

1

SUPPLEMENTARY INFORMATION

2

3 **Table S1.** Published progression-free survival (PFS) analyses, selected PFS cohorts, available risk tables, and published doubling
 4 times for each cancer type. The published PFS were used for data fitting and simulations, and the simulated output was compared to
 5 the published doubling times.

		Published PFS data		Published DBT	
Cancer	Cohort	Risk Table (Y/N)	Reference	DBT (months) ¹	Reference
Pancreatic	Gemcitabine	Y	(1)	5.30 (3.84, 6.76) [42]	(2)
				4.80 (2.1 – 8.5) ³	(4)
				2.67 (1.3 – 13.33) ³	(5)
				1.64 (1.31, 1.96) [112]	(6)
Melanoma	BRAF-mutant	Y	(3)	6.84 (4.37, 9.31) [76]	(7)
				1.43 (0.99, 1.86) [87]	(8)
				4.80 (2.1 – 8.5) ³	(4)
				5.26(3.78, 6.74) [103]	(10)
HCC	Placebo	Y	(9)	2.37 (1 – 4.9) ⁴	(12)
RCC	Placebo	Y	(11)	15.6 (13.34, 17.86) [18] ⁵	(14)
TN Breast	Tivantinib	Y	(13)		

				1.53 (0.85, 2.21) [96]	(16)
				Women: 22.93 (7.18, 38.69) [192]	(17)
				Men: 7.80 (0.92, 14.68) [191]	(17)
				15.07 (11.88, 18.25) [84]	(18)
				36.90 (0.13, 11.73) [36]	(19)
				2.07 (1.60, 2.93) [67]	(20)
NSCLC	Placebo	Y	(15)	8.03 (6.25, 9.82) [69]	(22)
HR+ Breast	Exemestane+Placebo	Y	(21)	5.40 (4.27, 6.53) [37]	(22)
HER-2+ Breast	Anastrazole	Y	(23)	10.08 (6.48, 13.67) [63]	(25)
Gastric	UFTM	N	(24)	1.65 ⁷	(27)
GBM	Procarbazine	N	(26)	3.17 (0.05 – 10.63) ⁸	(29)
CRC	BSC	Y	(28)	13.91 (4.75, 23.08) [82]	(31)
Prostate	Mitoxantrone	Y	(30)		

6

7 Note: references for all PFS curves included in the literature search can be found in (1,3,9,11,13,21,23,24,26,28,30,32-67).

8

9 Abbreviations: BSC = best supportive care; UFTM = uracil + fluorouracil + tegafur + mitomycin. CRC = colorectal cancer; GBM =
10 glioblastoma multiforme; HER-2⁺ = human epidermal growth factor receptor-2 positive, HR⁺ = hormone receptor positive, TN = triple
11 negative; NSCLC = non-small cell lung cancer; RCC = renal cell carcinoma; HCC = hepatocellular carcinoma

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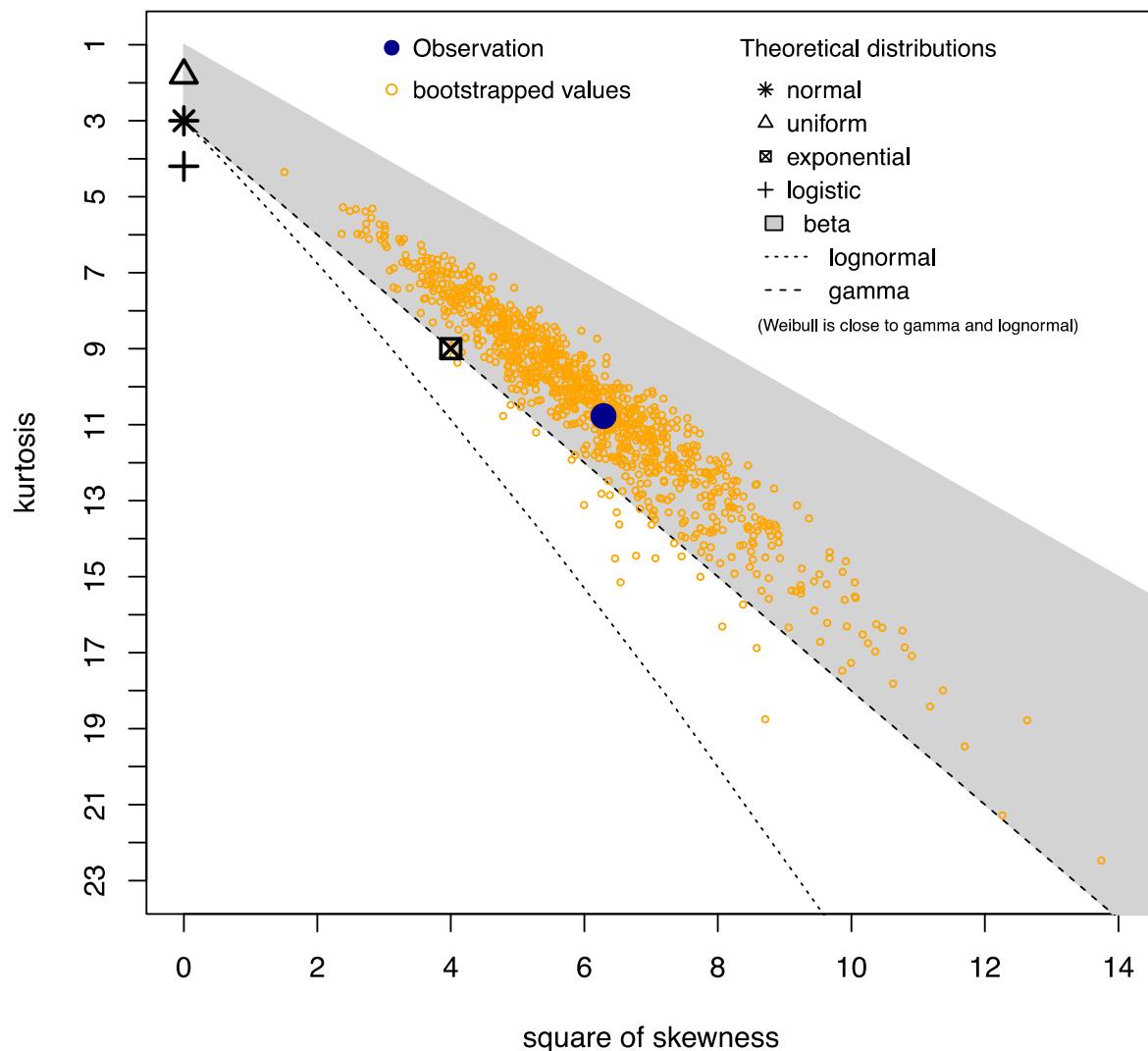
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- 241
- 242

243 **Figure S1.** Distribution fitting and simulation workflow for pancreatic cancer. Panel A:
244 Cullen and Frey plot with bootstrapped values. Panel B: Statistical fitting of calculated
245 growth rates using the following distribution models: normal, uniform, lognormal, gamma,
246 and weibull. For each distribution, the empirical and theoretical distribution (upper left),
247 quantile-quantile (QQ: upper right), probability-probability (PP: lower right) and
248 theoretical and empirical cumulative distribution function (CDF: lower left) plots are
249 shown.

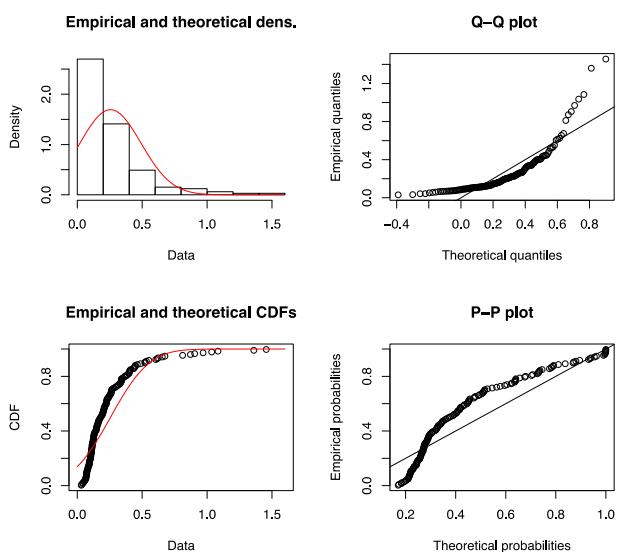
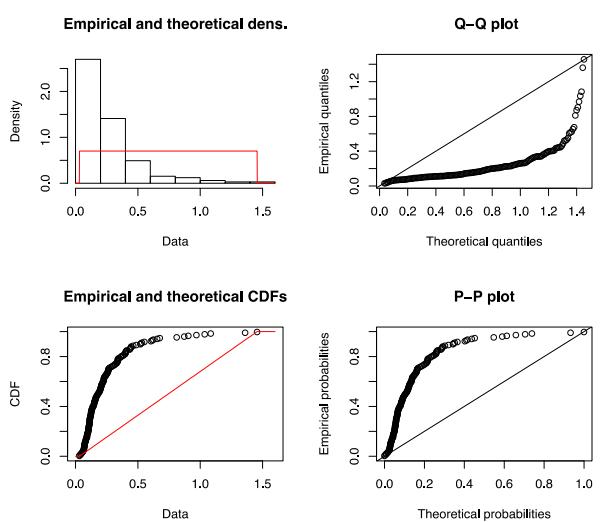
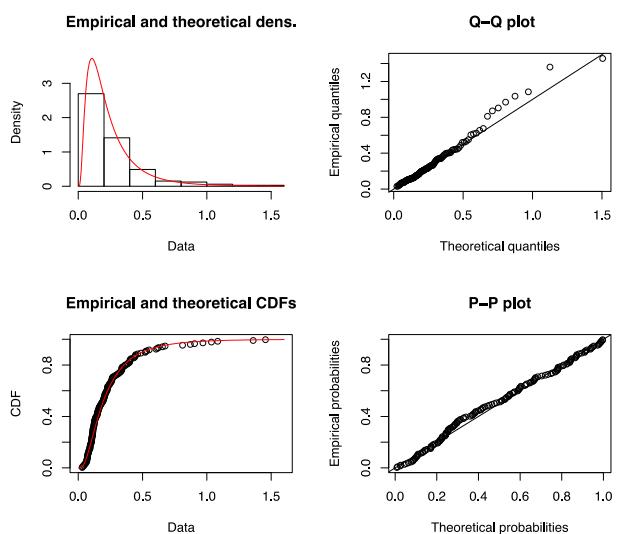
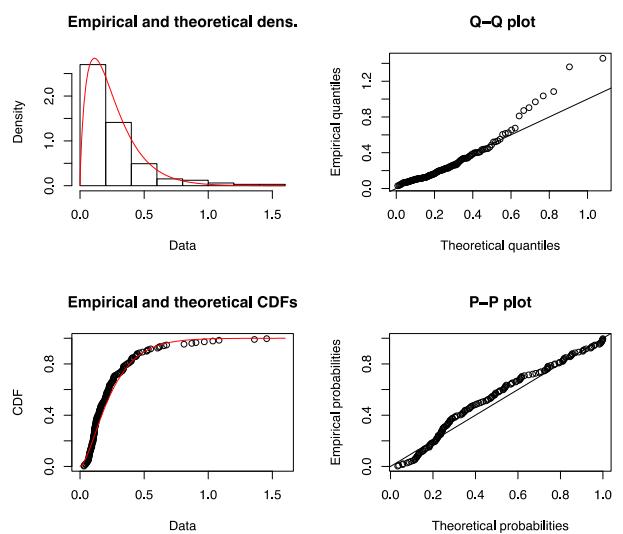
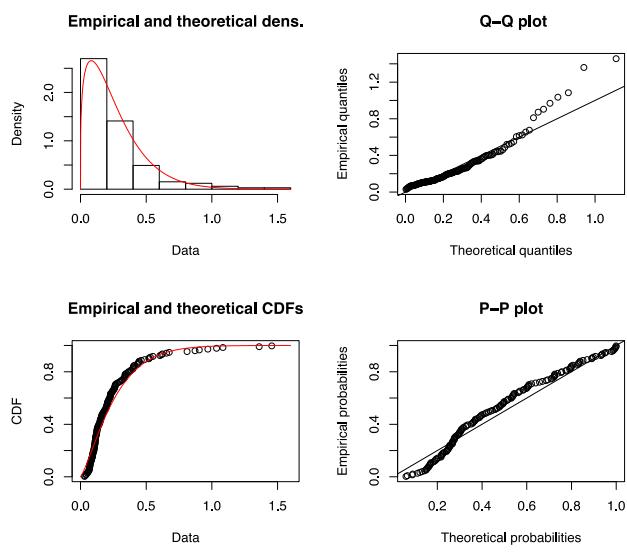
250 A.

251

Cullen and Frey graph



B.

Normal Distribution**Uniform Distribution****Log-normal Distribution****Gamma Distribution****Weibull Distribution**

255 **Figure S2.** The progression free survival (PFS) curves for melanoma.(3) (A) Kaplan-Meier
256 plot generated using the numbers at risk provided by *Kim et al.*(3) (B) Kaplan Meier plot
257 generated using the growth rate values extracted using the first approach.

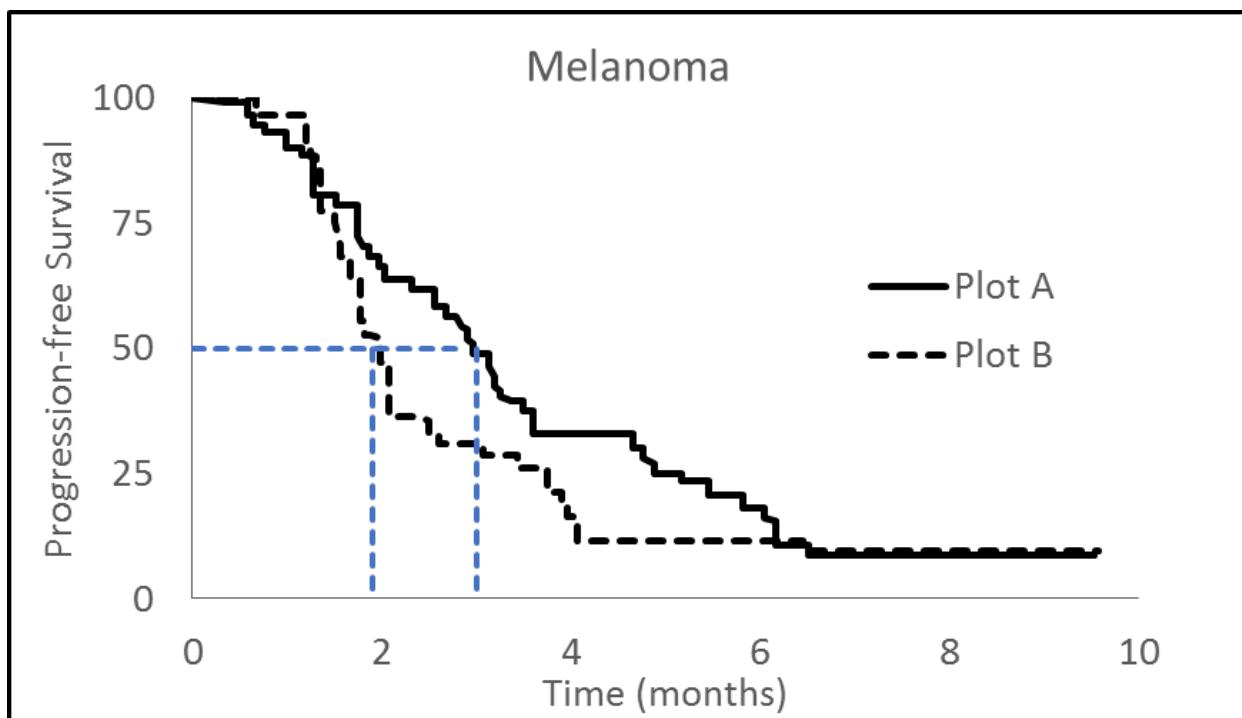
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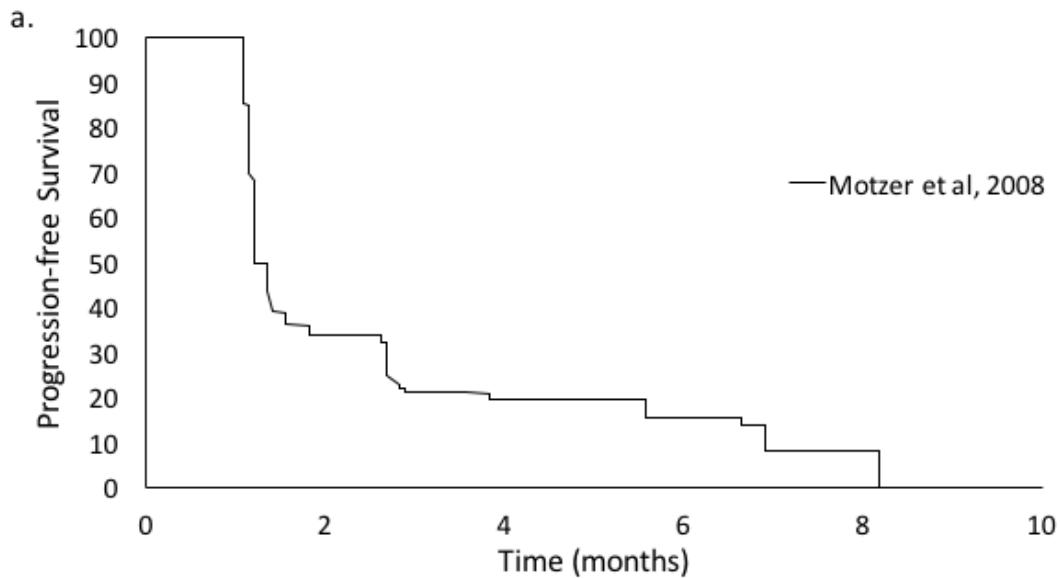
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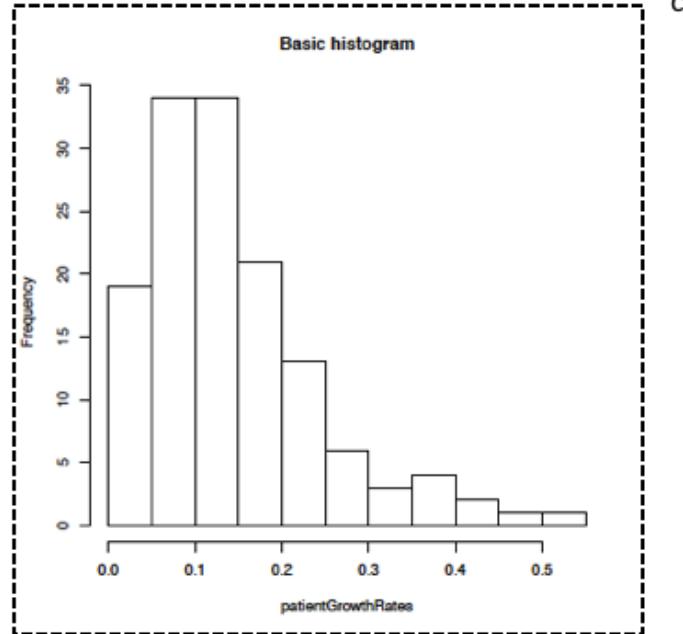
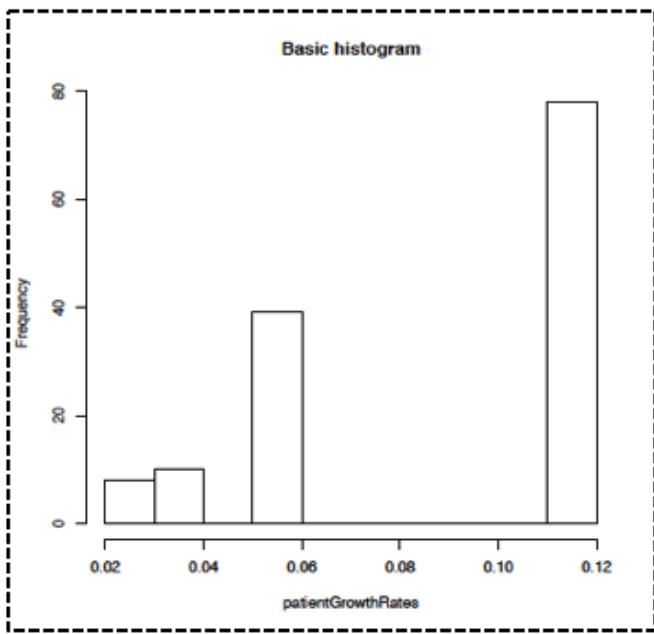


263 **Figure S3.** Visual representation of how random uniform distribution affects calculated
264 exponential growth rates of renal cell carcinoma. Panel a shows the published
265 progression free survival (PFS) plot from which growth rates in Panels b and c were
266 calculated.(11) The histograms in panels b and c represent the growth rates derived
267 without and with the application of random uniform distribution to the event times.

Renal Cell Carcinoma



b.



268

269 **Supplementary Equations 1: Deriving Kaplan Meier estimate for number of events**

270 Defining Kaplan Meier (KM) estimate for the survival function

271

272
$$S(t) = \prod_{i=1}^k \left(1 - \frac{d_i}{n_i}\right)$$
 Equation S1

273 Survival estimate for the first time point of observation, $S(t)_1$

274

275
$$S(t)_1 = 1 - \frac{d_1}{n_1}$$
 Equation S2

276

277 Solving for number of deaths at 1st time point of observation

278

279
$$d_1 = (1 - S(t)_1) \bullet n_1$$
 Equation S3

280

281 Survival estimate at 2nd time point of observation

282

283
$$S(t)_2 = \left(1 - \frac{d_1}{n_1}\right) \bullet \left(1 - \frac{d_2}{n_2}\right)$$
 Equation S4

284

285 Solving for number of deaths at 2nd time point of observation

286
$$d_2 = n_2 \left(1 - \frac{S(t)_2}{1 - \frac{d_1}{n_1}}\right)$$
 Equation S5

287

288 Using Equation S2 we know

289
$$d_2 = n_2 \bullet \left(1 - \frac{S(t)_2}{S(t)_1}\right)$$
 Equation S6

290

291 Generalizing the function for number of deaths

292

293
$$d_i = n_{i-1} \bullet \left(1 - \frac{S(t)_i}{S(t)_{i-1}}\right)$$
 Equation S7

294 where n_0 is the sample size and $S(t)_0 = 1$.

295 **Supplementary Equations 2: Determining the growth rate of a tumor progression**
296 “event”

297

298 An event is defined as a 20 or 25% growth in sum of longest diameter (SLD) by RECIST
299 and WHO respectively.

300

301 Here, the tumor is assumed to be spherical, and the standard equation is used to describe
302 the volume of a sphere

303

304 $Sphere\ volume = \frac{4}{3} \cdot \pi \cdot r^3$

305 Equation S8

306 Where r is the radius of the circle or diameter/2, D .

307

308 Assuming the initial tumor diameter $D_0=1\text{cm}$, the 20% increased diameter $D_{20\%}=1.2\text{cm}$
309 indicates a progression event and the corresponding spherical volumes are

310

311 $V_0 = \frac{4}{3} \cdot \pi \cdot \left(\frac{1}{2}\right)^3 = 0.5236\text{cm}^3$

312 Equation S9

313

314 $V_{20\%} = \frac{4}{3} \cdot \pi \cdot \left(\frac{1.2}{2}\right)^3 = 0.9048\text{cm}^3$

315 Equation S10

316

317

318 Equation 2 of the main manuscript is

319

320 $TV = TV_0 \cdot e^{k_g \cdot t}$

321

322 Rearranging this equation to find the time of the event (t_{event}) and using the solution to
323 Equations S9 and S10 allows us to find the growth rate

324

325 $0.9048 = 0.5236 \cdot e^{k_g \cdot t_{event}}$

326

327 $k_g = \frac{\ln(1.728)}{t_{event}}$

328 Equation S11

329

330 If a tumor progression event were defined by a 25% increase in diameter, $D_{25\%}=1.25\text{cm}$

331

332 $V_{25\%} = \frac{4}{3} \cdot \pi \cdot \left(\frac{1.25}{2}\right)^3 = 1.023\text{cm}^3$

333 Equation S12

334

335 Rearranging Equation 2 of the main manuscript to find the growth rate

336

337 $1.023 = 0.5236 \cdot e^{k_g \cdot t_{event}}$

338

339 $k_g = \frac{\ln(1.954)}{t_{event}}$

340 Equation S13

341

342 Equation S11 is equivalent to Equation 3 of the main text when an event is defined using

343 the RECIST criteria of 20% increase in SLD and Equation S13 is equivalent to Equation 3

344 of the main text when an event is defined using the WHO criteria of 25% increase in SLD.

345

346 Supplementary Equations 3: Assuming tumors are oblong rather than spherical

347

348 This manuscript assumes that tumors are spherical and grow accordingly. If we instead
349 assumed tumors were oblong shaped with equal short axes measurements, we find the
350 eventual values of growth rates of a progression “event” are equal to those derived under
351 the spherical assumption. In this supplementary document we show how that happens when
352 an event is defined as 20% increase in the diameter (results are the same when the WHO
353 25% increase criteria is used).

354

355 The oblong volume can be determined using

356

$$Oblong\ volume = \frac{4}{3} \cdot \pi \cdot w^2 \cdot L$$

Equation S14

359

360 where w is the radius of the two short axes and L is the radius of the longest length. We
 361 have no information to inform the relationship between L and w , so we first assume
 362 $w=0.5\cdot L$ and then $w=0.66\cdot L$

363

If the longest diameter of the initial tumor is $D_0=1\text{cm}$, the 20% increased diameter $D_{20\%}=1.2\text{cm}$ indicates a progression event and $w=0.5 \cdot L$. The corresponding oblong volumes are

367

$$V_0 = \frac{4}{3} \cdot \pi \cdot \left(0.5 \cdot \frac{1}{2}\right)^2 * \frac{1}{2} = 0.131 \text{ cm}^3$$

Equation S15

370

$$V_{20\%} = \frac{4}{3} \cdot \pi \cdot \left(0.5 \cdot \frac{1.2}{2}\right)^2 * \frac{1.2}{2} = 0.226 \text{ cm}^3$$

Equation S16

373

374 Rearranging Equation 2 of the main manuscript to find the growth rate

375

376
$$0.226 = 0.131 \cdot e^{k_g \cdot t_{event}}$$

377

378
$$k_g = \frac{\ln(1.728)}{t_{event}}$$

379

Equation S17

380

381 Note, this is the same equation we derived when assuming tumors are spherical (Equation
382 S11). If we instead assume the oblong width is two thirds the longest length

383
$$V_0 = \frac{4}{3} \cdot \pi \cdot \left(0.66 \cdot \frac{1}{2}\right)^2 * \frac{1}{2} = 0.228 \text{ cm}^3$$

384

Equation S18

385

386
$$V_{20\%} = \frac{4}{3} \cdot \pi \cdot \left(0.66 \cdot \frac{1.2}{2}\right)^2 * \frac{1.2}{2} = 0.394 \text{ cm}^3$$

387

Equation S19

388

389 Rearranging Equation 2 of the main manuscript to find the growth rate

390

391
$$0.394 = 0.228 \cdot e^{k_g \cdot t_{event}}$$

392

393
$$k_g = \frac{\ln(1.728)}{t_{event}}$$

394

Equation S20

395

396 Again, this is the same equation we derived when assuming tumors are spherical
397 (Equation S11).

398