})$. Although entropic forces could also impact unbinding of the polymer, we assume this influence to be negligible compared to the change in k_{on} . Therefore, we assume that the change in K_D manifests as a change in k_{on} . This leads to the final simple equation for attachment rates, $k_{\rm on} = P_{\rm occ} k_{\rm on}^0$, where we refer to $k_{\rm on}^0$ as the free-space (i.e., no occlusion) binding rate. Because we lack an estimate for k_{on}^0 (which we expect to depend on local concentration of binding partner), we report all rates proportional to k_{on}^0 .

Simulation of multistep processes from individual rates

Given the binding rates k_{on} , we use a Gillespie algorithm to investigate the rate-dependent behaviors of both irreversible and reversible (de)phosphorylation reactions. A matrix of occlusion probabilities to each site in each phosphorylation state is created from the Metropolis simulations.

For single-direction simulations, e.g., just phosphorylation, we make two calculations: 1) the probability of a specific sequence of irreversible (de) phosphorylation and 2) the sequence-weighted average binding rate to transition between phosphostates (e.g., from one to two total phosphorylations). At the end of each run of the multistep process, when all sites are modified, we record the event sequence and the times to transition between each step. Probabilities of each sequence are computed based on the total iterations of the algorithm. The path-weighted average binding rates are calculated as the inverse of the average transition time for a specific step. In other words, transitions between two states that are more likely are weighted higher. In the Supporting Materials and Methods, we show average binding rates that are not weighted by the probability of their path. For simulations of reversible reactions, we run until the system reaches a steady state ($\sim 10^6$ events) and then calculate the average number of phosphorylated sites.

Membrane interactions

Polymer-membrane interactions are modeled as potentials acting on each segment of the chain. We consider three groups of residues: tyrosines, phosphotyrosines, and basic residues. Each experiences a potential summarized in Fig. 5 A. Basic residues are needed to create membrane association (26), which we model with a piecewise parabolic potential with depth E_{B0} (43,44),

$$E_{\text{Basic}}(z_i) = \begin{cases} k_{PC} z_i^2 - E_{B0} & z_i < \sqrt{\frac{E_{B0}}{k_{PC}}} \\ 0 & z_i \ge \sqrt{\frac{E_{B0}}{k_{PC}}} \end{cases}$$
(5)

Tyrosine phosphorylation is sufficient to dissociate the polymer from the membrane (26). We therefore model phosphorylated tyrosines as having a repulsive interaction with the membrane,

$$E_{Y_p}(z_i) = E_{P0}e^{-z_i/z_{\text{Debye}}}, \qquad (6)$$

where the Debye length describes the length scale of electrostatic interactions. For cytoplasm, $z_{Debye} = 1$ nm and $\sqrt{E_{B0}/k_{PC}} = 1$ nm consistent with (31). A soft wall constraint

$$E_{\mathcal{S}}(z_j) = \begin{cases} k_{\mathcal{S}} z_j^2 & z_j < 0\\ 0 & z_j \ge 0 \end{cases}$$
(7)

with $k_S = 0.05k_BT$, is applied to the unphosphorylated tyrosines and remaining amino acids.

RESULTS

Site difference driven by position along chain

The residue-scale polymer model we developed simulates the T cell receptor as it explores its configurations, along with binding partners that we generically refer to as ligands. An example is shown in Fig. 1 C and Video S1.

In this section, we simulate only the ζ -chain. We first assume that phosphorylation does not change the polymer properties of the chain. We calculate the binding rate to each of the six tyrosines. The entropy calculations result in a relative rate from every possible reaction phosphostate, shown as the left columns in Fig. S1, to every phosphostate with one more phosphorylation, in the right column. From these, we obtain the phosphorylation sequences shown in Figs. 2 and 3 (pink curve, lowest in both panels).

Rate differences imply emergent preference of phosphorylation sequence

There are six binding sites on the ζ -chain, offering 720 (six factorial) possible sequences for phosphorylation. Using a Gillespie algorithm in conjunction with the binding rates

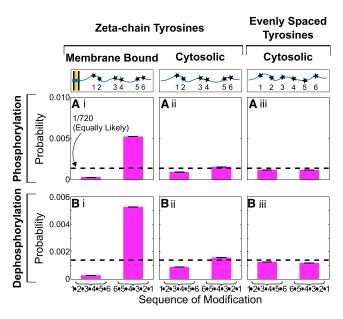


FIGURE 2 Binding rate differences imply emergent preference of (de) phosphorylation sequence. Probability of (A) phosphorylating or (B) dephosphorylating membrane proximal to distal (123456) compared with membrane distal to proximal (654321) is shown. Each of these is shown for (i) with a membrane, assuming sites spaced like tyrosines of ζ ; (ii) without a membrane, assuming sites spaced like tyrosines of ζ ; and (iii) without a membrane, assuming sites spaced evenly. Black dotted lines indicate the probability if all events were equally likely (1/6! = 1/720). Error bars (A and B) represent standard error of the mean. To see this figure in color, go online.

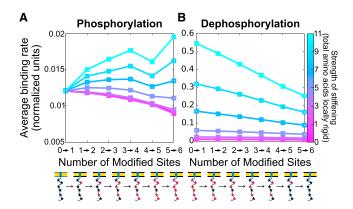


FIGURE 3 Local stiffening modulates binding rates to multisite disordered domain. (A) Average binding rates of a kinase binding to ζ at different phosphorylation states are shown for varying range of local stiffening (pink: no residues are stiffened; blue: 11 residues are stiffened, five on each side of site). (B) Average binding rates of a phosphatase binding to ζ at different dephosphorylation states are shown for varying ranges of local unstiffening per dephosphorylation event. For both (A) and (B), the schematic below the axis shows example configuration for each phosphorylation state. Kinase and phosphatase radii are 2.1 nm. Rates are normalized to the free-space binding rate k_{on}^0 . To see this figure in color, go online.

found above, we compute the probability of (de)phosphorylating in each sequence. For simplicity, Fig. 2, Ai and Bi shows only two extreme sequences: when (de)phosphorylation occurs membrane proximal to distal (123456, i.e., N- to C-terminus) and membrane distal to proximal (654321, i.e., C- to N-terminus). For membrane-bound ζ -chains, there is an \sim 10-fold increase in the probability of binding membrane distal to proximal compared with membrane proximal to distal for both the kinase and phosphatase. This suggested to us that disordered domains in the presence of a membrane can have an emergent preference of phosphorylation sequence.

To test this hypothesis, we simulate an unphosphorylated, cytosolic (i.e., no membrane) ζ-chain. Surprisingly, we found rate differences also persist without the presence of a membrane. Simulations of a cytosolic ζ show reduced preference, in agreement with intuition. However, phosphorylating the sequence 123456 (i.e., N- to C-terminus, membrane proximal to distal, if there were a membrane) is still twofold more likely than phosphorylating 654321 (i.e., C- to N-terminus, membrane distal to proximal, if there were a membrane), as shown in Fig. 2, Aii and Bii. When we resimulate cytosolic ζ -chain, but now with its six tyrosines spaced evenly along the amino acid sequence, there is no longer any preference for phosphorylation sequence (Fig. 2, Aiii and Biii). Thus, the emergent preference arises solely from the locations of the tyrosines in the ζ -chain. The membrane-distal tyrosine is 12 amino acids away from the C-terminus, whereas the membrane-proximal tyrosine is 21 amino acids away from the membrane. We intuitively understand it as follows. In all cases, the phosphorylation site is attached to a chain of the same length. However, steric hindrance depends on location—specifically, steric hindrance is reduced closer to the chain's free ends, where there are effectively fewer nearby amino acids to get tangled. These results suggest that changing binding site locations by as little as 10 amino acids is sufficient to induce a preferential binding sequence.

Local stiffening

One way in which disordered proteins can participate in signaling cascades is to undergo a disorder-to-order transition (8,22,45) upon posttranslational modification (e.g., tyrosine phosphorylation), becoming locally stiff, as shown schematically in Fig. 1 Bii.

Previous experimental-modeling work (19,20) suggest that the tyrosines on the ζ -chain experience phosphorylation rates that were enhanced by previous phosphorylations. Can this be explained by phosphorylation-induced local stiffening?

Local stiffening modulates binding rates to multisite disordered domain

In Fig. 3 A, we compute the average binding rate of a kinase to the membrane-bound ζ -domain in its unphosphorylated state. Here, each average binding rate is weighted by the most likely (de)phosphorylation sequences. (Average binding rates unweighted by their path's probability are shown in Fig. S3.) Without disordered-to-ordered transitions, the average kinase binding rate decreases as more phosphorylations occur. Because there is a natural preference to phosphorylate the membrane distal to proximal, it is most likely that the membrane-proximal tyrosine will be the last tyrosine phosphorylated. This tyrosine has a lower binding rate, bringing down the average binding rate of the last phosphorylation compared to the first event, when the faster, membrane-distal sites dominate.

However, if phosphorylation introduces local stiffening, then a single phosphorylation event creates an overall increase in the average binding rate of the kinase to another tyrosine. This effect increases with total phosphorylations and degree of local stiffening per phosphorylation. For example, if each phosphorylation locally stiffens 11 amino acids (\sim 1/12 of the polymer length), then the sixth kinase binding event will occur almost two times faster than the first (larger range shown in Fig. S4). In agreement with on-lattice simulations (22), local stiffening causes the polymer to be more elongated on average and sample more configurations in which the remaining tyrosines are kinase accessible. Through this mechanism, disordered-to-ordered transitions can increase the binding rate of a kinase to the remaining unphosphorylated tyrosines.

Interestingly, there is a decrease in the average binding rate between the fourth and fifth binding event. We explain this phenomenon, influenced by the second-last tyrosine Y83, in Fig. S5.

Although local stiffening at phosphorylated tyrosines enhances the binding rate of kinases to unphosphorylated tyrosines, it could also enhance the binding rate of phosphatases to phosphorylated tyrosines. We therefore explore how dephosphorylation (i.e., loss of local stiffening) impacts the binding rate of phosphatases to the domain in Fig. 3 B. For example, if each phosphorylation locally stiffens 11 amino acids, then we assume each dephosphorylation similarly relaxes 11 amino acids. As dephosphorylations occur, entropic flexibility is returned to the polymer. By the sixth dephosphorylation event, the average phosphatase binding rate is decreased by half.

Binding rate cooperativity creates ultrasensitivity, even in reversible symmetric phosphorylation cycles

To simulate reversible phosphorylation cycles, we explore two models of dephosphorylation: 1) constant dephosphorylation, in which the phosphatase enzymatic domain is assumed to be small enough that steric effects are insignificant, and 2) steric dephosphorylation, in which the phosphatase enzymatic domain is large enough that the steric effects we report above significantly influence dephosphorylation.

In the first model, the phosphatase is assumed to be of negligible size, and therefore, dephosphorylation occurs at a constant rate at each site. Using the site-specific binding rates determined above for membrane-bound ζ , we calculate the steady-state fraction of sites phosphorylated, with doseresponse curves shown in Fig. 4 A. As expected, when no local stiffening occurs, reversible phosphorylation has approximately Michaelis-Menten kinetics. However, as the number of amino acids stiffened per phosphorylation increases, the dose-response curves become steeper. This ultrasensitivity can be quantified as a Hill coefficient, here defined as the maximal logarithmic slope of each curve (see Supporting Materials and Methods and Fig. S6 for a definition of the Hill coefficient), attaining a Hill coefficient of 1.8 when $\sim 1/12$ of the chain is stiffened per phosphorylation event. Therefore, the binding rate cooperativity introduced by local disordered-to-ordered transitions can lead to ultrasensitivity in a signaling network.

In the second model, the phosphatase is assumed to experience the same steric constraints as the kinase. This model is reasonable because we estimate the size of the phosphatase domain of CD45 to be 3.4 nm. We find dose-response curves shown in Fig. 4 B. At 1/12 chain local stiffening per phosphorylation, the Hill coefficient is 1.3. Therefore, even under steric dephosphorylation, a reversible system with local disordered-to-ordered transitions is still capable of creating mild ultrasensitivity. Below, in Fig. 9, we show that if ZAP70 protects phosphorylated tyrosines from dephosphorylation, ultrasensitivity is further enhanced, and is still strong when dephosphorylation experiences the same steric enhancement.

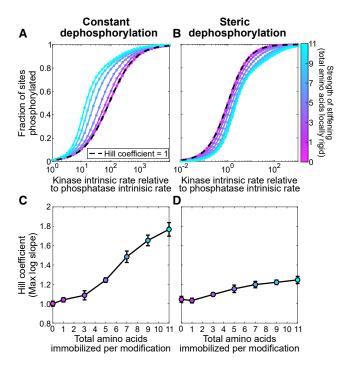


FIGURE 4 Emergent cooperativity from binding rate enhancement implies switch-like dose response, even in symmetric phosphorylationdephosphorylation cycles. (A and B) Fraction of sites phosphorylated as a function of the kinase/phosphatase activity ratio (measured by the ratio of free-space rates) for different ranges of local stiffening are shown (color bar), assuming a phosphatase with (A) negligible size or (B) radius of 2.1 nm, equal to the kinase. Black dashed line indicates a linear dose response, i.e., with Hill coefficient 1. (C and D) Hill coefficients for different ranges of local stiffening per phosphorylation event are given, assuming a phosphatase of (C) negligible size or (D) radius of 2.1 nm. Error bars indicate root mean-square error from a cubic polynomial fitted to slope. To see this figure in color, go online.

Note by "intrinsic rate," we mean k_{on}^0 , which is the freespace (solution) rate if the reaction did not experience any occlusion. In Fig. 4 A, the kinase activity is challenged by significant steric hindrance (but not the phosphatase), so, much more kinase is required to overcome a given phosphatase concentration compared to Fig. 4 B.

Membrane affinity

Recent evidence (24,46) suggests a model for T cell signaling in which, before receptor triggering, the ε - and ζ -chains are unphosphorylated and membrane associated, protecting them from phosphorylation by kinases (Fig. 1 Biii), only dissociating from the membrane after triggering, at which time they can become phosphorylated. But TCR phosphorylation is one of the first steps in triggering (23), raising a "chicken-or-the-egg" question: how are the first chains phosphorylated?

A possible hypothesis (27,47–49) to resolve this puzzle is that before triggering, the chain is biased toward the membrane but spends a small, yet significant, time in the cytoplasm, accessible to kinases. Then, upon initial phosphorylation, the bias is shifted toward the cytoplasm, allowing further phosphorylation. This hypothesis suggests a delicate balance between membrane affinity and phosphorylation. In this section, we ask, if phosphorylation controls membrane association, what are the quantitative constraints on the interaction strengths between the chain, the membrane, and the kinase? And what proportion of states are accessible to the kinase before and after initial phosphorylation?

Simplified membrane interaction model can explain both basic residue and phosphorylation effects

Experimental data suggest that ε membrane association before TCR triggering has two features: first, that the basic residues in ε are required for membrane association, and second, that fully phosphorylated ε does not associate with the membrane. We create a simplified electrostatic interaction model, in which phosphorylated tyrosines feel a repulsion from the cell membrane and basic residues feel an attraction, shown in Fig. 5 B and described by Eqs. 5, 6, and 7. Each potential is parameterized to reproduce the two experimental phenomena. We first look at how strong the basic residue-membrane attraction, $E_{\rm B0}$, needs to be to confine the tyrosines to the membrane, as defined by the horizontal line in Fig. 5 C, inset. We find that the minimal $E_{\rm B0}$ for basic residues to achieve this is 0.5 $k_{\rm B}T$. In other words, this is the energetic cost to overcome the chain's entropic pull away from the membrane.

We next tune the strength of the phosphorylation potential, E_{P0} , such that tyrosine phosphorylation compensates for the basic residues (i.e., to match the distribution where $E_{\rm B0}=0$), shown in Fig. 5 D. A priori, we expected that for full phosphorylation to be enough to counteract the membrane association created by the basic residues, we would require that

$$E_{\rm P0} \ge n_B/n_Y \times E_{\rm B0},\tag{8}$$

where n_B and n_Y are the numbers of basic residues and tyrosines, respectively. Indeed, in Fig. S7, we find that for the ζ chain, this is consistent with simulation. However, for ε , our simulations indicate that $E_{PO} \sim 2k_BT$ is sufficient for its two tyrosines to compensate for the basic residues (Fig. 5 D), in contrast to Eq. 8, which predicts a minimal E_{P0} of $3.5k_BT$. We can explain this by examining the distribution of basic residues compared to tyrosines. For ζ , there are both tyrosines and basic residues along the full length of the domain. In ε , the two tyrosines are clumped at the membrane-distal end of the domain, with fewer basic residues nearby.

Phosphorylation-modulated membrane association allows some early phosphorylation and at least a small acceleration for late phosphorylation

Using the parameter constraints found above, we examine how phosphorylation influences binding kinetics for ε , shown in Fig. 6 A. At the minimal $E_{P0} = 2k_BT$, the average

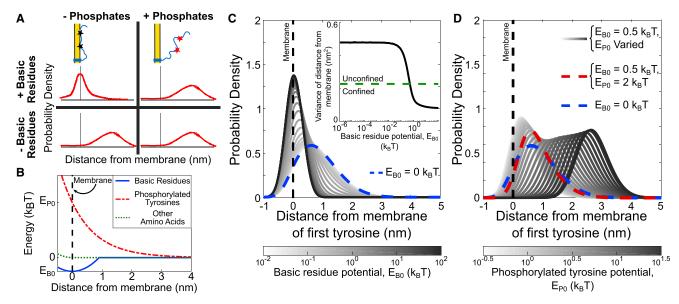


FIGURE 5 Simplified membrane interaction model sets constraints on the strength of basic residue attraction and phosphorylation-driven repulsion from membrane. (A) Schematic diagrams reflecting probability density of tyrosines under different conditions are given. Based on previous experimental studies, our model must be consistent with the following: probability density of tyrosines is narrow and close to the membrane for wild-type ε but widens and shifts away from the membrane when it is phosphorylated or the basic residues are mutated. (B) Interaction potentials used in the simplified model are shown. Basic residues experience an attractive potential of depth $E_{\rm B0}$ near the membrane and experience zero potential one Debye length (\sim 1 nm) away from the membrane (blue solid line). Phosphorylated tyrosines experience a repulsive potential with strength E_{P0} (red dashed line). Unphosphorylated tyrosines and all other amino acids are hindered from entering the membrane but otherwise experience no potential (green dotted line). (C) Probability density of the distance from the membrane of the first tyrosine of ε , assuming no phosphorylated tyrosines, is shown for varying strengths of the basic residue potential, $E_{\rm B0}$ (white: low; black: high). The tyrosine moves close to the membrane as $E_{\rm B0}$ is increased. Probability density when there is no basic residue potential ($E_{\rm B0}=0~k_{\rm B}T$) is shown as blue dotted line. (Inset) Variance of probability density of first tyrosine over range of basic residue potential strengths is shown. Green dashed line shows the characteristic $E_{B0} = 0.5k_BT$ required to confine the tyrosine to the membrane, defined in the text. (D) Probability density of the location of first tyrosine assuming all tyrosines are phosphorylated is shown for $E_{B0} = 0.5k_BT$ (the value required to confine the tyrosine to the membrane assuming no tyrosines are phosphorylated) and varying phosphorylated tyrosine potential strength, E_{P0} (low: white, high: black). Probability density when $E_{P0} = 2k_BT$ is shown as red dashed line, reflecting the E_{P0} -value needed to approximately return to the distribution when $E_{B0} = 0k_BT$ (blue dashed line). To see this figure in color, go online.

kinase binding rate increases $\sim 10\%$ between the first and the second phosphorylation. When E_{P0} is stronger ($E_{P0} \ge$ $2k_{\rm B}T$), the average kinase binding rate increases signifi-

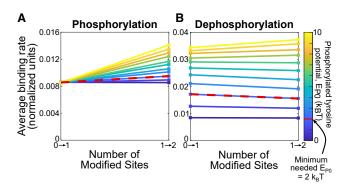


FIGURE 6 Phosphorylation-driven modulation of membrane association allows tyrosines to operate as a regulatory switch yet still remain accessible in the "off" state. Average binding rates of (A) kinase and (B) phosphatase binding to ε at different (de)phosphorylation states for varying strengths of phosphorylated tyrosine potential (E_{P0}) are shown (blue: weak; yellow: strong). Both kinase and phosphatase are assumed to have a radius of 2.1 nm. Rates are normalized to the free-space binding rate. To see this figure in color, go online.

cantly for future phosphorylation events (up to 50% for $E_{\rm P0} = 10k_{\rm B}T$).

We next investigate dephosphorylation in Fig. 6 B. Interestingly, there is a weak increase in dephosphorylation rates, in contrast to the stiffening model above. We understand this as follows. As more residues become dephosphorylated, more sections of the chain become restricted to the membrane. The remaining phosphorylated tyrosines remain far from the membrane by the repulsive phosphate-membrane interaction and therefore more accessible to the phosphatase. The cooperative effect of dephosphorylation only produces a small increase (1.15-fold) in binding rate because the membrane still creates a large steric barrier to phosphatase binding.

Investigation of the reversible system, shown in Fig. 8, shows that stronger phosphate-membrane interactions (E_{P0} $> 2k_{\rm B}T$) cause the dose-response curve to diverge slightly from Michaelis-Menten kinetics under both constant and sterically influenced dephosphorylation.

Multiple simultaneous binding

One of the first molecular participants in signaling downstream of TCR is ZAP70, which binds phosphorylated tyrosines (18,19,29,50,51). A recent in vivo experimental study found that approximately six ZAP70 molecules are bound per TCR (29), despite there being 10 possible binding sites. This raises two questions: do entropic constraints arising from polymer flexibility prevent more ZAP70 ligands from binding (in addition to possible low occupancy set by dissociation constant)? And, if so, are there advantages to the cell in not using the full array of possible ZAP70 binding sites? To address this question, we simulate binding of a ligand, ZAP70, to the full TCR when other ligands are already bound, shown schematically in Fig. 1 Biv.

Multiple binding to multisite disordered domain gives rise to negative cooperativity

We calculate the average binding rates of ligands to all six membrane-bound chains of TCR, assuming a given number of previously bound ligands. In this section, rather than a single chain, we simulate all six chains anchored to the membrane (38), and rather than represent all tyrosines as individual sites, we place a binding site at the center of each ITAM. In other words, in the previous sections, we independently treated LCK and CD45 enzymatic domains interacting with single tyrosines, whereas here we treat ZAP70 interacting with two tyrosines on an ITAM.

First, we ran simulations to see whether there is a hard limit to the number of ZAP70 molecules that can bind to the TCR. We find that at our estimate for the size of ZAP70, there are configurations that allow binding a full 10 ZAP70 molecules to the six chains. Indeed, 10 molecules with radius of up to 6.9 nm (larger than our estimate of the size of ZAP70) can still fit, as shown in Fig. 7 B. Given that the steric limit is not being reached, is there a limit set by entropic effects?

As more ligands are simultaneously bound to the TCR, the average binding rate decreases. For a ligand with the size of ZAP70, \sim 2.7 nm radius, the binding rate for the seventh ligand is \sim 200 times lower than the binding rate of the first ligand (Fig. 7 Ci). Simulations in which the chains are anchored further apart, as shown in Fig. 7 Ciii, exhibit significantly less hindrance.

In both cases, the rate decrease implies a "negative cooperativity" effect, which could allow TCRs to recruit a regulated number of ZAP70 molecules while still maintaining high binding rate. The first few ZAP70 molecules are able

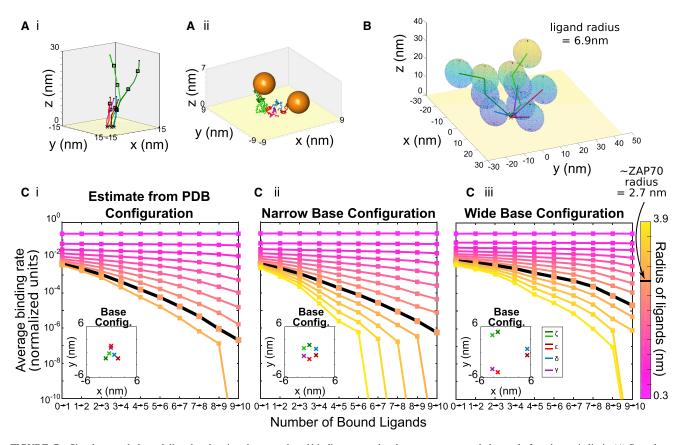


FIGURE 7 Simultaneously bound disordered regions have a reduced binding rate as they become more crowded, even before the steric limit. (A) Snapshots of simulated TCR subunits and binding sites (black squares) (Ai) in extended conformation and (Aii) at equilibrium with two bound ligands are given. (B) Simultaneous binding of full TCR is not sterically prohibited at physiological ligand radii. View of single TCR configuration with 10 bound ligands in which each ligand has radius of 6.9 nm is shown. (C) Average binding rates to TCRs against number of ligands bound are shown for varying ligand size (color bar; pink: small; blue: large) and TCR subunit configuration (Ci) estimated from PDB structure of TCR, (Cii) 1.5 nm, and (Ciii) 5 nm. To see this figure in color, go online.

to bind to the domain relatively easily, but it quickly becomes prohibitive to bind more. The alternative way of regulating a limit around six ZAP70 molecules would be to have only six binding sites, but then the total binding rate would be lower (because there would be four fewer opportunities to bind).

Optimal distribution of binding sites on multiple nearby chains

The above finding suggests that the chain's entropy influences how readily a multichain receptor can become loaded with signaling molecules. This led us to ask: given 10 binding sites, if the goal is fast loading, is it preferable to have 10 different chains with one binding site each or one chain with all 10 binding sites (or, perhaps, have the 10 sites distributed on six chains, as they are for TCRs)? A priori, it could be that the two effects of a nearby membrane and ligands bound to neighboring chains "in trans" together prohibit binding, leading to a preference for concentrating the sites on fewer chains. Alternatively, it could be that other molecules bound "in cis" on the same chain prohibit binding, leading to a preference for sites that are distributed across many chains.

We simulate 10 sites (for a ligand approximately the size of ZAP70) distributed on 1, 2, 3, 5, 9, or 10 chains, as shown in Fig. 8 A. The chains are assumed to each be anchored to the membrane on the perimeter of a circle. The radius of the circle is either 1.5 nm, similar to the spacing found in the crystal structure of the TCR (38), or wider at 5 nm. We report the average rate of the sixth binding event.

We find that if the chains are in the narrow configuration, the fastest binding occurs when the sites are all on a single chain (Fig. 8 Bi). This result holds over a wide range of spacings between the sites on the chain. When the chains are anchored further apart, we find that the fastest binding is achieved when the 10 sites are distributed across 10 chains (Fig. 8 Bii), in agreement with intuition. These results suggest a consideration for engineered receptors; there are significant rate differences obtained by having the same signaling modules on multiple versus single chains. Specifically, for the base separation distance estimated for TCR, we find that it is beneficial to have the sites on the same chain to minimize neighbor interference.

For these simulations, we explore different spacings between the tyrosines. For simplicity, we assume these sites are evenly spaced, unlike the real TCR, with spacing ranging from 8 to 20 amino acids, indicated by color in Fig. 8. The relative performance of different filament distributions does not depend on within-chain spacing, although overall steric hindrance increases with less spacing, as intuitively expected.

For a receptor with 10 binding sites, the sixth binding event can happen in 1260 ways. Interestingly, we find that the rates of these 1260 configurations can have multimodal distributions. In Fig. S11, we explore how this multimodality arises.

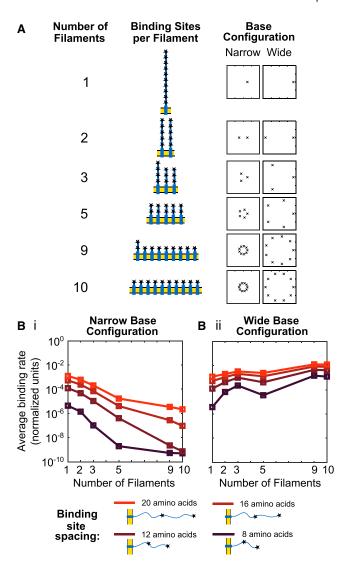
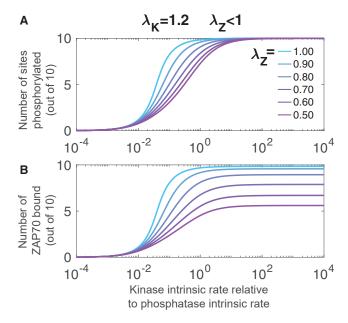


FIGURE 8 Optimal distribution of 10 binding sites on multiple chains is dependent on membrane spacing of subunits. (A) A schematic for distribution of 10 binding sites on multiple chains is given. For each, chains are distributed evenly on 1) a narrow circle of radius 1.5 nm and 2) wide circle of radius 5 nm. (B) Average path-weighted binding rates of sixth binding event to constructed domain are shown against number of chains in domain (color bar; dark red: short spacing between binding sites; bright red: long spacing) and subunit configuration (Bi) 1.5 nm radius or (Bii) 5 nm radius. Simulations explore different spacings between binding sites from 8 to 20 amino acids, indicated by color. Ligand radius is 2.7 nm. To see this figure in color, go online.

Integrative model of nonlinear modules

The models above each lead to nonlinear behavior in different modules of the TCR triggering process. To roughly summarize: first, for the tyrosines on a single ζ -chain or ε-chain, phosphorylation-induced stiffening or membrane affinity control leads to positive rate enhancements for the accessibility to kinases and/or phosphatases. Second, for the full six-chain TCR, multiple simultaneous binding by ZAP70 leads to a rate decrease for subsequent accessibility. So, the question arises: what is the net effect?



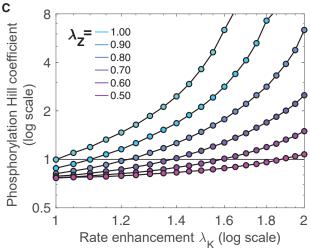


FIGURE 9 Integrative model shows counteracting effects of rate enhancement and rate reduction. Rate reduction from ZAP70 binding ($\lambda_Z < 1$ indicated by color) abrogates the switch-like dose response conferred by rate enhancement of kinase phosphorylating TCR $\lambda_K = 1.2$ for both amount of phosphorylation (A) and amount of ZAP70 bound (B), in addition to reducing the saturating value ($E_{\rm max}$) of ZAP70 binding (B). (C) Ultrasensitivity quantified using the log-effective-concentration definition of Hill coefficient (Eq. S2) is shown for a range of $\lambda_K \geq 1$ and $\lambda_Z \leq 1$. To see this figure in color, go online.

We explore this question in an integrative model combining phosphorylation, dephosphorylation, and ZAP70 binding of all 10 sites on a TCR. We coarsen the modeling approach and make the simplifying assumption that rate modifications act similarly independent of the site. This allows a continuous-state model expressed as a system of nonlinear differential equations. We assume that of N = 10 sites, n_P are phosphorylated and n_Z are ZAP70 bound. Only phosphorylated sites can be ZAP70 bound, and ZAP70 sites are protected from dephosphorylation

(which is a simplification of the tandem ZAP70-ITAM interaction (17)). Therefore,

$$\frac{dn_P}{dt} = k_K (N - n_P) - k_F (n_P - n_Z)$$
 (9)

and

$$\frac{dn_Z}{dt} = k_{\text{on}}(n_P - n_Z) - k_{\text{off}}(n_Z), \tag{10}$$

where k_K , k_F , $k_{\rm on}$, and $k_{\rm off}$ are the rates of phosphorylation, dephosphorylation, ZAP70 binding, and ZAP70 unbinding, respectively. The nonlinear modules that emerged in previous sections of this work represent nonconstant rates, which we approximate from the previous sections by fitting to exponential forms

$$k_K = k_K(n_P, n_Z) \approx k_K^0 \lambda_K^{n_P} \lambda_Z^{n_Z}, \tag{11}$$

$$k_F = k_F(n_P, n_Z) \approx k_F^0 \lambda_K^{n_P} \lambda_Z^{n_Z}, \tag{12}$$

and

$$k_{\text{on}} = k_{\text{on}}(n_P, n_Z) \approx k_{\text{on}}^0 \lambda_K^{n_P} \lambda_Z^{n_Z}, \tag{13}$$

where $\lambda_K > 1$ is the rate enhancement, either from stiffening or membrane dissociation, and $\lambda_Z < 1$ is the rate decrease from multiple ZAP70 binding. For kinetic rates, $k_{\rm off} \approx 0.2~{\rm s}^{-1}$ (17), and we sweep over a range of k_K and k_F to produce dose-response curves. For the nonlinearities, we estimate $\lambda_K \approx 1.2$ for stiffening from Fig. S3, and similarly $\lambda_K \approx 1.2$ from Fig. S7. In other words, each phosphorylation increases the subsequent phosphorylation by $\sim 20\%$. We estimate $\lambda_Z \approx 0.6$ from the rate reductions shown in Fig. 7. Code is available at https://github.com/allardjun/EntropicMultisiteIntegrative (https://doi.org/10.5281/zeno do.4118734).

Counteracting effects of rate enhancement and rate reduction

Dose-response curves for various combinations of λ_K and λ_Z are shown in Figs. 9 and S12.

First, we simulate in the absence of steric inhibition from multiple ZAP70 binding ($\lambda_Z = 1$). We find that when ZAP70 is present and protects phosphorylated sites from dephosphorylation, then even with symmetric phosphorylation and dephosphorylation, the rate enhancement $\lambda_K > 1$ leads to significant ultrasensitivity. This is related to a known phenomenon in which sequestration of sites gives ultrasensitivity (52). In addition to ultrasensitivity, the rate enhancement effect reduced the EC50—in other words, it increases potency.

Next, we include the steric inhibition from multiple ZAP70 binding ($\lambda_Z < 1$). The multiple binding rate reduction reduces the saturating number ($E_{\rm max}$) of ZAP70

binding, but not phosphorylation. Depending on k_{off} , this leads to a steady state of ~6 ZAP70 per TCR, even though the rate reduction is not a sharp cutoff. In agreement with intuition, this occurs around when $k_{\text{on}}^0 \lambda_Z^6 = k_{\text{off}}$.

The rate reduction of ZAP70, when $\lambda_K = 1$ (no rate enhancement), leads to shallow dose-response curves. For this reason, in Fig. 9 C, we quantify the ultrasensitivity using the log-concentration definition (see Eq. S2), which can be negative to indicate shallow responses. When both $\lambda_K > 1$ and $\lambda_{Z} < 1,$ the effects counteract each other. Roughly, an enhancement of $\lambda_K = 2$ is required to counteract a reduction of $\lambda_Z = 0.5$.

At $\lambda_Z = 0.6$ and $\lambda_P = 1.2$, the reduction effect dominates, leading to a negative Hill coefficient. Interestingly, in previous work (19), we found a lack of ultrasensitivity in the presence of multiple ITAMs. Note that at these parameters, the rate enhancement still leads to increased potency; this is not abrogated by the multiple-binding-induced reduction.

DISCUSSION

Multisite modification of signaling molecules leads to high combinatorial complexity that is challenging to study. Because there are 10 ITAMs on a TCR, we were required to simulate $\sim 1000 \ (= 2^{10})$ binding states and ~ 3.6 million (= 10 factorial) possible sequences of phosphorylation. Other explorations in this work have similar combinatorial complexity; for example, the six tyrosines on CD3 ζ imply 64 binding states and 720 sequences. Furthermore, a major opportunity of computational simulation is its ability to simulate counterfactual parameters, for example, larger or smaller ligand radii and ITAMs arranged on different numbers of chains, because these counterfactuals provide insight into the real parameters. The coarse-grain modeling approach we use here—representing structured domains as simple rigid bodies, disordered regions as simple polymers, and membrane interactions with simple potentials—are computationally efficient enough for us to perform such parameter exploration.

Previous modeling work on TCR largely falls in two categories. First are models of the kinetics of signaling by TCR, in which the system is modeled as transitions between distinct molecular states (e.g., membrane bound or not (27)), for example, using differential equations or Markov chains to model binding to multisite molecules (53-57). Second, several detailed molecular models have focused on the TCR's transmembrane and extracellular domains (e.g., see (58,59)) because of the challenges of simulating the highintrinsic disorder of the chains (60,61), with the notable exception of (43). Our work attempts to bridge this gap, connecting submolecular states with the kinetics that provide inputs for models of the signaling cascade. Although the coarse granularity omits many details, such as sequencedependent persistence lengths (62), we join a growing body of modeling efforts (63,64) at the granularity between particles representing individual proteins and particles representing individual atoms, which has been particularly fruitful for intrinsically disordered domains (10–12,22,65).

Multisite reactions can be classified in two categories: sequential or random. For CD3ζ, evidence for sequential phosphorylation is mixed (54,66,67). Our work offers a possible resolution. As opposed to obligate sequential modification, meaning the previous event is required before the next event can occur, we find that multisite disordered domains can display preferential sequential modification, meaning that previous events reduce the probability of future sequences but do not prohibit them. Note that the extensive theoretical studies of the consequences of sequential binding (21,53-56) assumed obligate sequences. In some cases, the sequence is assumed, and the mechanism enforcing it is unclear. In contrast, in our model, the sequence is an emergent property of the distribution of sites along the chain. We find that the membrane increases the differences in binding rate and therefore amplifies the preference, but it is the positions of the tyrosines along the chain that are the primary drivers.

Previous results suggested that the ζ -chains exhibit cooperative phosphorylation (19). We demonstrate that phosphorylation-induced local structuring of ζ naturally leads to cooperativity, offering a possible explanation for these results. Alternative models to explain the TCR ultrasensitivity include TCR clustering (68) and changes in lipid composition (49,69,70). Thus, our model suggests the following experiments: if it is local structuring that drives cooperativity, adding extra residues to increase the spacing between ITAMs would reduce ultransensitivity, whereas reducing the number of residues between ITAMs would increase ultrasensitivity.

Before T cell triggering, the CD3 ε domains of the TCR associate with the cell membrane, with the tyrosines primarily embedded in the bilayer (24–26). Post-triggering, they dissociate from the membrane, revealing the tyrosines for phosphorylation (26). Thus, membrane association could act as a switch controlling the activity state of the CD3 ε chain. However, given that tyrosine phosphorylation is one of the first events in TCR triggering, this hypothesis features a "chicken-or-the-egg" paradox. A plausible resolution (26) is that the unphosphorylated chain is exploring an ensemble of configurations in which its accessibility to kinases is limited but not totally forbidden. The question, then, is whether this accessibility changes enough between unphosphorylated and semiphosphorylated states to provide a switch. We find that to be consistent with the two observations that both basic residues and phosphostate control membrane proximity, phosphotyrosines in CD3 ε must experience a repulsive potential of approximately $E_{P0} \approx 2k_BT$. However, at this repulsion energy, the semiphosphorylated state is only $\sim 10\%$ more accessible than the unphosphorylated state. To get an increase in accessibility of 50% would require $E_{P0} \approx 10k_BT$, which is several times larger than typical residue-membrane energies (44). Our results do not preclude the membrane association switch hypothesis but do set a requirement for large interaction energies for it to hold, for example, because of dynamic changes in lipid composition.

As shown in Fig. 7, we find that 10 ZAP70 molecules readily fit on a TCR but that the seventh ZAP70 molecule binds at a rate \sim 200-fold slower than the first. To clarify the difference between these two forms of steric occlusion, in the first case, we ask whether all microstates (polymer configurations) in the fully bound macrostate are forbidden, whereas in the second case, we ask what proportion of microstates are forbidden. Our finding is that a significant proportion of microstates are forbidden, even at ligand sizes at which the fully bound macrostate is not forbidden. In other words, entropy limits binding much before volume exclusion forbids it. When we include these entropic effects in a model of both attachment and detachment (Fig. 9), we find a steady state with 6-ZAP70-per-TCR stoichiometry, as previously reported (29). This occurs even though the entropic effects do not lead to a sharp cutoff in attachment

These steric effects imply negative cooperativity. Negative cooperativity can endow signaling systems with two features: high turnover of ligands even in high ligand concentration (which might be advantageous if ligands are involved in other reactions) and constant signaling activity in low ligand concentration. Similarly, this might reduce the impact of inhibitors, requiring much higher concentrations of inhibitor to completely turn off signaling (71). This leads to a model prediction: if the non-TCR-binding domains of ZAP70 are removed, the model predicts an increase in ultrasensitivity and a higher bound fraction.

Our model predicts that multiple ITAMs on the same chain will bind to ZAP70 faster than the same number of ITAMs on multiple clustered chains, provided the chains have membrane domains with similar relative spacing as the TCR. For larger relative spacing of chains, the relationship flips, and it is better to have ITAMs on multiple chains (Fig. 8 B). This is a testable prediction. Furthermore, even without experiments that modify the spacing, our model predicts the fold-change reduction in binding rates for subsequent ZAP70 molecules. The rate of a single ZAP70 binding to an ITAM has been measured (17). We predict that, for example, the second ZAP70 will bind at a rate 20% slower (Fig. 7). If realized, this would add to a growing body of work demonstrating the importance of the disordered regions of amino acids between catalytically active or posttranslationally modified parts of proteins (10,13).

Although we propose several experimental tests of the model (e.g., addition of residues between ITAMs or removal of the nonbinding domain of ZAP70), these are mostly positive tests. There is also a negative test: if the freely jointed chain model is applicable to TCR chains, then replacing residues between ITAMs in any of the chains should have minimal effect on phosphostate, ZAP70 binding, and ultimately on TCR signaling, provided that the number of residues, intrinsic disorder, and electrostatic properties of the residues are preserved.

SUPPORTING MATERIAL

Supporting Material can be found online at https://doi.org/10.1016/j.bpj. 2020.11.2266.

AUTHOR CONTRIBUTIONS

L.C. wrote simulation code, carried out simulations, analyzed the data, and prepared the manuscript. O.D. helped design the research and prepare manuscript. J.A. designed the research, supervised the project, and helped prepare the manuscript.

ACKNOWLEDGMENTS

We thank Sean Lawley (University of Utah) for valuable discussion.

This work was supported by National Science Foundation (NSF) CAREER grant DMS 1454739 to J.A., NSF grant DMS 1715455 to J.A., and NSF grant DMS 1763272 and a grant from the Simons Foundation (594598, QN), and Wellcome Trust grant SRF 207537/Z/17/Z to O.D.

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Clemens et al.

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Biophysical Journal, Volume 120

Supplemental Information

Intrinsic Disorder in the T Cell Receptor Creates Cooperativity and Controls ZAP70 Binding

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Supporting Material

Intrinsic disorder in the T cell receptor creates cooperativity and controls ZAP70 binding

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List of Supporting Figures

	S1	Local stiffening: Transition Rates	4
	S2	Local stiffening: Emergent sequential binding	5
	S3	Local stiffening: Unweighted average binding rates for short-range stiffening	6
	S4	Local stiffening: Binding rates for long-range stiffening	7
	S5	Local stiffening: Probability of second-to-last event	8
	S6	•	9
	S7	Membrane affinity: Zeta distributions	10
	S8	Membrane association: ζ binding rates and dose response curves	
	S9	Membrane affinity: Dose response curves for ϵ alternative Hill coefficient definitions	
	S10	Simultaneous binding: Filament sweep binding rates	
	S11	Simultaneous binding: Filament sweep binding rates histograms	
	S12	Integrative model full results	15
L	ist (of Supporting Text	
1	Sum	nmary of interactions	2
2	Loca	al stiffening	2
3	Ultr	easensitivity and alternate definitions of Hill coefficients	2
4			
	Mul	timodality in binding rates	3

1 Summary of interactions

To summarize interactions between physical elements: Ligands are treated as hard spheres, so there is zero repulsion until they approach the chain, or each other, until within 1 radius, after which there is infinite repulsion. Bound ligands are constrained to move with the chain, equivalent to an infinitely-strong bond. Interactions with the membrane are modeled using the general forms in Main Text Eqs. 5-6, where the parameters E_{P0} and E_{B0} are estimated by constraining the model to satisfy two experimental observations (tyrosine phosphorylation and basic residue mutation). Within-chain interactions are omitted, i.e., it is a non-interacting FJC.

2 Local stiffening

As described in Main Text Fig. 4, we explore the consequences of assuming that a phosphorylation event locally stiffens the region around the tyrosine. Here, we explore stiffening ranges beyond 11 amino acids in Fig. S4. For maximal local stiffening, i.e. all residues becoming stiff upon first phosphorylation, the binding rate increases to 1.0 in units relative to the free-space (unoccluded) rate, since the kinase is uninhibited and always able to access the binding sites.

At intermediate values of local stiffening, the average binding rate does not consistently increase but oscillates (Fig. S4A). This phenomenon can be understood by considering the distribution of tyrosines along ζ . The six tyrosines are grouped in pairs, constituting ITAMs. The tyrosines in each pair are significantly closer to each other than to the tyrosines of the next ITAM, leading to an evens-odds effect in which even-numbered tyrosines are fast compared to odd-numbered tyrosines.

The Main Text figures weight the phosphorylation rates by their likelihood. Without weighting by most likely phosphorylation states, the average binding rate smoothly increases with number of phosphorylations, as shown in Fig. S3.

3 Ultrasensitivity and alternate definitions of Hill coefficients

Here we investigate two complementary defintions of ultrasensitivity. Both definitions extract a Hill coefficient from the dose-respone curves. We refer to them here as switch-like behavior and threshold behavior. The switch-like behavior of a dose-response curve describes how quickly it increases from a less-phosphorylated state to a more-phosphorylated state and can be used as a measure of cooperativity. Mathematically, the switch-like behavior is the maximum logarithmic slope of each curve. Specifically, for a kinase-phosphatase ratio r, if the fraction of tyrosines phosphoryated is p(r), then

$$H_{\text{switch}} = \max\left(\frac{d}{dr}\left(\log\left(\frac{p(r)}{1-p(r)}\right)\right)\right).$$
 (1)

Alternatively, the threshold behavior of the curve describes how high of a dose is required before a response occurs. We calculate this value as

$$H_{\text{threshold}} = \log_{10}(81)/\log_{10}(\text{EC90/EC10}).$$
 (2)

We calculate the switch-like and threshold behavior of the dose-response curves under constant and steric dephosphorylation in Fig. S6.

For constant dephosphorylation, the switch-like behavior increases with the number of amino acids stiffened per phosphorylation event. When 1/12 chain is stiffened per event, the switch hill coefficient is 1.8, suggesting

moderate switch-like behavior, while the threshold hill coefficient is less than 1.2, suggesting a poor threshold (Fig. S6C). For steric dephosphorylation, the same increasing trend persists, but at 1/12 chain local stiffening, the switch hill coefficient is only 1.3 and the threshold hill coefficient is about 0.8 (Fig. S6D). Local stiffening therefore creates cooperativity, even under reversible phosphorylation, but makes a poor threshold.

In Fig. S9 we show the Hill coefficients for the ϵ membrane affinity model presented in the Main Text, but with the threshold definition of Hill coefficient in Eq. 2.

4 Multimodality in binding rates

We simulate simultaneous ligand binding to 10 sites distributed among 1, 5, and 10 chains. Specifically, we consider the rate of binding a sixth ligand to the complex. Under this construction, there are 1260 ways (= 5×10 choose 5) a sixth ligand may bind to the complex. Histograms of these 1260 binding rates for each complex construction show that multimodality can arise in some cases. When there are 5 filaments, with 2 binding sites each, we see bimodality in the binding rates when the space between binding sites is 8 amino acids (Fig. S11). We find weak tri-modality when the binding site spacing is longer (20 amino acids).

To explore how this multi-modality arises, we investigated characteristics of the binding sites. We split the binding sites into two categories: binding sites on a filament with no ligands bound and binding sites on a filament that already has a ligand bound. When we plot the histograms of the binding rates by category, we find that the bimodal distribution can be explained. Binding a second ligand to a filament is harder than binding the first ligand, since the second filament will experience steric occlusion from the other ligand in addition to the filament itself. This results in a lower binding rate compared to ligands binding to empty filaments (Fig. S11). Steric occlusion from ligands on the same filament is increased when the space between the binding sites is shorter. This explains the high separation between the two modes of binding rates for the shorter binding site spacing compared to the longer binding site spacing.

5 List of Supporting Movies

• Supporting Movie SM1: Example of simulated TCR with two bound ligands. The chains of the TCR are shown simulated as freely-jointed chains (ζ - green, ϵ - red, δ - blue, γ - purple) with ITAM binding sites shown as black squares. Chains are anchored (black x) in a narrow base configuration, $\sim 1.5 \, \mathrm{nm}$ apart and not allowed to pass below the membrane (yellow). Two bound ligands (opaque orange spheres) are shown attached to TCR. A third ligand attempts to bind a specific binding site. When binding region is occluded in a configuration, ligand cannot bind (transparent orange sphere). When polymers, bound ligands, and membrane are all outside of binding region, the ligand may bind (not shown). Radius of ligands is 2.1 nm.

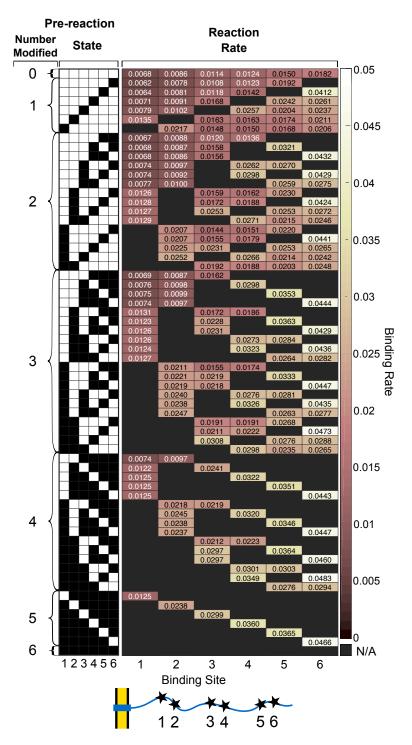


Fig. S1: Disorder leads to accessibility differences, which implies binding rate differences between phosphorylation sites. Reaction rates of a kinase binding to the six binding sites of membrane bound ζ in a given phosphorylation state. In this case, results are shown assuming each phosphorylation event locally stiffens 11 amino acids. Dark red: low binding rate; white: high binding rate; black: phosphorylated site. Left two columns show the pre-reaction number modified and phosphorylation state before the next binding event (white: unphosphorylated site; black: phosphorylated site).

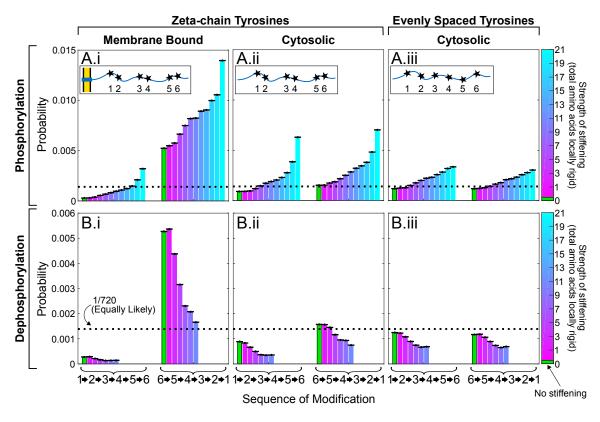


Fig. S2: Binding rate differences imply emergent preference of (de)phosphorylation sequence. Probability of (A) phosphorylating or (B) dephosphorylating membrane proximal-to-distal (123456) compared to membrane distal-to-proximal (654321). Colors represent simulations of different ranges of local stiffening/unstiffening per binding event. No stiffening (0 stiffening) shown in green. Each of these is shown for: (i) with a membrane, assuming sites spaced like tyrosines of ζ , (ii) without a membrane, assuming sites spaced like tyrosines of ζ , and (iii) without a membrane, assuming sites spaced evenly along the length of ζ . The black dotted lines indicate the probability if all events were equally likely (1/6!=1/720). Error bars (A,B) represent standard error of the mean, treating each Gillespie run as an individual Bernoulli trial. Phosphorylation and dephosphorylation are more likely to occur membrane distal-to-proximal compared to proximal-to-distal for both the membrane bound and cytosolic ζ chain. For cytosolic ζ with evenly spaced tyrosines, both (de)phosphorylation sequences are approximately equally probable.

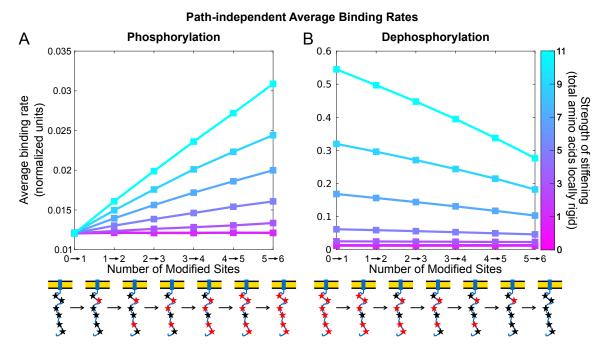


Fig. S3: Local stiffening: Unweighted average binding rates for short-range stiffening (A) Sequence-independent average binding rates of a kinase binding to ζ at different phosphorylation states for varying range of local stiffening (pink: no residues are stiffened; blue: 11 residues are stiffened, 5 on each side of site). The kinase average binding rate increases with each phosphorylation and also with local stiffening range. (B) Sequence-independent average binding rates of a phosphatase binding to ζ at different dephosphorylation states for varying ranges of local un-stiffening per dephosphorylation event. When local stiffening occurs, the phosphatase average binding rate decreases with each phosphorylation and also with local stiffening level. For both (A) and (B), schematic below axis shows example configuration for each phosphorylation state. Unphosphorylated residues represented by black stars, phosphorylated residues are red stars. Kinase and phosphatase radius is 2.1nm. Rates are normalized to the free-space binding rate.

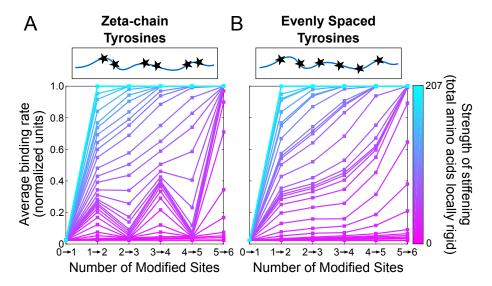


Fig. S4: Local stiffening: Binding rates for long-range stiffening. Sequence-dependent average binding rates of a kinase binding to cytosolic ζ (A) and cytosolic ζ with evenly spaced tyrosines (B) at different phosphorylation states for varying range of local stiffening (pink: no residues are stiffened; blue: all residues are stiffened after first phosphorylation). For small and large magnitudes of local stiffening, the average binding rate increases with each phosphorylation. For intermediate magnitudes of local stiffening, cytosolic ζ exhibits oscillations in the average binding rate with an overall increase (A) while cytosolic ζ with evenly spaced tyrosines increases without oscillations (B). In both cases at maximal local stiffening per phosphorylation, the entire domain is stiff leading to uninhibited kinase binding. Schematic below axis shows example configuration for each phosphorylation state. Unphosphorylated residues represented by black stars, phosphorylated residues are red stars. Kinase and phosphatase radius is 2.1nm. Rates are normalized to the free-space binding rate.

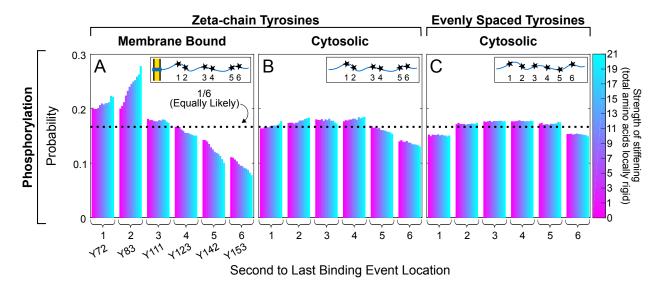


Fig. S5: Local stiffening: Probability of second-to-last event. Probability of the second-to-last binding event occurring at a specific site. Colors represent simulations of different ranges of local stiffening/unstiffening per binding event. Shown for: (A) with a membrane, assuming sites spaced like tyrosines of ζ , (B) without a membrane, assuming sites spaced like tyrosines of ζ , and (C) without a membrane, assuming sites spaced evenly along the length of ζ . The black dotted lines indicate the probability if all events were equally likely (1/6). As reported in Main Text Fig. 3, there is a decrease in the average binding rate between the fourth and fifth binding event. To understand this effect, we examine the probability of the identity of the second-to-last binding event For membrane-bound ζ -chains, the fifth binding event is most likely to occur at the second tyrosine from from the membrane, Y83. Therefore, the average binding rate is most heavily influenced by the binding rate at the Y83. The dip in binding rate seen there marks a competition between disordered-to-ordered transitions, which tends to make all sites more accessible, versus the increasing difficulty of phosphorylating sites that are highly occluded. Although occlusion by the chain is reduced by disordered-to-ordered transitions, it is not enough to overcome the high membrane occlusion that Y83 experiences. Therefore, since the fifth binding event is dominated by the low binding rate that Y83, the average rate decreases.

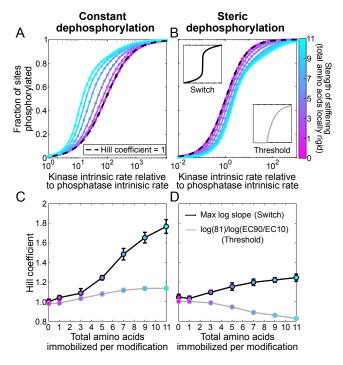


Fig. S6: Local stiffening: Dose response curves and alternative Hill coefficient definitions. (A,B) Fraction of sites phosphorylated as a function of the kinase-to-phosphatase activity ratio (measured by the ratio of free-space rates) for different ranges of local stiffening (colorbar), assuming a phosphatase with (A) negligible size or (B) radius of 2.1 nm, equal to the kinase. Black dashed line indicates a linear doseresponse, i.e., with Hill coefficient 1. (C,D) Hill coefficients for different ranges of local stiffening per phosphorylation event, assuming a phosphatase of (C) negligible size or (D) radius of 2.1 nm. Hill coefficients calculated from maximum log-log slope (black line) or log(81)/log(EC90/EC10) (gray line) of the dose response curves. Error bars for max log slope indicate root-mean-square error from a cubic polynomial fit to slope. Error bars for log(81)/log(EC90/EC10) indicate standard deviation of hill coefficients from bootstrap sampling from dose-response curve.

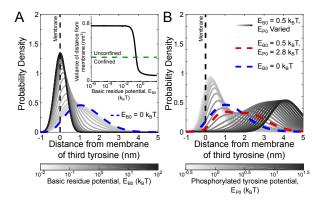


Fig. S7: Simplified membrane interaction model sets constraints on the strength of basic residue attraction and phosphorylation-driven repulsion from membrane. (A) Probability density of the distance from the membrane of the 3rd tyrosine of ζ , assuming no phosphorylated tyrosines, for varying strengths of the basic residue potential, $E_{\rm B0}$ (white: low; black: high). The tyrosine moves close to the membrane as $E_{\rm B0}$ is increased. Probability density when there is no basic residue potential $(E_{B0} = 0 \ k_B T)$ is shown as blue dotted line. (Inset) Variance of probability density of 3rd tyrosine over range of basic residue potential strengths. Green dashed line shows the characteristic $E_{\rm B0} = 0.5k_{\rm B}T$ required to confine the tyrosine to the membrane, defined in the text. (B) Probability density of the location of 3rd tyrosine assuming all tyrosines are phosphorylated, for $E_{\rm B0}=0.5~k_{\rm B}T$ (the value required to confine the tyrosine to the membrane assuming no tyrosines are phosphorylated), and varying phosphorylated tyrosine potential strength, $E_{\rm P0}$ (low white, high - black). Probability density when $E_{P0} =$ $2.8 k_{\rm B}T$ is shown as red dashed line, reflecting the $E_{\rm P0}$ value needed to approximately return to the distribution when $E_{\rm B0} = 0 \ k_{\rm B}T$ (blue dashed line).

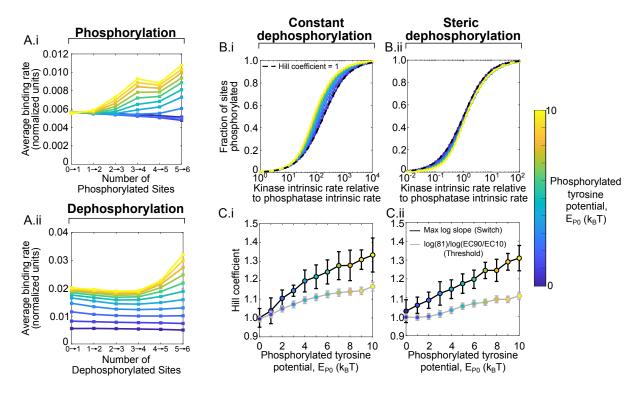


Fig. S8: Phosphorylation-driven modulation of membrane association of ζ leads to cooperativity and sequential binding. (A) Sequence-dependent average binding rates of (i) kinase and (ii) phosphatase binding to ζ at different (de)phosphorylation states for varying strengths of phosphorylated tyrosine potential (E_{P0}) (blue: weak; yellow: strong). Both kinase and phosphatase binding rates increase with each phosphorylation and also with increasing E_{P0} . (B) Fraction of sites phosphorylated over kinase intrinsic rate compared to phosphatase intrinsic rate for varying strengths of phosphorylated tyrosine potential (E_{P0}) , assuming a phosphatase with (i) negligible size (constant dephosphorylation) or (ii) 2.1 nm radius, equivalent to the kinase (steric dephosphorylation). Black dashed line indicates linear dose response, i.e., Hill coefficient 1. (C) Hill coefficients for varying strengths of phosphorylated tyrosine potential (E_{P0}) , assuming a phosphatase of (i) negligible size or (ii) radius of 2.1 nm, equal to the kinase. Hill coefficients calculated from maximum log-log slope (black line) or log(81)/log(EC90/EC10) (gray line) of the dose response curves. Error bars for max log slope indicate root-mean-square error from a cubic polynomial fit to slope. Error bars for log(81)/log(EC90/EC10) indicate standard deviation of hill coefficients from bootstrap sampling from dose-response curve. In both cases, the Hill coefficient increases with the strength of phosphorylated tyrosine potential, even when dephosphorylation is assumed to be sterically hindered. For (A)-(C), both kinase and phosphatase are assumed to have radius 2.1 nm. Rates are normalized to the free-space binding rate.

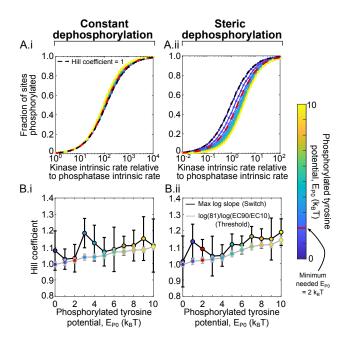
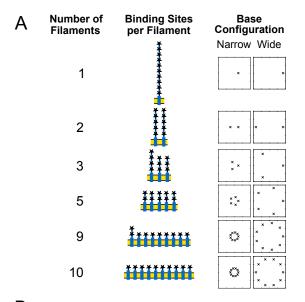


Fig. S9: Membrane affinity: Dose response curves for ϵ alternative Hill coefficient definitions. (A) Fraction of sites phosphorylated over kinase intrinsic rate compared to phosphatase intrinsic rate for varying strengths of phosphorylated tyrosine potential (E_{P0}) , assuming a phosphatase with (i) negligible size (constant dephosphorylation) or (ii) 2.1 nm radius, equivalent to the kinase (steric dephosphorylation). Black dashed line indicates linear dose response, i.e., Hill coefficient 1. (B) Hill coefficients for varying strengths of phosphorylated tyrosine potential (E_{P0}) , assuming a phosphatase of (i) negligible size or (ii) radius of 2.1 nm, equal to the kinase. Hill coefficients calculated from maximum log-log slope (black line) or log(81)/log(EC90/EC10) (gray line) of the dose response curves. Error bars for max log slope indicate root-mean-square error from a cubic polynomial fit to slope. Error bars for $\log(81)/\log(EC90/EC10)$ indicate standard deviation of hill coefficients from bootstrap sampling from dose-response curve. In both cases, the Hill coefficient increases with the strength of phosphorylated tyrosine potential, even when dephosphorylation is assumed to be sterically hindered (B). Rates are normalized to the free-space binding rate.



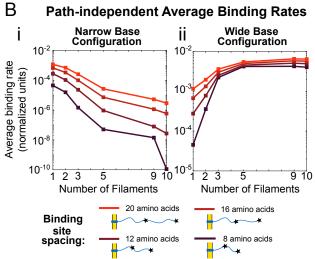


Fig. S10: Optimal distribution of ten binding sites on multiple chains is dependent on membrane spacing of subunits. (A) Schematic for distribution of 10 binding sites on multiple chains. For each, filaments are distributed evenly on a (1) narrow circle of radius 1.5 nm, and (2) wide circle of radius 5 nm. (B) Average binding rates of sixth binding event to constructed domain against number of filaments in domain (color bar; dark red: short spacing between binding sites; bright red: long spacing) and subunit configuration (Bi) 1.5nm radius, (Bii) 5nm radius. Simulations sweep over binding site spacing from 8 to 20 amino acids, indicated by color. Ligand radius is 2.7 nm.

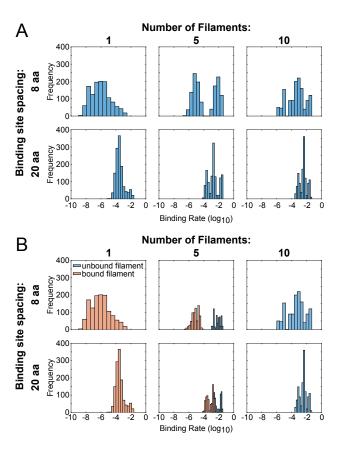


Fig. S11: Bimodality of binding rates can be explained by ligands bound to target filament. (A) Histograms of binding rates of sixth binding event to constructed domains in wide base configuration. (B) Histograms of binding rates from (A) colored by binding to filaments with no ligands bound (blue) and filaments with ligands bound (orange). Ligand radius is 2.7 nm.

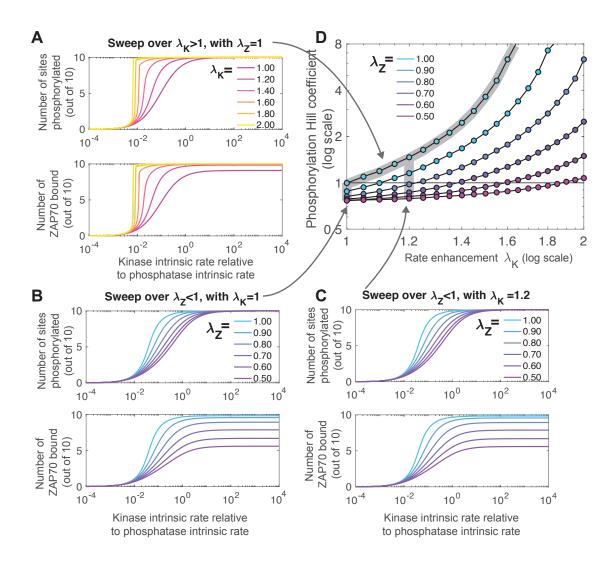


Fig. S12: Full results of integrative model shows counteracting effects of rate enhancement and rate reduction. (A) Rate enhancement of kinase phosphorylating TCR $\lambda_K > 1$ leads to more switch-like dose response of both amount of phosphorylation (top) and amount of ZAP70 bound (bottom). (B) Rate decrease of ZAP70 binding $\lambda_Z < 1$ leads to shallow dose-response for both amount of phosphorylation and amount of ZAP70 bound. In addition, for ZAP70-bound, the rate decrease also leads to a lower saturating value, i.e., $EC_{\rm max}$. (C) When both rate enhancement ($\lambda_K = 1.2$) and rate decrease ($\lambda_Z < 1$, different values explored) are present, the switch-like response is abrogated. (D) Ultrasensitivity quantified using the log-effective-concentration definition Eq. 2 for a range of $\lambda_K \geq 1$ and a range of $\lambda_Z \leq 1$.