# CoCoA-diff: Counterfactual inference for single-cell gene expression analysis

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#### **Author names and affiliations**

Yongjin P Park<sup>1,2</sup>, Manolis Kellis<sup>3,4</sup>

- 1. Department of Pathology and Laboratory Medicine, Department of Statistics, University of British Columbia, Vancouver, BC, Canada
- 2. Department of Molecular Oncology, BC Cancer, Vancouver, BC, Canada
- 3. Computer Science and Artificial Intelligence Laboratory, Massachusetts Institute of Technology, Cambridge, MA, United States of America
- 4. Broad Institute of MIT and Harvard, Cambridge, MA, United States of America

Contact:

- Yongjin P. Park: ypp@stat.ubc.ca
- Manolis Kellis: manoli@mit.edu

## **Supplementary Figures**

**Fig S1.**



Variation by Disease Effect (%)

#### **Simulation experiments with the invalidating collider bias.**

**(a)** Data generation scheme for simulation experiments. We simulate 50 causal and 9,950 non-causal genes with or without disease-causing mechanisms (an edge between W and  $\lambda$ ).  $W_i$ : disease label assignment for an individual *i*.  $X_i$ : confounding effects for an individual *i*.  $\lambda_{gi}$ : unobserved gene expression for a gene g of an individual *i* as a function of X and W.  $Y_{gj}$ : realization of cell-level gene expression of a gene g with a cell *j*-specific sequencing depth  $\rho_j$  (stochastically sampled from Gamma distribution). Here, we simulated total five covariates consisting of confounding  $(X)$  and batch effect variables  $(B)$ .

**(b)** Empirical false discovery rates of the differential expression methods when there were no confounding effect, but the 30% of individual-level expression variation is attributed to the disease effect  $(W \to \lambda; \sigma_{W \to Y}^2)$ on 50 causal genes. *Y-axis*: empirical false discovery rate, the frequency of the non-causal among genes with the estimated q-value below 0.01.

**(c)** Simulation results when all the five covariates are confounding disease label assignment and gene expression values, accounting for 50% of mean expression variation  $(\sigma_{X,B\to Y}^2)$ . Different subpanels correspond to different configurations of the number of individuals and cells per individual. *Y-axis* (AUPRC): area under precision recall curve (numerically integrated by DescTool<sup>1</sup> implemented in R); *x-axis*: the proportion of variation contributed by the disease label  $(\sigma_{W\to Y}^2)$ . The following methods were considered: *CoCoA*: Wilcoxon's ranksum test using individual-specific confounder-adjusted gene expression values  $\delta_{qi}$  (the step 3 of Fig. 1c); *Total*: pseudo-bulk expression aggregated within each individual; *Bayesian*: Bayesian estimate of pseudo-bulk expression averaged over cells within each individual; *Mean*: pseudo-bulk expression averaged over cells within each individual; *MAST*: Model-based Analysis of Single-cell Transcriptomics<sup>2</sup> implemented in R (cell-level differential expression analysis); *Confoudner*: the estimated confounding effect  $\mu_{qi}$  (the step 2 of Fig. 1c).







**(a)** Data generation scheme for simulation experiments. We simulate 50 causal and 9,950 non-causal genes with or without disease-causing mechanisms (an edge between W and  $\lambda$ ).  $W_i$ : disease label assignment for an individual *i*.  $X_i$ : confounding effects for an individual *i*.  $\lambda_{gi}$ : unobserved gene expression for a gene g of an individual *i* as a function of X and W.  $Y_{gj}$ : realization of cell-level gene expression of a gene g with a cell *j*-specific sequencing depth  $\rho_j$  (stochastically sampled from Gamma distribution). Here, we simulated

total five covariates consisting of confounding  $(X)$  and batch effect variables  $(B)$ .

**(b)** Simulation results with different numbers of confounding factors and batch effect variables (horizontal subpanels) and different number of individuals (vertical subpanels). *Y-axis* (AUPRC): area under precision recall curve (numerically integrated by  $DescTool<sup>1</sup>$  implemented in R); *x-axis*: the proportion of variation contributed by the disease label  $(\sigma_{W\to Y}^2)$ . The following methods were considered: *CoCoA*: Wilcoxon's ranksum test using individual-specific confounder-adjusted gene expression values  $\delta_{gi}$  (the step 3 of Fig. 1c); *Total*: pseudo-bulk expression aggregated within each individual; *CoCoA + PC*: CoCoA followed by PCA on the resulting gene by individual matrix, where the PCs were selected if they are not correlated with the disease labels;  $Total + PC$ : pseudo-bulk expression followed by PCA, where the PCs were selected if they are not correlated with the disease labels.

**Fig S3.**



**Average cell-type-specific profiles of 1,726 marker genes**





**Correspondence with Mathys et al.<sup>3</sup>**

**Fig S5.**



**The annotations of the major neuronal and glial cell types are not biased by known biological variables.**

**Fig S6.**



**The annotations of the excitatory neuron types are not biased by known biological variables.**

**Fig S7.**



**The annotations of the inhibitory neuron types are not biased by known biological variables.**

**Fig S8.**



**CoCoA algorithm does not create a skewed distribution of variance.**

**Fig S9.**



**Histogram of p-value distributions**

**Fig S10.**



**Top**: Correlations between the average disease effects (ADE) and gene-level associations with the confounding factors. **Bottom**: Correlations between the average disease effects computed on the disease cohort (ADD) and the average disease effects computed on the control cohort (ADC).

### **References**

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