

Supplement for:

Isotopic evidence for the formation of the Moon
in a canonical giant impact

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Supplementary Note 1: Correction for GCR production of ^{50}V in lunar rocks and chondrites

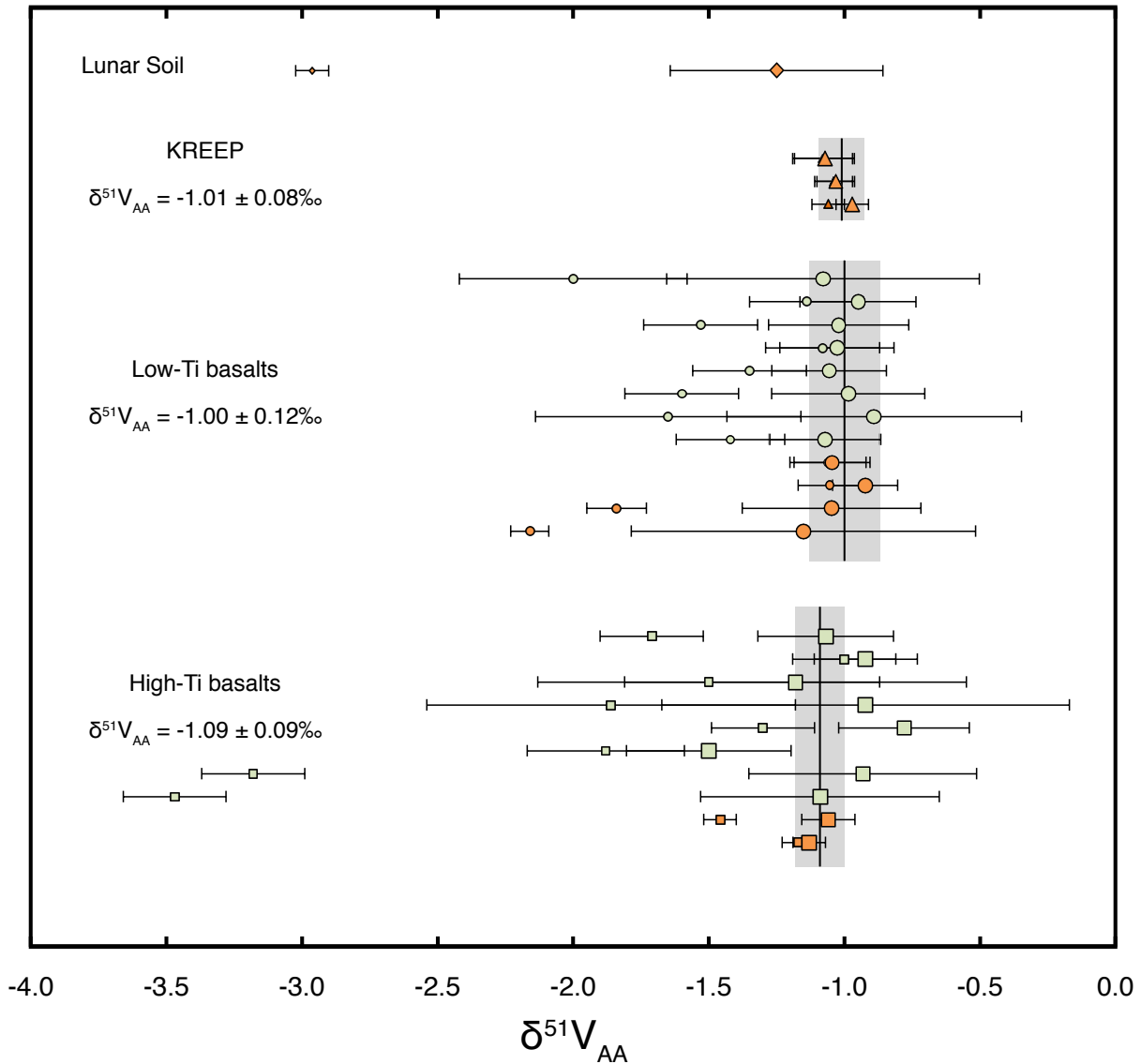
The V isotope compositions of many lunar rocks are strongly perturbed by galactic cosmic ray (GCR) effects (Fig. 1) that lead to production of ^{50}V most likely through interaction with target nuclei of Fe¹. It is also possible to produce ^{50}V enrichments via GCR interactions with isotopes of Ti and Cr, but these have been shown to be very limited, first because Cr cross sections are not very favorable for ^{50}V production and secondly because V isotope anomalies in lunar rocks produce poor correlations with Ti/V ratios¹. Furthermore, V isotope analyses of chondrites reveal significant scatter if corrected using Ti/V ratios abundances, whereas corrections using Fe/V ratios produce entirely invariant V isotope ratios in chondrites².

Here we combine all the available lunar V isotope data with their respective cosmic ray exposure (CRE) ages (available in the literature) and Fe/V ratios to produce an empirical calibration line that allows for correction of GCR effects (Fig. 1). The best-fit line through all the data is a York-regression³ that takes into account all the errors on the CRE ages, Fe/V ratios, and V isotope compositions. The slope of the line is $-2.132 \times 10^{-6} \pm 0.188 \times 10^{-6}$ (2SE) and the intercept with the y-axis (e.g., the calculated irradiation-free V isotope composition of the Moon) is $\delta^{51}\text{V}_{\text{Moon}} = -1.037 \pm 0.031\text{‰}$ (2SE). The best-fit curve also includes one lunar soil sample (10084), which, despite a large error on the CRE age, plots on the curve. Although we here include the lunar soil sample in our regression, it is important to note that lunar soil samples in many cases are not expected to conform to the GCR curve (Fig. 1) because they can be contaminated by chondritic debris from relatively recent impacts. Furthermore, lunar soils are often heterogeneous, which can render different sub-samples with significantly different CRE ages. Hence, lunar soils are generally not ideal samples to construct V isotope GCR corrections from. Here, we do include the one lunar soil sample in our regression because it plots together with 25 other lunar samples. In addition, our regression weights according to sample error bars and, therefore, the lunar soil has a negligible effect on the calculated slope due to the large CRE age uncertainty.

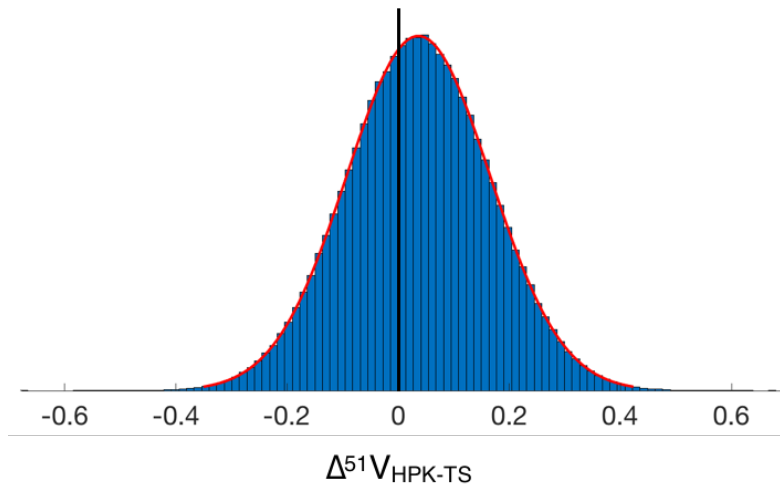
In order to test whether this value is biased by samples with large GCR corrections, we can correct individual samples for irradiation by using the best fit correlation line in Fig. 1. In this approach we only include samples with GCR corrections $< 0.3\text{‰}$ (Samples 12004, 12063, 14053, 14321, 15535, 68815, 68115, 74255, 74275, and LAP02205), as smaller GCR corrections are associated with smaller systematic errors. These samples yield an error-weighted average value of $\delta^{51}\text{V}_{\text{Moon}} = -1.033 \pm 0.031\text{‰}$ ($n = 10$, 2SE), demonstrating that our average GCR-corrected value for all lunar rocks is not biased by samples with large irradiation corrections. Hence, the slope of the GCR correction curve does not have a large impact on the overall value of $\delta^{51}\text{V}_{\text{Moon}}$. Here, we choose to use the irradiation free intercept in Fig. 1 as the best estimate for the V isotope composition of the Moon ($\delta^{51}\text{V}_{\text{Moon}} = -1.037 \pm 0.031$; $n = 26$, 2SE). In section 2 we also discuss two alternative statistical means to calculate the average composition of the Moon in order to emphasize the robustness of the value employed here.

Supplementary table 1 and Supplementary figure 1 show the GCR corrected data and the average V isotope compositions for all lunar rocks measured to date. Samples with larger uncertainties either have large errors for their CRE ages, larger V isotope measurement errors, or both (Supplementary table 1). To investigate the consistency between our V isotope data sets for lunar rocks and that from¹, we calculate the average $\delta^{51}\text{V}_{\text{Moon}}$ for samples from each of the two studies. In both cases we calculate weighted means of the two data populations whereby samples are assigned a weight of one divided by the total propagated error squared. The two error-weighted average values are remarkably similar at $\delta^{51}\text{V} = -1.012 \pm 0.067$ ($n = 16$, 2SE) and $\delta^{51}\text{V} = -1.041 \pm$

74 0.030‰ (n = 10, 2SE), which implies excellent agreement between both studies. This conclusion
 75 is further supported by Monte Carlo simulations, whereby raw data (actual values and their
 76 associated uncertainties) are used to artificially generate 1 million datasets for each study. At each
 77 iteration step, the difference of mean $\delta^{51}\text{V}$ between the two studies is computed as $\Delta^{51}\text{V}_{\text{HPK-TS}} =$
 78 $\delta^{51}\text{V}_{\text{HPK}} - \delta^{51}\text{V}_{\text{TS}}$, where "HPK" and "TS" refer to Hopkins et al.^(ref 1) and this study, respectively.
 79 The outcomes of this simulation are reported in Supplementary figure 2, supporting the excellent
 80 agreement between the two datasets, with a mean $\Delta^{51}\text{V}_{\text{HPK-TS}}$ value very close to zero (i.e., no
 81 statistical difference).
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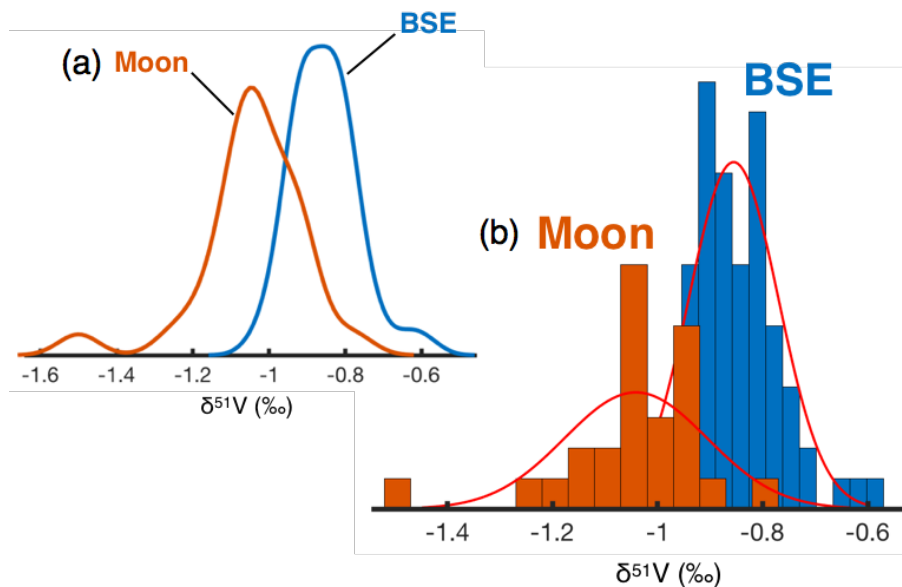
83 **Supplementary figure 1:** Plot of uncorrected (small symbols) and irradiation corrected (large
 84 symbols) lunar vanadium isotope data. Data are grouped into Lunar soils (diamonds), KREEP
 85 (triangles), Low-Ti basalts (circles), and High-Ti basalts (squares). Green samples are literature
 86 data¹, orange data are from this study. Grey bars denote weighted averages and 2SE uncertainties
 87 of each sample group. Data are listed in Supplementary Table 1.
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92 **Supplementary figure 2:** Difference in the mean $\delta^{51}\text{V}$ of the Moon computed from datasets of
93 ref. 1 and this study ($\Delta^{51}\text{V}_{\text{HPK-TS}}$), as derived from 1 million runs of Monte Carlo simulation.
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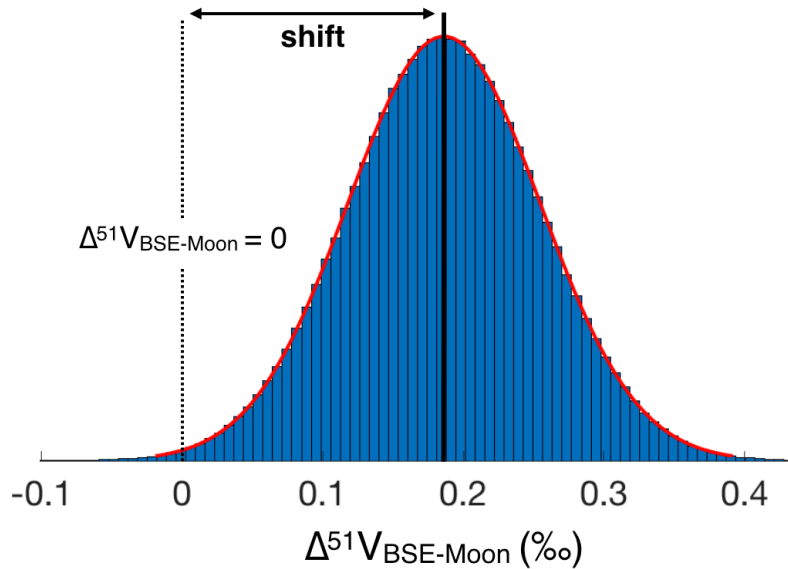
95 **Supplementary Note 2: The vanadium isotopic difference between the BSE**
96 **and the Moon**
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98 The difference between the mean $\delta^{51}\text{V}$ value of the Moon and BSE is small, being $\sim 0.2\%$, but
99 resolvable at our present level of precision. To demonstrate and quantify this difference, we present a
100 series of statistical considerations. Supplementary figure 3 shows the densities we obtained through
101 Kernel density estimation, as well as the histograms and corresponding Gaussian fits for the Moon and
102 BSE vanadium isotope data. It is notable that the density of Moon $\delta^{51}\text{V}$ statistics is shifted towards the
103 left-hand side with respect to the density of Earth statistics. This suggests that Moon and Earth $\delta^{51}\text{V}$
104 statistics do not have the same means and that the mean for the Moon is lower.



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106 **Supplementary figure 3:** Comparison between the V isotopic datasets for the Moon and BSE,
107 with (a) Kernel estimate densities and (b) frequency distributions showed as histograms with their
108 associated Gaussian best fits.

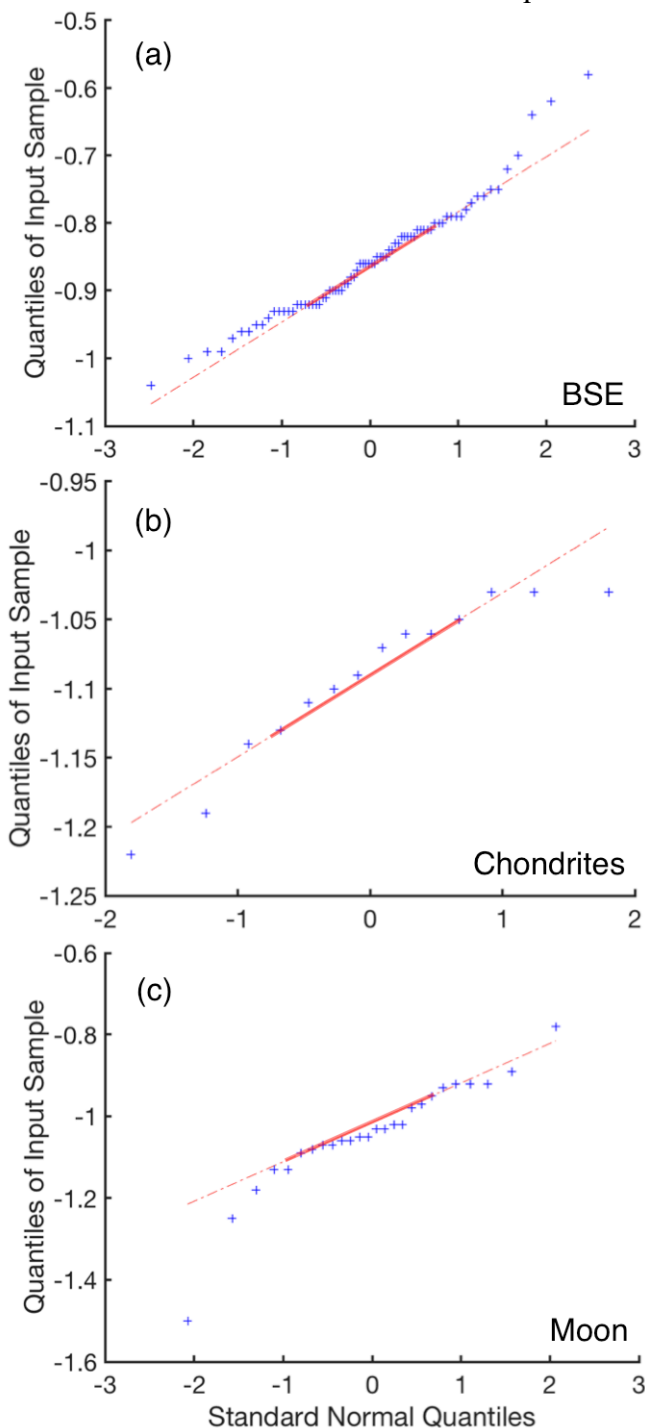
109 Here, we carried out Monte Carlo simulations using the raw data for the BSE and Moon
 110 data sets and their associated individual uncertainties to artificially generate 1 million datasets, and
 111 hence compute 1 million $\delta^{51}\text{V}$ mean values for the Moon and BSE. At each iteration step, the
 112 difference between the mean $\delta^{51}\text{V}$ of the BSE and the Moon was computed as $\Delta^{51}\text{V}_{\text{BSE-Moon}} =$
 113 $\delta^{51}\text{V}_{\text{BSE}} - \delta^{51}\text{V}_{\text{Moon}}$. The distribution of $\Delta^{51}\text{V}_{\text{BSE-Moon}}$ values is shown in Supplementary figure 4,
 114 demonstrating that the probability for the silicate Earth to have a higher mean $\delta^{51}\text{V}$ than the Moon
 115 (i.e., $\Delta^{51}\text{V}_{\text{BSE-Moon}} > 0$) is extremely high (99.67%). These simulations imply that a shift of 0.186
 116 ± 0.068 (1SD) exists between the V isotope compositions of the Moon and BSE (Supplementary
 117 figure 7). The corresponding mean $\delta^{51}\text{V}$ of the BSE, Chondrites and Moon are $\delta^{51}\text{V}_{\text{BSE}} = -0.855 \pm$
 118 0.012 (1SD), $\delta^{51}\text{V}_{\text{ch.}} = -1.094 \pm 0.038$ (1SD), and $\delta^{51}\text{V}_{\text{Moon}} = -1.041 \pm 0.067$ (1SD), respectively.
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 121 **Supplementary figure 4:** Frequency distribution of the V isotope difference between the BSE and
 122 the Moon ($\Delta^{51}\text{V}_{\text{BSE-Moon}}$) as generated by Monte Carlo simulations where the raw data and their
 123 associated uncertainties are used to artificially generate 1 million mean $\delta^{51}\text{V}_{\text{BSE}}$ and $\delta^{51}\text{V}_{\text{Moon}}$
 124 values.
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126 When calculating the mean values and error weighted 2SE for each of BSE, chondrites,
 127 and the Moon, it is necessary to make the assumption that all three populations are normally
 128 distributed. One first-order observation that supports this inference is that all individual samples
 129 in the chondrite² and Moon datasets (once corrected for GCR effects) exhibit V isotope
 130 compositions that are all within error of each other. The same is true for 92% of the samples
 131 representing BSE, which is expected within the 95% confidence interval for any given data
 132 population. However, we can further perform a series of tests to investigate whether or not the
 133 corresponding datasets are normally distributed and, hence, allow us to demonstrate the statistical
 134 validity of the calculated averages and associated errors for each data population. In this approach,
 135 the main limiting factor corresponds to the small amount of available data for each end-member.
 136 However, note that the frequency distributions of $\delta^{51}\text{V}_{\text{BSE}}$ and $\delta^{51}\text{V}_{\text{Moon}}$ broadly follow Gaussian
 137 distributions (Supplementary figure 3). Furthermore, quantile-quantile (Q-Q) plots of our datasets
 138 are broadly consistent with Gaussian distributions for all three end-members (Supplementary
 139 figure 5). These plots correspond to a graphical method for comparing two probability distributions
 140 - here the quantiles of the sample datasets versus theoretical quantile values generated from normal

141 distributions - by plotting their quantiles against each other. However, these graphical
142 considerations do not allow quantitatively validating/refuting the hypothesis of our datasets being
143 normally distributed, and further statistical tests are therefore required.



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146 **Supplementary figure 5:** Q-Q plots comparing the probability distributions of the BSE,
147 Chondrites and Moon V isotope raw data (Supplementary Table 1 and ref ²) with normal
148 distributions.
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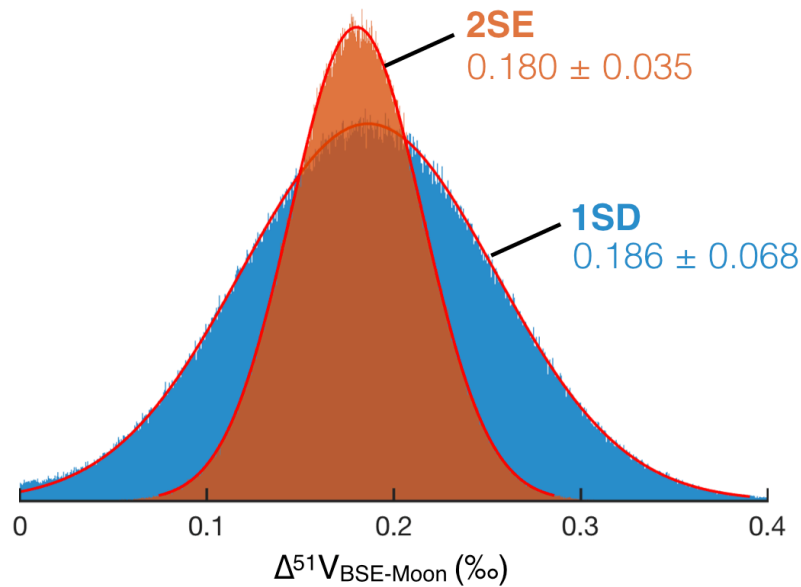
150 First, we postulate the null hypothesis that our three sets of data come from normal
151 distributions with mean compositions of $\delta^{51}\text{V}_{\text{BSE}} = -0.86$, $\delta^{51}\text{V}_{\text{ch.}} = -1.09$, $\delta^{51}\text{V}_{\text{Moon}} = -1.04$, and
152 unknown variances. Student's t-tests carried out for each dataset do not reject the null hypothesis
153 at the 5% significance level ($\alpha = 0.05$). In order to compensate for the small size of our datasets
154 and further investigate the reliability of these results, we used Monte Carlo simulations to
155 artificially generate 1 million datasets for the BSE, chondrites and Moon from the raw data and
156 associated uncertainties. We found that Student's t-test rates of success (i.e., no rejection of the
157 null hypothesis at the 5% significance level) of 98.50%, 96.75% and 96.97% for the BSE,
158 chondrites and Moon, respectively, indicating that Student's t-tests consistently fail to reject the
159 null hypothesis.

160 We further tested the null hypothesis by carrying Lilliefors tests, which correspond to a
161 test for goodness of fit to a normal distribution based on the Kolmogorov–Smirnov test. Unlike
162 Student's t-tests, Lilliefors tests return p-values, which represent the probability of observing a test
163 statistic as extreme as, or more extreme than, the observed value under the null hypothesis. In other
164 words, small values of p cast doubt on the validity of the null hypothesis. If the p-value is less than
165 or equal to α (i.e., $p \leq 0.05$), then the Lilliefors test rejects the null hypothesis. If the p-value is
166 greater than α (i.e., $p > 0.05$), then the Lilliefors test fails to reject the null hypothesis. Here, we
167 again used Monte Carlo simulations to artificially generate 1 million datasets for the BSE,
168 chondrites and Moon from the raw data and associated uncertainties. We found that Lilliefors tests
169 give mean p-values of 0.106, 0.209 and 0.131, with rates of success (i.e., no rejection of the null
170 hypothesis) of 52.33%, 82.01% and 60.44% for the BSE, chondrites and Moon, respectively.
171 Although these results cannot demonstrate that our datasets are normally distributed, they support
172 the absence of significant evidence for them not to be normally distributed. In the absence of
173 statistical arguments to reject the null hypothesis, and in light of all graphical and numerical
174 considerations presented in this section, it appears justified to define the BSE, Moon and chondrite
175 end-members by their "real" values (i.e., using error-weighted mean and 95% c.i.).

176 Error-weighted $\delta^{51}\text{V}$ means are computed using IsoplotR. These give $\delta^{51}\text{V}_{\text{BSE}} = -0.861 \pm$
177 0.005 ($n = 76$, 2SE, MSWD=10.165), $\delta^{51}\text{V}_{\text{ch.}} = -1.089 \pm 0.029$ ($n = 14$, 2SE, MSWD=0.690), and
178 $\delta^{51}\text{V}_{\text{Moon}} = -1.036 \pm 0.028$ ($n = 26$, 2SE, MSWD=1.539). MSWD values close to 1 for Chondrites
179 and the Moon indicate that error-weighted means and their associated errors are representative of
180 the raw data dispersion. In addition, this $\delta^{51}\text{V}_{\text{Moon}}$ value is in excellent agreement with the
181 irradiation-free composition of the Moon as derived from the y-intercept of the best fit line to lunar
182 V isotope data plotted against their respective CRE ages ($\delta^{51}\text{V} = -1.037 \pm 0.031\%$; $n = 26$, 2SE,
183 Supplementary figure 1). However, the high MSWD value for the BSE ($\gg 1$) indicates that
184 $\delta^{51}\text{V}_{\text{BSE}}$ values are overdispersed with respect to the stated analytical uncertainties, implying that
185 the error-weighted mean and 2SE cannot be used most likely due to individual uncertainties being
186 underestimated. This inference is also supported by the fact that some studies have reported
187 individual sample uncertainties far lower than the long-term external reproducibility of the V
188 isotope measurement technique^{4,5}. We therefore compute the unweighted mean of the $\delta^{51}\text{V}_{\text{BSE}}$,
189 which gives $\delta^{51}\text{V}_{\text{BSE}} = -0.856 \pm 0.020$ (2SE, $n=76$). Computing the mean and 2SE of the $\delta^{51}\text{V}_{\text{BSE}}$
190 from the mean $\delta^{51}\text{V}$ and 2SE of peridotites, MORBs, komatiites and OIBs produces a MSWD of
191 0.77, which is suggestive of uncertainties being representative of the overall data dispersion. The
192 mean and 2SE of the $\delta^{51}\text{V}_{\text{BSE}}$ ($n=76$) is, hence, used for mixing calculations (see section 3).

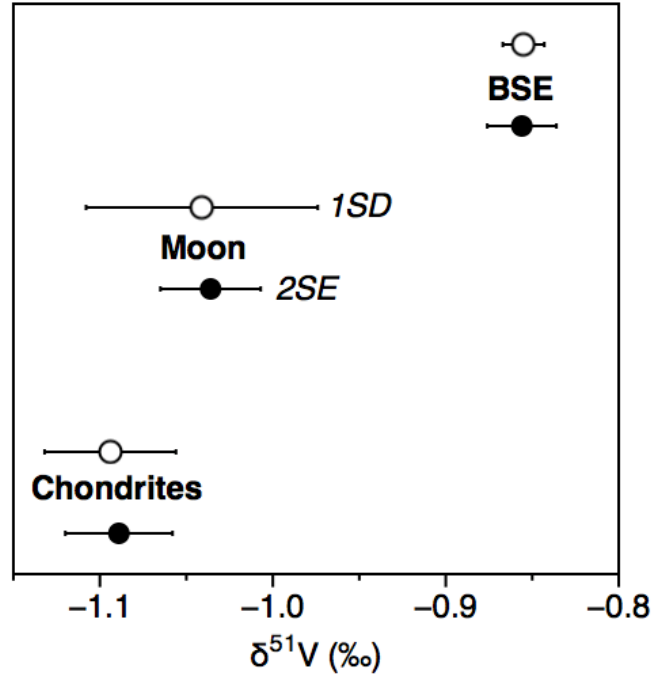
193 We ran Monte Carlo simulations (1 million runs) to investigate the range of possible $\Delta^{51}\text{V}_{\text{BSE-}}$
194 Moon using $\delta^{51}\text{V}_{\text{BSE}} = -0.856 \pm 0.020$ and $\delta^{51}\text{V}_{\text{Moon}} = -1.037 \pm 0.031$. These give mean $\Delta^{51}\text{V}_{\text{BSE-Moon}}$
195 of 0.180 ± 0.035 (2SE; Supplementary figure 6), in good agreement with our estimate from Monte

196 Carlo simulations using raw data to artificially generate $\delta^{51}\text{V}$ datasets for the Earth and Moon
 197 (0.186 ± 0.068 , 1SD; Supplementary figure 4).
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 201 **Supplementary figure 6:** Frequency distribution of the V isotope difference between the BSE
 202 and the Moon ($\Delta^{51}\text{V}_{\text{BSE-Moon}}$) as generated by Monte Carlo simulations. In the first case (blue plot),
 203 the raw data and their associated uncertainties are used to artificially generate 1 million mean
 204 $\delta^{51}\text{V}_{\text{BSE}}$ and $\delta^{51}\text{V}_{\text{Moon}}$ values and compute $\Delta^{51}\text{V}_{\text{BSE-Moon}}$ (cf. Supplementary figure 4). In the second
 205 case (orange plot), our estimated "real values" for the $\delta^{51}\text{V}$ of the Moon and BSE and associated
 206 2SE are used as input parameters for Monte Carlo simulations.

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 209 **In conclusion,** we have adopted two complementary approaches to compute the V isotope
 210 difference between the Moon and BSE. The first one (**A1**) relies on Monte Carlo simulations using
 211 the raw data and their associated uncertainties to artificially generate 1 million datasets and
 212 compute mean V isotope compositions for the Moon, BSE and chondrites. This approach yields
 213 $\Delta^{51}\text{V}_{\text{BSE-Moon}} = 0.186 \pm 0.068$ (1SD), $\delta^{51}\text{V}_{\text{BSE}} = -0.855 \pm 0.012$ (1SD), $\delta^{51}\text{V}_{\text{ch.}} = -1.094 \pm 0.038$
 214 (1SD), and $\delta^{51}\text{V}_{\text{Moon}} = -1.041 \pm 0.067$ (1SD). The second approach (**A2**) uses the means and 2SE
 215 of the three end-members. This approach yields $\Delta^{51}\text{V}_{\text{BSE-Moon}} = 0.180 \pm 0.035$ (2SE), $\delta^{51}\text{V}_{\text{BSE}} = -$
 216 0.856 ± 0.020 (2SE), $\delta^{51}\text{V}_{\text{ch.}} = -1.089 \pm 0.029$ (2SE), and $\delta^{51}\text{V}_{\text{Moon}} = -1.036 \pm 0.028$ (2SE). The
 217 results of these two approaches are in very good agreement with each other, and are summarized
 218 in Supplementary figure 7.
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Supplementary figure 7: Comparison between the mean V isotopic compositions of the Moon, chondrites and BSE from (i) the raw data-driven Monte Carlo approach (open symbols, errors bars at 1SD), and (ii) computation of the "real" values of these end-members (closed symbols).

227 **Supplementary Note 3: Vanadium isotope constraints the Moon-forming**
228 **event**

229 Mixing calculations presented in this paper rely on the fundamental principle of mass
230 conservation during two-component mixing, for a system with pre-impact (proto-Earth, Theia) and
231 post-impact (Earth, Moon, escaping mass (EM)) components (see ref⁶ for description of a similar
232 approach). We consider $\delta^{51}\text{V}_{\text{P-E}}$, $\delta^{51}\text{V}_{\text{Theia}}$, $\delta^{51}\text{V}_{\text{BSE}}$, and $\delta^{51}\text{V}_{\text{Moon}}$ the $\delta^{51}\text{V}$ values of the proto-Earth,
233 Theia, BSE and Moon, respectively. The $\delta^{51}\text{V}_{\text{BSE}} = -0.856 \pm 0.020$ (2SE), $\delta^{51}\text{V}_{\text{ch.}} = -1.089 \pm 0.029$
234 (2SE), and $\delta^{51}\text{V}_{\text{Moon}} = -1.037 \pm 0.031$ (2SE) are taken from the respective best estimates for each
235 reservoir, which yields a best estimate for the V isotope composition difference between BSE and
236 the Moon of $\Delta^{51}\text{V}_{\text{BSE-Moon}} = 0.180 \pm 0.035$ (2SE). The V isotope composition of Theia is assumed
237 to be indistinguishable from chondrites ($\delta^{51}\text{V}_{\text{Theia}} = \delta^{51}\text{V}_{\text{ch.}}$), which is conventionally assumed in
238 most Giant Impact simulations and also reasonable given that all chondrite groups have identical
239 V isotope compositions². Given that V is only mildly siderophile and, therefore, core formation
240 does not tend to produce a silicate portion of a planet with concentrations significantly different to
241 bulk chondrites, we here assume that the proto-Earth, Theia and the Moon all have similar V
242 concentrations. Most chondrites have V concentrations that are within error of BSE (82 ± 12 $\mu\text{g/g}$
243 ²). So far we only have V data for two enstatite chondrites and these suggest the potential for the
244 chondritic impactor to have had lower V concentrations than considered here (~ 50 $\mu\text{g/g}$ ²).
245 However, a lower V concentration for the impactor would only change our model in a minor way,
246 and would invariably lead to slightly higher mass fractions of Theia (ϕ_{M}) being required in the
247 Moon to account for its present-day V isotope composition. Thus, a lower V concentration for

248 Theia would further strengthen our conclusion that the observed $\Delta^{51}\text{V}_{\text{BSE-Moon}}$ is only compatible
 249 with the canonical giant impact simulations. The mass fractions of the present-day Moon and Earth
 250 that originate from Theia are denoted φ_M and φ_E , respectively, with:

$$251 \quad \delta^{51}\text{V}_{\text{BSE}} = \varphi_E * \delta^{51}\text{V}_{\text{Theia}} + (1 - \varphi_E) * \delta^{51}\text{V}_{\text{P-E}} \quad (\text{Eq. 1})$$

$$252 \quad \delta^{51}\text{V}_{\text{Moon}} = \varphi_M * \delta^{51}\text{V}_{\text{Theia}} + (1 - \varphi_M) * \delta^{51}\text{V}_{\text{P-E}} \quad (\text{Eq. 2})$$

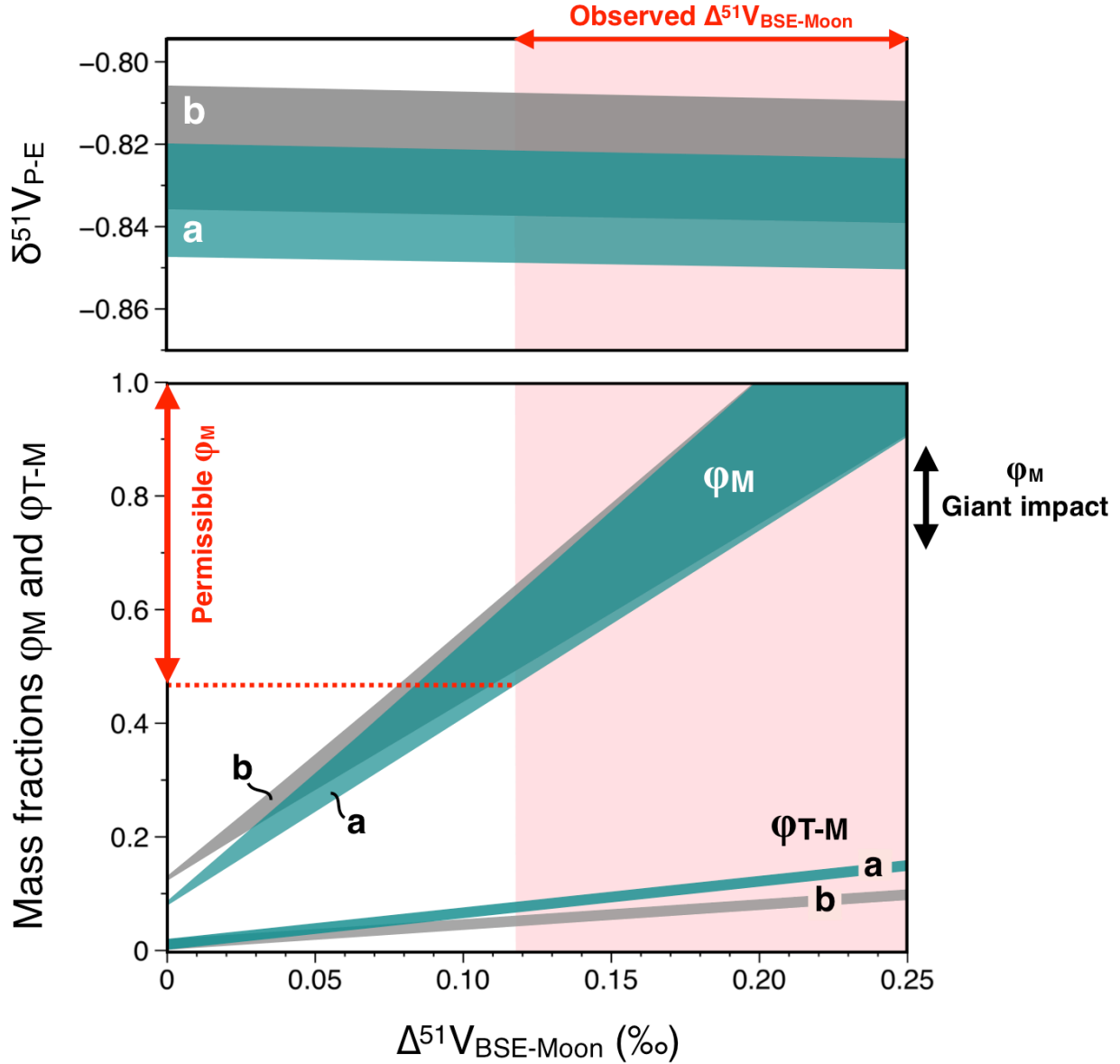
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 256 These two equations contain 3 unknowns, which are φ_E , φ_M and $\delta^{51}\text{V}_{\text{P-E}}$. Mass conservation
 257 implies:

$$258 \quad M_{\text{Theia}} = \varphi_E * M_{\text{Earth}} + \varphi_M * M_{\text{Moon}} + EM \quad (\text{Eq. 3})$$

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 260 where M_{Theia} , M_{Earth} and M_{Moon} are the total masses of Theia, Earth and Moon, respectively.
 261 Whereas the two latter are known, M_{Theia} is taken as a free parameter that will be varied from 0.8
 262 $* M_{\text{Mars}}$ to $0.5 * M_{\text{Earth}}$, where M_{Mars} corresponds to the total mass of Mars. In this approach, the
 263 EM (ejected mass) term can be neglected, as only the fraction of Theia's material ultimately
 264 entering either the Moon or Earth is considered in the mass balance. In other words, two scenarios
 265 where $M_{\text{Theia}} = 1.2 * M_{\text{Mars}}$ and $EM = 0.2 * M_{\text{Mars}}$, or $M_{\text{Theia}} = 1.0 * M_{\text{Mars}}$ and $EM = 0 * M_{\text{Mars}}$ will
 266 give the exact same outcomes. The system of Eq. 1-3 hence contains 3 unknowns, and can
 267 therefore be fully resolved to investigate the ranges of admissible φ_E , φ_M and $\delta^{51}\text{V}_{\text{P-E}}$ values as
 268 constrained by V isotope systematics. We also note φ_{M-T} the fraction of Theia that ends up being
 269 incorporated in the Moon:

$$270 \quad \varphi_{T-M} = \varphi_M * M_{\text{Moon}} / M_{\text{Theia}} \quad (\text{Eq. 4})$$

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 273 A summary of the main outcomes of these mixing calculations is reported in Table 1,
 274 whereas Fig. 3 of the main manuscript presents illustrations of the mixing calculations where M_{Theia}
 275 represents $0.8 * M_{\text{Mars}}$, $1.2 * M_{\text{Mars}}$, and $M_{\text{Theia}} = 0.45 * M_{\text{Earth}}$. As illustrated in Supplementary figure
 276 8, using $\delta^{51}\text{V}_{\text{BSE}}$, $\delta^{51}\text{V}_{\text{Theia}}$, $\delta^{51}\text{V}_{\text{Moon}}$ and $\Delta^{51}\text{V}_{\text{BSE-Moon}}$ values as derived from our first approach A1
 277 would essentially give the same outcomes (at the 1SD level) as what is presented in the manuscript.
 278 This supports our conclusion that V isotope systematics for lunar samples requires the Moon to be
 279 predominantly derived from the impactor, as predicted by the canonical giant impact scenario.
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Supplementary figure 8: Results of mass balance calculations for giant impacts where Theia's mass (M_{Theia}) represents 0.8 (a) or 1.2 (b) times that of Mars (M_{Mars}), using end-member values from approach A1 (instead of approach A2, as presented in Figure 3 of the main manuscript). Given the observed $\Delta^{51}\text{V}_{\text{BSE-Moon}} = 0.186 \pm 0.068$ (1SD), it can be seen that the minimum fraction of Theia in the Moon is $\sim 50\%$, in very good agreement with constraints from Figure 3 of the main manuscript based on end-member compositions from approach A2. ϕ_{M} : mass fraction of the present-day Moon that originates from Theia. $\phi_{\text{T-M}}$: mass fraction of Theia that has been incorporated in the Moon ($= \phi_{\text{M}} * M_{\text{Moon}} / M_{\text{Theia}}$). $\delta^{51}\text{V}_{\text{P-E}}$: V isotopic composition of the proto-Earth.

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Supplementary Table 1: Vanadium isotope compositions and GCR corrections for lunar samples.

Sample	Type	V ($\mu\text{g/g}$)	Fe ($\mu\text{g/g}$)	CRE age (Myr) [§]	error (2sd)	$\delta^{51}\text{V}_{\text{meas}}$	error (2sd)	n	$\delta^{51}\text{V}_{\text{corr}}$	error* (2sd)
<u>Hopkins et al 2019</u>										
10017	High-Ti basalt	68	157635	479	60	-3.47	0.19	1	-1.09	0.35
10017	High-Ti basalt	70	154955	479	60	-3.18	0.19	1	-0.93	0.34
10020	High-Ti basalt	104	146310	127	25	-1.88	0.29	2	-1.50	0.30
10044	High-Ti basalt	42	147476	70	17	-1.30	0.19	3	-0.78	0.23
70255	High-Ti basalt	92	144242	280	85	-1.86	0.68	3	-0.92	0.74
71135	High-Ti basalt	101	144756	103	3	-1.50	0.63	3	-1.18	0.63
74275	High-Ti basalt	118	141629	32	1	-1.00	0.19	3	-0.92	0.19
75035	High-Ti basalt	37	143636	77.4	19.3	-1.71	0.19	2	-1.07	0.25
12018	Low-Ti basalt	182	160419	195	16	-1.42	0.20	3	-1.05	0.20
12054	Low-Ti basalt	118	161584	260	70	-1.65	0.49	3	-0.89	0.53
12054	Low-Ti basalt	143	158737	260	70	-1.60	0.21	4	-0.98	0.27
12063	Low-Ti basalt	115	166756	95	5	-1.35	0.21	3	-1.06	0.21
14053	Low-Ti basalt	108	133525	21.2	5	-1.08	0.21	3	-1.02	0.21
15016	Low-Ti basalt	234	173167	322	83	-1.53	0.21	2	-1.02	0.25
15535	Low-Ti basalt	217	178968	110	20	-1.14	0.21	2	-0.95	0.21
15556	Low-Ti basalt	211	166707	546	214	-2.00	0.42	2	-1.08	0.55
									weighted average [#]	-1.012
									weighted 2SE	0.067
<u>This study</u>										
10084	Soil	53	81177	520	120	-2.96	0.06	8	-1.25	0.40
12004	Low-Ti basalt	117	148628	49	10	-1.05	0.12	7	-0.92	0.12
15495	Low-Ti basalt	101	151612	320	200	-2.16	0.07	3	-1.13	0.65
15556	Low-Ti basalt	224	155451	546	214	-1.84	0.11	4	-1.03	0.33
LAP02205	Low-Ti basalt	99	171363	4	1	-1.06	0.14	3	-1.05	0.14
70215	High-Ti basalt	94	139463	126	3	-1.46	0.06	4	-1.06	0.10
74255	High-Ti basalt	102	102272	17	2	-1.17	0.06	4	-1.13	0.06
68815	KREEP-rich	21	40272	2.04	0.2	-1.04	0.07	4	-1.03	0.07
68115	KREEP-rich	21	32458	2.08	0.08	-1.08	0.11	4	-1.07	0.11
14321	KREEP-rich	56	100850	23.8	2	-1.06	0.06	4	-0.97	0.06
									weighted average [#]	-1.041
									weighted 2SE	0.030

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* - total propagated error combines uncertainties on V isotope measurement, CRE age, Fe and V concentrations.

[#] - Averages and associated 2 sigma errors weighted by total propagated error on each measurement

[§] - CRE ages are based on noble gas isotope measurements in each sample^{1,7-15}, except for 15495 that is based on range of CRE ages for samples at the edge of the Dune Crater where this sample was collected⁸

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