Supplementary material describing the all-body model allmin

Johannes Walter, Marc Jacob, Katrin Stollenmaier, Patrick Lerge, and Syn Schmitt

Figure 1: (a) Frontal and side view of the visualization of the musculoskeletal model of the human body. The green lines show the muscle geometry. (c) Structure of the model: the motor command $U(t) \in$ $\mathbb{R}^{n_{\text{MTU}}}$ is fed into the model of activation dynamics [\(Hatze,](#page-8-0) [1977;](#page-8-0) [Rockenfeller and Günther,](#page-9-0) [2018\)](#page-9-0) of muscles which relates the neuronal stimulation to muscular activity $A(t) \in \mathbb{R}^{n_{\text{MTU}}}$ that drives the muscle model [\(Haeufle et al.,](#page-8-1) [2014\)](#page-8-1). The muscles produce forces $F^{\text{MTU}}(t) \in \mathbb{R}^{n_{\text{MTU}}}$ that act on the rigid bodies of the skeletal system. The resultant joint torques \mathcal{F}^{MTU} depend on the respective moment arms $\frac{\partial L^{MTU}}{\partial \Omega}$. In combination with external forces, this results in a movement of the [DoFs](#page-8-2) $\mathcal{Q}(t) \in \mathbb{R}^{n_{\text{DoF}}}$ of the body.

The musculoskeletal model *allmin* consists of $n_{RGB} = 15$ rigid bodies (see [Table 1\)](#page-3-0). The rigid bodies are connected via 14 joints (see [Table 2\)](#page-4-0) including $n_{DoF} = 20$ degrees of freedom. Each Degree of Freedom [\(DoF\)](#page-8-2) (except for the wrist) is controlled by an Agonistic-Antagonistic Setup [\(AAS\)](#page-8-3) beeing congruent with the Elementary Biological Drive [\(EBD\)](#page-8-4) as described by [Schmitt et al.](#page-9-1) [\(2019\)](#page-9-1). The musculoskeletal model is actuated by $n_{\text{MTU}} = 36$ Muscle Tendon Units [\(MTU\)](#page-8-5) (see [Table 4](#page-6-0) and [Figure 1a](#page-0-0) for first impression).

The model is implemented in $C/C++$ code within our in-house multi-body simulation code *demoa*.

1 The Multibody System

The skeletal system is modeled as a chain of rigid bodies, connected by rotational joints and described by differential equations. The resulting [DoFs](#page-8-2) $\mathcal{Q}(t) = [q_1(t), \ldots, q_{n_{\text{DoF}}}(t)]^T \in \mathbb{R}^{n_{\text{DoF}}}$ of these rotational joints describe the movement of the rigid bodies over time and are referred to as generalized coordinates. For the equations of motion, a Lagrangian formulation with the generalized coordinates $\mathcal{Q}(t)$ as state variables is realized, which can be set up algorithmically, e.g. as described by [Legnani et al.](#page-9-2) [\(1996\)](#page-9-2). The evaluation of this algorithm leads to the differential equation of motion of the rigid body system in the form

$$
\mathbf{M}(\mathbf{Q})\ddot{\mathbf{Q}} + C(\mathbf{Q}, \dot{\mathbf{Q}}) = \mathcal{F},\tag{1}
$$

where $\mathbf{M} \in \mathbb{R}^{n_{\text{DoF}} \times n_{\text{DoF}}}$ is the mass matrix, $C \in \mathbb{R}^{n_{\text{DoF}}}$ is a vector of gravitational, centrifugal and Coriolis forces and $\mathcal{F} \in \mathbb{R}^{n_{\text{DoF}}}$ is a vector of forces (internal and external) acting on the mechanical part of the system. Hereby $\mathcal F$ includes forces, e.g. due to contact of the body to the environment (external), as well as forces of the biological structures, such as muscles, joint limitations (internal).

2 Joint limitations

The joint limitations are modeled as linear one-sided spring-damper elements, acting directly on the respective [DoF:](#page-8-2)

$$
f_i^{\text{lmt}} = \begin{cases} k_l(q_i - q_{l,i}) + d_l \dot{q}_i, & q_i < q_{l,i} \\ 0, & q_{l,i} \le q_i \le q_{u,i} \\ k_u(q_i - q_{u,i}) + d_u \dot{q}_i, & q_i > q_{u,i} \end{cases}
$$
 (2)

with the lower and upper threshold angles $q_{l/u}$, corresponding to the respective Range of Motion [\(RoM\)](#page-8-6) [\(Table 2\)](#page-4-0), and linear spring and damping parameters $k_{l/u} = 100 \left[\frac{\text{Nm}}{\text{rad}}\right]$ and $d_{l/u} = 0.001 \left[\frac{\text{Nm}\cdot\text{s}}{\text{rad}}\right]$. For the joints of the lumbar and cervical spine, as well as the wrist, the same force law is used to model passive properties with different parameters. The upper and lower threshold angles are set to $q_{l/u} = 0$ and the spring and damping parameters are set to $k_{cs} = 10 \frac{\text{Nm}}{\text{rad}}$, $d_{cs} = 0.2 \frac{\text{Nm}\cdot \text{s}}{\text{rad}}$, $k_{ls} = 20 \frac{\text{Nm}}{\text{rad}}$, $d_{ls} = 0.2 \frac{\text{Nm}\cdot \text{s}}{\text{rad}}$, $k_{wr} = 15 \frac{\text{Nm}}{\text{rad}}$, $d_{wr} = 1 \left[\frac{\text{Nm} \cdot \text{s}}{\text{rad}} \right].$

3 Muscles

The muscles are modeled as lumped muscles, i.e. they represent a multitude of anatomical muscles and motor units. A list of all included muscle elements can be found in [Table 4.](#page-6-0)

The [MTU](#page-8-5) structure is modeled using an extended Hill-type muscle model as described in [Haeufle et al.](#page-8-1) [\(2014\)](#page-8-1) with muscle activation dynamics as introduced by [Hatze](#page-8-0) [\(1977\)](#page-8-0) and simplified by [Rockenfeller and Günther](#page-9-0) (2018) . Herein, the muscles are activated using a 1st order differential equation of normalized calcium ion concentration [\(Rockenfeller et al.,](#page-9-3) [2014\)](#page-9-3)

$$
\dot{\gamma}(t) = M_{\rm H}(u(t) - \gamma(t))\tag{3}
$$

and a nonlinear mapping onto the muscles activation

$$
a(t) = \frac{a_0 + \varpi}{1 + \varpi},\tag{4}
$$

with $\varpi(\gamma(t), l^{\text{CE}}(t)) = (\gamma(t) \cdot \rho(l^{\text{CE}}))^{\nu}$ and $\rho(l^{\text{CE}}) = \varpi_{\text{opt}} \cdot \frac{l^{\text{CE}}}{l_{\text{opt}}}$ $\frac{l^{\rm CE}}{l_{\rm opt}} = \gamma_{\rm c} \cdot \rho_0 \cdot \frac{l^{\rm CE}}{l_{\rm opt}}$ $\frac{l^{CD}}{l_{opt}}$. The parameter values are chosen muscle non specifically and are given in [Table 5.](#page-7-0)

The muscle model is a macroscopic model consisting of four elements: the Contractile Element [\(CE\)](#page-8-7), the Parallel Elastic Element [\(PEE\)](#page-8-8), the Serial Elastic Element [\(SEE\)](#page-8-9) and Serial Damping Element [\(SDE\)](#page-8-10), as illustrated in [Figure 1b.](#page-0-0) Herein, the muscle fibers and their contraction dynamics are described by a contractile element [\(CE\)](#page-8-7) representing the cross-bridge-cycle of the myosin heads and a parallel elastic element [\(PEE\)](#page-8-8) representing the passive connective tissue in the muscle belly. The viscoelastic properties of tendons are approximated using a series elastic element [\(SEE\)](#page-8-9) and a serial damping element [\(SDE\)](#page-8-10).

The inputs to the muscle model are the length of the [MTU](#page-8-5) l^{MTU} , the contraction velocity of the MTU l^{intu} and the muscular activity a. The output of the muscle model is a one-dimensional muscle force f^{MTU} . This force drives the movement of the skeletal system.

For the routing of the muscle path around the joints, deflection ellipses are implemented as described by [Hammer et al.](#page-8-11) [\(2019\)](#page-8-11). The muscle path can move within these ellipses and is deflected as soon as it touches the boundary. For the investigations presented here, we set the length of both half-axes of all ellipses to zero, resulting in fixed via points. The position of these points can be found in [Table 3.](#page-5-0) The resulting moment arms translate the muscle force F^{MTU} to generalized forces \mathcal{F}^{MTU} acting on the [DoFs](#page-8-2) of the system

$$
\mathcal{F}^{\text{MTU}} = \frac{\partial L^{\text{MTU}}}{\partial \mathcal{Q}} \cdot F^{\text{MTU}}.
$$
\n(5)

All in all, the governing model dependencies for all muscles $i = 1, ..., n$ are:

$$
\dot{l}_i^{\text{CE}} = f^{\text{CE}}(l_i^{\text{CE}}, l_i^{\text{MTU}}, \dot{l}_i^{\text{MTU}}, a_i) \tag{6}
$$

$$
\dot{a}_i = f^a(a_i, u_i, l_i^{\text{CE}})
$$
\n
$$
(7)
$$

$$
f_i^{\text{MTU}} = f_i^{\text{MTU}}(l_i^{\text{MTU}}, l_i^{\text{MTU}}, l_i^{\text{CE}}, a_i) \tag{8}
$$

$$
\ddot{\mathcal{Q}} = f^{\mathcal{Q}}(\dot{\mathcal{Q}}, \mathcal{Q}, F^{\mathrm{MTU}}, \mathcal{F}^{\mathrm{lmt}}, \mathcal{F}^{\mathrm{ext}}), \tag{9}
$$

where $\mathcal{Q} = \{q_i\}_{i=1}^{n_{\text{DoF}}}$ denotes a generalized state vector that contains all joint angles and $F^{\text{MTU}} = \{f_i^{\text{MTU}}\}_{i=1}^n$ $\mathcal{F}^{\text{lmt},i} = \left\{f_i^{\text{lmt}}\right\}_{i=1}^n$ and $\mathcal{F}^{\text{ext}} = \left\{f_i^{\text{ext}}\right\}_{i=1}^n$ contain the muscle forces, the joint limitation forces and the external forces, respectively.

4 Model parameters

Table 1: List of all bodies included in the model with their mechanical properties with m: mass, r_x, r_y : radius in x and y direction, h_z : height in z direction, \mathbf{d}_1 : distance proximal joint to the body's center of mass and \mathbf{d}_2 : distance center of mass to distal joint. The spine body has an underlying curvature based on [Kitazaki](#page-9-4) and Griffin [\(1997\)](#page-9-4). The allover body dimensons are based on data describing ^a 50th percentile male from [NASA](#page-9-5) ([1978\)](#page-9-5).

Name	Type	Movement	RoM [$^{\circ}$]
Lumbar spine	Universal	$left/$ right	$[-3030]$
Lumbar spine	Universal	flexion/extension	$[0 \ldots 30]$
Cervival spine	Universal	$left/$ right	$[-3030]$
Cervival spine	Universal	flexion/extension	$[-3030]$
Shoulder (Right)	Universal	abduction/adduction	$[-10 \ldots 60]$
Shoulder (Right)	Universal	flexion/extension	$[-10010]$
Ellbow (Right)	Revolute	flexion/extension	$[-12010]$
Wrist (Right)	Revolute	flexion/extension	$[0 \ldots 0]$
Shoulder (Left)	Universal	abduction/adduction	$[-10 \ldots 60]$
Shoulder (Left)	Universal	flexion/extension	$[-10010]$
Ellbow (Left)	Revolute	flexion/extension	$[-12010]$
Wrist (Left)	Revolute	flexion/extension	$[0 \ldots 0]$
Hip (Right)	Universal	flexion/extension	$[-120\cdots -10]$
Hip (Right)	Universal	abduction/adduction	$[-10 \ldots 70]$
Knee (Right)	Revolute	flexion/extension	$[-1 \dots 120]$
Ankle (Right)	Revolute	flexion/extension	$[-20 \ldots 40]$
Hip (Left)	Universal	flexion/extension	$[-12010]$
Hip (Left)	Universal	abduction/adduction	$[-10 \ldots 70]$
Knee (Left)	Revolute	flexion/extension	$[-1 \dots 120]$
Ankle (Left)	Revolute	flexion/extension	$[-20 \dots 40]$

Table 2: List of all joints included in the model.

Table 3: Muscle routing parameters: Origin R_O , Deflection Point 1 R_{DF1} and 2 R_{DF2} and Insertion R_I relative to their parent body. All numbers in this table are rounded to four decimal digits. Muscle names: [EF,](#page-8-32) [EE,](#page-8-33) [FF,](#page-8-27) [FE,](#page-8-26) [HAbd,](#page-8-22) [HAdd,](#page-8-23) [HF,](#page-8-21) [HE,](#page-8-20) [CSF,](#page-8-17) [CSSBL,](#page-8-18) [CSSBR,](#page-8-19) [CSE,](#page-8-16) [KF,](#page-8-24) [KE,](#page-8-25) [LSF,](#page-8-13) [LSSBL,](#page-8-14) [LSSBR,](#page-8-15) [LSE,](#page-8-12) [SAbd,](#page-8-30) [SAdd,](#page-8-31) [SF,](#page-8-29) [SE.](#page-8-28)

	F ^{max} [N]	ICE, opt m	$\Delta W^{\rm asc}$	ISEE,0 m
ΕF	1420.0	0.1885	1.0	0.1845
EF.	1550.0	0.171	0.525	0.18
FF	3000.0	0.15	1.0	0.133
FE	3000.0	0.13	1.0	0.115
HAbd	2000.0	0.18	1.0	0.121
HAdd	2000.0	0.204	0.75	0.136
HF	5000.0	0.195	1.0	0.135
HE	5000.0	0.192	1.0	0.191
\rm{CSF}	5000.0	0.07	1.5	0.01
CSSBL	5000.0	0.05	1.5	0.01
CSSBR	5000.0	0.046	1.5	0.01
CSE	5000.0	0.062	$1.5\,$	0.01
ΚF	6000.0	0.258	0.525	0.112
KE	6000.0	0.264	1.0	0.28
LSF	15000.0	0.2	1.5	0.11
LSSBL	15000.0	0.09	1.5	0.02
LSSBR	15000.0	0.09	1.5	0.02
$_{\rm LSE}$	15000.0	0.075	1.5	0.04
SAbd	6000.0	0.12	1.0	0.08
SAdd	6000.0	0.225	1.0	0.12
SF	10000.0	0.1	1.0	0.073
SЕ	6000.0	0.165	1.0	0.105

Table 4: Muscle-specific actuation parameters, with F^{max} : maximum isometric force, $l^{\text{CE,opt}}$ $l^{\text{CE,opt}}$ $l^{\text{CE,opt}}$: optimal length of the CE, ΔW^{asc} : width of normalized bell curve in ascending branch of the force-length relationship, $l^{SEE,0}$ $l^{SEE,0}$ $l^{SEE,0}$ rest length of the SEE, $l^{CE,init}$: initial length of the [CE.](#page-8-34) Muscle names: Elbow Flexion [\(EF\)](#page-8-32), Elbow Extension ([EE\)](#page-8-33), Foot Flexion [\(FF\)](#page-8-27), Foot Extension [\(FE\)](#page-8-26), Hip Abduction ([HAbd\)](#page-8-22), Hip Adduction [\(HAdd\)](#page-8-23), Hip Flexion ([HF\)](#page-8-21), Hip Extension [\(HE\)](#page-8-20), Cervical Spine Flexion [\(CSF\)](#page-8-17), Cervical Spine Side Bend Left [\(CSSBL\)](#page-8-18), Cervical Spine Side Bend Right ([CSSBR\)](#page-8-19), Cervical Spine Extension [\(CSE\)](#page-8-16), Knee Flexion [\(KF\)](#page-8-24), Knee Extension [\(KE\)](#page-8-25), Lumbar Spine Flexion ([LSF\)](#page-8-13), Lumbar Spine Side Bend Left ([LSSBL\)](#page-8-14), Lumbar Spine Side Bend Right [\(LSSBR\)](#page-8-15), Lumbar Spine Extension [\(LSE\)](#page-8-12), Shoulder Abduction [\(SAbd\)](#page-8-30), Shoulder Adduction [\(SAdd\)](#page-8-31), Shoulder Flexion ([SF\)](#page-8-29),Shoulder Extension ([SE\)](#page-8-28).

Table 5: Muscle non-specific actuation parameters for the muscles and the activation dynamics.

List of Abbreviations

HF Hip Flexion

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