Supplementary information for

Shear band-driven precipitate dispersion for ultrastrong ductile medium-entropy alloys

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Supplementary Note. The details of phase stability calculations. To investigate the precipitation reactions in Al0.2CoNiV, DFT calculations were conducted for the relative phase stability of the ordered phases $L1_2$ -(Co,Ni)₃Al, B2-(Co,Ni)Al, and $L2_1$ -(Co,Ni)₂VAl. The phase stability is determined by the free energy of both the precipitate and the matrix, whose composition balances that of the precipitate. The construction of a multi-dimensional convex hull for the free energy of Al_{0.2}CoNiV with DFT is impractical in the multicomponent phase space and thus beyond the scope of the present work. To provide an appropriate comparison of the candidate precipitates at reasonable computational costs, two approximations were made: (1) to fix the compositions and phase fractions of the precipitate and matrix, all available Al $(6.25 \text{ at} \%)$ was assumed to be sequestered by the precipitates, i.e., the matrix was completely depleted of Al; and (2) the lattice parameters were determined such that a Wigner–Seitz radius of 1.411 Å was obtained for every structure, corresponding to the computed 0 K equilibrium volume of the initial FCC $Al_{0.2}CoNiV$ solid solution.

For the $L2_1$ phase, different populations of the (C_0,N_i) lattice were considered, with a Co concentration in the sublattice ranging from 0 to 100%. For each configuration, the first bar corresponds to the energy difference at 0 K in the ferromagnetic state, the second in the paramagnetic DLM state (+magn), while the third adds the electronic and configurational contributions (+el, +conf) at 1150 K (within the annealing temperature window). In agreement with the experiments, the most stable precipitate among the candidates was determined to be the Co-rich $L2_1$ phase.

From an electronic-structure viewpoint, the stabilization of this Co-rich phase originates from the opening of a pseudogap in the electronic density of states of the $L2₁$ phase in proximity to the Fermi level (E_F) . The larger the Co concentration, the closer the pseudogap to E_F ; hence, the more stable the electronic configuration at 0 K. The ferromagnetic simulations at 0 K predicted that, for the most stable configuration, Ni was completely absent, whereas the APT analysis and experimental lattice parameter rather suggest a Co and Ni ratio of approximately 2:1. Notably, however, if finite-temperature contributions are included (magnetic disorder and configurational and electronic free energy at 1150 K), the $L2_1$ phases with 67%, 75%, and 100% Co become almost degenerate (free energy difference less than 5 meV/at.), and with a further

increase in the temperature, a progressively larger Ni content becomes energetically favorable in the $L2_1$ phase, in good qualitative agreement with the experiments.

The different free energy contributions can be understood as follows: (1) the pseudogap being closest to E_F for the L2₁-Co phase also causes a smaller electronic free energy contribution due to the less available electronic states near E_F with respect to the $L2_1$ -(Co,Ni) phase; (2) paramagnetism shifts the Fermi energy of the $L2₁-Co$ phase away from the pseudogap; and (3) configurational entropy in the ideal mixing favors a random (Co,Ni) sublattice in the $L2_1$ phase, thereby further stabilizing a partial Ni segregation in the $L2_1$ phase. Given the delicate balance of the individual contributions and the overall small energy differences, the inclusion of other contributions (e.g., lattice vibrations, short-range order, elastic contributions, and relaxation effects) may provide a more quantitative agreement with the experimentally observed composition. It is also confirmed that the results remain qualitatively unaltered when V partially occupies the Al sublattice in the $L2₁$ phase (not shown here).

Supplementary Fig. 1 a Tensile stress-strain curve of the homogenized state, b, c SEM image and corresponding EDS elemental maps exhibiting L21 islands.

Supplementary Fig. 2 a Tensile stress-strain curve of the cold-rolled state, b, c optical and SEM images showing macro-shear bands along \sim 10–45 degrees to the rolling direction, **d-f** EBSD IPF, IQ, and KAM maps showing macro-shear bands and micro-shear bands indicated by yellow and white arrows, respectively.

Supplementary Fig. 3 a, b Low- and high- magnification SEM images, and c EDS elemental maps exhibiting L21 island of the RA sample.

Supplementary Fig. 4 Microstructures revealed by EBSD analysis for the annealed Al0.2CoNiV alloy. a EBSD IQ map, b IPF map of FCC, c IPF map of L21, and d IPF map of sigma phase for the alloy annealed at 800 °C for 1 h. e EBSD IQ map, f IPF map of FCC, g IPF map of L21, and h IPF map of sigma phase for the alloy annealed at 850 °C for 1 h.

Supplementary Fig. 5 EBSD IQ maps of annealed Al_{0.2}CoNiV alloys superimposed by phase color. White-gray, turquoise, and yellow colors represent FCC , $L2₁$, and σ phases, respectively. a non-recrystallized region of the alloy annealed at 800 °C and b recrystallized region of the alloy annealed at 900 °C. Red line indicates FCC and $L2_1$ phases having a K-S orientation relationship.

Supplementary Fig. 6 a High-resolution TEM and corresponding FFT images, b inverse FFT image showing semi-coherent interface between γ and L2₁.

Supplementary Fig. 7 Tensile fractographies of the a A800, b A850, and c A900 alloys. Only ductile-dimple fracture was observed.

Supplementary Fig. 8 Summarized chart showing calculated strengthening contributions from each mechanism for alloys annealed at 800, 850, and 900 °C for 1 h.

Supplementary Fig. 9 ECCI micrographs of the Al0.2CoNiV alloy annealed at 850 °C after tensile test at room temperature. a recrystallized region, b non-recrystallized region.

Region		A800	A850	A900
$L21$ island	Total	11.3 ± 2.6	9.6 ± 3.7	9.6 ± 3.0
	FCC	5.5 ± 0.5	4.0 ± 0.2	2.8 ± 0.3
	$L2_1$	4.8 ± 0.4	5.2 ± 0.2	6.8 ± 0.3
	σ	1.0 ± 0.1	0.4 ± 0.1	$\boldsymbol{0}$
Recrystallized	Total	33.9 ± 2.7	60.7 ± 3.5	90.4 ± 3.0
	FCC	27.8 ± 0.4	53.4 ± 0.9	83.9 ± 0.2
	$L2_1$ at GB^*	5.6 ± 0.4	6.3 ± 0.5	5.4 ± 0.1
	$L2_1$ at IG^{**}	0.5 ± 0.1	1.1 ± 0.3	1.1 ± 0.3
Non-Recrystallized	Total	54.8 ± 5.0	29.7 ± 4.0	$\boldsymbol{0}$
	FCC	46.0 ± 1.3	25.3 ± 0.2	$\boldsymbol{0}$
	$L2_1$ at SB ^{***}	8.8 ± 1.3	4.40 ± 0.2	$\boldsymbol{0}$

Supplementary Table 1. Fractions of constituent phases for the Al0.2CoNiV alloy annealed under three conditions (%).

*GB: Grain boundary, **IG: Inside grain, ***SB: Shear band

Region	Phase	A800	A850	A900
$L21$ island	$L2_1(\mu m)$	7 ± 4	10 ± 8	8 ± 6
	FCC (nm)	40 ± 20	200 ± 90	300 ± 100
	σ (nm)	120 ± 80	110 ± 80	
Recrystallized FCC	FCC (μ m)	1.1 ± 0.7	1.7 ± 0.9	2 ± 2
	$L2_1$ at $GB^*(nm)$	210 ± 10	200 ± 200	300 ± 200
	L21 at $IG^{**}(nm)$	90 ± 3	143 ± 6	146 ± 6
Non-Recrystallized	FCC (μ m)	210 ± 70	90 ± 20	
	L2 ₁ at $SB^{***}(nm)$	57 ± 7	90 ± 30	

Supplementary Table 2. Sizes of FCC, $L2_1$, and σ phases for the Al_{0.2}CoNiV alloy annealed under three conditions.

*GB: Grain boundary, **IG: Inside grain, ***SB: Shear band

Specimen	Yield Strength (MPa)	Tensile Strength (MPa)	Elongation $(\%)$
A800	1500 ± 10	1730 ± 20	8 ± 1
A850	1260 ± 10	1590 ± 10	27 ± 3
A900	1050 ± 20	1480 ± 10	32 ± 4
RA	570 ± 8	1120 ± 10	49 ± 2

Supplementary Table 3. Room-temperature tensile properties of the Al0.2CoNiV alloys.

Supplementary Table 4. Compositions, processing, constituent phases, grain size and tensile properties of the MEAs and HEAS reported previously.

*Note that the following abbreviations are used in Table S1: AC (as-cast), CR (cold-rolled), HR (hot-rolled), HF (hot forged), UF (upset forged), SC (slow cooled), WQ (water quench), AC (air cooling), IA (intermediate annealing), HIP (hot isostatic pressing), SLM (selective laser melting), FSP (friction stir processing), and GS (grain size).

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