

Supplementary information for “Classification in biological networks with hypergraphlet kernels”

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1 Enumeration of labeled hypergraphlets

Here we characterize the feature space of fully labeled hypergraphlets by describing the dimensionality of count vectors $\phi_{(n,\tau)}(v)$. We are interested in the order of growth of $\kappa(n, \Sigma, \Xi)$ as a function of n , Σ and Ξ , as introduced in the main text.

Suppose that G and H are base hypergraphlets with n vertices and m hyperedges. We say that G and H belong to the same equivalence class if and only if the total number of (non-isomorphic) fully labeled hypergraphlets corresponding to the base cases G and H are equal for any Σ and Ξ . The total counts of labeled hypergraphlets over all alphabet sizes induce a partition of base hypergraphlets into equivalence classes. We

Table S1: **Equivalence classes over vertex- and hyperedge-labeled hypergraphlets.** List of equivalence classes and their cardinality produced by partitioning the set of undirected base hypergraphlets for $n \in \{1, 2, 3, 4\}$ over vertex-labels alphabet Σ and hyperedge-labels alphabet Ξ . We also list the number of vertex-labeled n -hypergraphlets over an alphabet Σ denoted as $m_i(n, \Sigma, 1)$, as well as fully labeled n -hypergraphlets over an alphabet Σ and Ξ denoted as $m_i(n, \Sigma, \Xi)$.

Vertex-labeled hypergraphlets		
$S_i(n)$	$ S_i(n) $	$m_i(n, \Sigma, 1)$
$S_1(1)$	1	$ \Sigma $
$S_1(2)$	1	$ \Sigma ^2$
$S_1(3)$	3	$ \Sigma ^3$
$S_2(3)$	6	$1/2(\Sigma ^3 + \Sigma ^2)$
$S_1(4)$	221	$ \Sigma ^4$
$S_2(4)$	212	$1/2(\Sigma ^4 + \Sigma ^3)$
$S_3(4)$	28	$1/6(\Sigma ^4 + 3 \cdot \Sigma ^3 + 2 \cdot \Sigma ^2)$
Fully-labeled hypergraphlets		
$S_i(n)$	$ S_i(n) $	$m_i(n, \Sigma, \Xi)$
$S_1(1)$	1	$ \Sigma $
$S_1(2)$	1	$ \Sigma ^2 \cdot \Xi $
$S_1(3)$	1	$ \Sigma ^3 \cdot \Xi ^3$
$S_2(3)$	2	$ \Sigma ^3 \cdot \Xi ^2$
$S_3(3)$	1	$1/2(\Sigma ^3 \cdot \Xi ^4 + \Sigma ^2 \cdot \Xi ^3)$
$S_4(3)$	2	$1/2(\Sigma ^3 \cdot \Xi ^3 + \Sigma ^2 \cdot \Xi ^2)$
$S_5(3)$	1	$1/2(\Sigma ^3 \cdot \Xi ^2 + \Sigma ^2 \cdot \Xi ^2)$
$S_6(3)$	1	$1/2(\Sigma ^3 \cdot \Xi ^2 + \Sigma ^2 \cdot \Xi)$
$S_7(3)$	1	$1/2(\Sigma ^3 \cdot \Xi + \Sigma ^2 \cdot \Xi)$

denote the set of all equivalence classes over the hypergraphlets of order n as $S(n) = \{S_1(n), S_2(n), \dots\}$. For example, the set of vertex- and hyperedge-labeled 3-hypergraphlets can be partitioned into either: two symmetry classes when $|\Xi| = 1$: $S_1(3) = \{3_2, 3_4, 3_7\}$ and $S_2(3) = \{3_1, 3_3, 3_5, 3_6, 3_8, 3_9\}$, or seven symmetry classes when $|\Xi| > 1$: $S_1(3) = \{3_2\}$, $S_2(3) = \{3_4, 3_7\}$, $S_3(3) = \{3_9\}$, $S_4(3) = \{3_6, 3_8\}$, $S_5(3) = \{3_3\}$, $S_6(3) = \{3_5\}$ and $S_7(3) = \{3_1\}$. Table S1 summarizes equivalence classes induced by partitioning base hypergraphlets up to the order of 4 along with the cardinality of each set. Overall, observe that the cardinality of $S(n)$ can be significantly larger than those reported for graphlets [3] because the possible number of hyperedges in a hypergraphlet is generally much larger than the possible number of edges in a graphlet. Additionally, hyperedge-labels require base hypergraphlets G and H to have an equal number of hyperedges.

This approach can be generalized to hypergraphlets labeled by any alphabet Σ and Ξ , such that

$$\kappa(n, \Sigma, \Xi) = \sum_{i=1}^{|S(n)|} m_i(n, \Sigma, \Xi) \cdot |S_i(n)|,$$

where $m_i(n, \Sigma, \Xi)$ is the number of (non-isomorphic) fully labeled hypergraphlets corresponding to any base hypergraphlet from the equivalence class $S_i(n)$. We use this decomposition to compute the total dimensionality of the count vectors by first finding the equivalence classes corresponding to the base hypergraphlets and then counting the number of labeled hypergraphlets for any one member of the group.

In the case of undirected fully labeled hypergraphlets, $m_i(n, \Sigma, \Xi)$ can also be computed by applying the theory of enumeration developed by Pólya [5]. In order to get the derivation of the complete generating function for each equivalence class $S_i(n)$, we first define the automorphism group \mathcal{A} of a given vertex- and hyperedge-labeled hypergraph $G = (V, E)$. That is, in the case of fully-labeled hypergraphs, set \mathcal{A} is a collection of permutations (automorphisms) of V and E . Therefore, the counting problem can be re-formulated as follows: Let G be a base hypergraphlet of n vertices and m hyperedges, and \mathcal{A} be the automorphism group of G over V and E . Then, each permutation $\alpha \in \mathcal{A}$ can be written uniquely as the

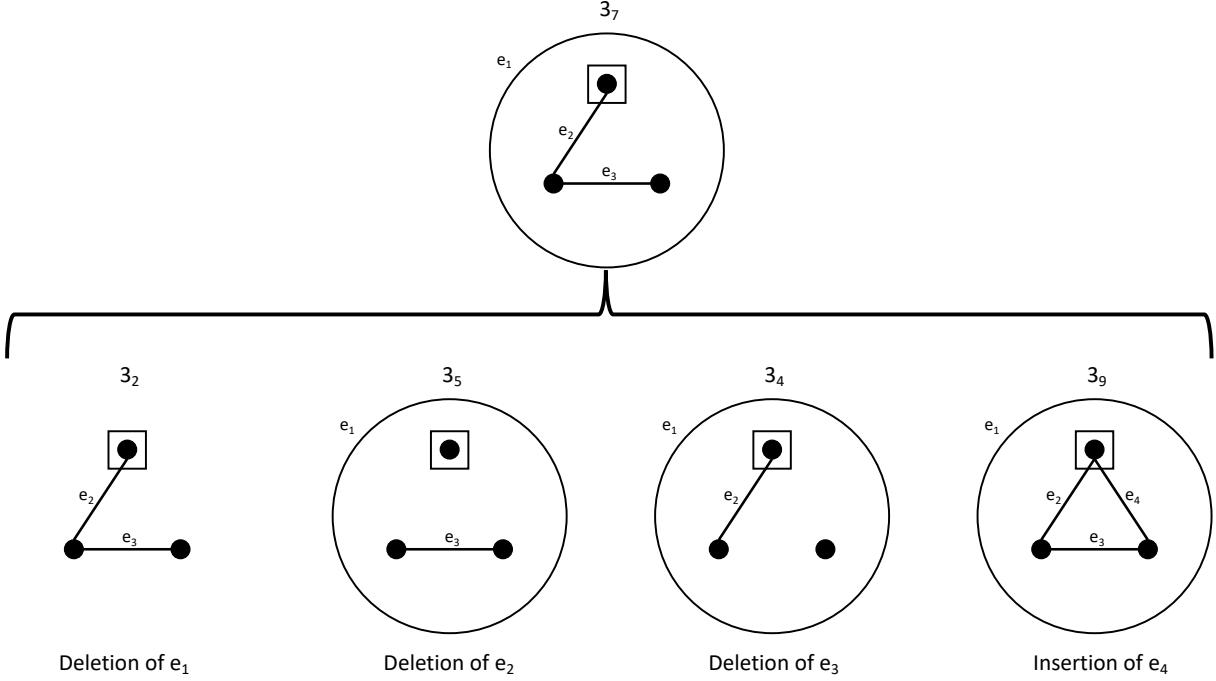


Figure S1: Example of precomputed level-1 insertions/deletions (indels) of hyperedges for base hypergraphlet 3_7 . The precomputed level-1 indels include three hyperedge deletions and one hyperedge insertion.

product of disjoint cycles such that for each integer $k \in \{1, \dots, n\}$ ($k' \in \{1, \dots, m\}$), we define $j_k(\alpha)$ ($j_{k'}(\alpha)$) as the number of cycles of length k (k') in the disjoint cycle expansion of α . Interestingly, the generalized formula for the cycle index of \mathcal{A} , denoted as $Z(\mathcal{A})$, is a polynomial in $s_1, \dots, s_n; s'_1, \dots, s'_m$ given by

$$Z(\mathcal{A}; s_1, \dots, s_n; s'_1, \dots, s'_m) = \frac{1}{|\mathcal{A}|} \sum_{\alpha \in \mathcal{A}} \prod_{k=1}^n \prod_{k'=1}^m s_k^{j_k(\alpha)} \cdot s'_{k'}^{j_{k'}(\alpha)}.$$

By applying Pólya's theorem in the context of enumerating vertex- and hyperedge-labeled hypergraphlets corresponding to any base hypergraphlet in $S_i(n)$, we get that $m_i(n, \Sigma, \Xi)$ is determined by substituting $|\Sigma|$ for each variable s_k and $|\Xi|$ for each variable $s'_{k'}$ in $Z(\mathcal{A})$. Hence,

$$m_i(n, \Sigma, \Xi) = Z(\mathcal{A}; |\Sigma|, |\Sigma|, \dots, |\Sigma|; |\Xi|, |\Xi|, \dots, |\Xi|),$$

where \mathcal{A} is the automorphism group of a base hypergraphlet from $S_i(n)$. As an example, consider the equivalence class $S_3(3) = \{3_9\}$ with $\Sigma = \{A, B, C\}$ and $\Xi = \{X, Y\}$ (Figure 2 in the main paper illustrates an unlabeled version of hypergraphlet 3_9). The automorphism group is given by

$$\mathcal{A} = \{(v_1)(v_2)(v_3)(e_1)(e_2)(e_3)(e_4), (v_1)(v_2v_3)(e_1e_2)(e_3)(e_4)\},$$

thus, $Z(\mathcal{A}; s_1, s_2, s_3; s'_1, s'_2) = \frac{1}{2}(s_1^3 \cdot s'_1^4 + s_1 \cdot s_2 \cdot s'_1^2 \cdot s'_2)$. Therefore, it follows that, $m_3(3, \Sigma, \Xi) = Z(\mathcal{A}; 3, 3, 3; 2, 2) = \frac{1}{2}(3^3 \cdot 2^4 + 3 \cdot 3 \cdot 2^2 \cdot 2) = 252$.

2 Computational complexity

The implementation and the analysis of hypergraphlet kernels is an extension of the available solutions for string kernels [6]. Let $G_l(r) = (V_r, E_r)$ be a *neighborhood hypergraph* of a rooted hypergraph $G = (V, r, E)$ such that there exists a walk w of length at most l between any node $u \in V$ and root vertex r , denoted as $|w(u, r)| \leq l$. Formally, $E_r = \{e \mid e \in E \wedge e \subseteq V_r \wedge |w(u, r)| \leq l, \forall u \in V_r, l \geq 0, r \in V_r\}$. In this work,

we consider the set of undirected base hypergraphlets for $n \in \{1, 2, 3, 4\}$, thus, neighborhood hypergraph $G_{n-1}(r)$ contains all possible n -hypergraphlets rooted at vertex r . Suppose $G_{n-1}(r)$ is significantly smaller than G . An upper bound on the complexity of the counting algorithm for all n -hypergraphlets rooted at vertex r is $\mathcal{O}(|V_r||E_r| + (\delta_{\max}d_{\max})^{n-1})$, where d_{\max} is the maximum degree of a vertex in V_r and δ_{\max} is the maximum degree of a hyperedge in E_r . The first term is related to computing the neighbors for each node $v \in V_r$, whereas the second term reflects the cost of counting over all base hypergraphlets. Similarly, an upper bound on the complexity of generating the minimum cost edit path is $\mathcal{O}((n|\Sigma| + 2^n|\Xi|) + (2^n|\Xi|))$ per single hypergraphlet edit operation. In this case, the first term reflects the cost of generating all vertex and hyperedge label substitutions, whereas the second term corresponds to the cost of performing hyperedge insertions and deletions (indels); see Figure S1 for an example of level-1 indels on a base hypergraphlet. Therefore, for each vertex v an order of

$$\mathcal{O}(\min \{|V_r|^n, \kappa(n, \Sigma, \Xi)\} ((n|\Sigma| + 2^n|\Xi|) + (2^n|\Xi|))^{\tau})$$

operations are necessary, where the $|V_r|^n$ term enumerates possible n -hypergraphlets in $G_{n-1}(r)$. Note that the possible number of hyperedges in a hypergraph $|E_r|$ can be significantly larger than the possible number of edges in a standard graph. Hence, in a practical setting, the edit-distance hypergraphlet kernels could greatly benefit from effective sampling techniques or exploitation of special types of hypergraphlets. The proposed implementation for computing hypergraphlet kernel functions is computed in time linear in the number of non-zero elements.

2.1 Converting hypergraphs to graphs

A commonly used approach for learning from hypergraph data is to construct a standard graph representation from the input hypergraph and use well-established graph approaches. Among these hypergraph-to-graph transformations, the two most popular are *clique expansion* and *star expansion* [7]. A clique expansion of a hypergraph $G = (V, E)$ is defined as graph $G^x = (V, E^x \subseteq V^2)$ such that each hyperedge $e = \{v_1, \dots, v_{\delta(e)}\} \in E$ is replaced with an edge for each pair of vertices in hyperedge e , thus, forming a clique in G^x ; mathematically, $E^x = \{(u, v) | u, v \in e, e \in E\}$. A star expansion of a hypergraph $G = (V, E)$ is defined as a graph $G^* = (V^*, E^*)$ such that for each hyperedge $e = \{v_1, \dots, v_{\delta(e)}\} \in E$, a new vertex e is introduced in G^* connecting e to each $v \in e$, hence, $V^* = V \cup E$; mathematically, $E^* = \{(v, e) | v \in e, e \in E\}$.

We used the clique expansion to evaluate the benefits of using hypregraphs in the second stage of our approach. Note that the first stage consists of converting graphs into dual extended hypergraphs and formulating edge classification and link prediction as a vertex classification approach on hypergraphs. A combination of the dual hypergraph construction, subsequent clique expansion, with graphlet kernel-based prediction is referred to here as *dual graphlet kernel* to distinguish this method from standard graphlet kernels used on the vertices of the original network (note that edge classification on standard graphs corresponds here to the vertex classification on line graphs). The dual graphlet kernels that here integrate vertex and edge alphabets into edit-distance similarity functions were not available in prior work and were implemented within our proposed methodology.

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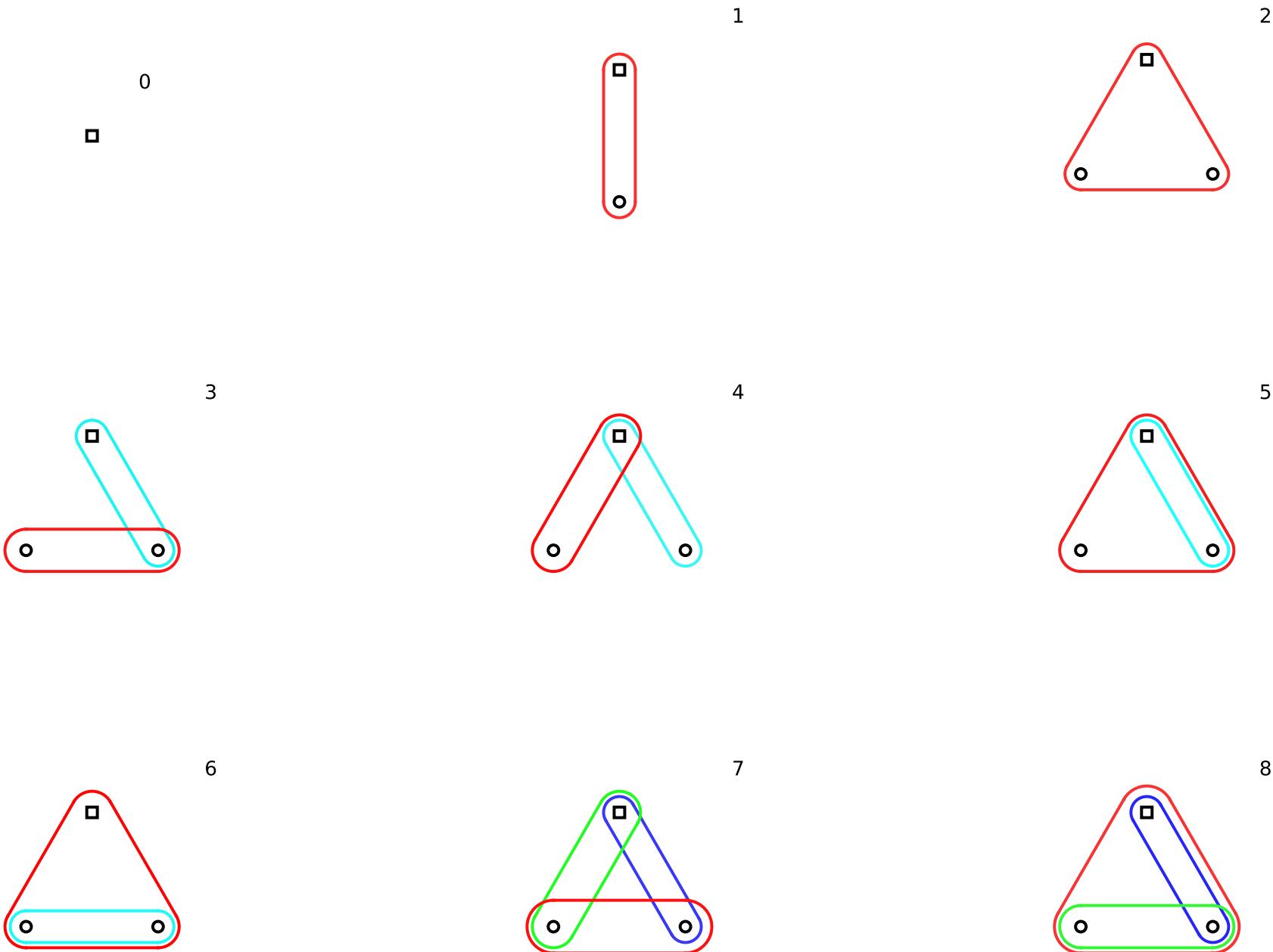
Table S2: Area under the ROC curve estimates for each method on the PPI data sets using 10-fold cross-validation based on the three categories C_1, C_2, C_3 of difficulty identified by Park and Marcotte [4]. The highest performance for each class and data set pair is shown in boldface. Since L3 framework relies on paths of a specific length, it cannot predict on all possible protein pairs. Therefore, the last two rows compare the AUC between L3 and the best hypergraphlet kernel on the same set of predicted protein pairs.

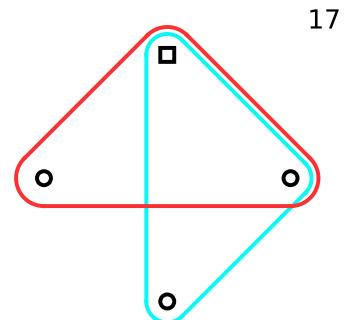
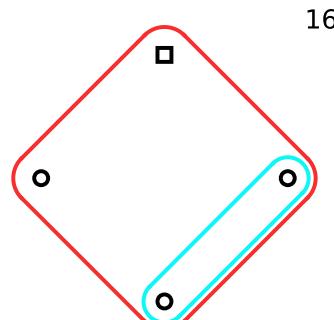
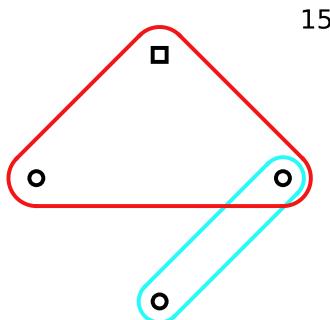
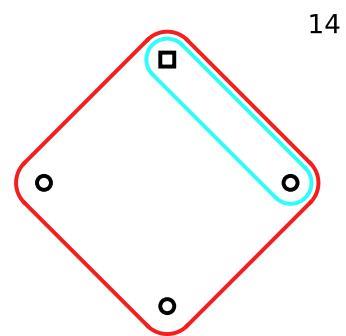
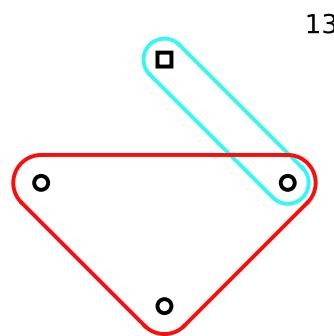
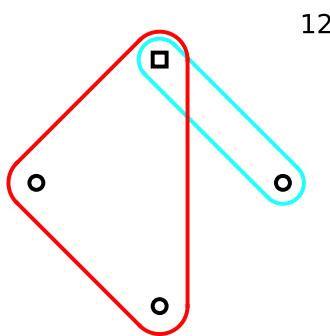
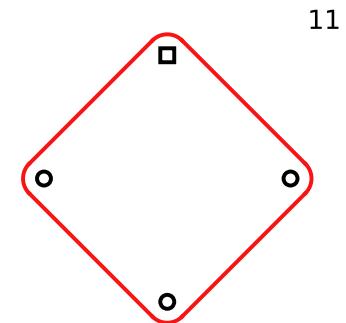
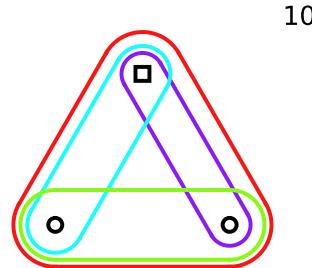
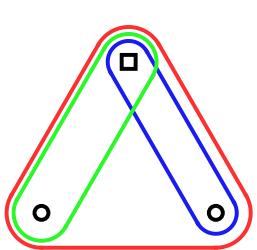
Method/Dataset	EC			SP			RN			MM			CE			AT		
	C_1	C_2	C_3	C_1	C_2	C_3	C_1	C_2	C_3	C_1	C_2	C_3	C_1	C_2	C_3	C_1	C_2	C_3
Dual graphlet kernel ($\tau = 0$)	0.715	0.705	0.674	0.719	0.718	0.712	0.693	0.691	0.637	0.635	0.625	0.623	0.633	0.633	0.635	0.681	0.683	0.681
Section hypergraphlet kernel ($\tau = 0$)	0.724	0.713	0.719	0.639	0.646	0.628	0.671	0.672	0.628	0.630	0.620	0.647	0.633	0.633	0.762	0.774	0.755	0.563
Sub-hypergraphlet kernel ($\tau = 0$)	0.692	0.687	0.681	0.691	0.691	0.680	0.651	0.647	0.633	0.612	0.610	0.605	0.873	0.872	0.872	0.578	0.578	0.588
Dual graphlet kernel ($\tau = 1$)	0.678	0.669	0.649	0.698	0.699	0.691	0.671	0.670	0.647	0.623	0.620	0.614	0.869	0.869	0.869	0.683	0.683	0.681
Section hypergraphlet kernel ($\tau = 1$)	0.708	0.695	0.700	0.641	0.643	0.623	0.678	0.678	0.666	0.668	0.628	0.633	0.772	0.781	0.781	0.671	0.671	0.670
Sub-hypergraphlet kernel ($\tau = 1$)	0.681	0.682	0.660	0.686	0.687	0.682	0.649	0.649	0.634	0.611	0.610	0.606	0.871	0.870	0.870	0.683	0.683	0.682
L3 framework [2]	0.717	0.597	0.556	0.577	0.529	0.497	0.634	0.634	0.573	0.550	0.506	0.511	0.504	0.504	0.501	0.501	0.501	0.502
Preferential attachment [1]	0.814	0.675	0.639	0.492	0.456	0.453	0.552	0.504	0.511	0.498	0.485	0.463	0.660	0.523	0.549	0.449	0.449	0.441
Random walk	0.762	0.755	0.739	0.636	0.617	0.574	0.537	0.521	0.422	0.585	0.563	0.497	0.805	0.803	0.802	0.613	0.605	0.585
Random hy-pewalk	0.815	0.817	0.786	0.610	0.599	0.550	0.589	0.587	0.484	0.588	0.567	0.531	0.597	0.594	0.594	0.601	0.601	0.580
Cumulative random hyperwalk	0.799	0.791	0.789	0.706	0.701	0.680	0.587	0.585	0.466	0.641	0.641	0.613	0.716	0.708	0.708	0.643	0.643	0.629
Pairwise spectrum kernel ($k = \{3, 4, 5\}$)	0.848	0.841	0.820	0.681	0.666	0.641	0.647	0.616	0.524	0.670	0.669	0.646	0.552	0.561	0.637	0.614	0.614	0.624
Dual graphlet kernel ($\tau = 0$)	0.816	0.754	0.618	0.584	0.505	0.432	0.716	0.648	0.580	0.689	0.632	0.548	0.754	0.659	0.650	0.629	0.616	0.541
Section hypergraphlet kernel ($\tau = 0$)	0.802	0.763	0.733	0.734	0.704	0.609	0.673	0.665	0.528	0.630	0.663	0.595	0.846	0.848	0.843	0.678	0.678	0.671
Sub-hypergraphlet kernel ($\tau = 0$)	0.861	0.840	0.840	0.815	0.677	0.664	0.634	0.698	0.670	0.637	0.655	0.647	0.641	0.804	0.799	0.798	0.559	0.555
Dual graphlet kernel ($\tau = 1$)	0.796	0.771	0.747	0.720	0.665	0.676	0.637	0.500	0.708	0.692	0.641	0.846	0.848	0.843	0.678	0.678	0.671	0.619
Section hypergraphlet kernel ($\tau = 1$)	0.816	0.776	0.742	0.745	0.719	0.630	0.682	0.691	0.559	0.702	0.673	0.611	0.853	0.854	0.851	0.689	0.689	0.687
Sub-hypergraphlet kernel ($\tau = 1$)	0.875	0.843	0.880	0.697	0.684	0.649	0.706	0.695	0.686	0.667	0.648	0.639	0.786	0.784	0.783	0.574	0.574	0.576
L3 framework [2]	0.568	0.449	0.691	0.638	0.635	0.565	0.751	0.755	0.613	0.622	0.616	0.531	0.130	0.100	-	0.677	0.549	0.639
Hypergraphlet kernel (highest)	0.896	0.687	0.833	0.759	0.728	0.712	0.683	0.696	0.632	0.738	0.726	0.596	0.966	0.714	-	0.652	0.843	0.846

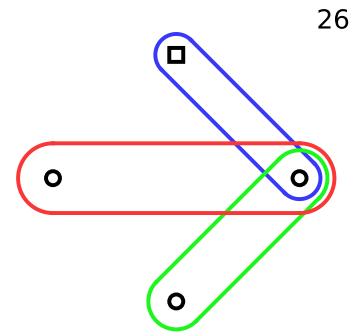
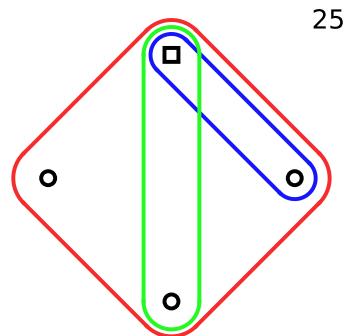
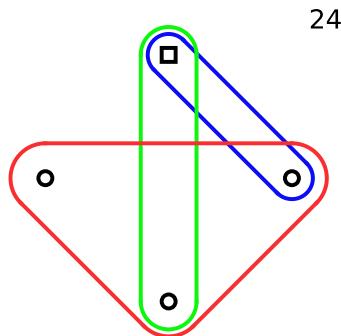
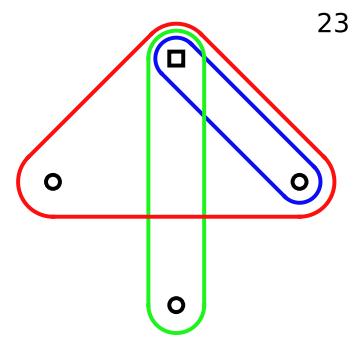
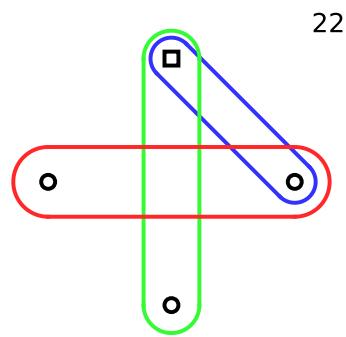
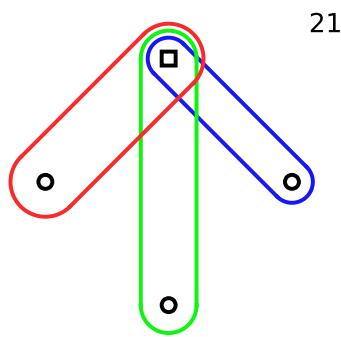
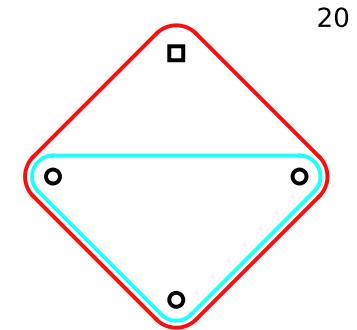
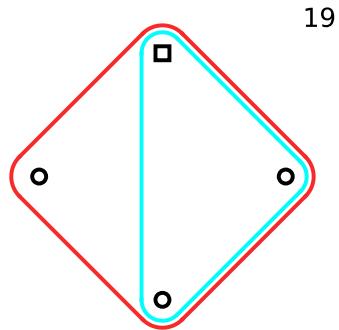
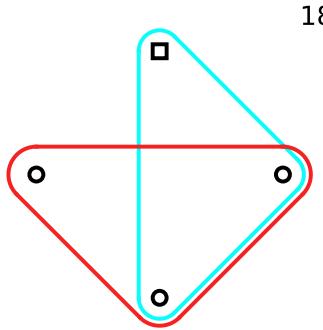
Table S3: **Area under the ROC curve estimates for each method on the DTI data sets using 10-fold cross-validation based on the three categories C_1, C_2, C_3 of difficulty identified by Park and Marcotte [4].** The highest performance for each class and data set pair is shown in boldface. Since L3 framework relies on paths of a specific length, it cannot predict on all possible drug-target pairs. Therefore, the last two rows compare the AUC between L3 and the best hypergraphlet kernel on the same set of predicted drug-target pairs.

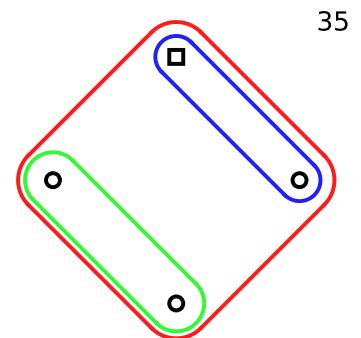
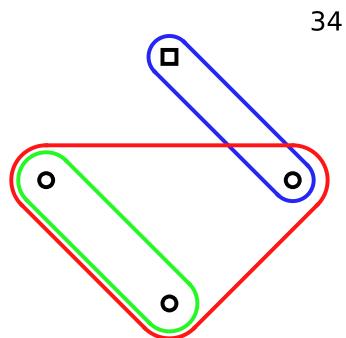
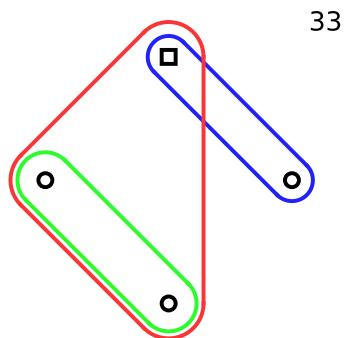
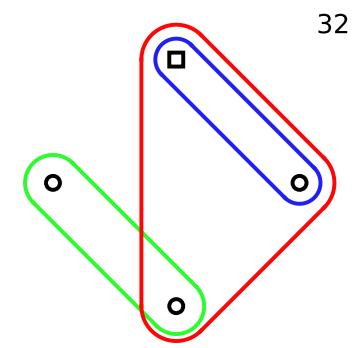
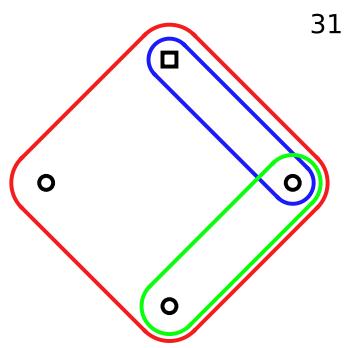
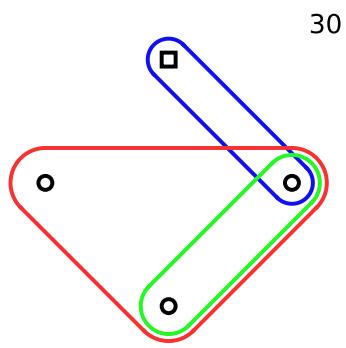
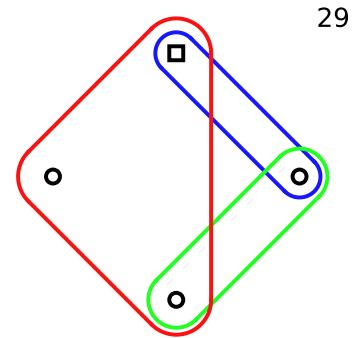
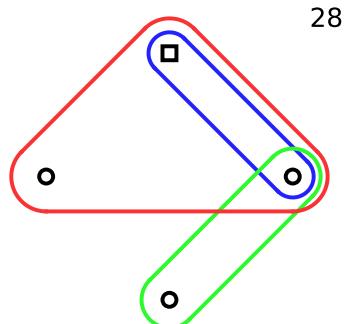
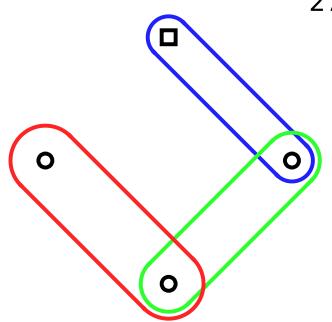
Method/Dataset	EZ			IC			GR			NR		
	C_1	C_2	C_3									
Without domain information, $ \Sigma = 1$												
Dual graphlet kernel ($\tau = 0$)	0.871	0.865	0.838	0.759	0.729	0.714	0.624	0.606	0.525	0.714	0.676	0.712
Section hypergraphlet kernel ($\tau = 0$)	0.537	0.541	0.514	0.542	0.506	0.509	0.552	0.542	0.493	0.783	0.772	0.679
Sub-hypergraphlet kernel ($\tau = 0$)	0.788	0.786	0.778	0.711	0.697	0.680	0.579	0.566	0.484	0.732	0.719	0.735
Dual graphlet kernel ($\tau = 1$)	0.851	0.836	0.792	0.713	0.689	0.651	0.599	0.580	0.519	0.734	0.725	0.728
Section hypergraphlet kernel ($\tau = 1$)	0.535	0.541	0.502	0.550	0.510	0.524	0.542	0.504	0.513	0.791	0.736	0.704
Sub-hypergraphlet kernel ($\tau = 1$)	0.784	0.780	0.770	0.702	0.684	0.671	0.580	0.566	0.482	0.736	0.733	0.731
L3 framework [2]	0.629	0.626	0.500	0.642	0.534	0.500	0.596	0.584	0.500	0.505	0.420	0.500
Preferential attachment [1]	0.534	0.502	0.500	0.561	0.457	0.500	0.545	0.530	0.500	0.497	0.431	0.500
With domain information, $ \Sigma = \{4, 8, 16\}; \Sigma = \Sigma_{GO} \cup \Sigma_{SS}$												
Dual graphlet kernel ($\tau = 0$)	0.952	0.914	0.830	0.883	0.830	0.659	0.756	0.679	0.534	0.771	0.709	0.694
Section hypergraphlet kernel ($\tau = 0$)	0.633	0.630	0.596	0.583	0.546	0.527	0.625	0.581	0.518	0.775	0.605	0.638
Sub-hypergraphlet kernel ($\tau = 0$)	0.936	0.885	0.801	0.879	0.834	0.678	0.724	0.641	0.531	0.757	0.717	0.709
Dual graphlet kernel ($\tau = 1$)	0.953	0.923	0.832	0.900	0.845	0.686	0.758	0.684	0.533	0.778	0.719	0.719
Section hypergraphlet kernel ($\tau = 1$)	0.637	0.605	0.605	0.585	0.543	0.523	0.619	0.591	0.550	0.777	0.707	0.713
Sub-hypergraphlet kernel ($\tau = 1$)	0.944	0.913	0.845	0.884	0.852	0.715	0.747	0.693	0.526	0.764	0.713	0.730
L3 framework [2]	0.658	0.668	-	0.655	0.534	-	0.624	0.609	-	0.577	0.501	-
Hypergraphlet kernel (highest)	0.953	0.921	-	0.900	0.858	-	0.760	0.687	-	0.802	0.818	-

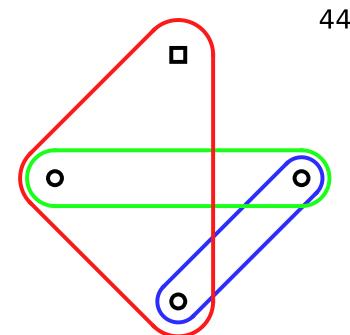
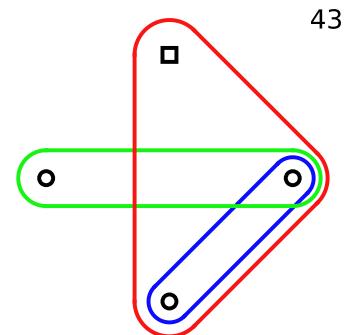
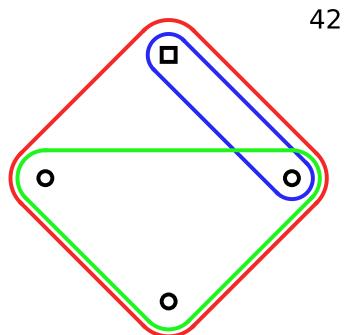
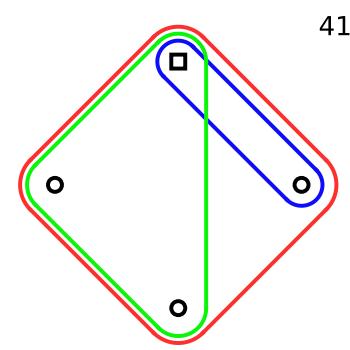
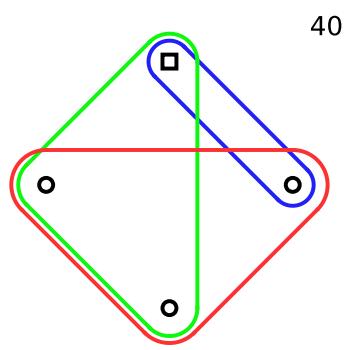
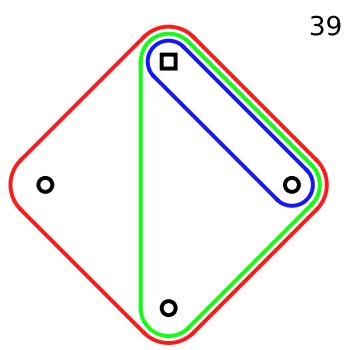
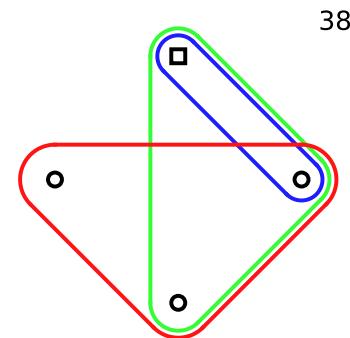
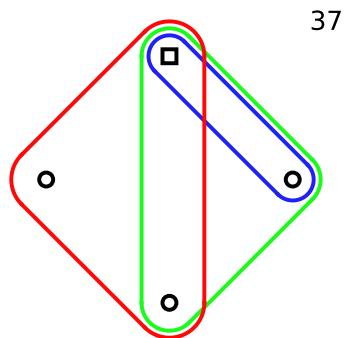
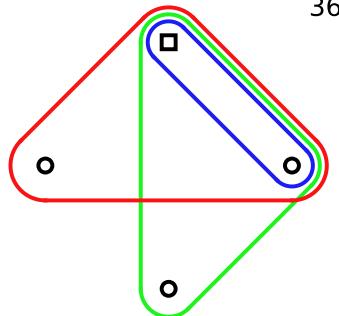
Base hypergraphlets up to 4 vertices

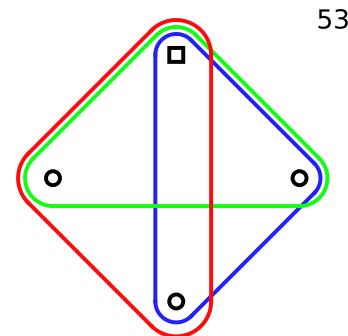
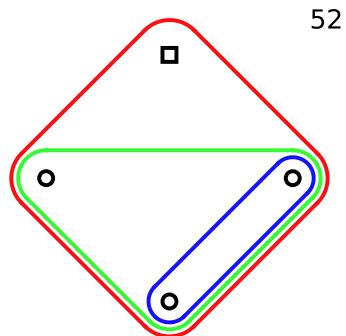
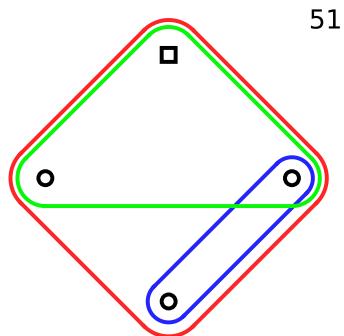
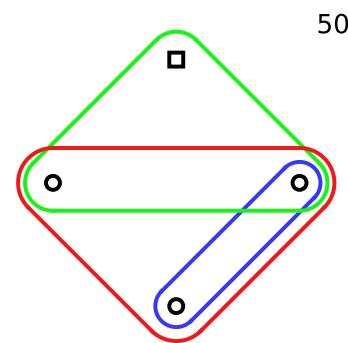
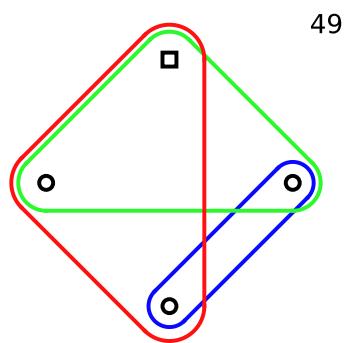
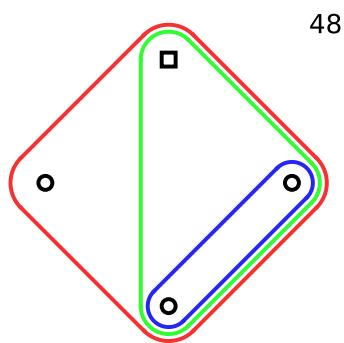
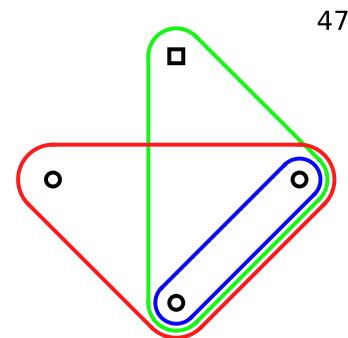
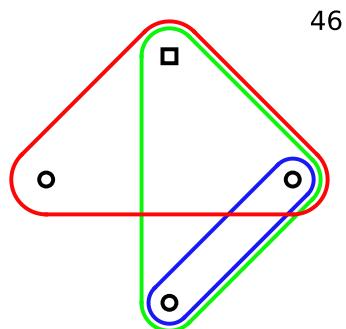
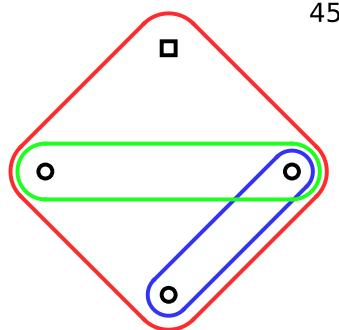


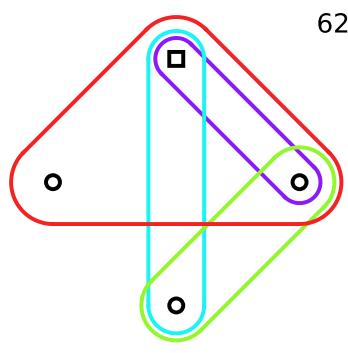
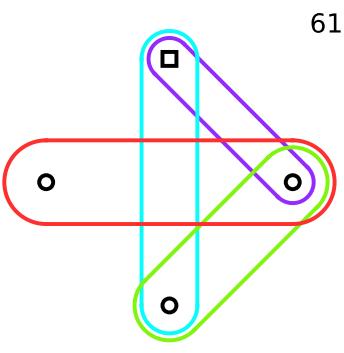
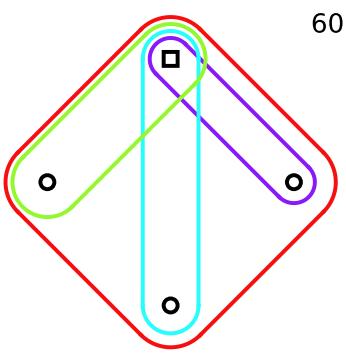
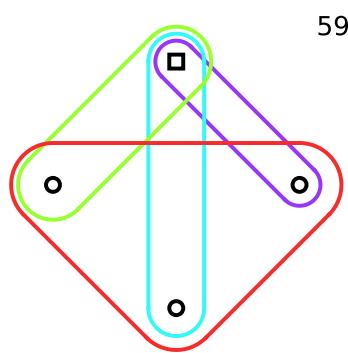
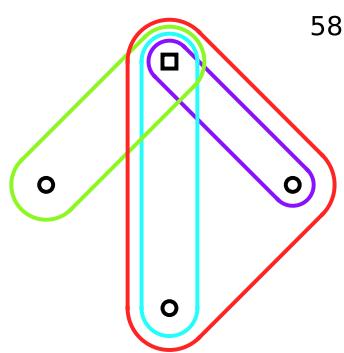
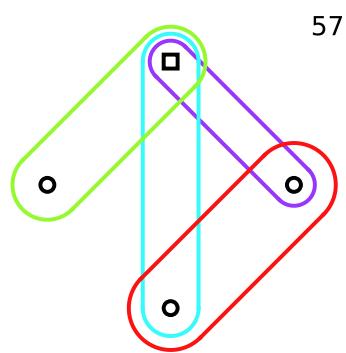
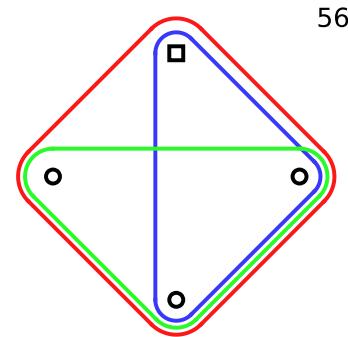
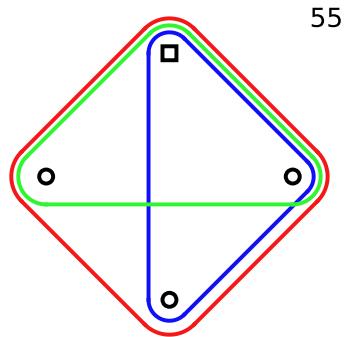
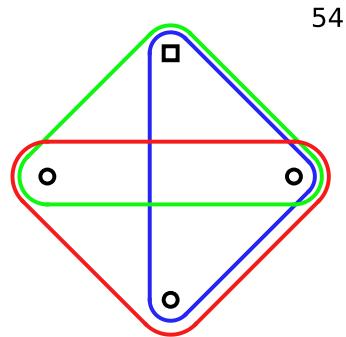


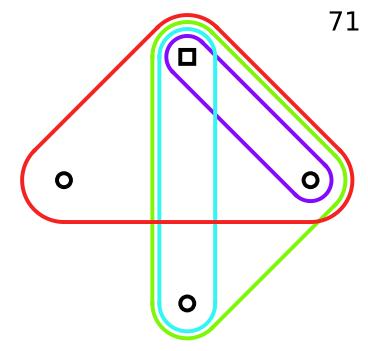
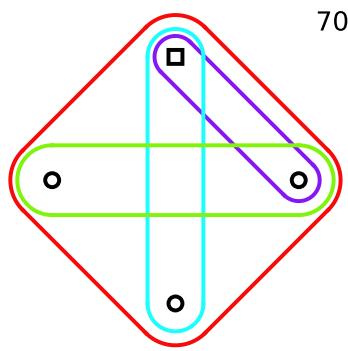
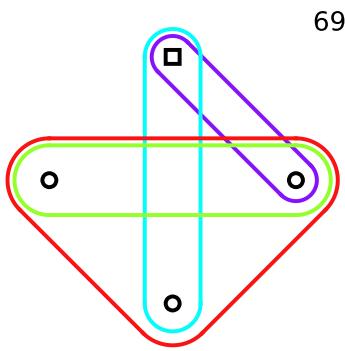
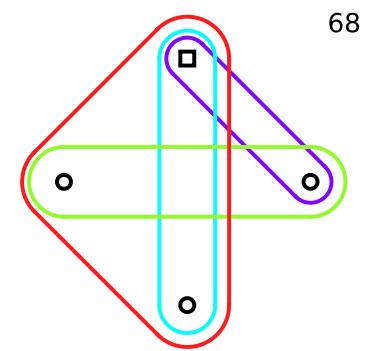
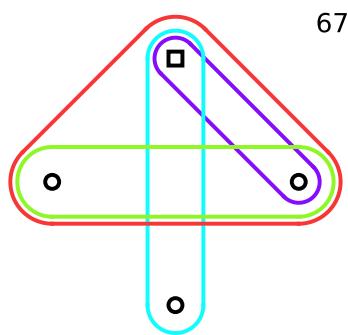
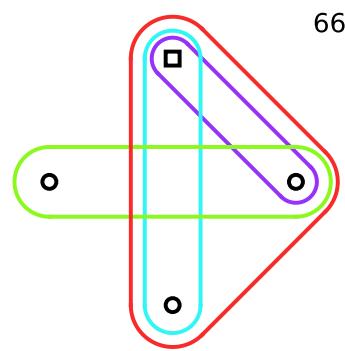
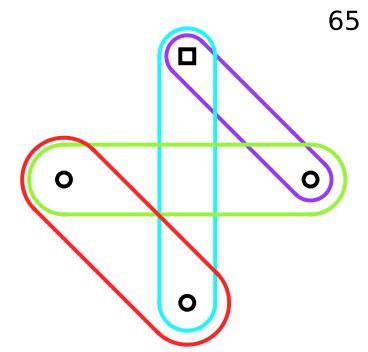
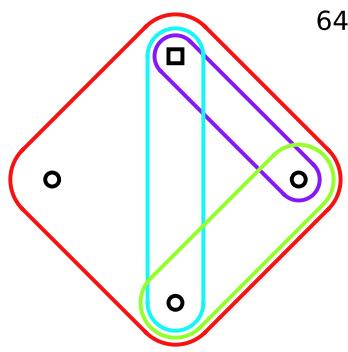
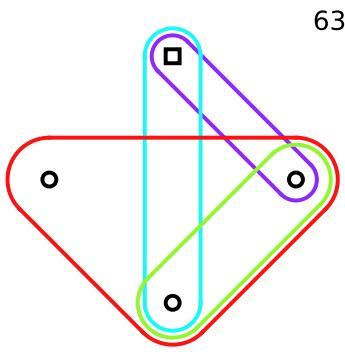


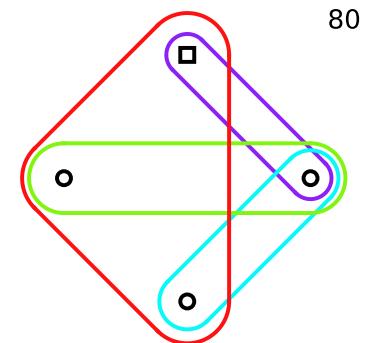
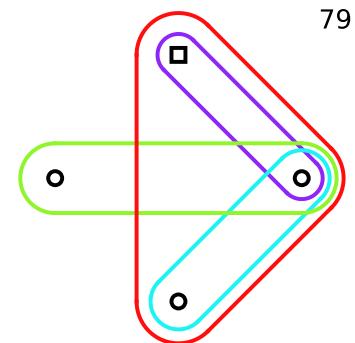
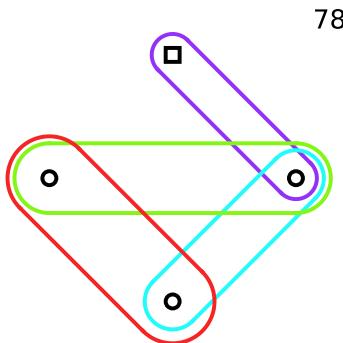
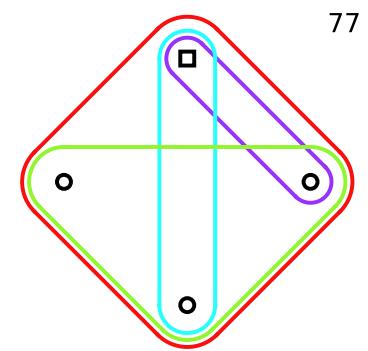
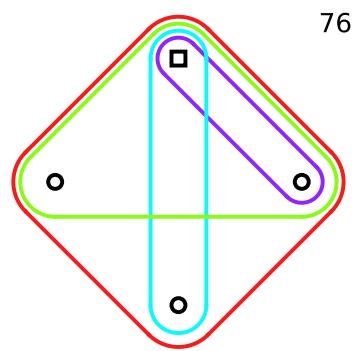
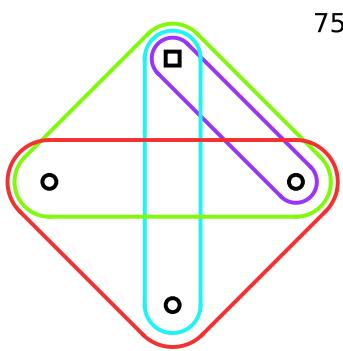
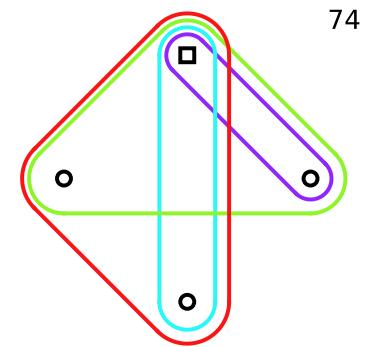
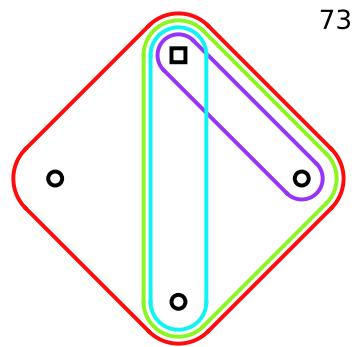
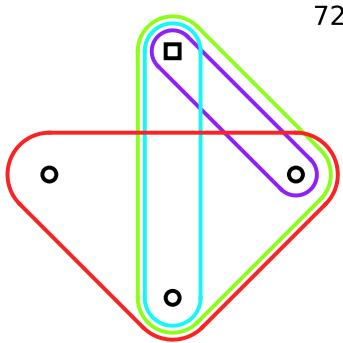


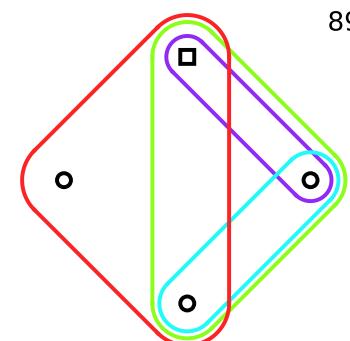
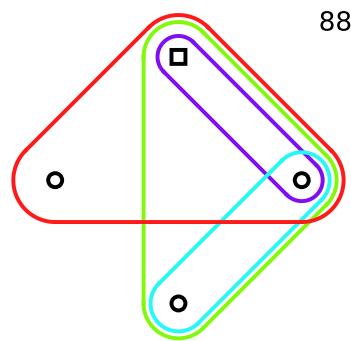
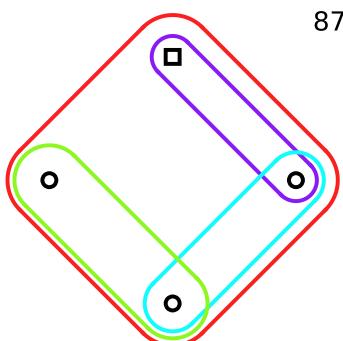
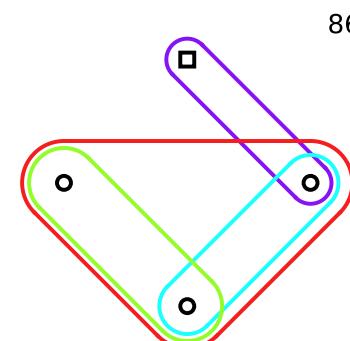
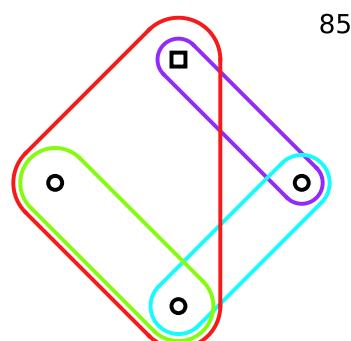
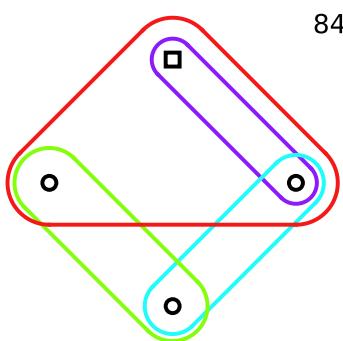
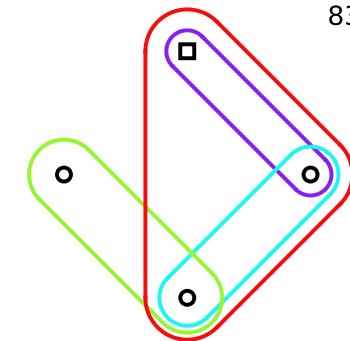
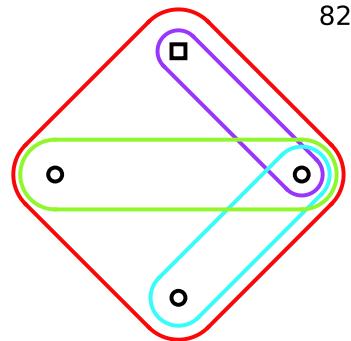
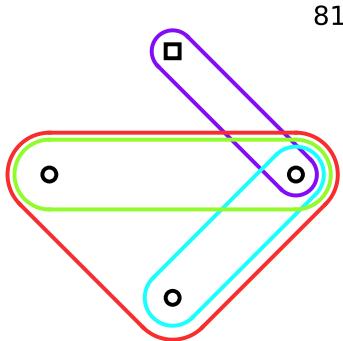


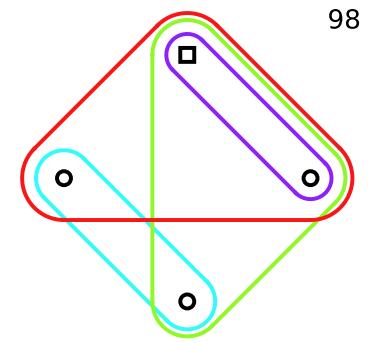
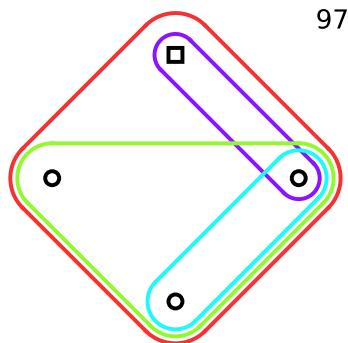
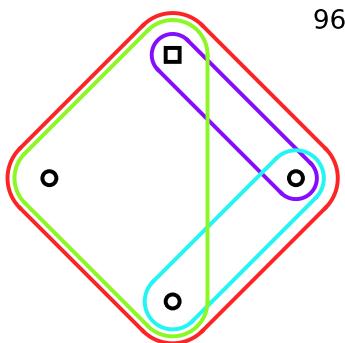
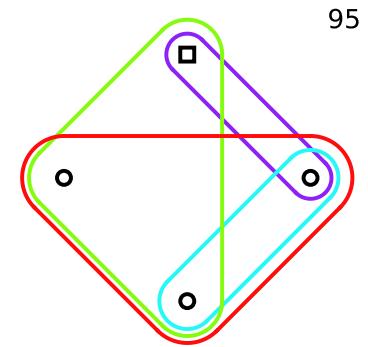
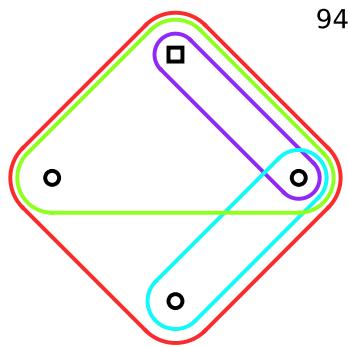
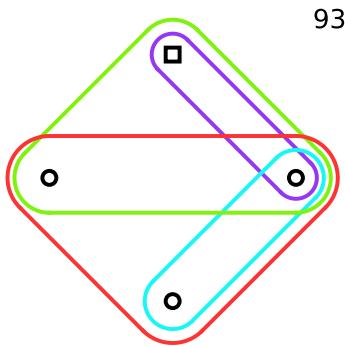
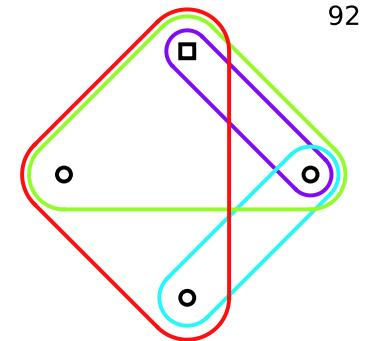
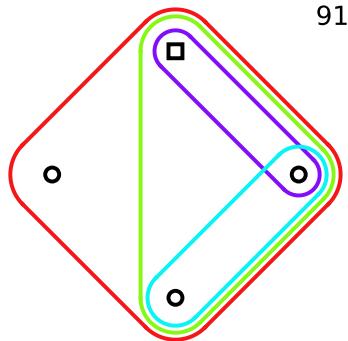
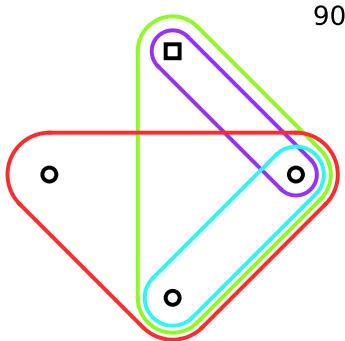


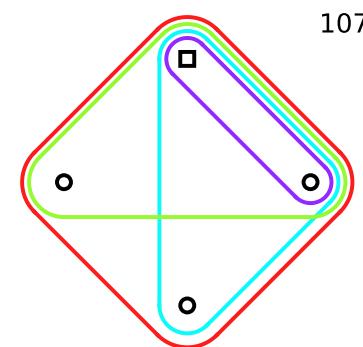
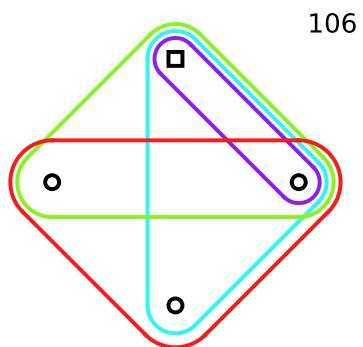
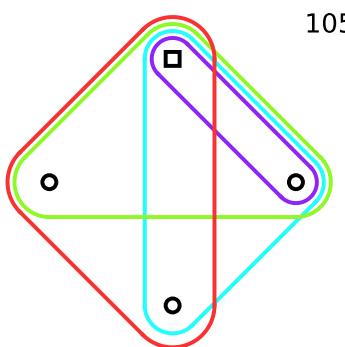
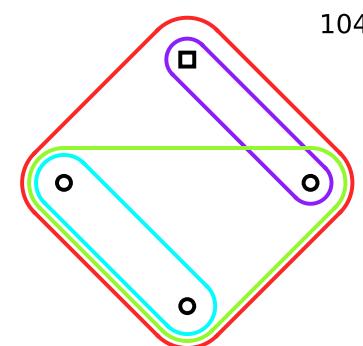
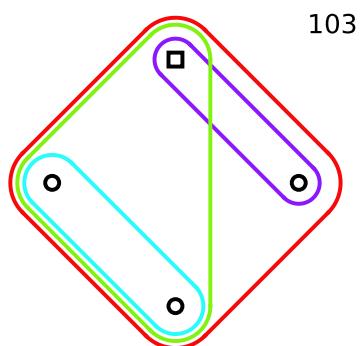
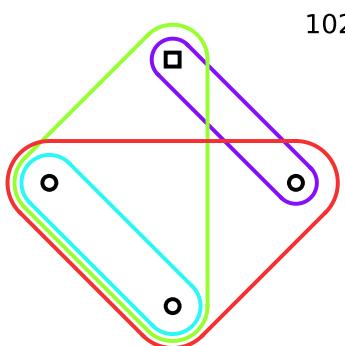
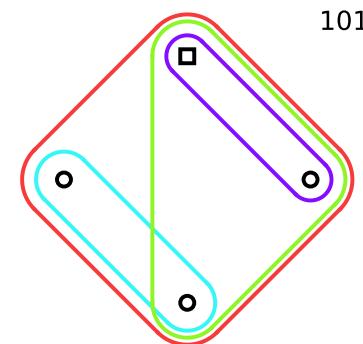
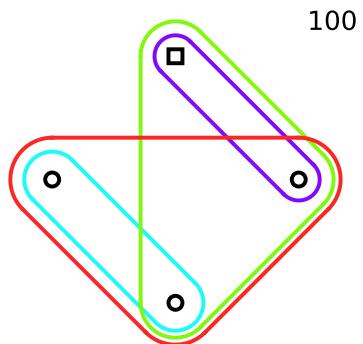
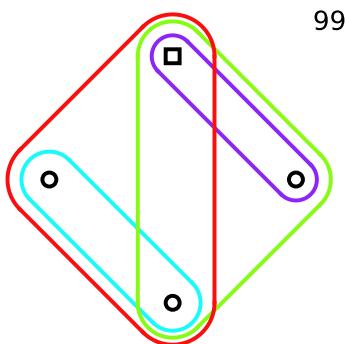


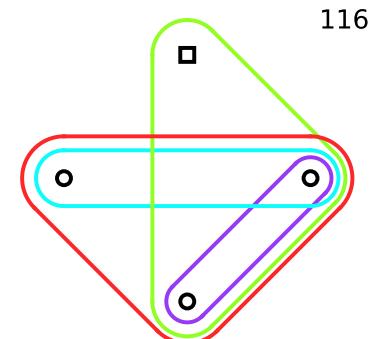
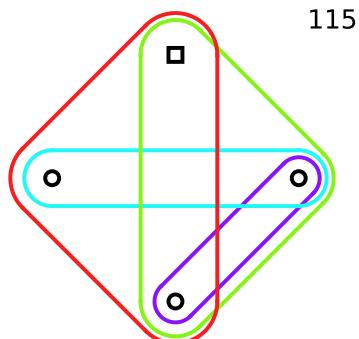
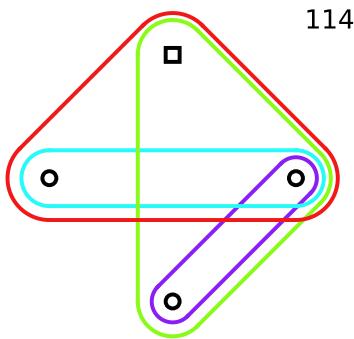
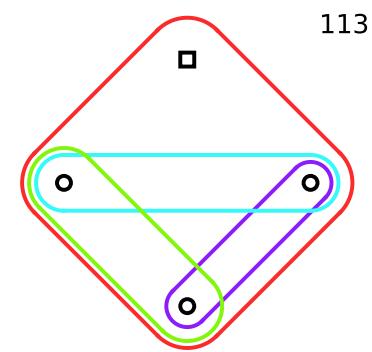
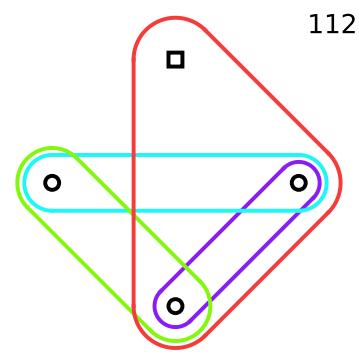
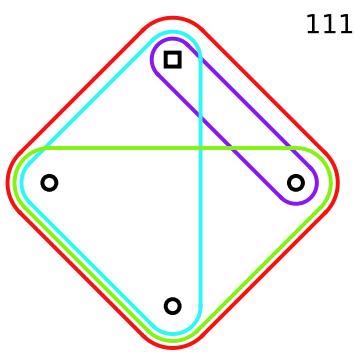
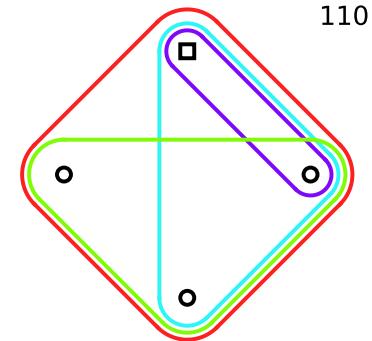
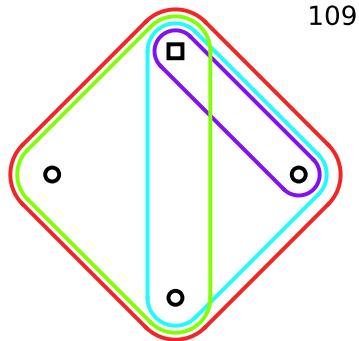
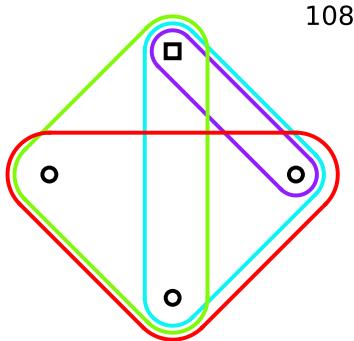


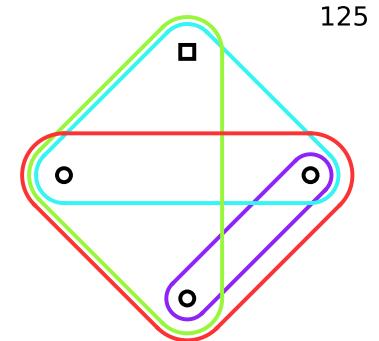
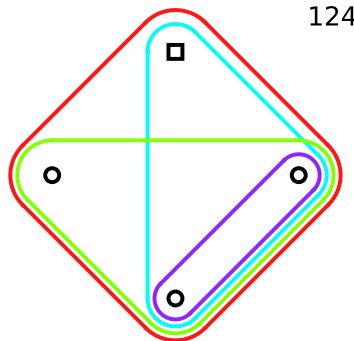
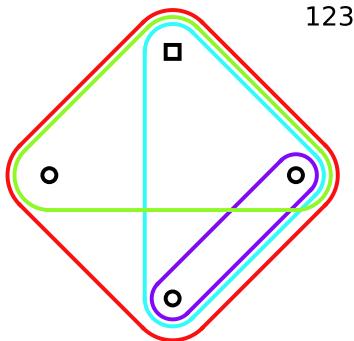
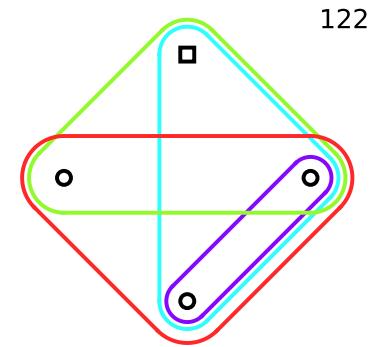
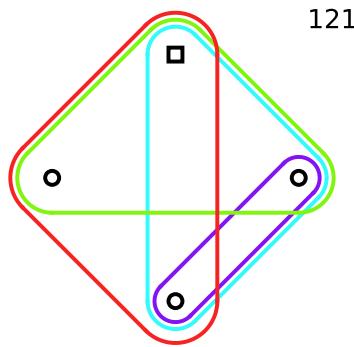
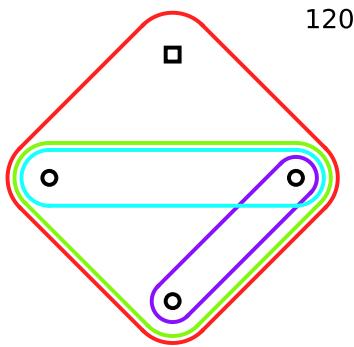
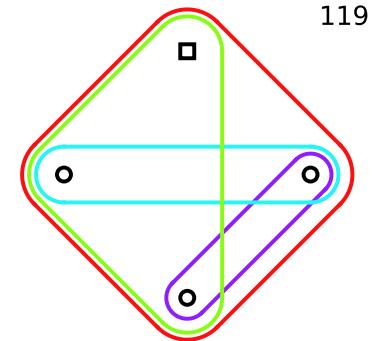
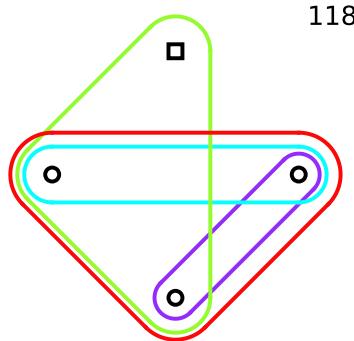
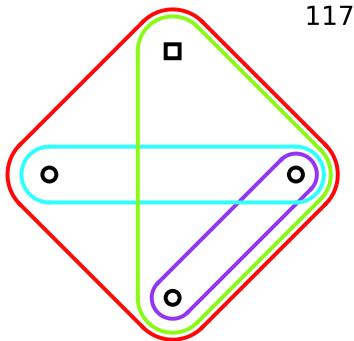


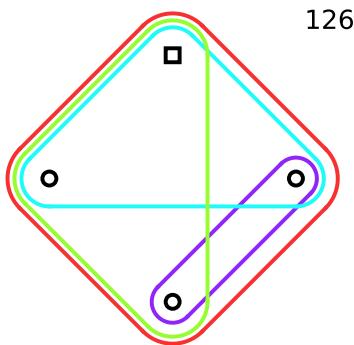




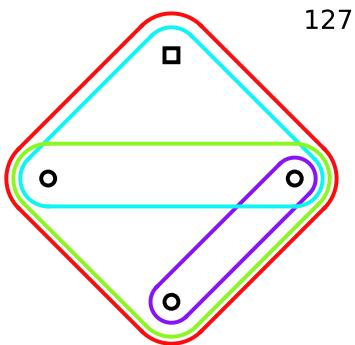




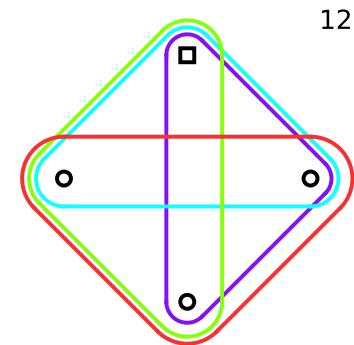




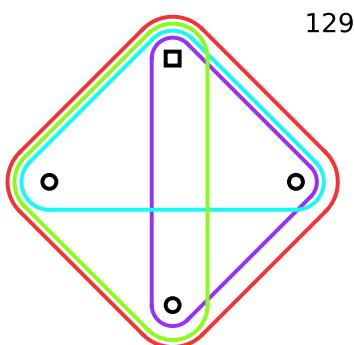
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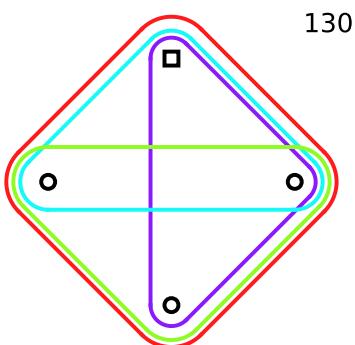
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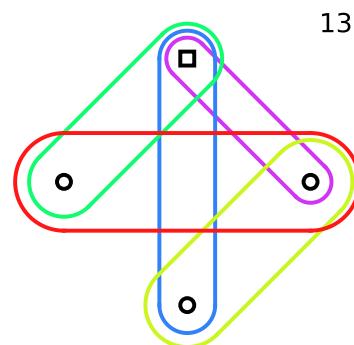
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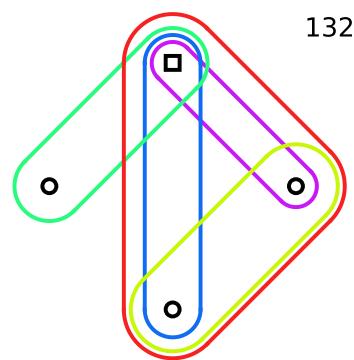
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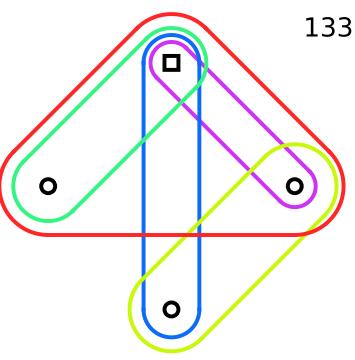
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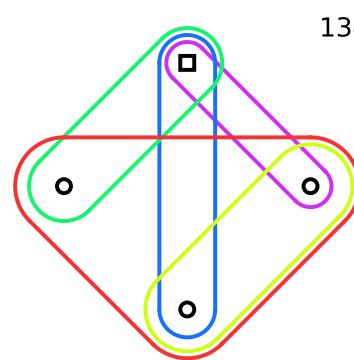
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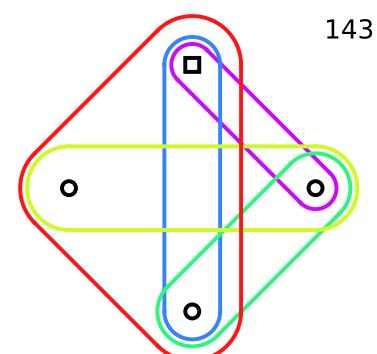
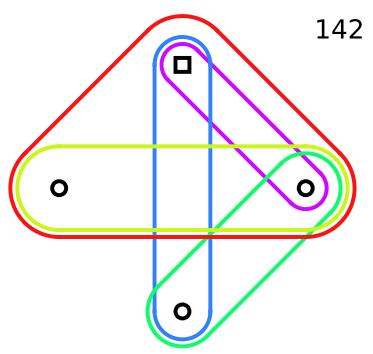
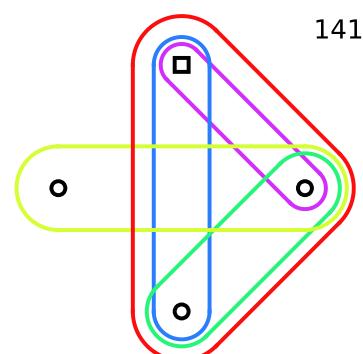
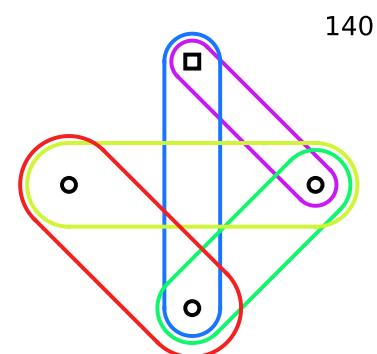
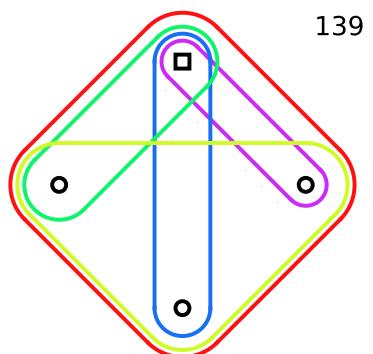
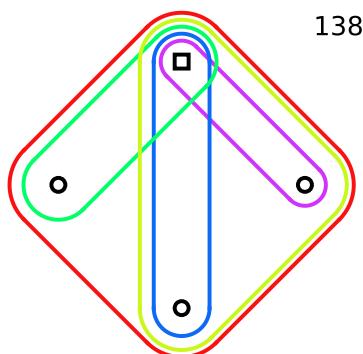
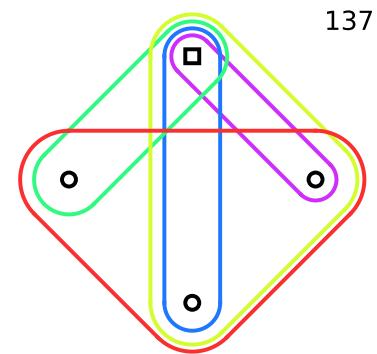
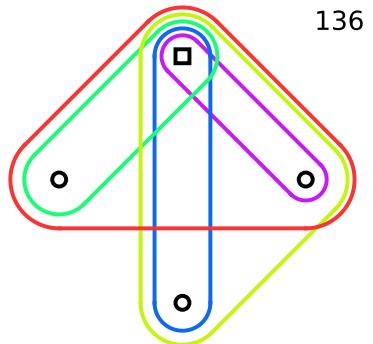
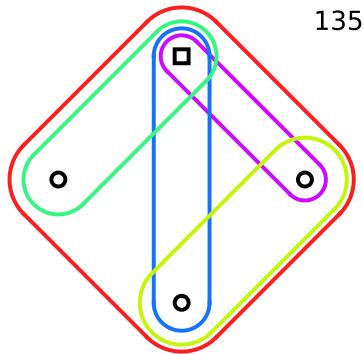
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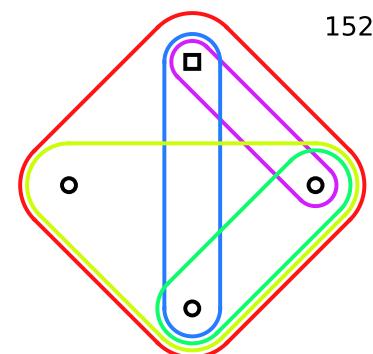
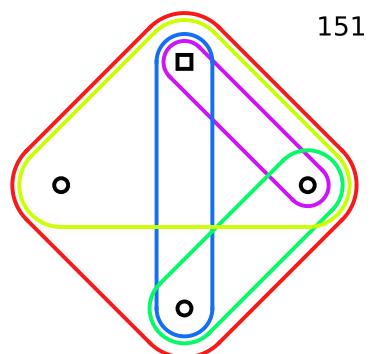
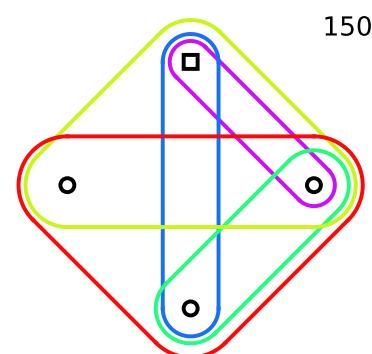
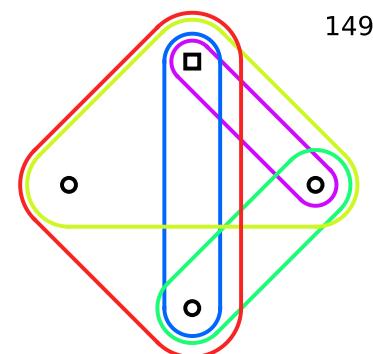
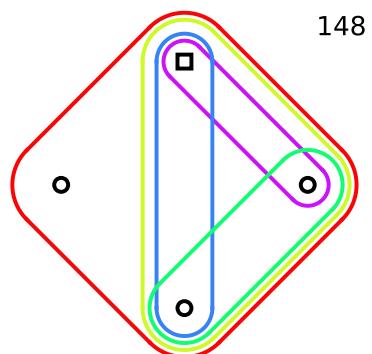
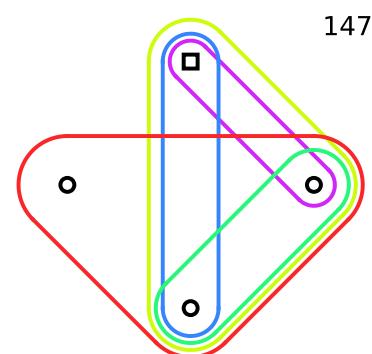
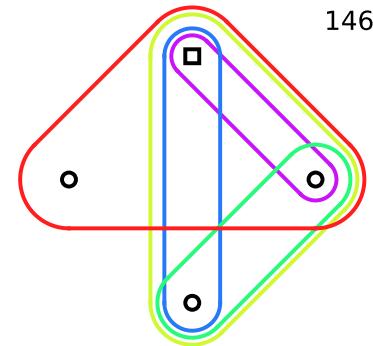
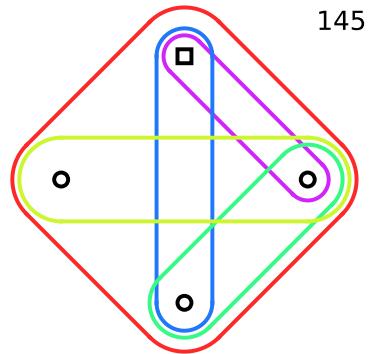
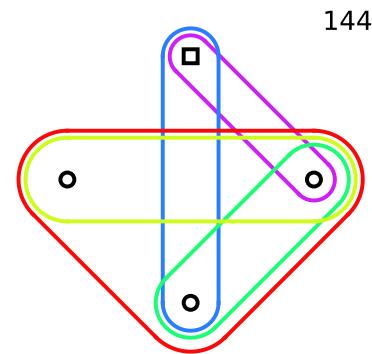


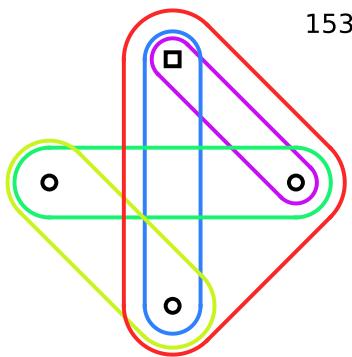
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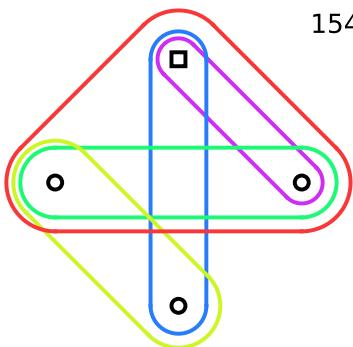
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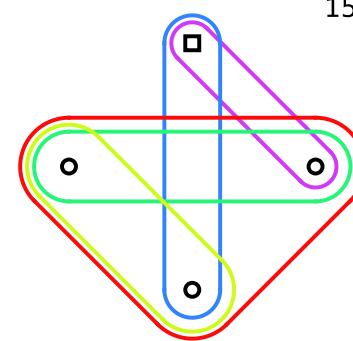




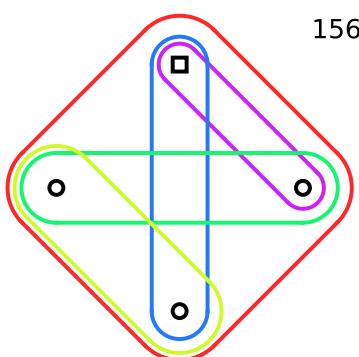
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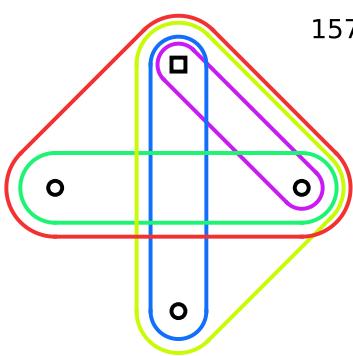
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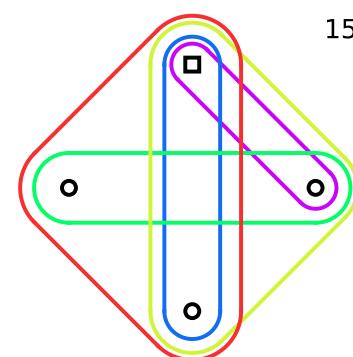
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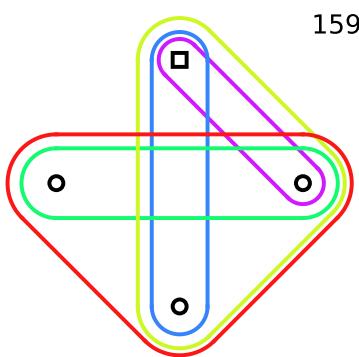
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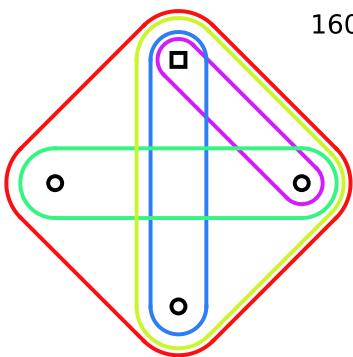
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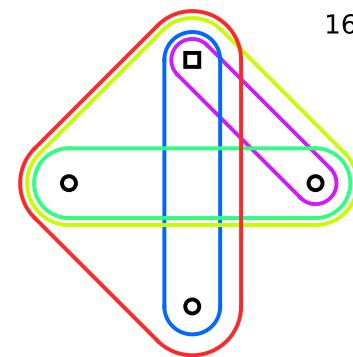
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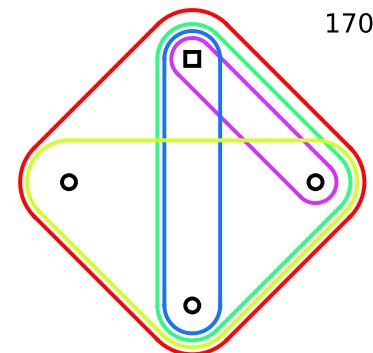
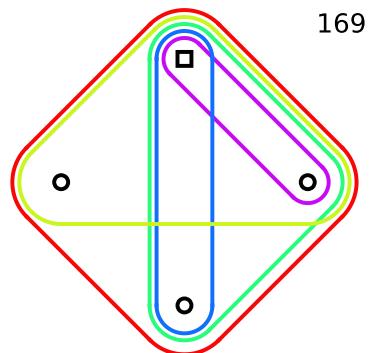
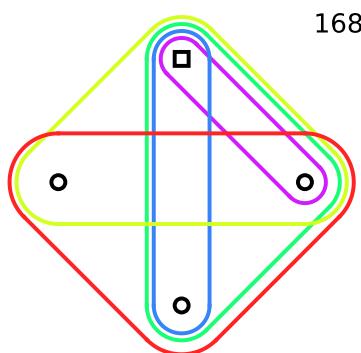
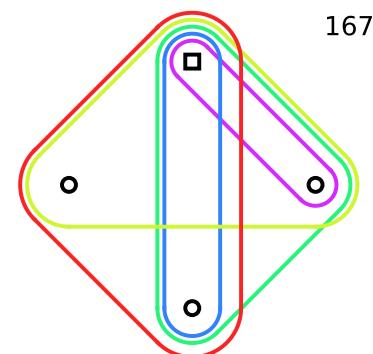
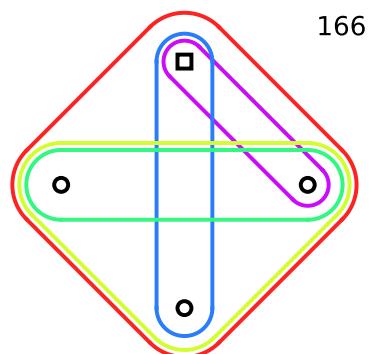
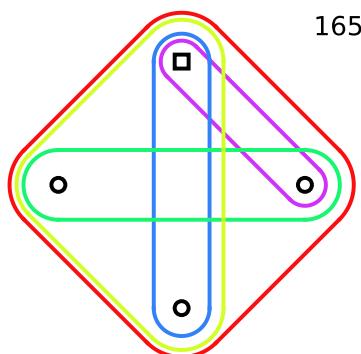
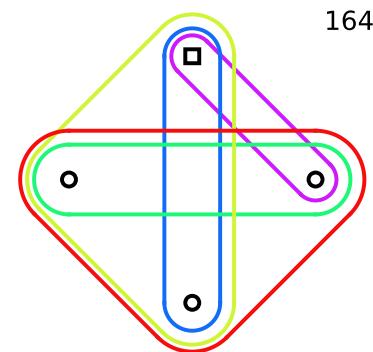
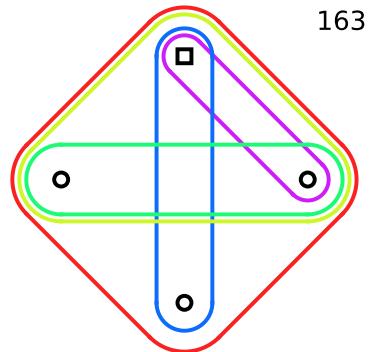
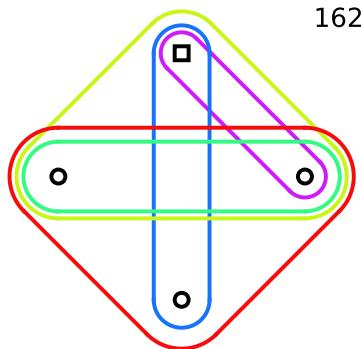
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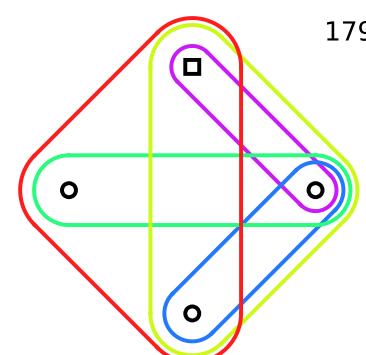
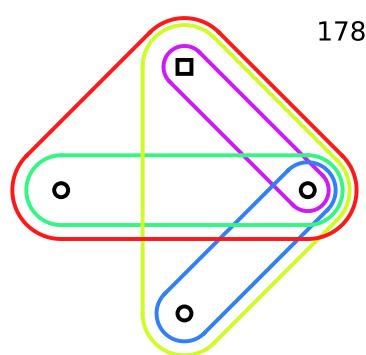
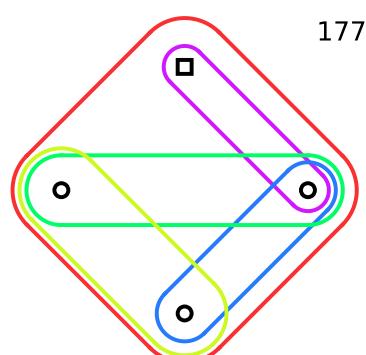
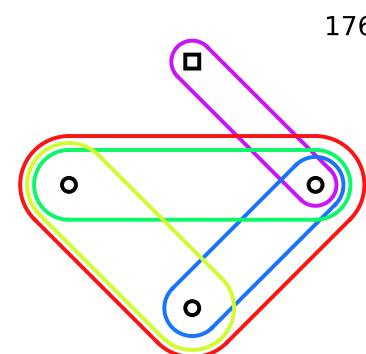
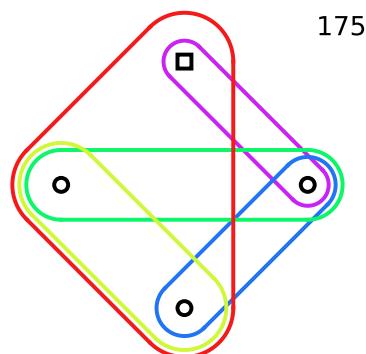
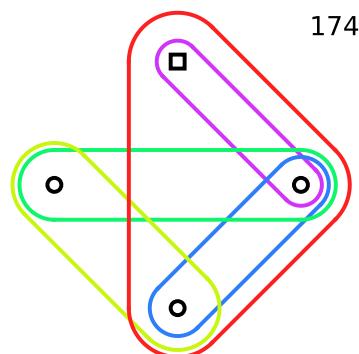
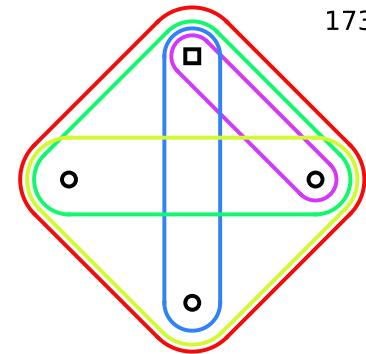
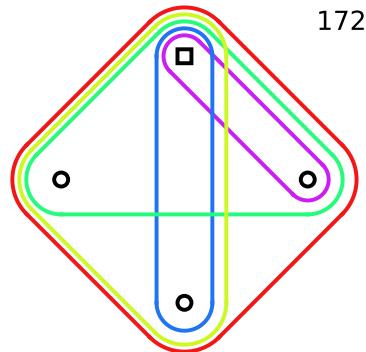
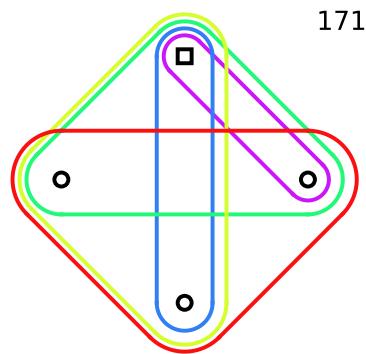


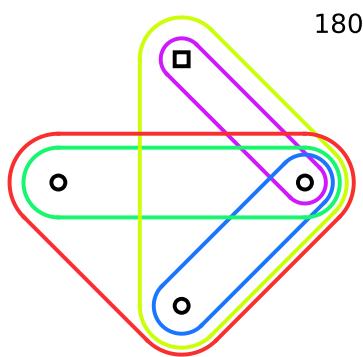
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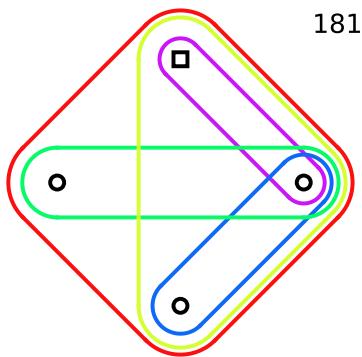
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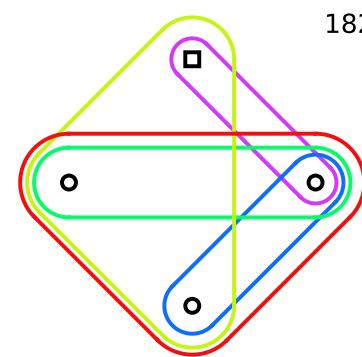




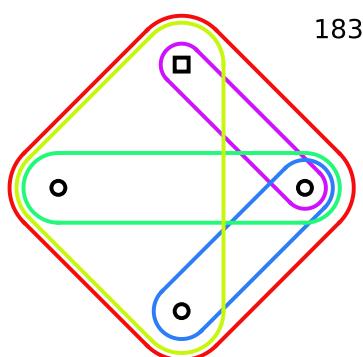
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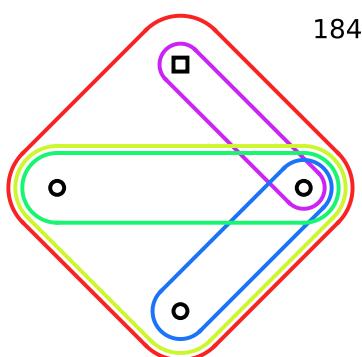
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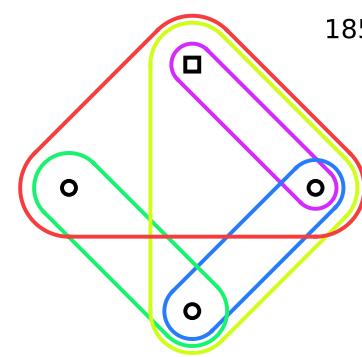
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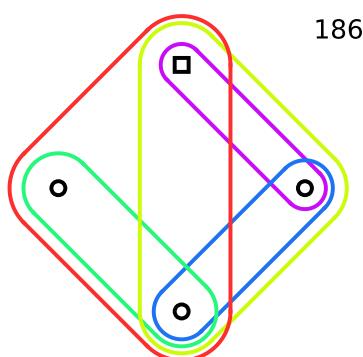
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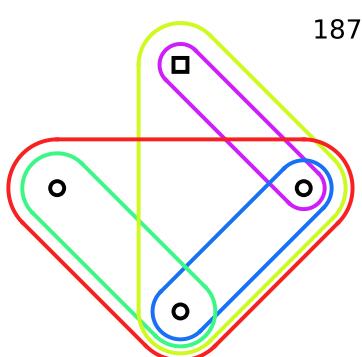
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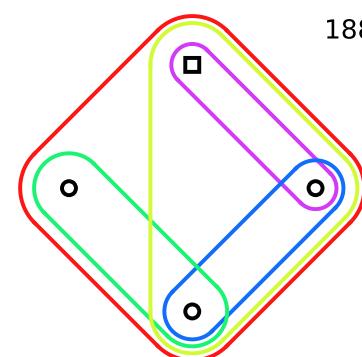
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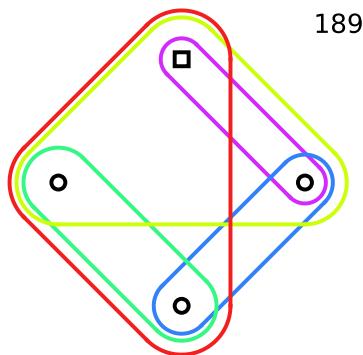
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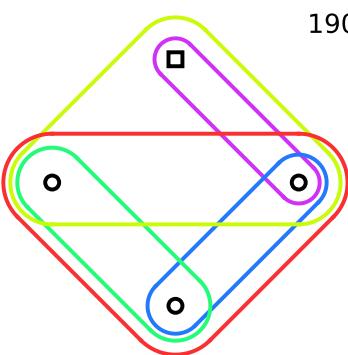
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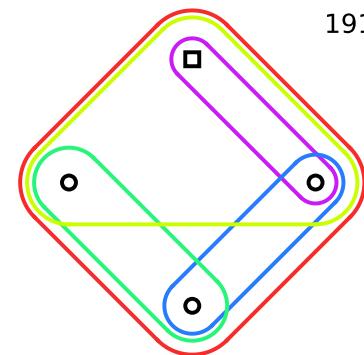
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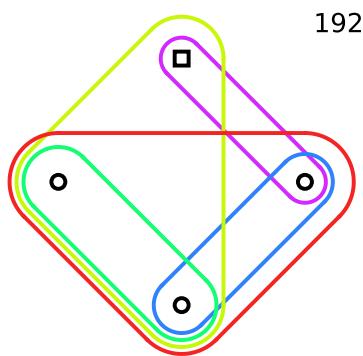
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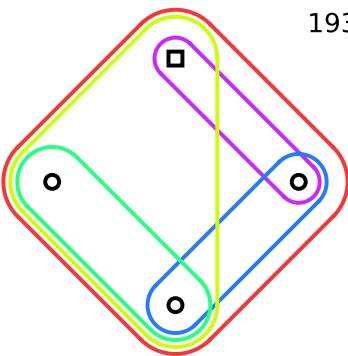
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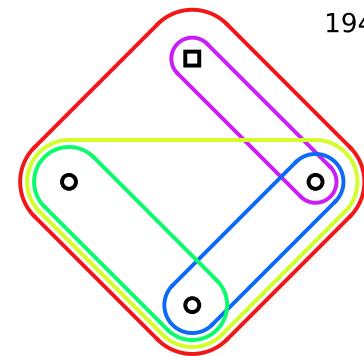
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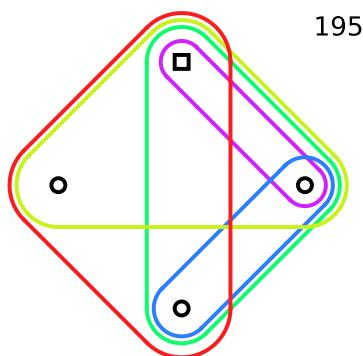
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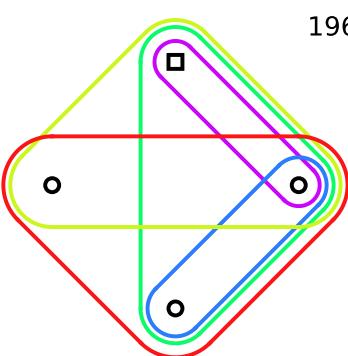
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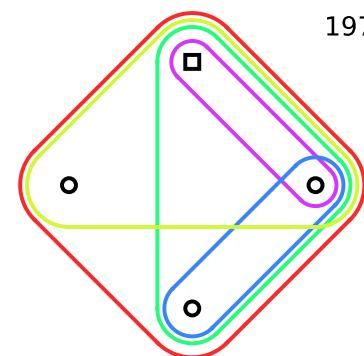
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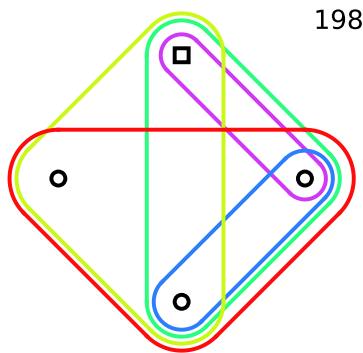
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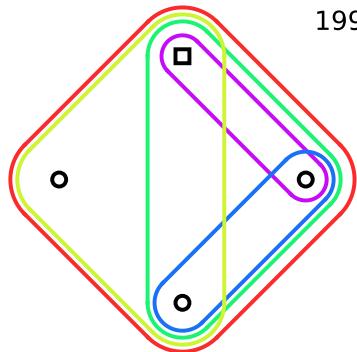
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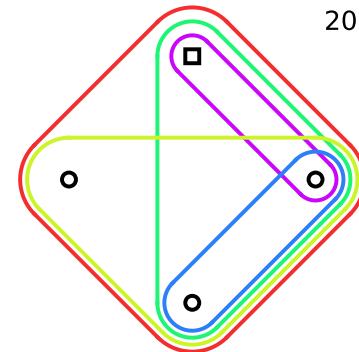
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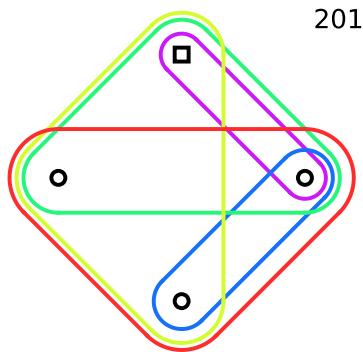
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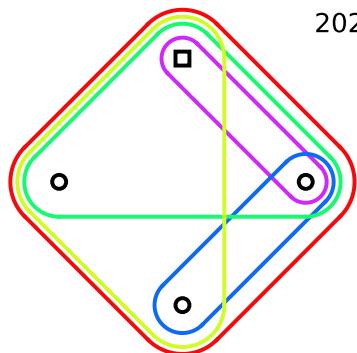
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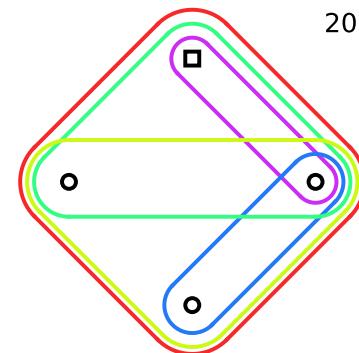
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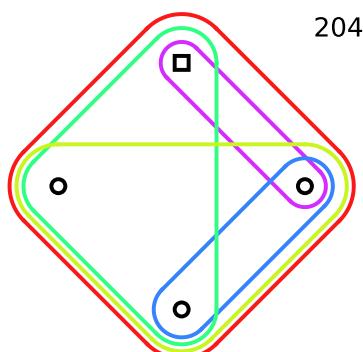
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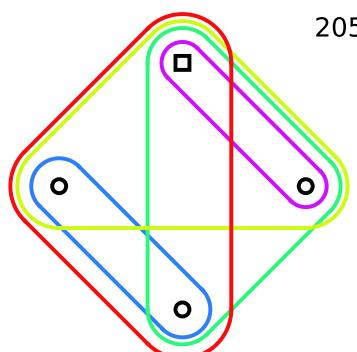
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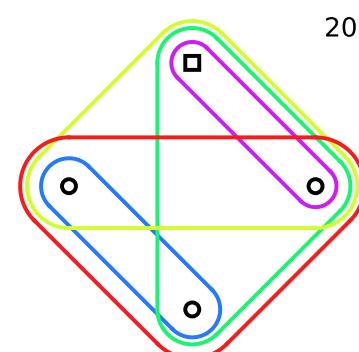
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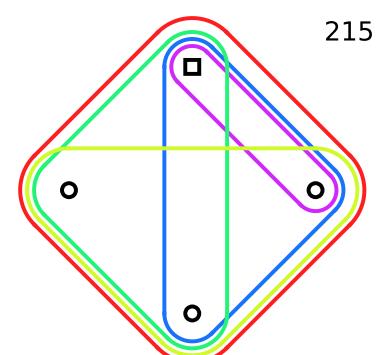
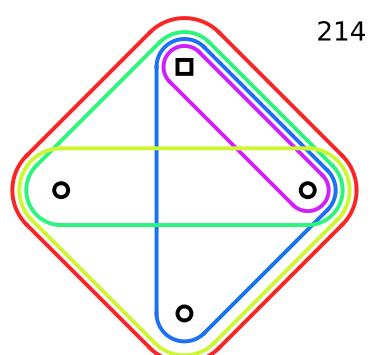
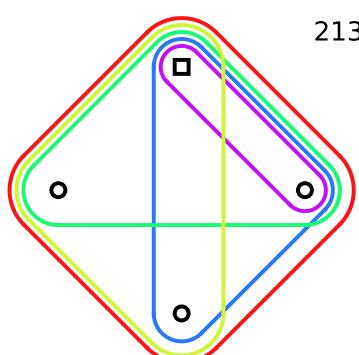
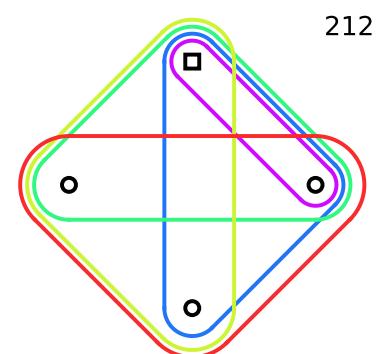
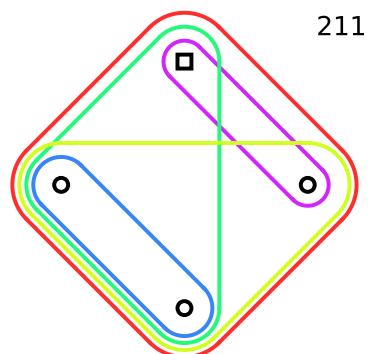
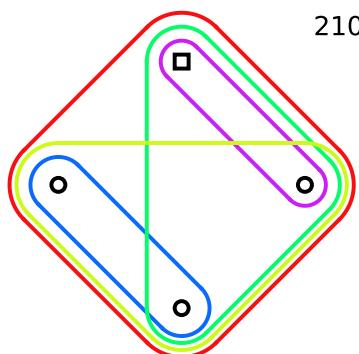
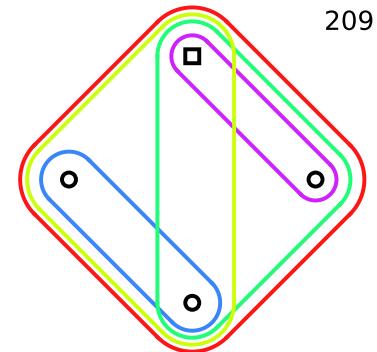
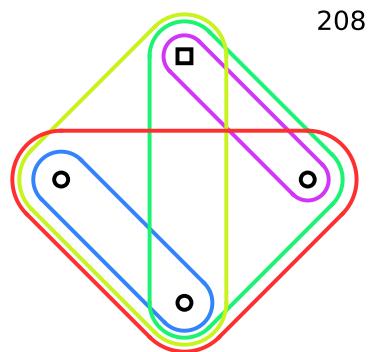
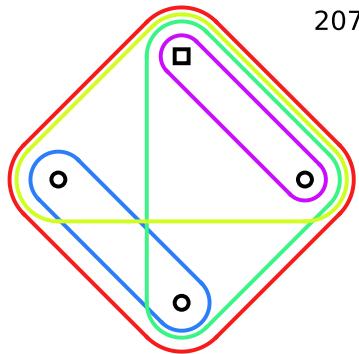
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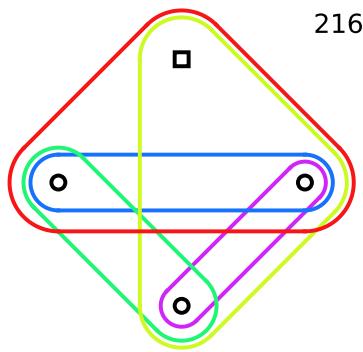


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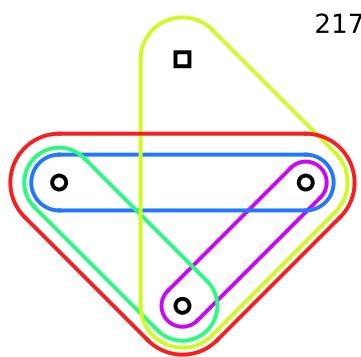


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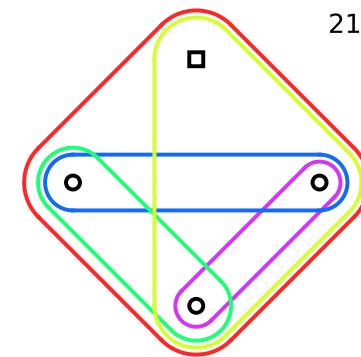




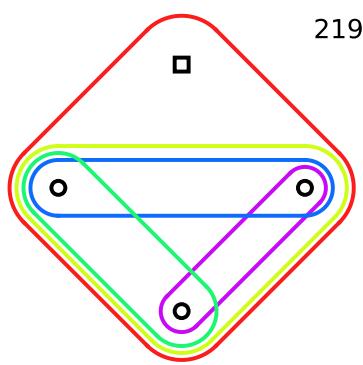
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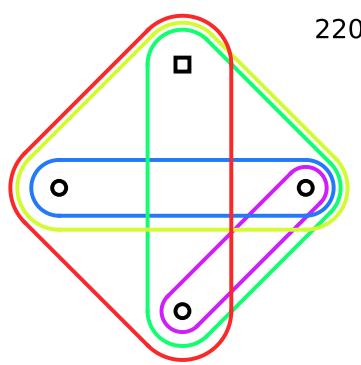
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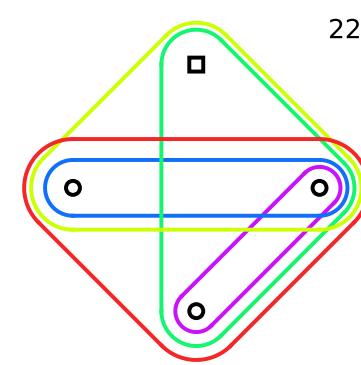
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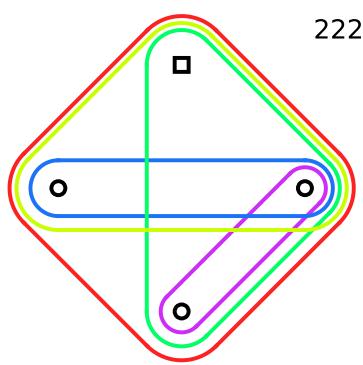
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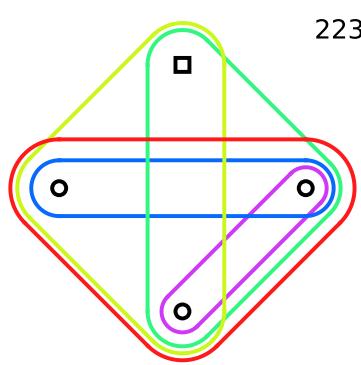
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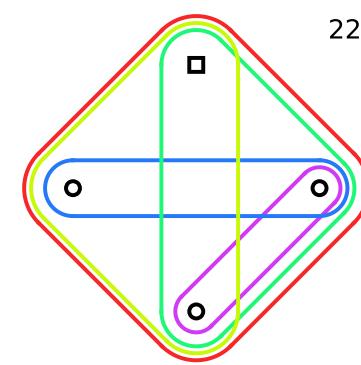
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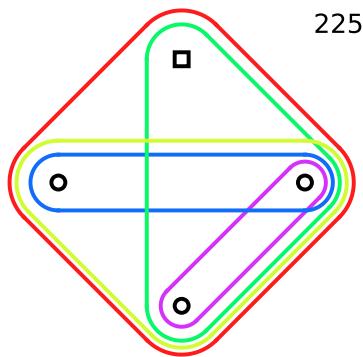
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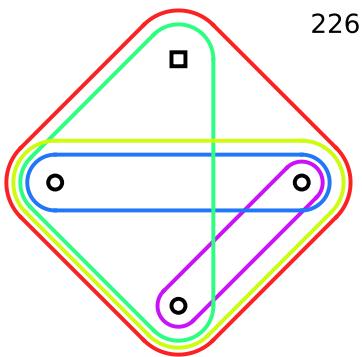
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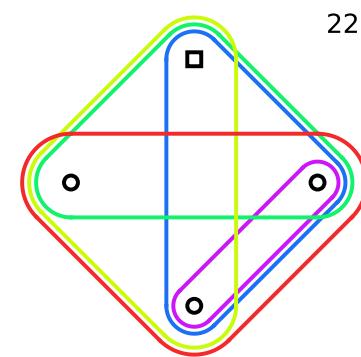
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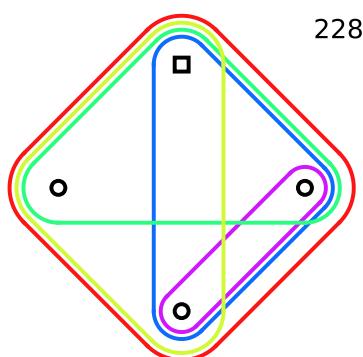
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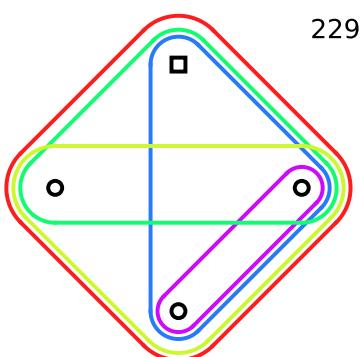
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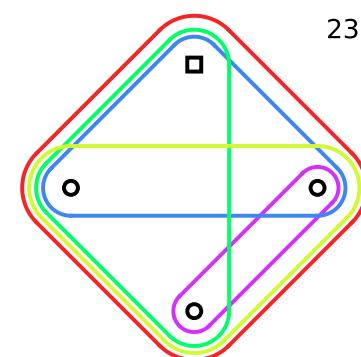
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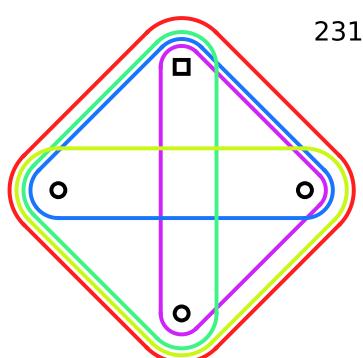
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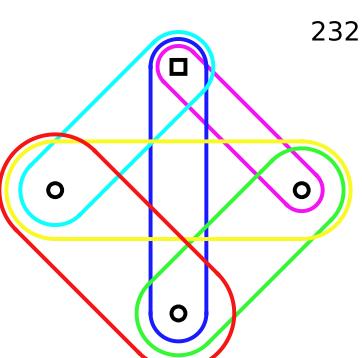
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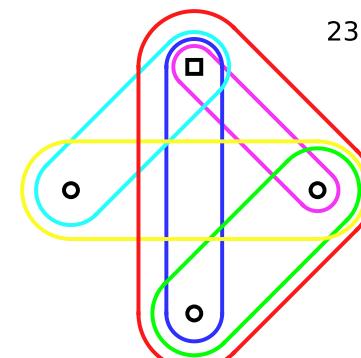
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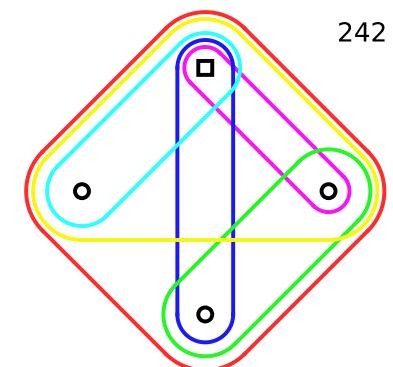
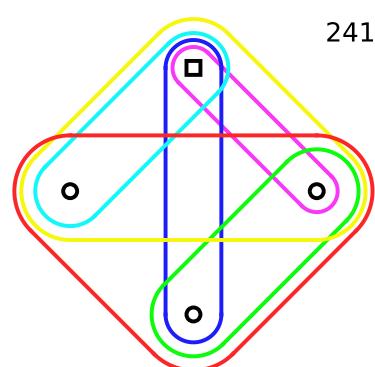
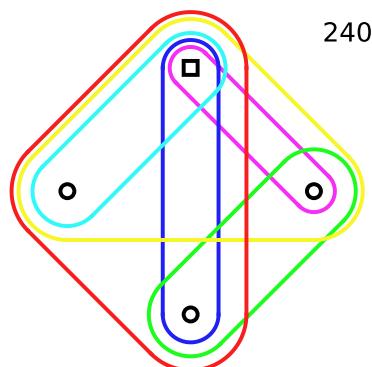
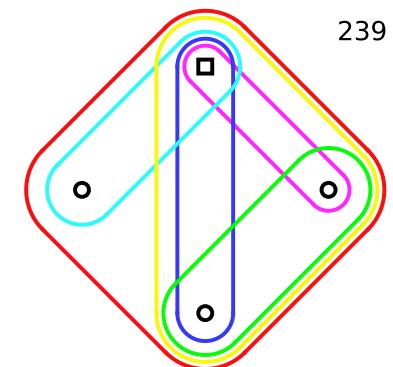
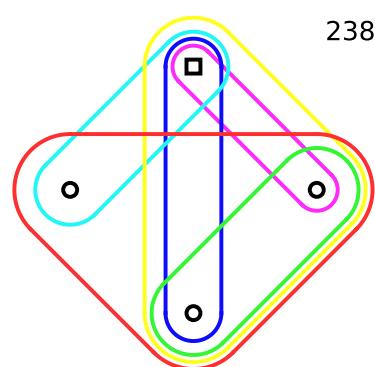
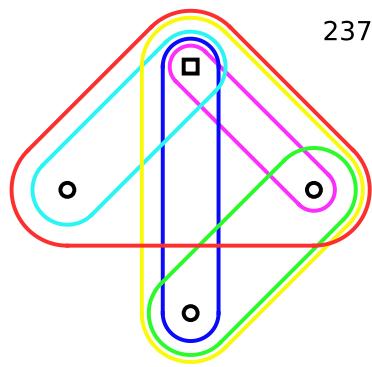
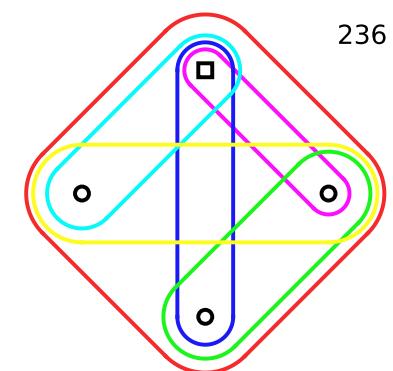
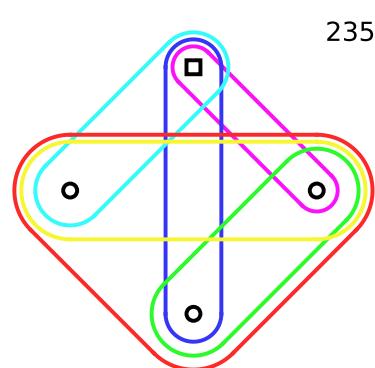
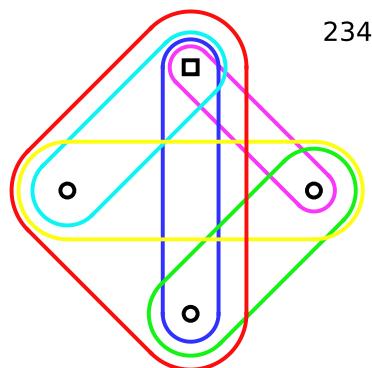
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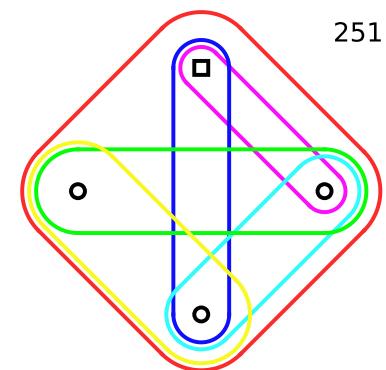
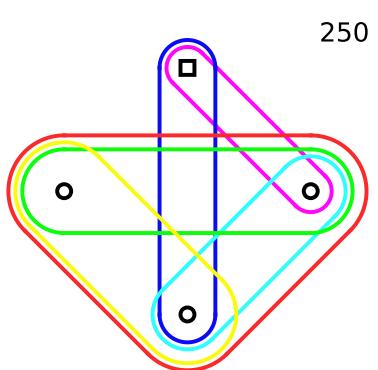
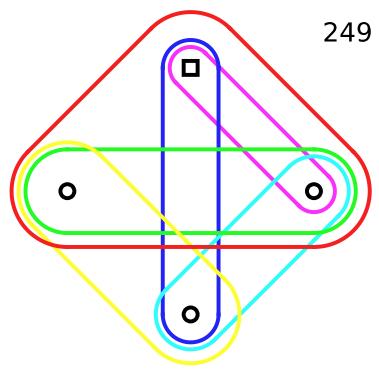
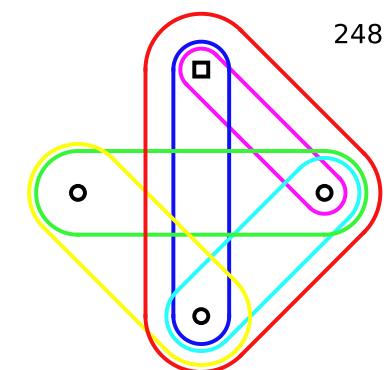
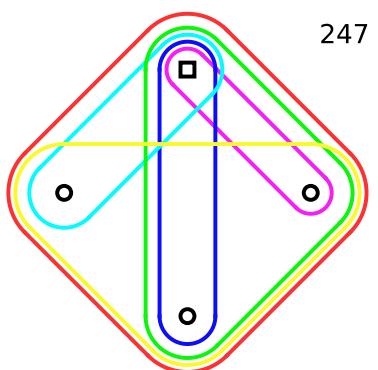
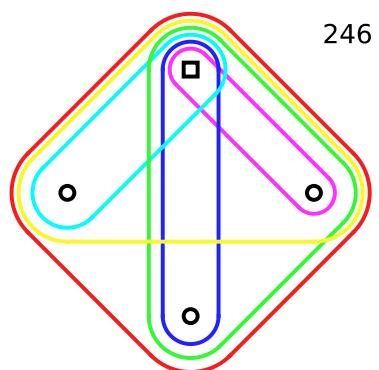
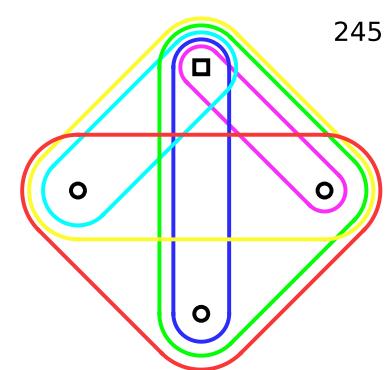
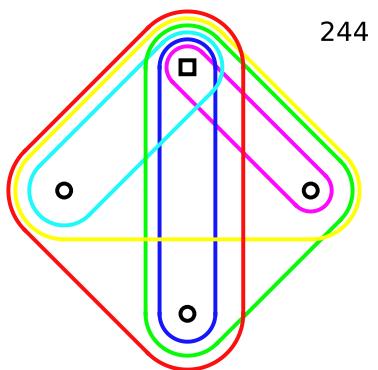
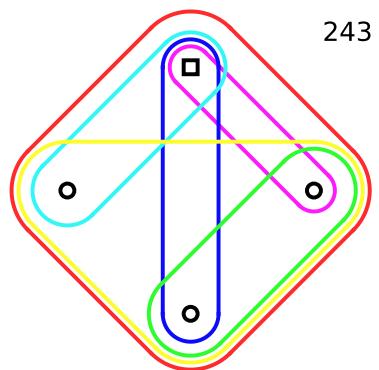


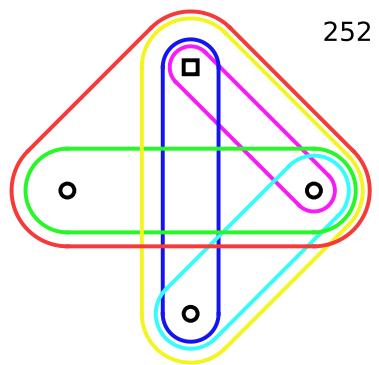
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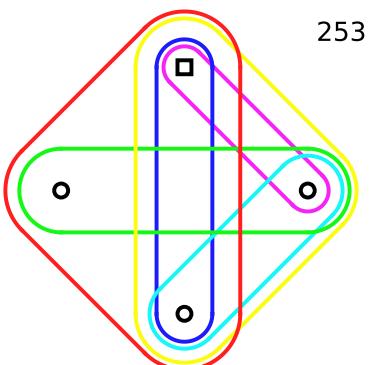
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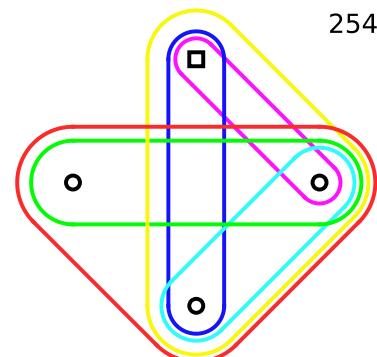




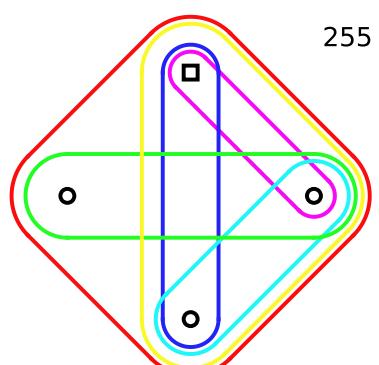
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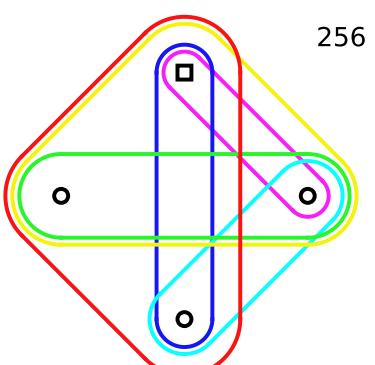
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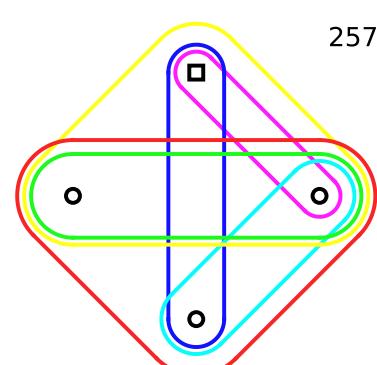
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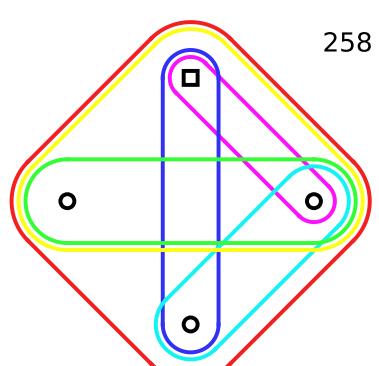
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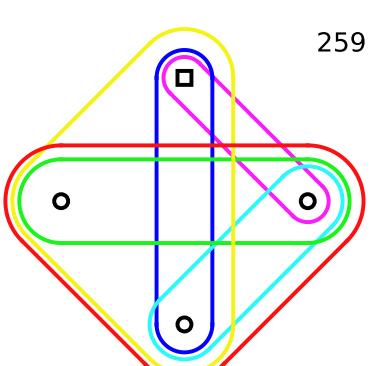
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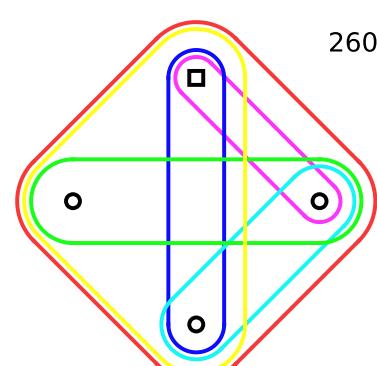
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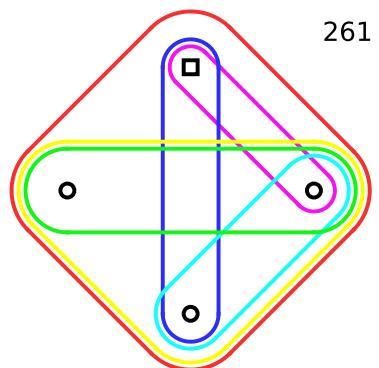
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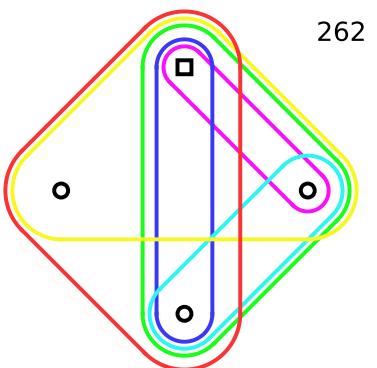
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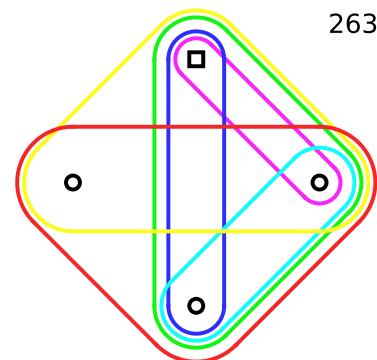
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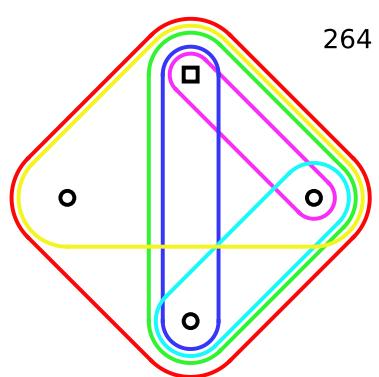
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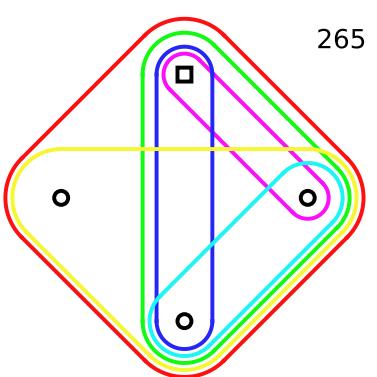
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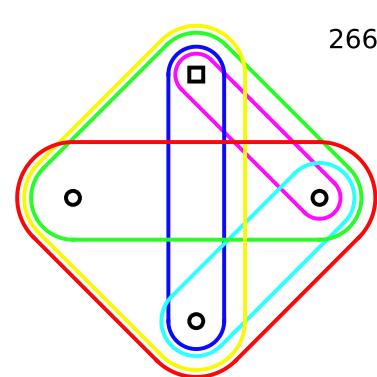
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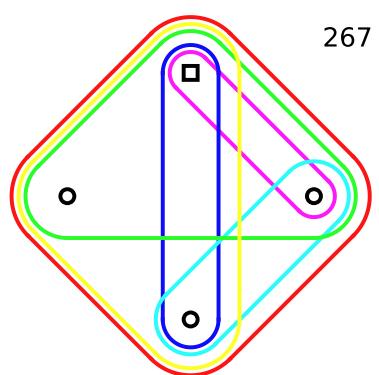
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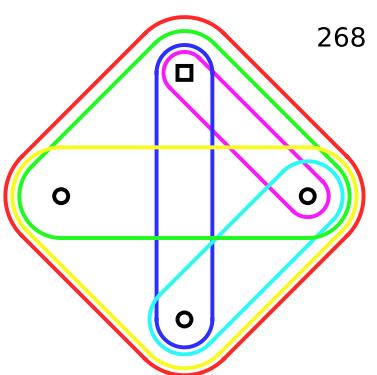
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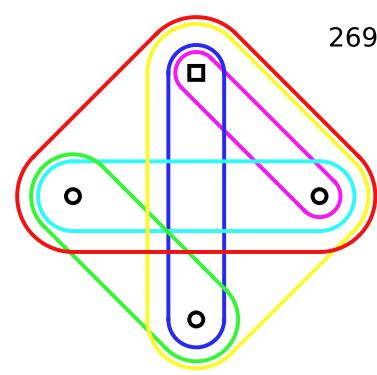
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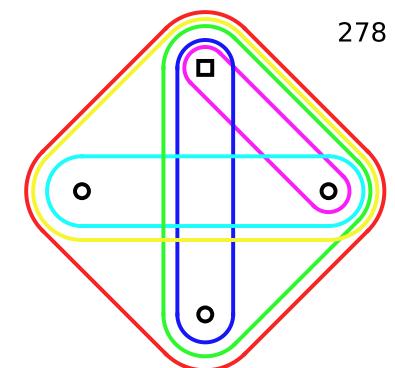
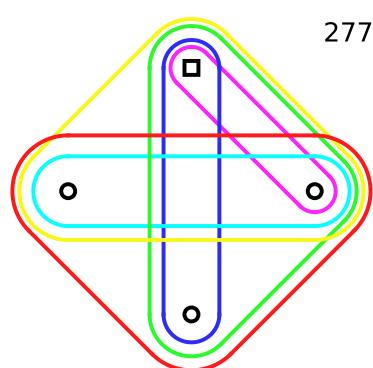
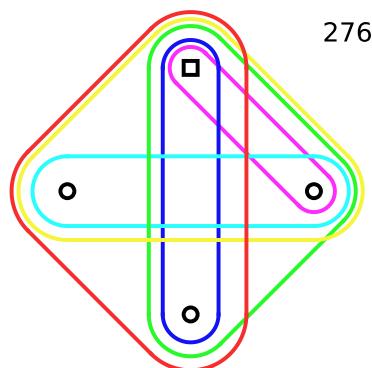
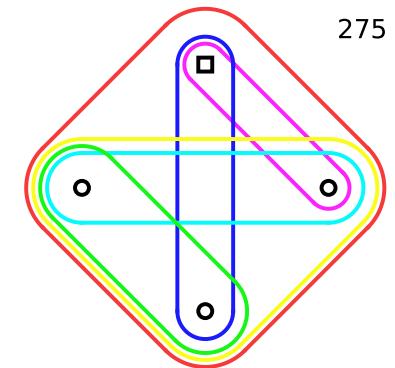
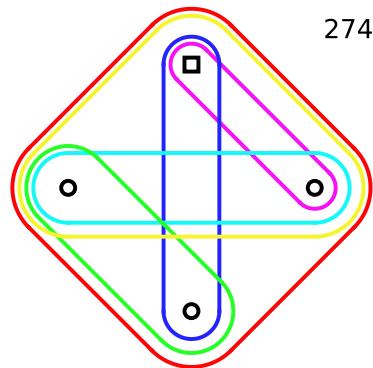
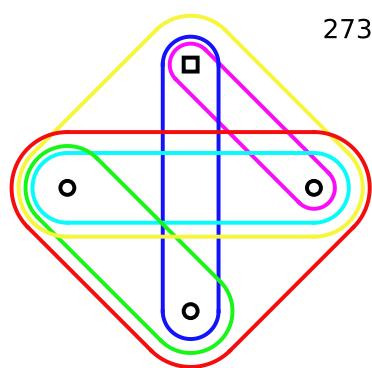
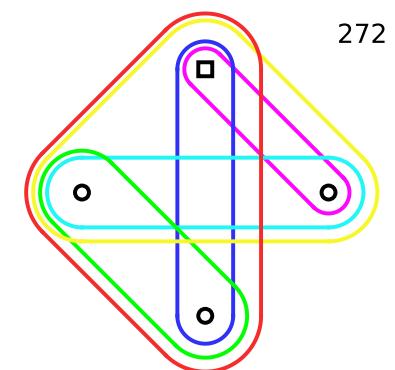
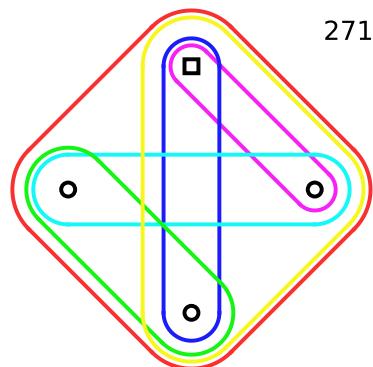
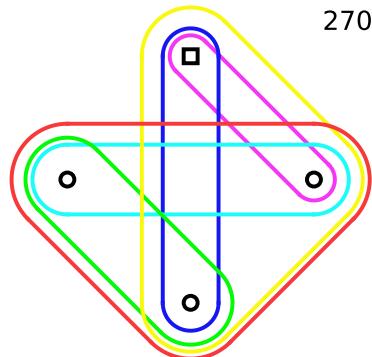
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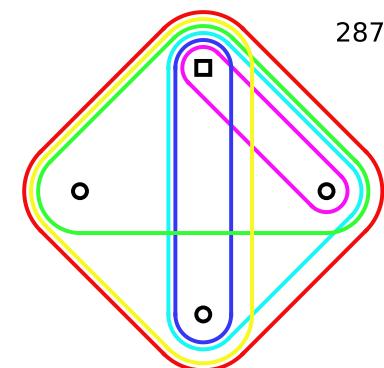
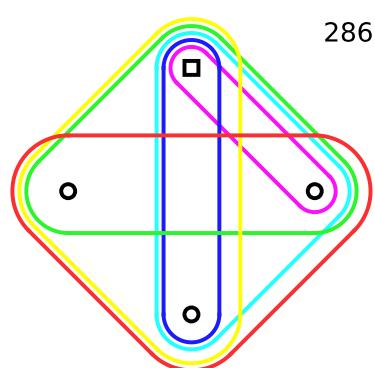
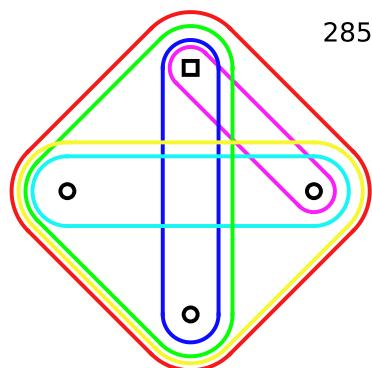
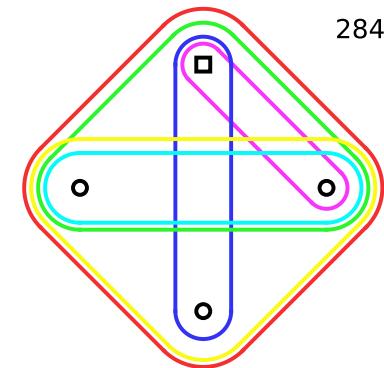
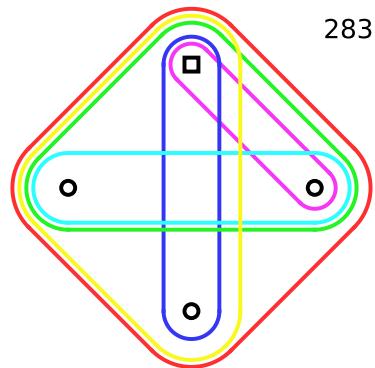
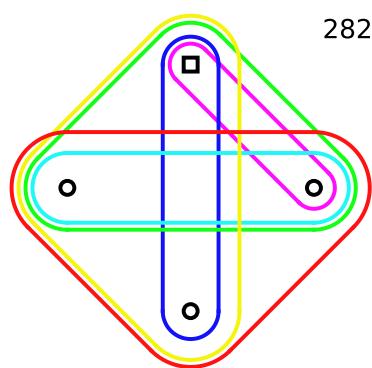
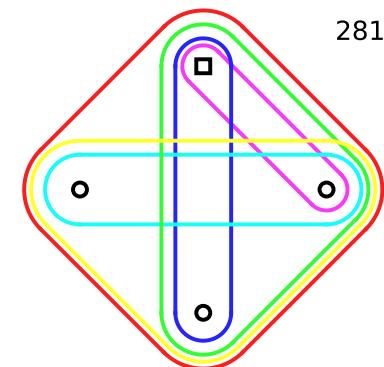
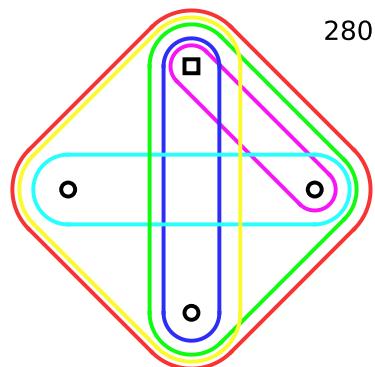
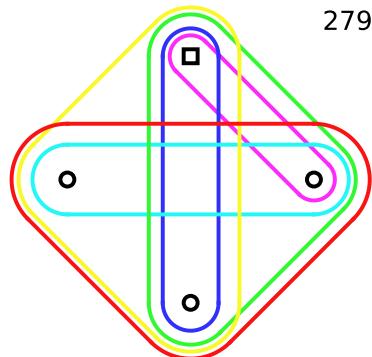


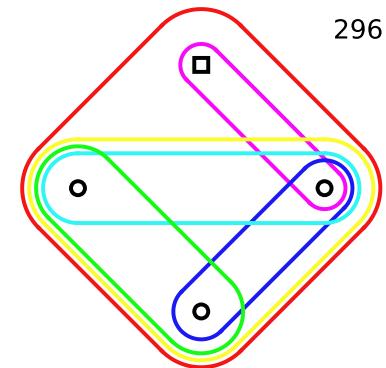
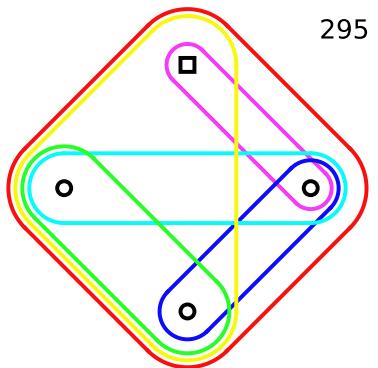
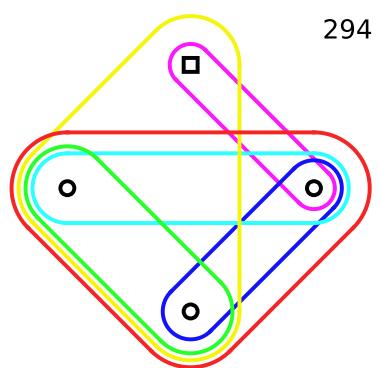
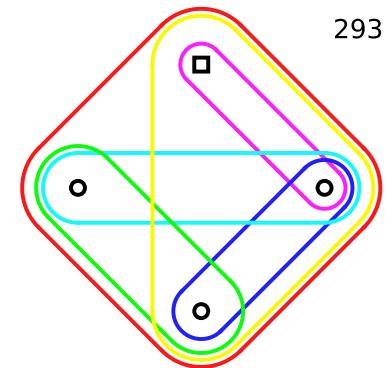
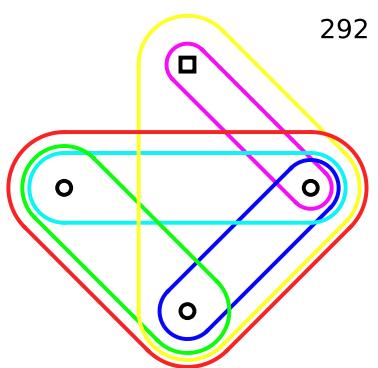
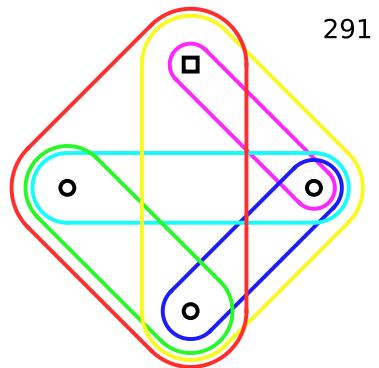
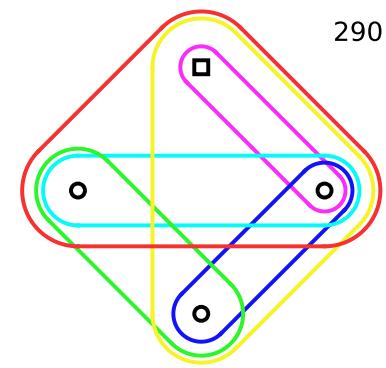
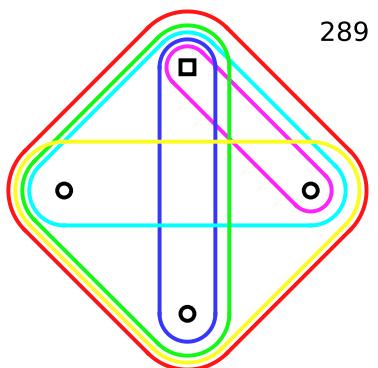
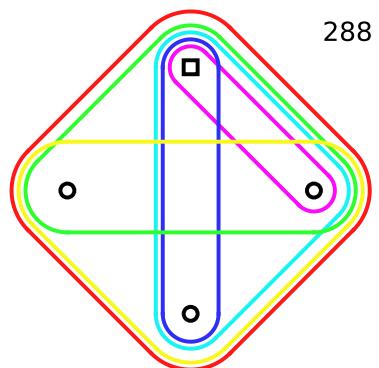
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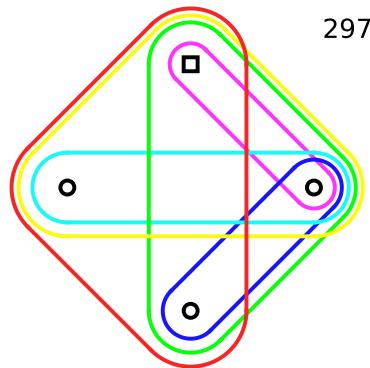


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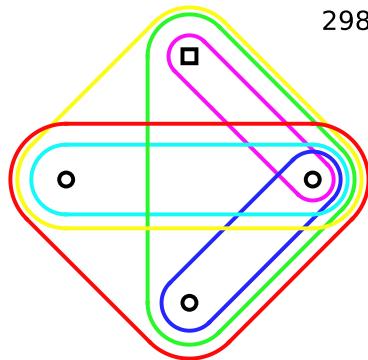




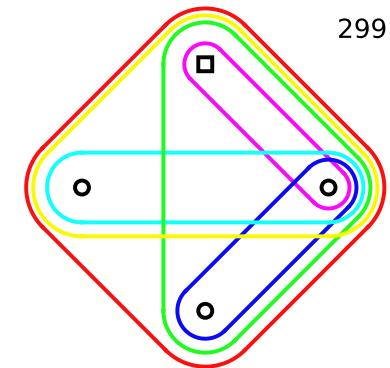




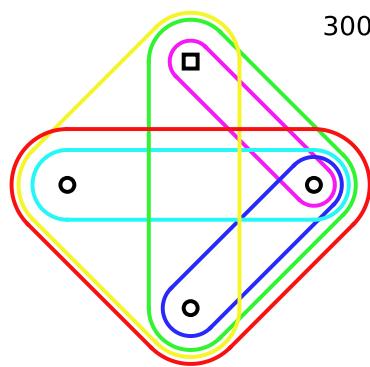
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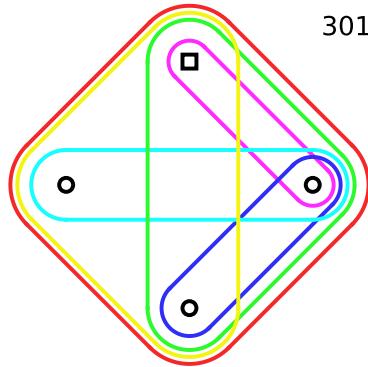
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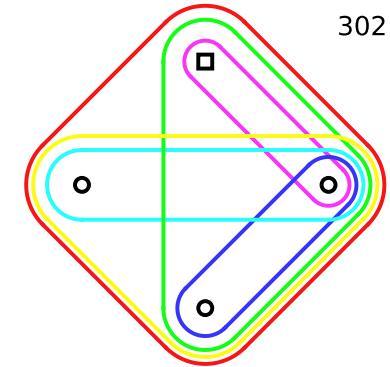
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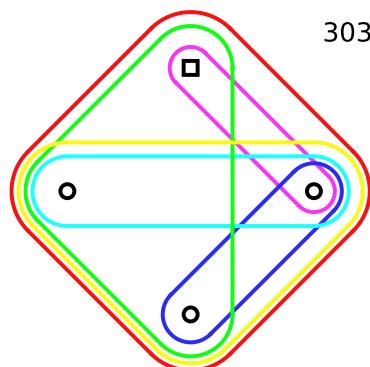
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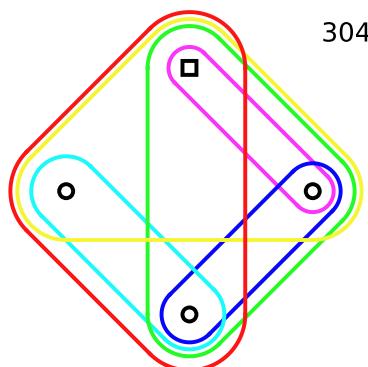
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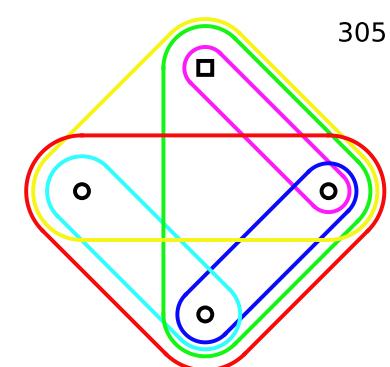
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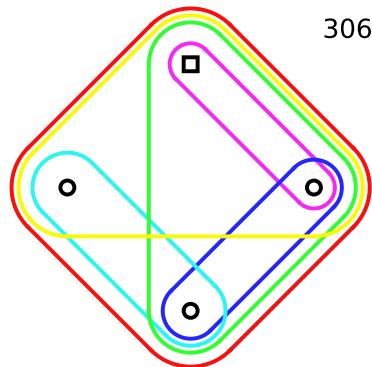
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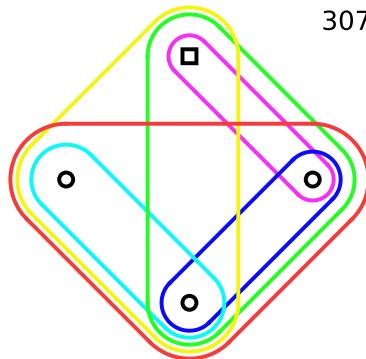
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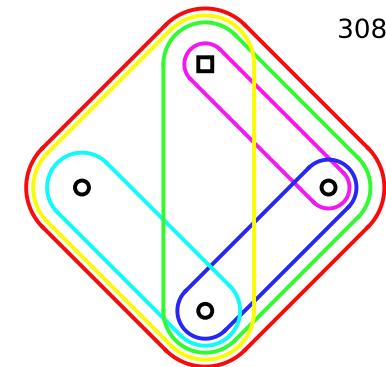
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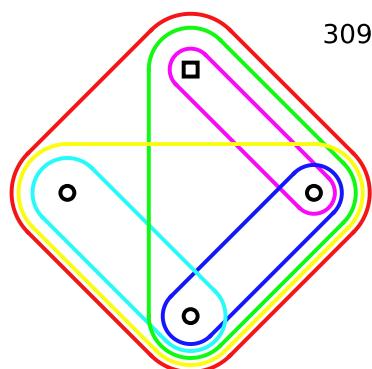
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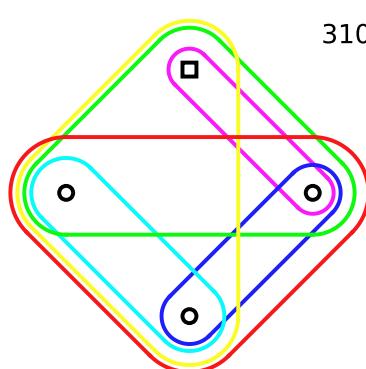
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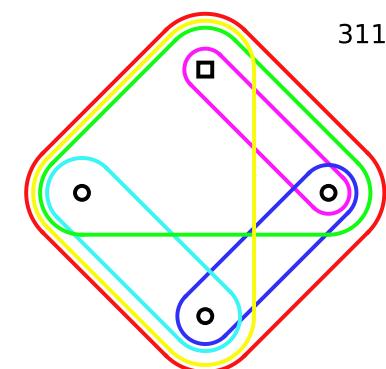
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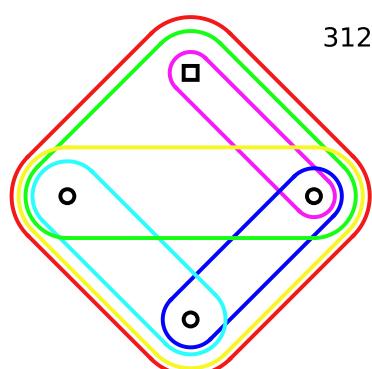
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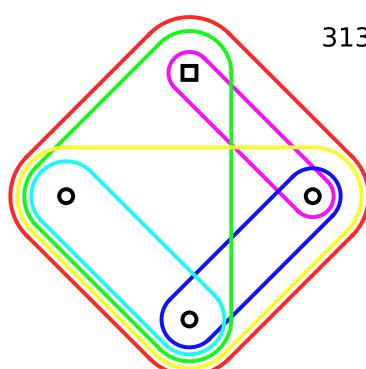
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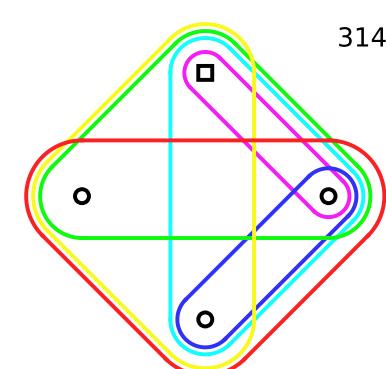
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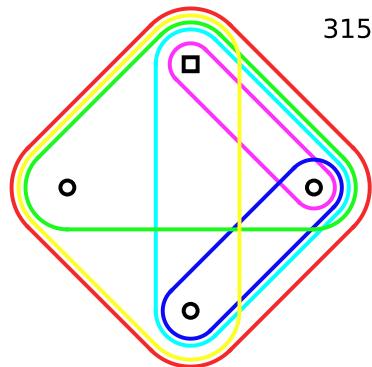
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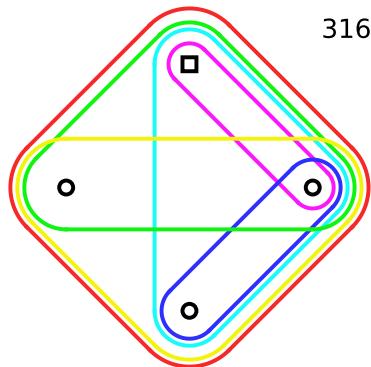
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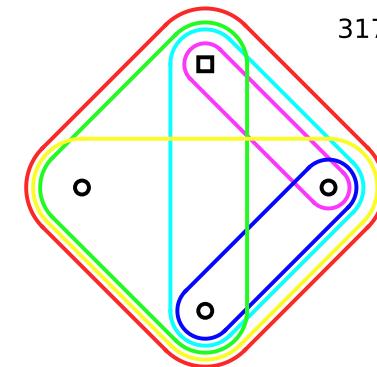
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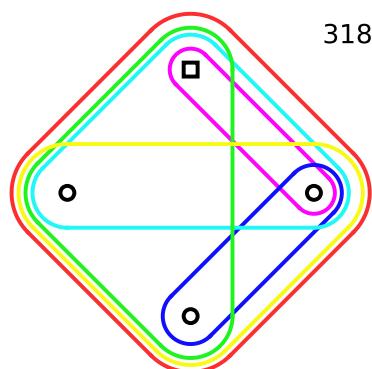
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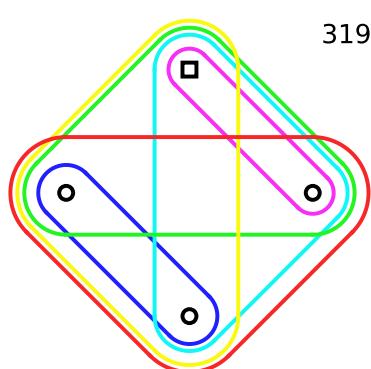
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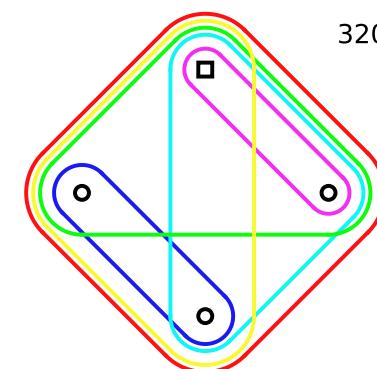
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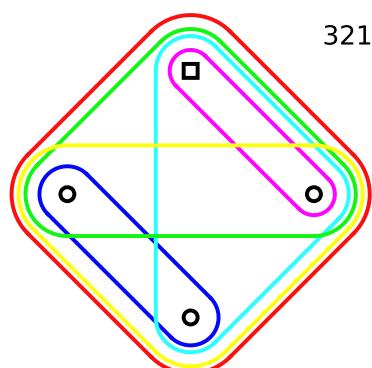
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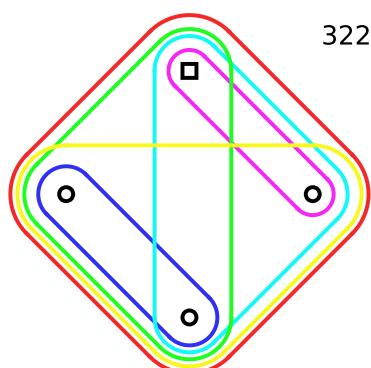
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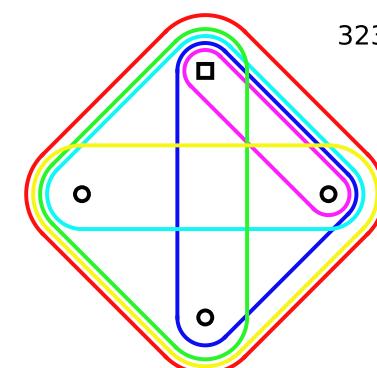
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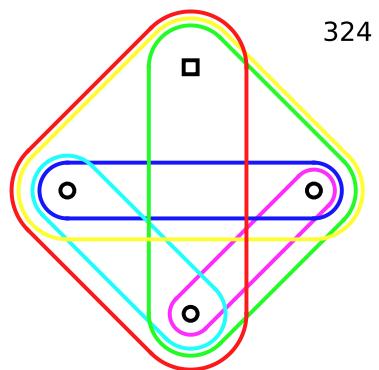
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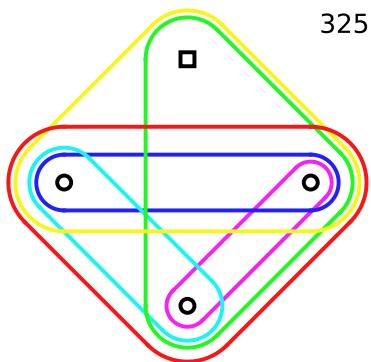
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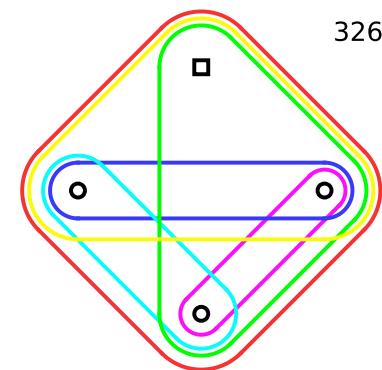
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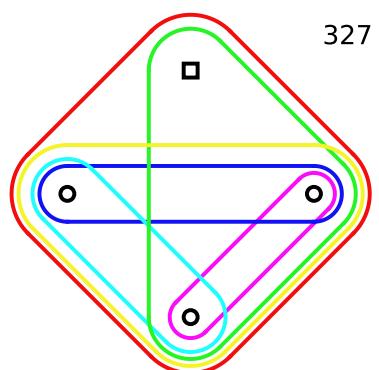
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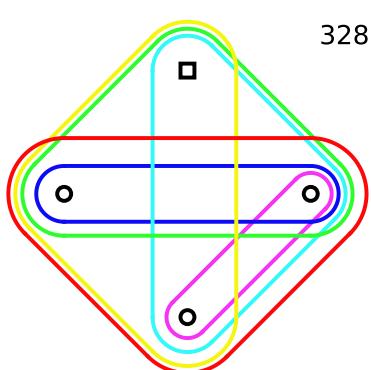
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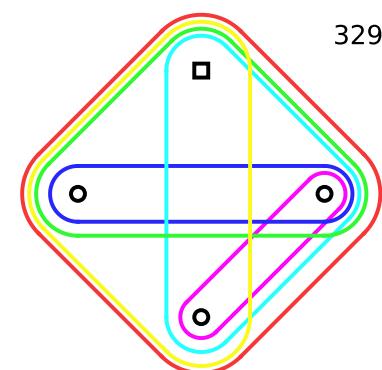
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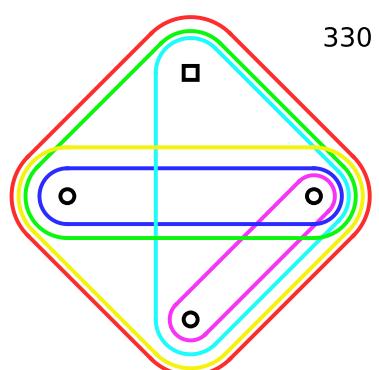
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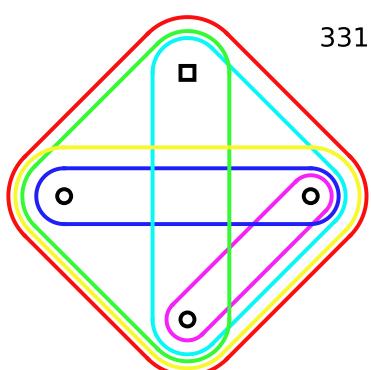
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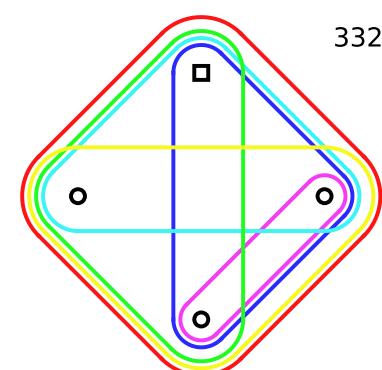
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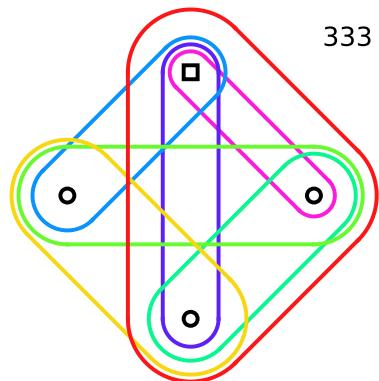
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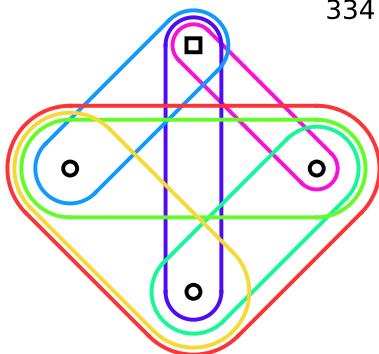
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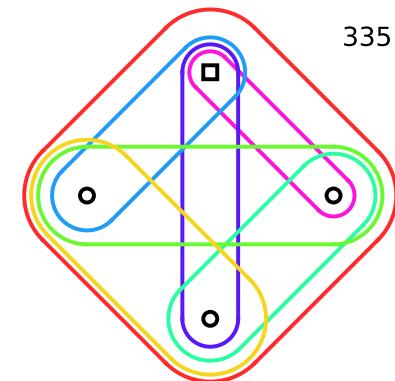
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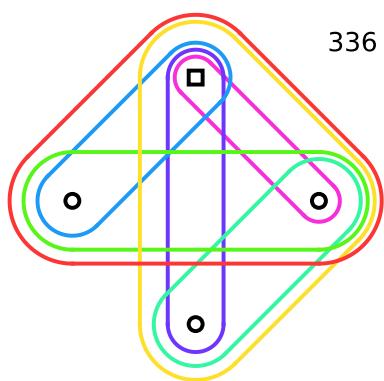
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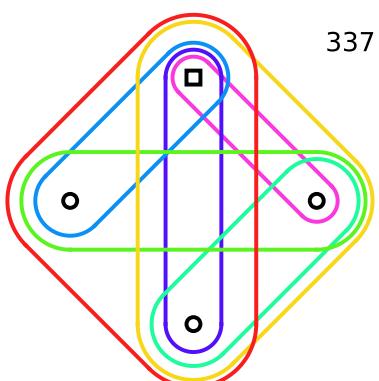
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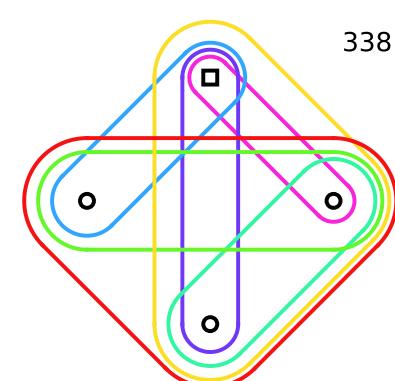
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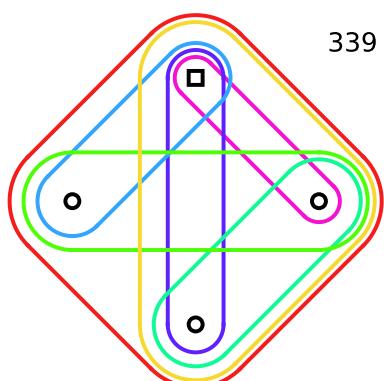
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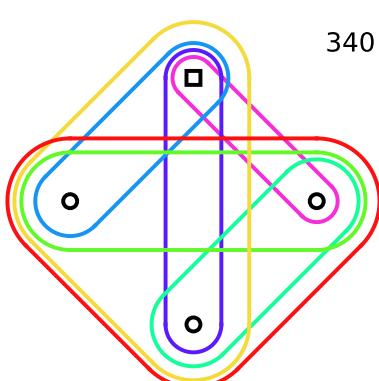
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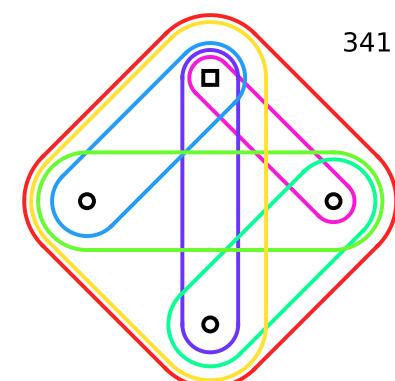
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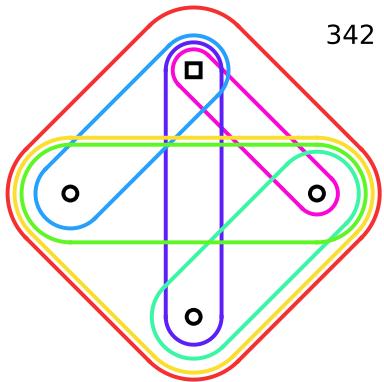
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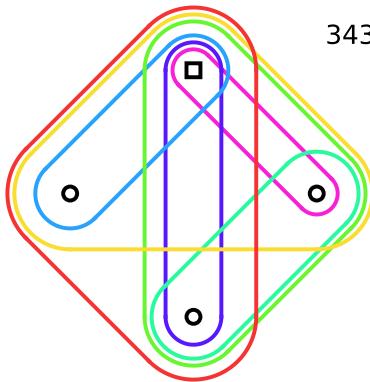
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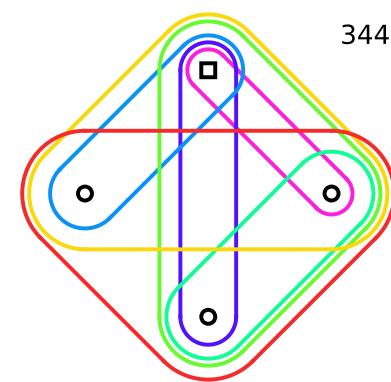
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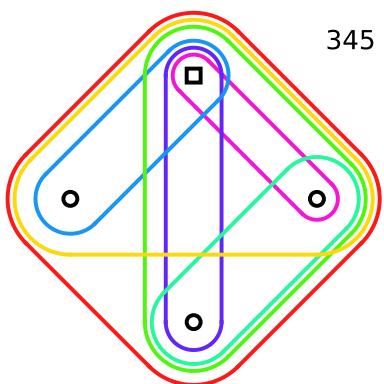
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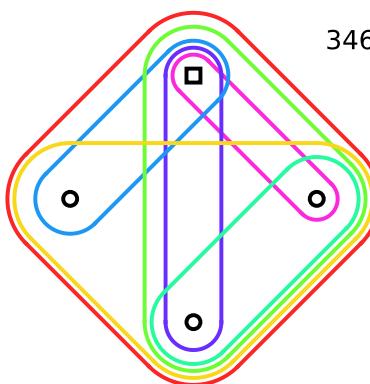
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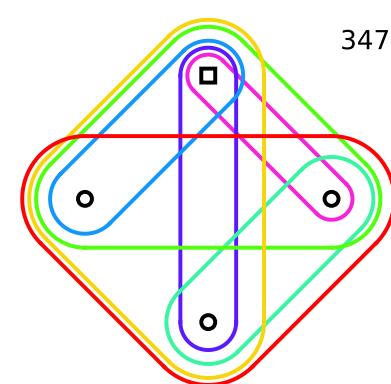
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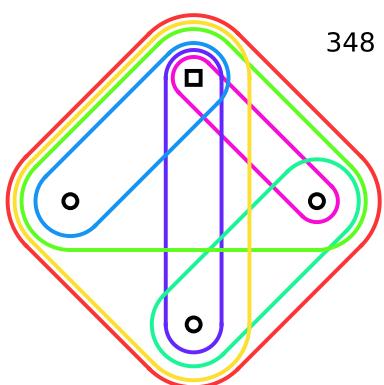
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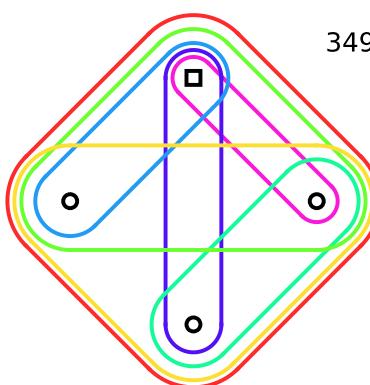
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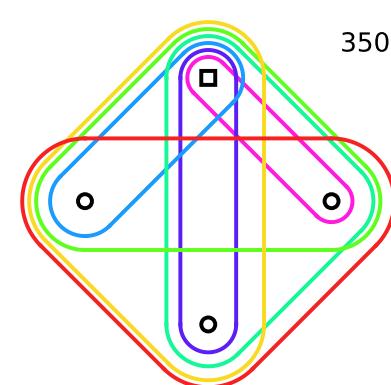
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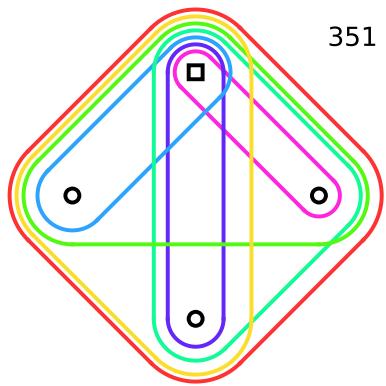
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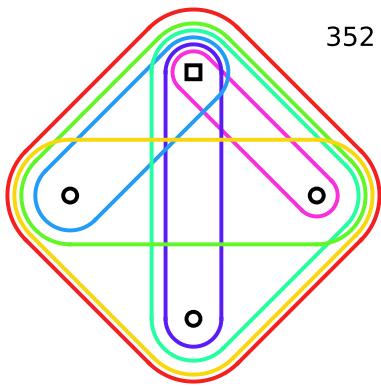
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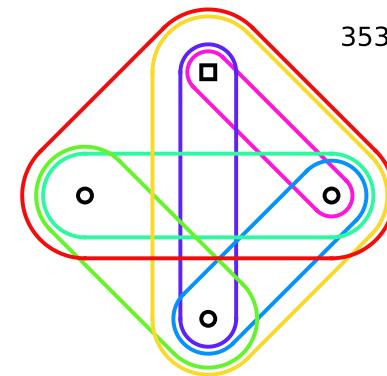
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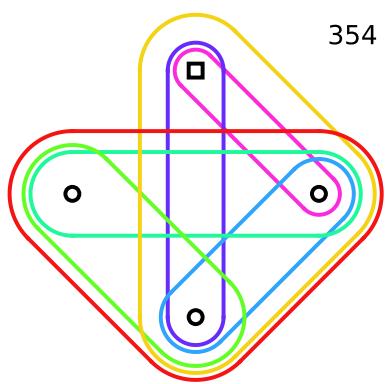
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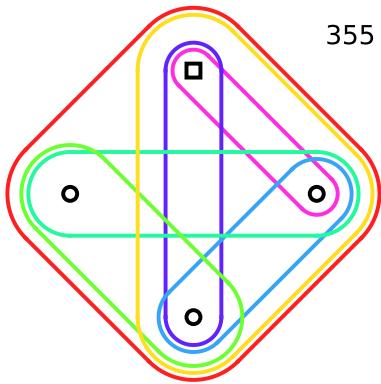
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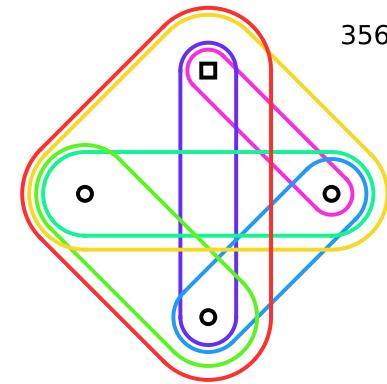
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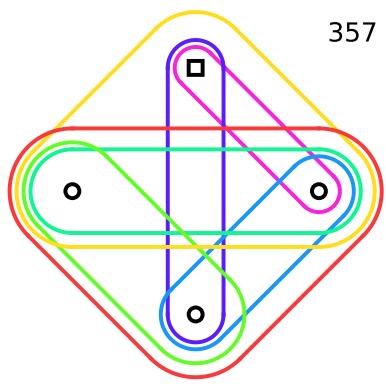
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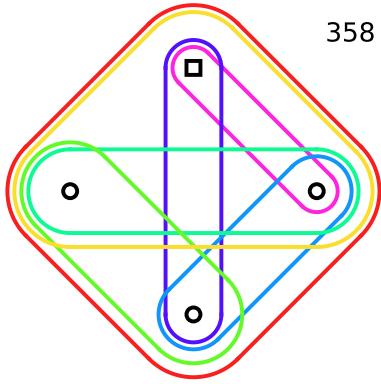
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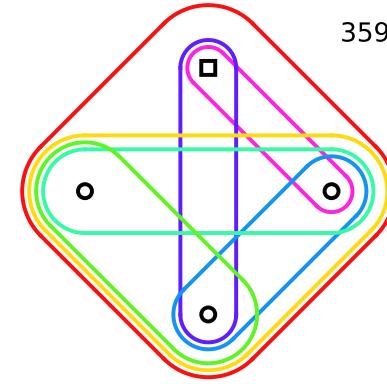
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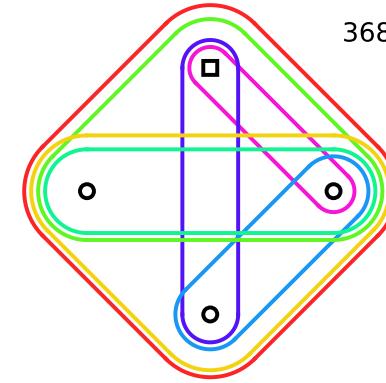
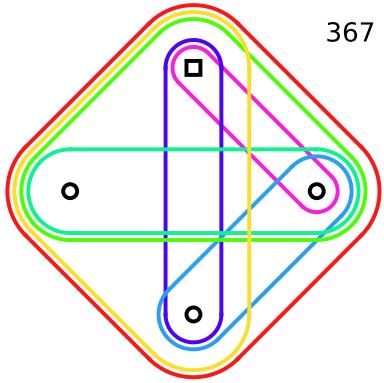
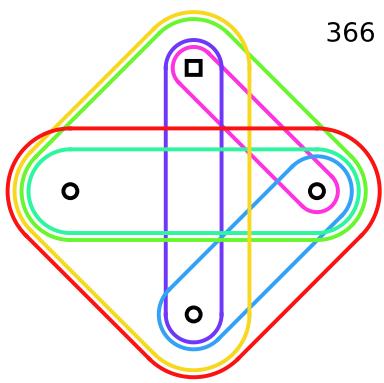
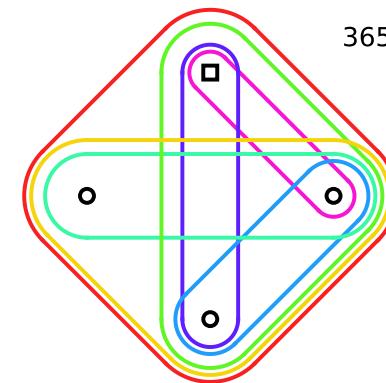
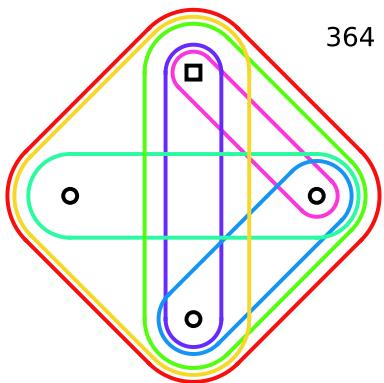
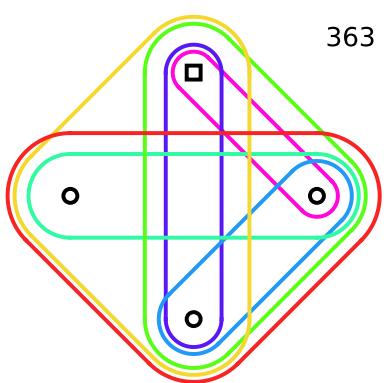
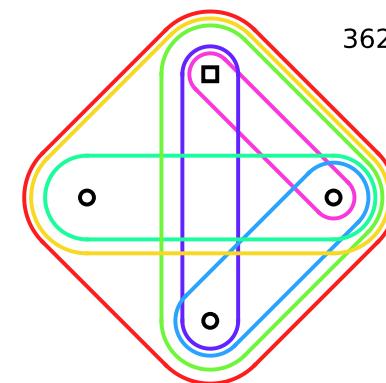
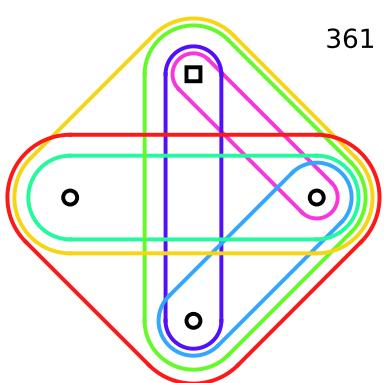
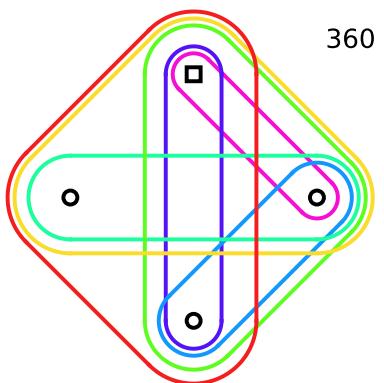
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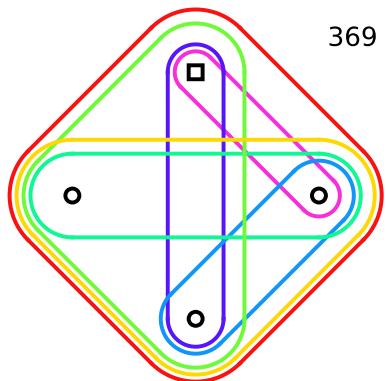


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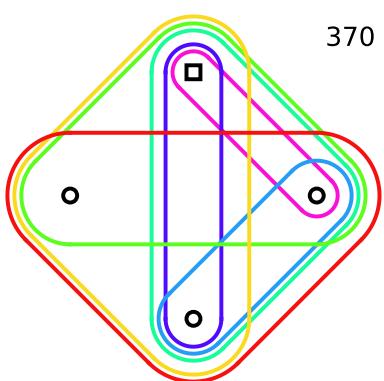


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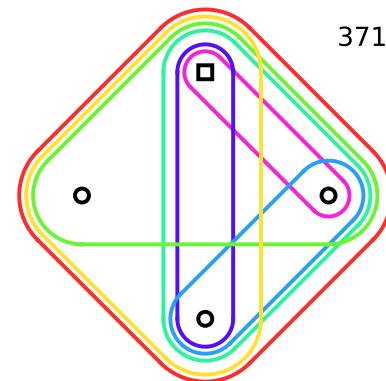




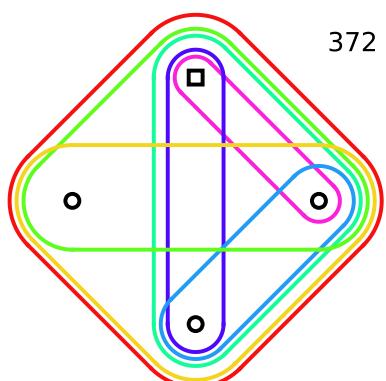
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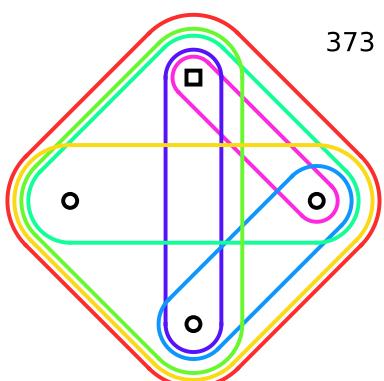
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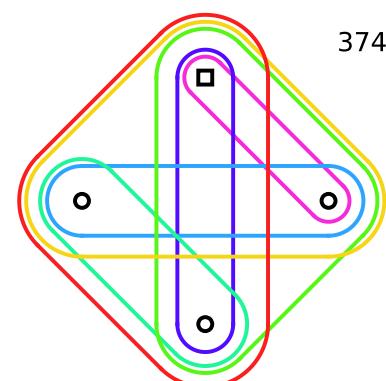
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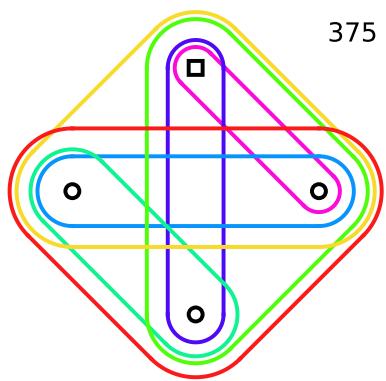
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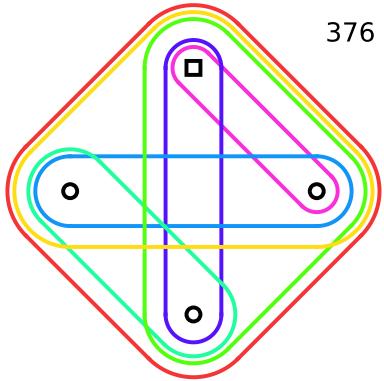
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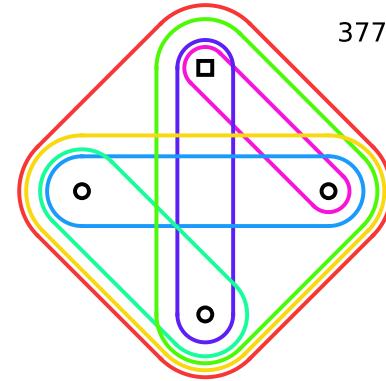
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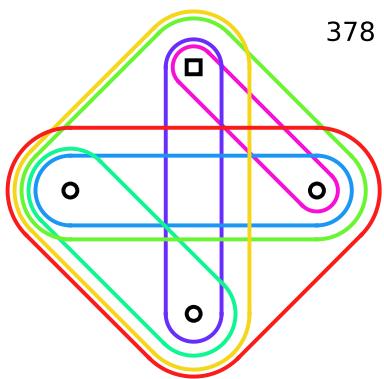
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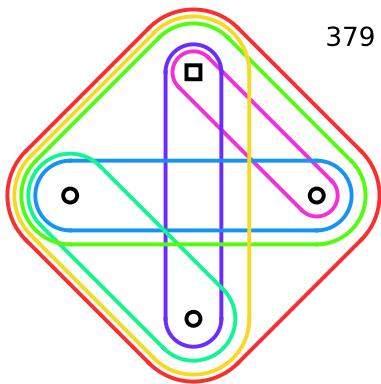
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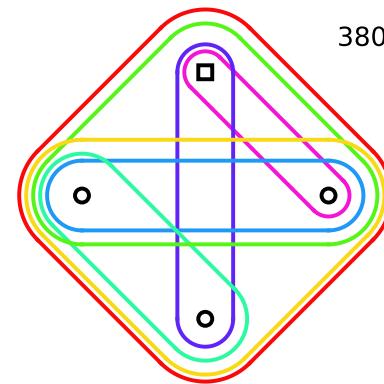
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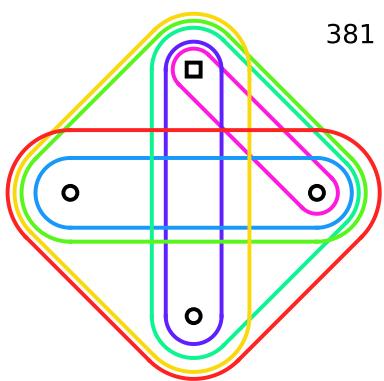
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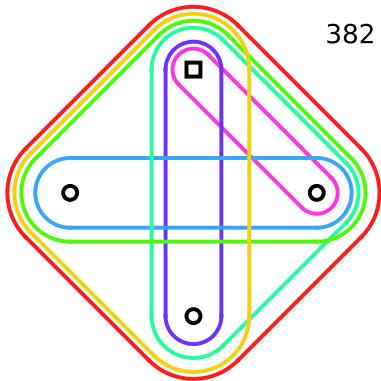
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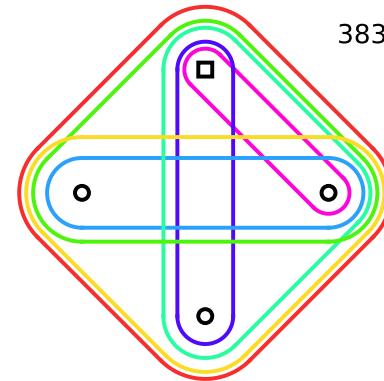
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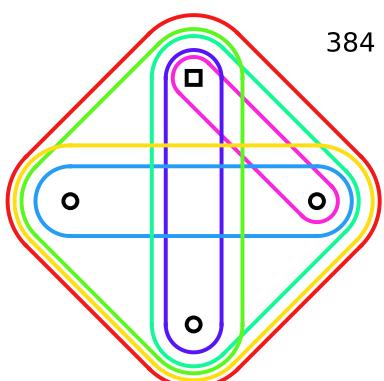
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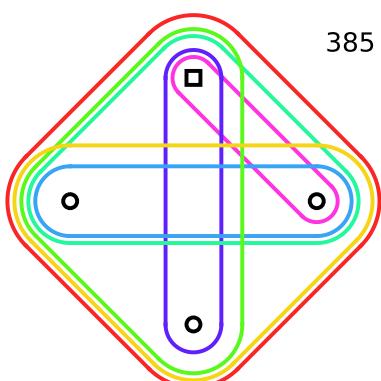
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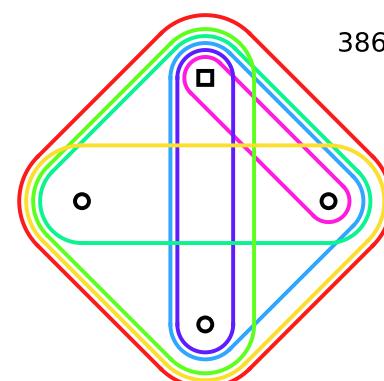
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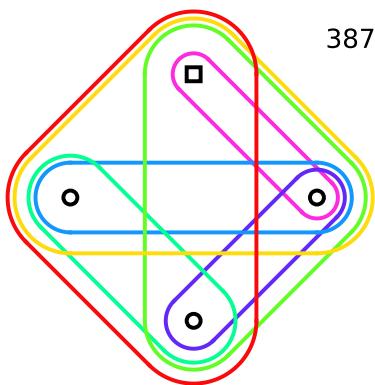
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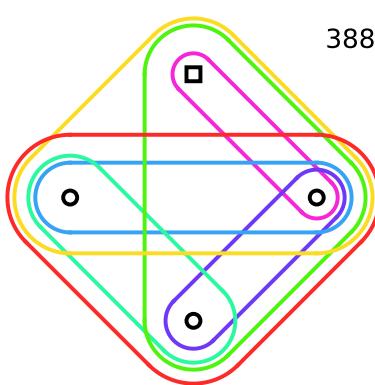
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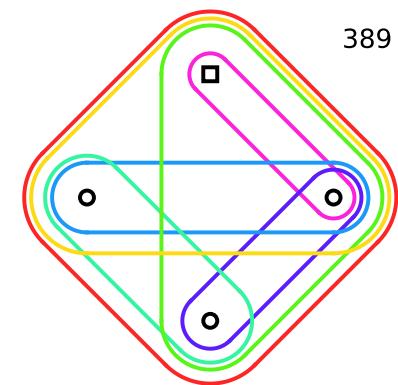
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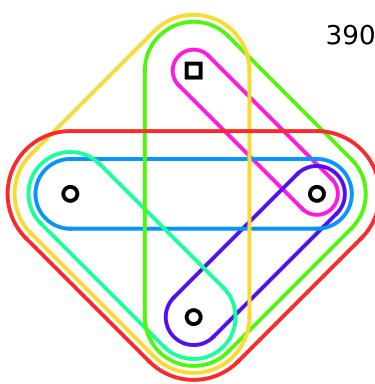
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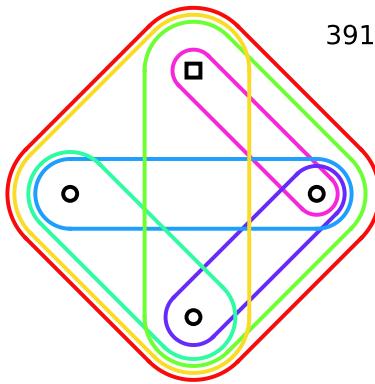
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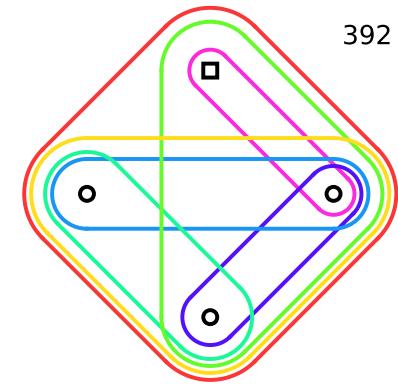
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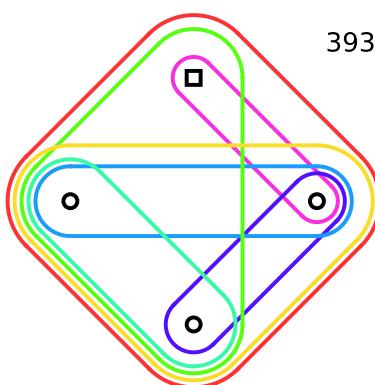
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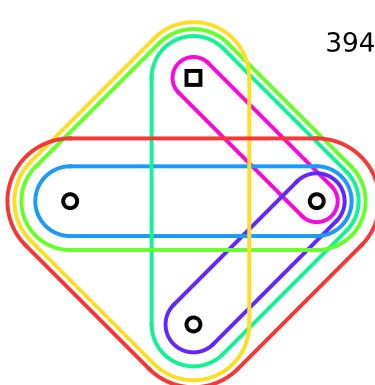
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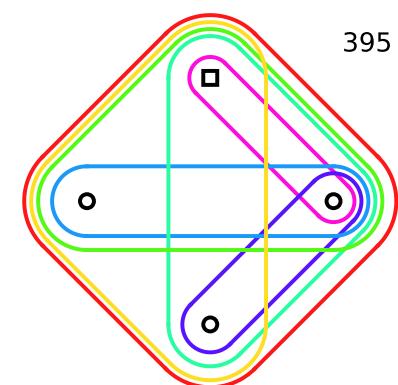
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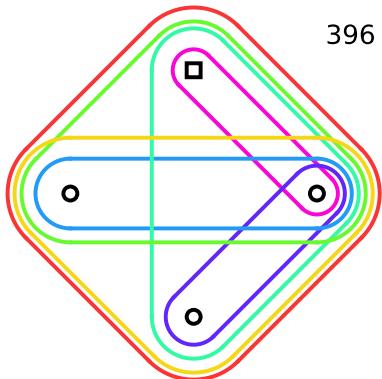
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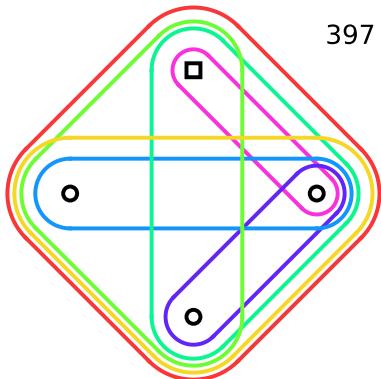
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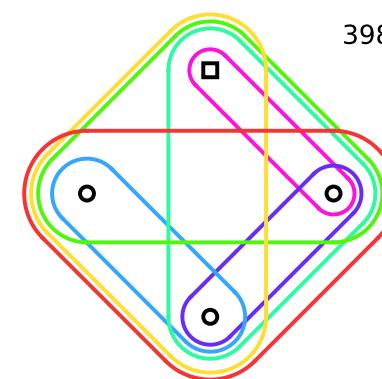
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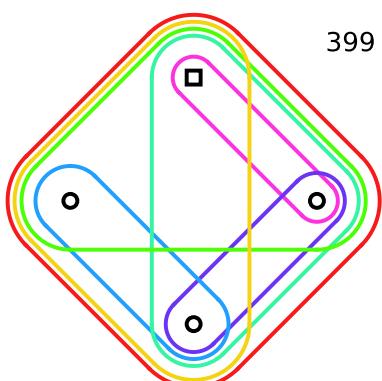
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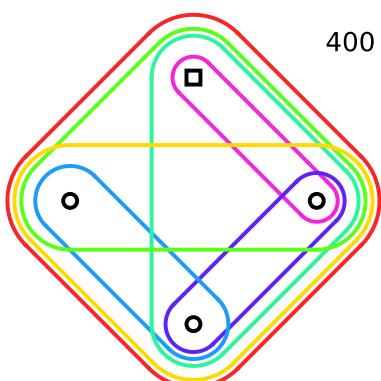
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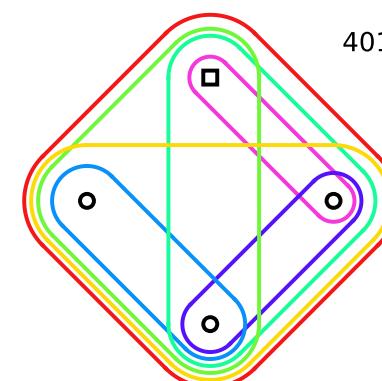
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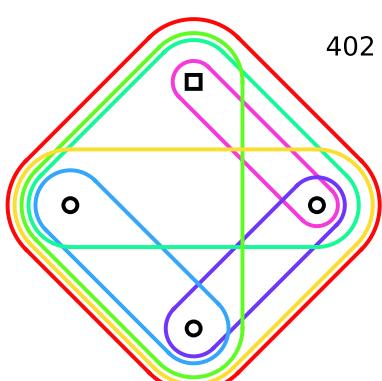
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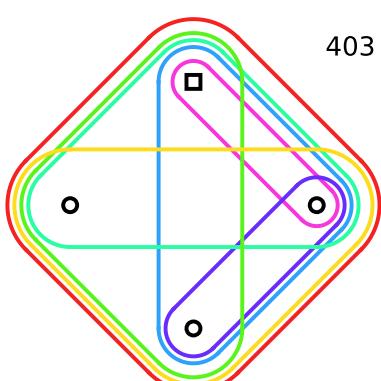
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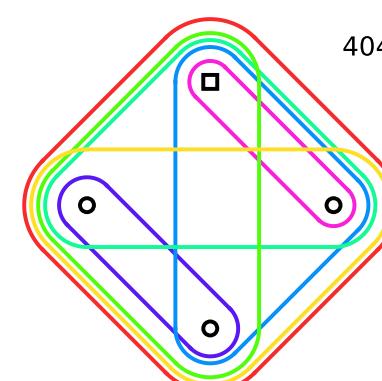
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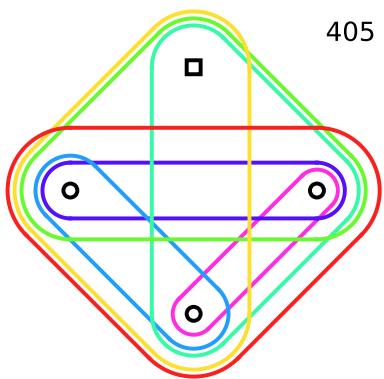
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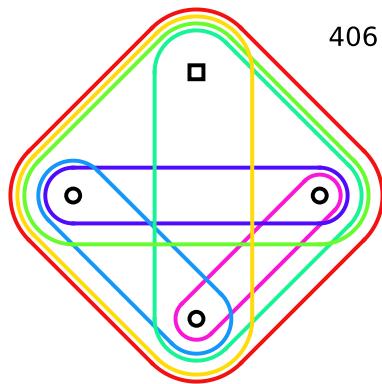
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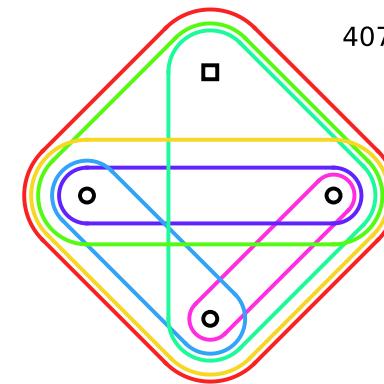
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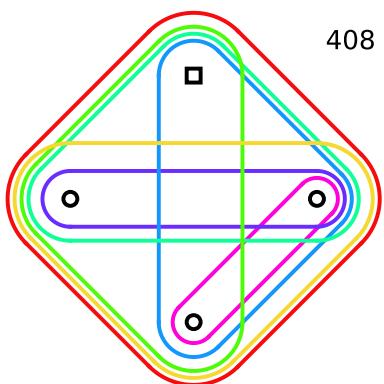
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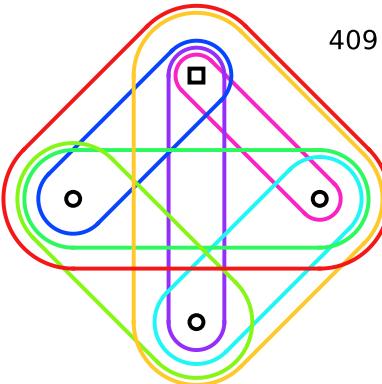
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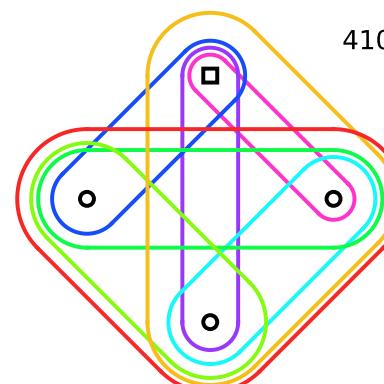
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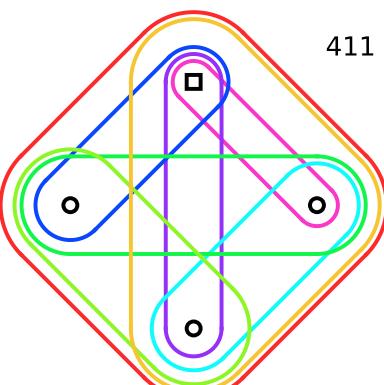
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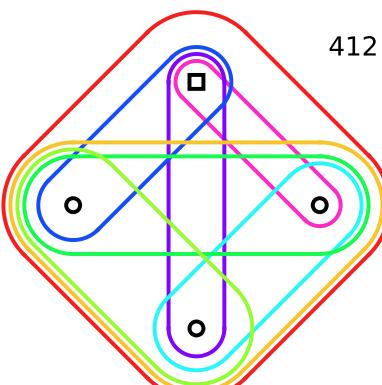
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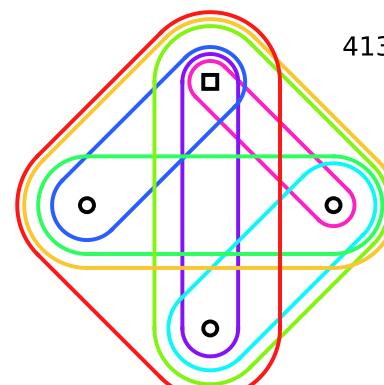
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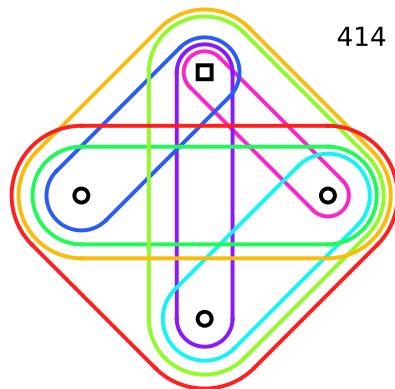
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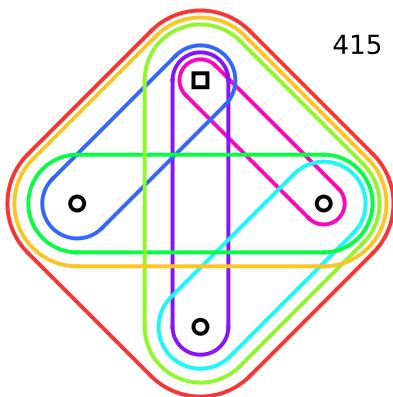
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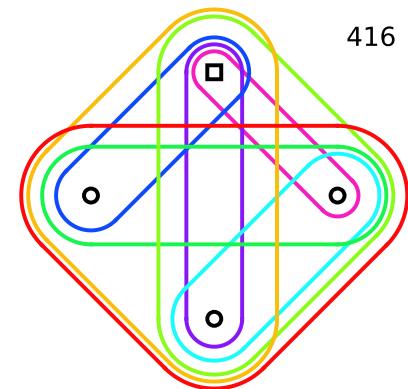
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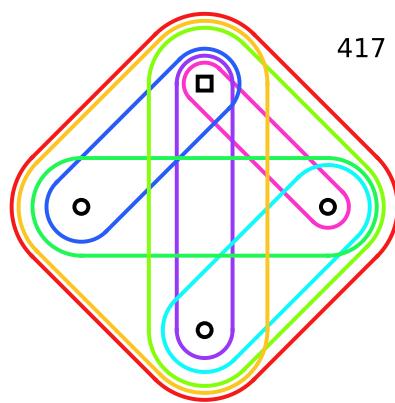
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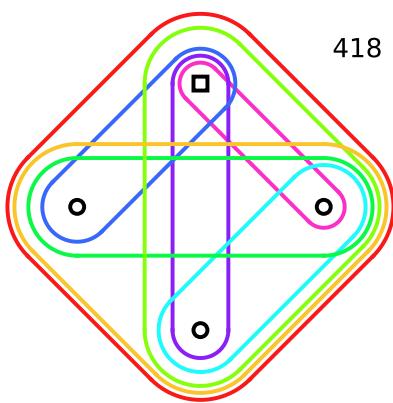
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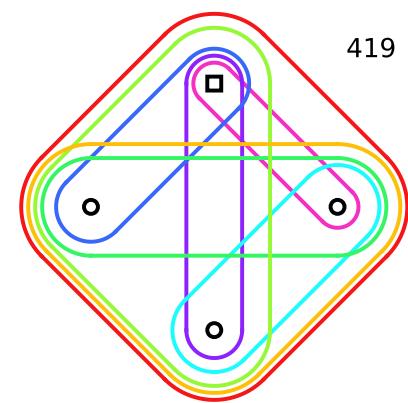
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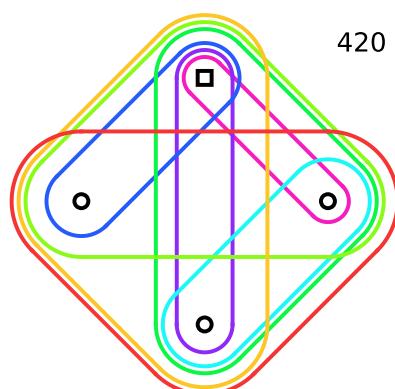
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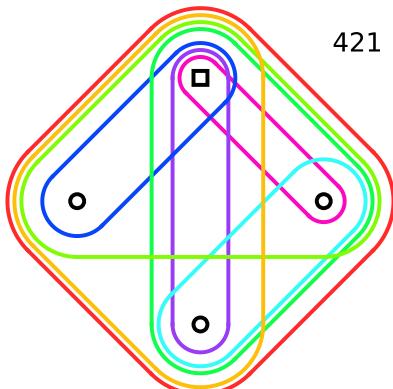
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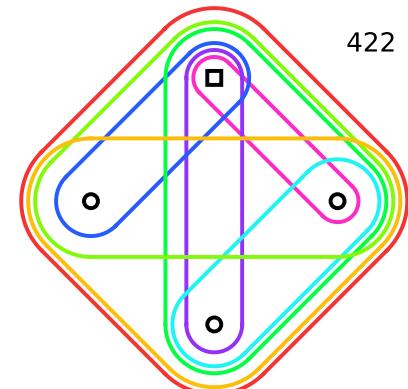
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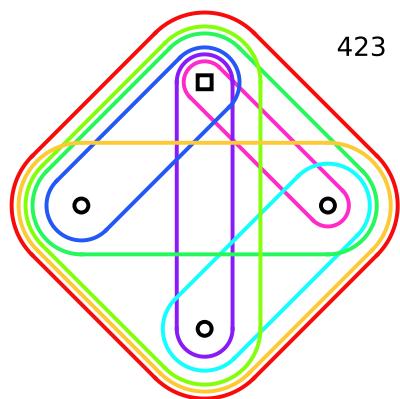
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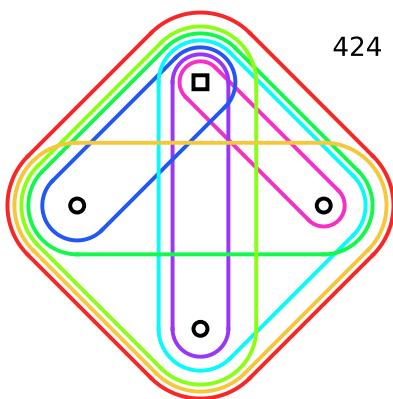
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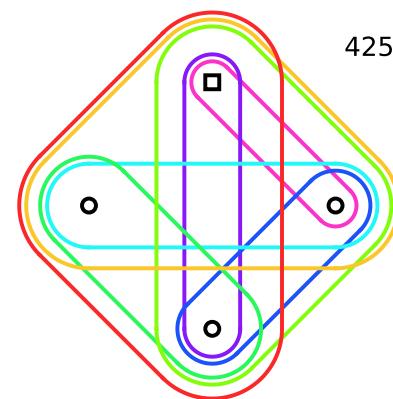
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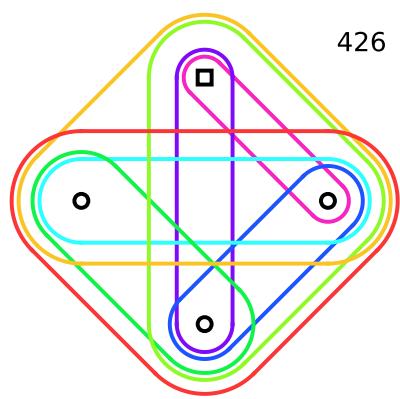
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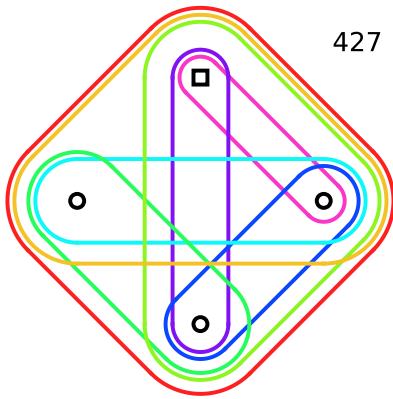
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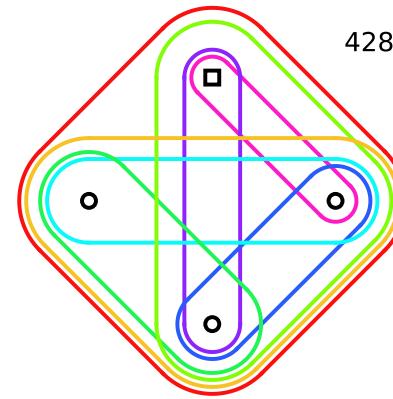
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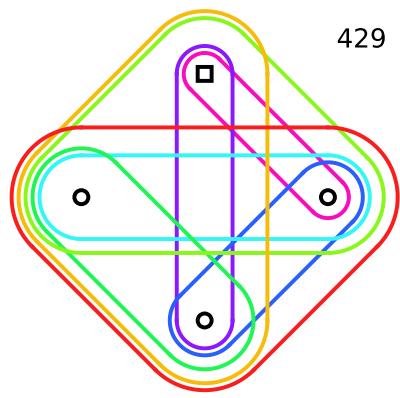
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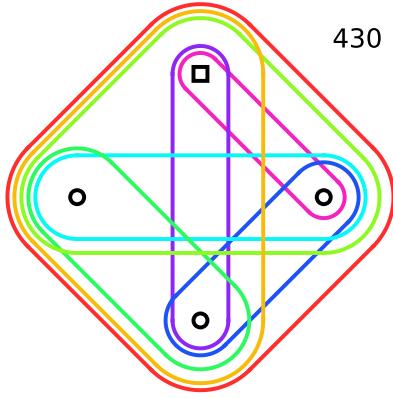
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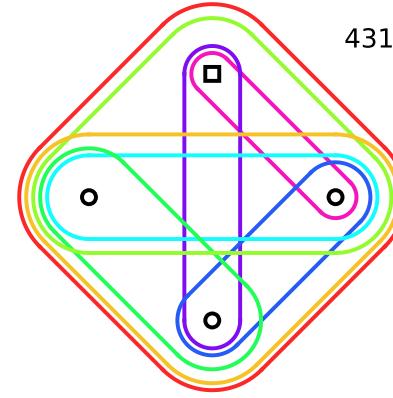
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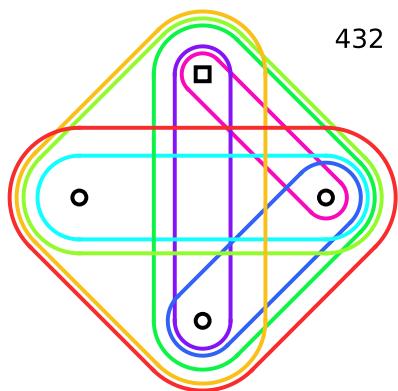
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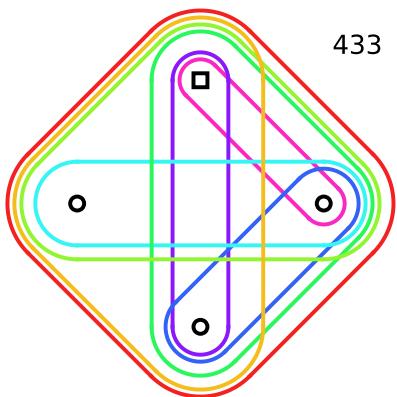
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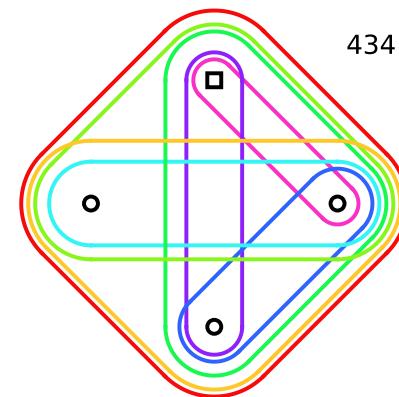
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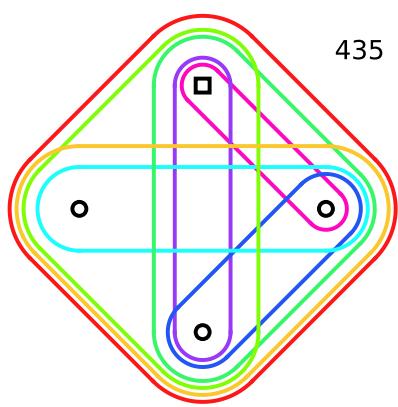
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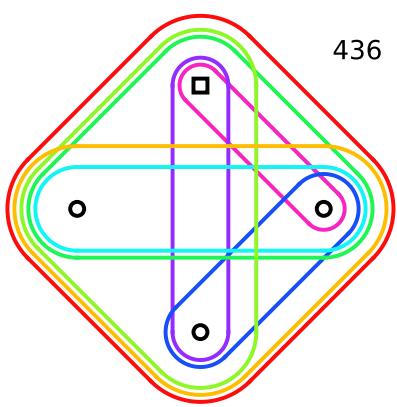
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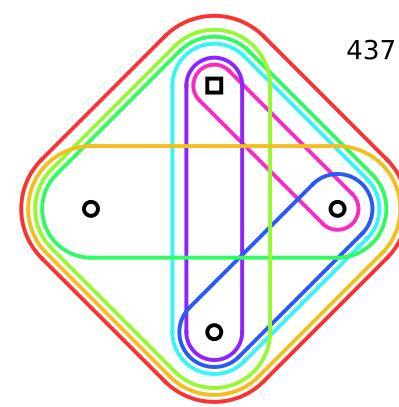
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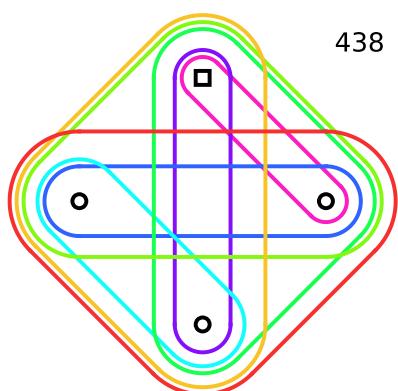
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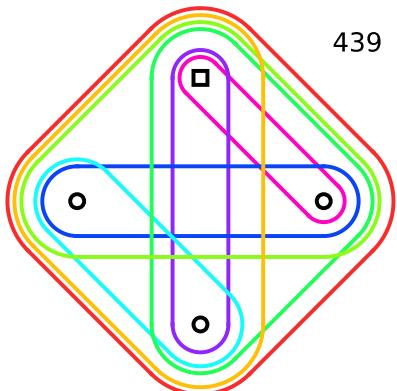
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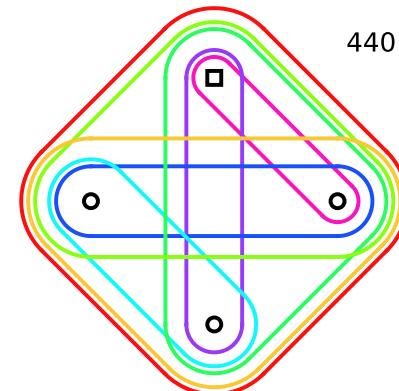
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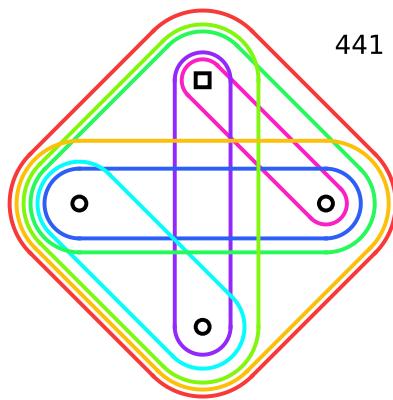
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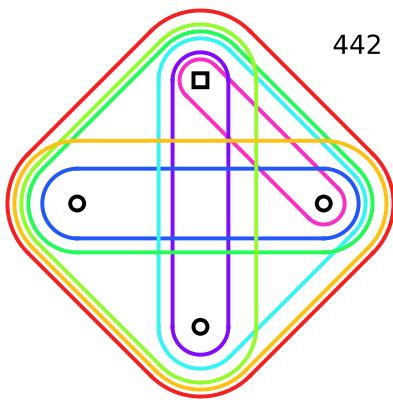
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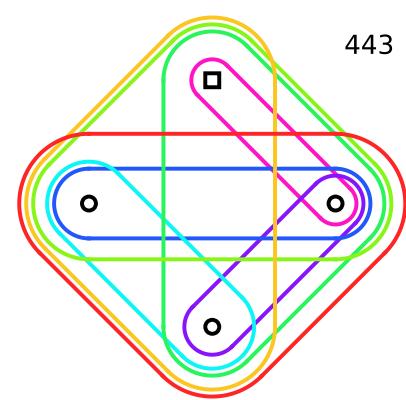
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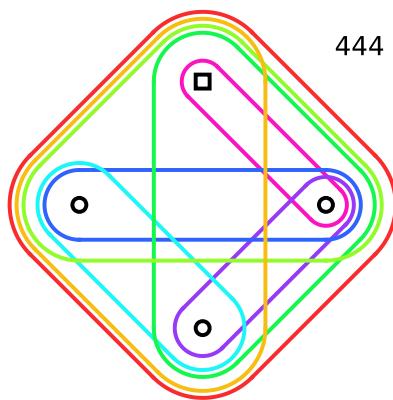
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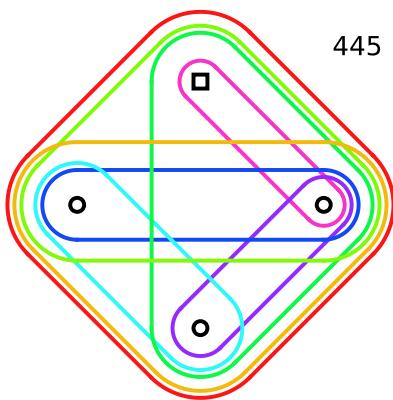
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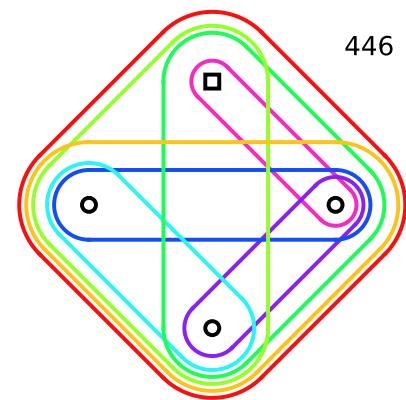
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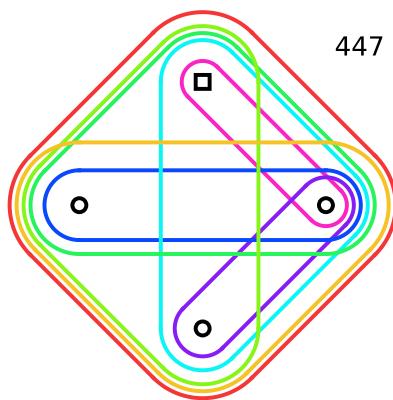
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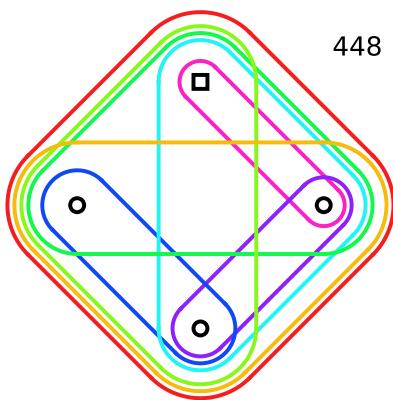
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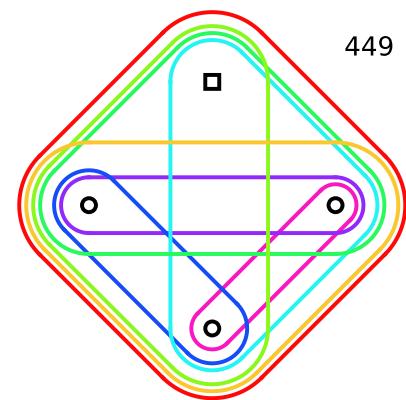
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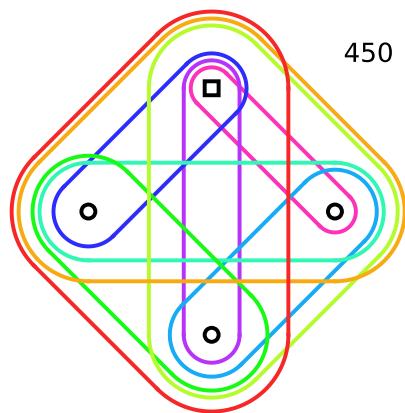
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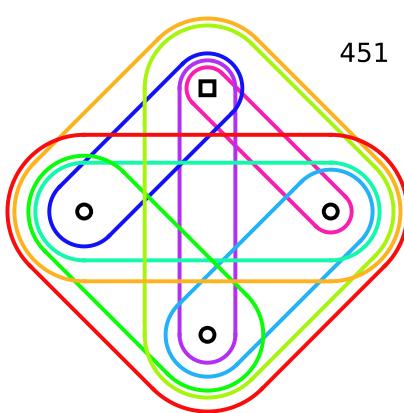
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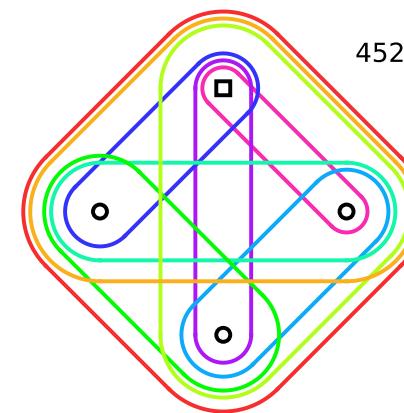
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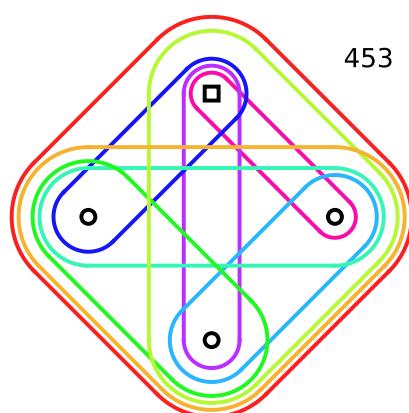
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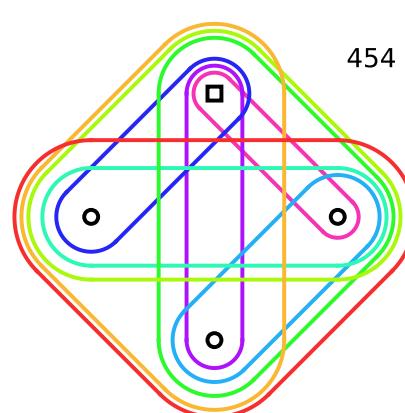
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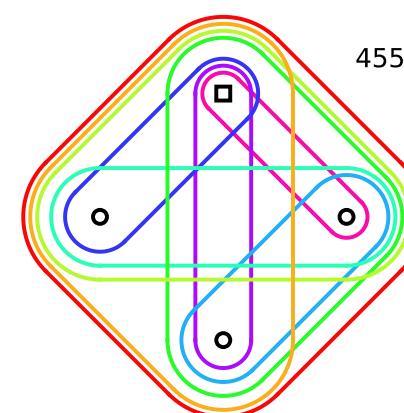
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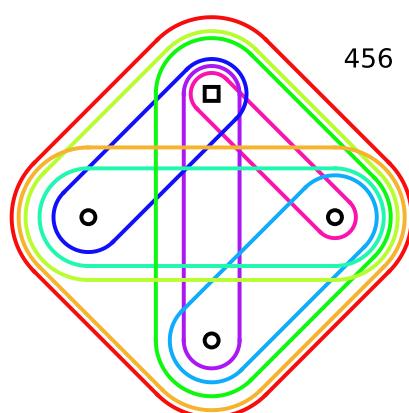
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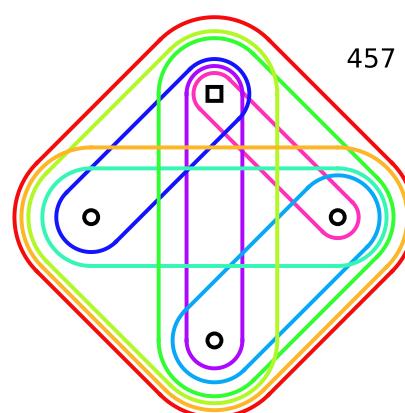
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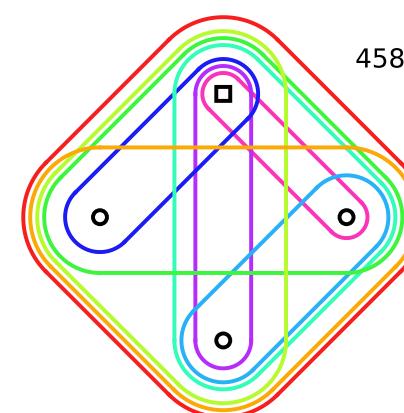
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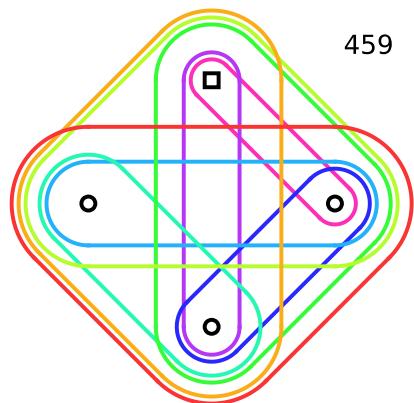
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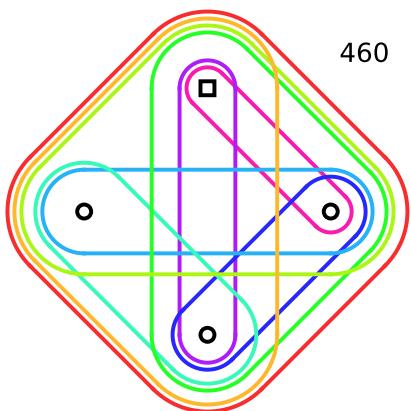
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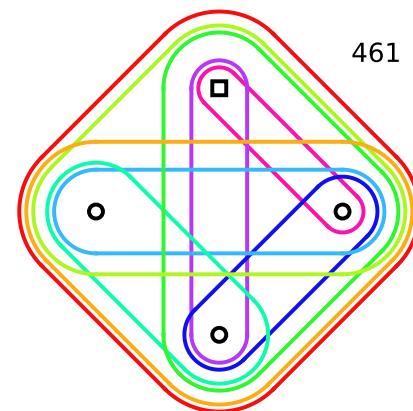
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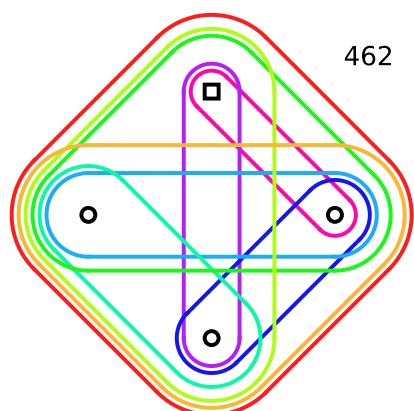
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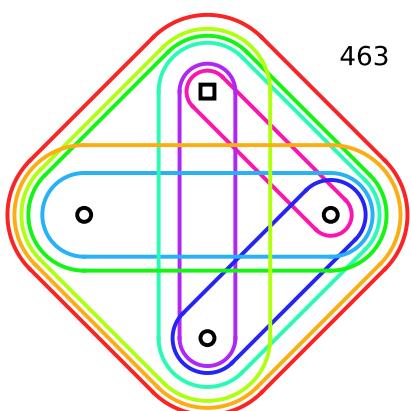
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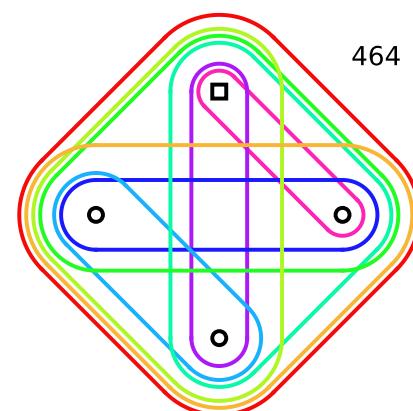
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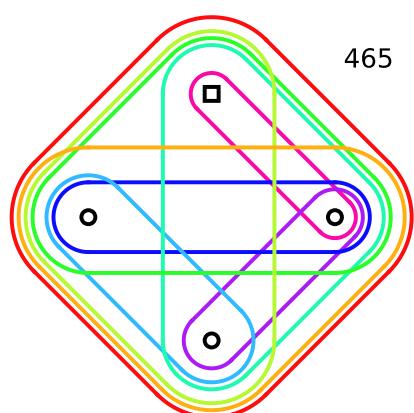
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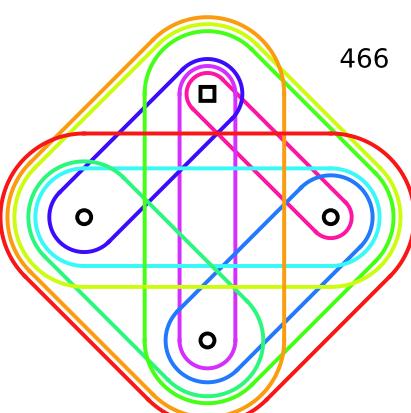
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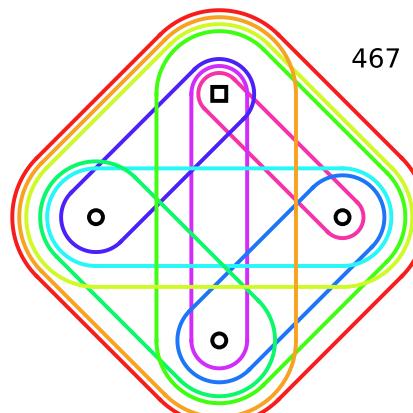
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