

Supplementary Information -S1

The ρ DCCA method¹⁶ is based on the ratio between the detrended covariance function F_{xy}^2 of the Detrended Cross-Correlation Analysis method²⁰ and the variance function without trend F_{zz} (with $z = x$ or $z = y$) of the Detrended Fluctuation Analysis method (DFA)¹⁹. It is shown in five steps below:

- **Step I:** Starting from two different time series, x_i and y_i , with $i = 1, 2, \dots, N$ (time series length). From the original time series two new integrated time series are obtained (Eq.1):

$$X_k = \sum_{i=1}^k [x_i - \bar{x}] \text{ and } Y_k = \sum_{i=1}^k [y_i - \bar{y}] \quad (1)$$

where \bar{x} and \bar{y} represent the mean value of each time series, and $k = 1, \dots, N$.

Step II: We divide these two integrated time series, X_k and Y_k , into $(N - n)$ overlapping boxes of equal length n , where $4 \leq n \leq \frac{N}{4}$, as shown in Figures 1 and 2. The original data present a total N of dengue case observations equal to 3,404 days, with a minimum scale equal to 4 days and a maximum scale of $N/4$. As we have 3,404 observations, the maximum would be 851 boxes. The scale of growth of each time series follows the DFA algorithm¹⁹. On The Research Resource for Complex Physiologic Signals (PhysioNet) website the DFA scale method is available, (PhysioNet - software projects, <https://physionet.org/content/dfa>).

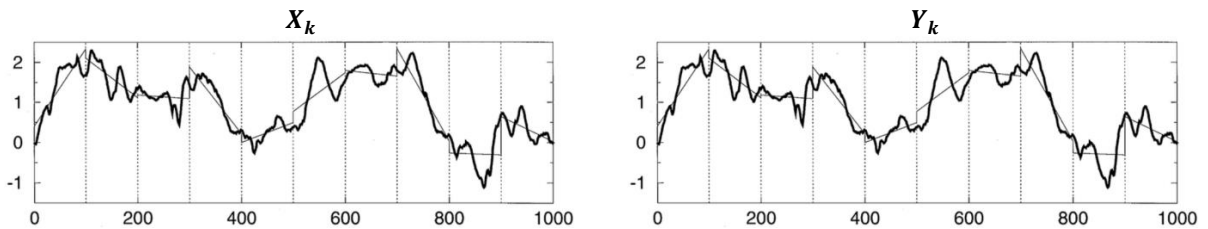


Figure 1: The illustration of the division of the two integrated signals X_k and Y_k .

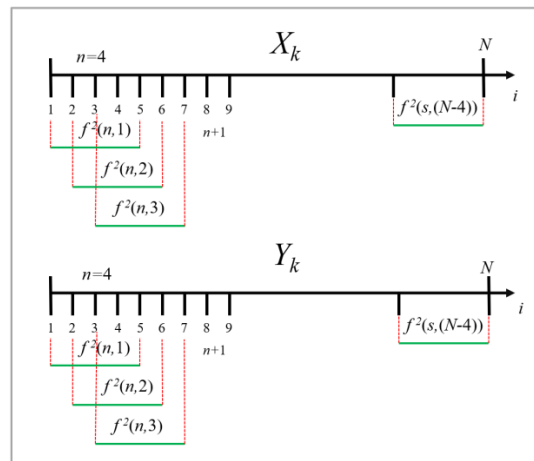


Figure 2: Division of the integrated signals X_k and Y_k into $(N - n)$ overlapping boxes n size $n = 4$, each containing $n + 1$ values.

- Step III: After this step, the polynomials (order one here) that best adjust the points (by least-squares fit) in each box of each series, $\tilde{R}_{K,i}$ and $\tilde{R}'_{K,i}$, are calculated and therefore the covariance of the residuals in each box (length n):

$$f^2 DCCA(n, i) = \frac{1}{n+1} \sum_i^{i+n} (R_k - \tilde{R}_{K,i})(R'_k - \tilde{R}'_{K,i}) \quad (2)$$

- Step IV: The mean over all $(N - n)$ overlapping boxes is calculated to obtain the detrended covariance function:

$$F_{xy}^2(n) \equiv \frac{1}{N+n} \sum_{i=1}^{N-n} f^2 DCCA(n, i) \quad (3)$$

- Step V: Finally, $\rho DCCA$ can be calculated by:

$$\rho DCCA(n) = \frac{F_{xy}^2}{F_{xx}(n)F_{yy}(n)} \quad (4)$$

According to [1] the functions F_{xx} and F_{yy} are respectively the root mean square fluctuation of each time series x_i and y_i separately. $\rho DCCA(n)$ ranges from: $-1 \leq \rho DCCA(n) \leq 1$. When $\rho DCCA(n) = 1$ this means a perfect cross-correlation, $\rho DCCA(n) = 0$ there is no cross-correlation, and $\rho DCCA(n) = -1$ means a perfect anti cross-correlation.