SUPPLEMENTARY MATERIAL

	¹⁸ F-FDG to ¹⁸ F-FTP	¹⁸ F-FDG to ¹¹ C-PIB	¹⁸ F-FTP to ¹¹ C-PIB
Absolute interval in days Mean (SD) [min-max]	36.6 (154.8) [1-1622]	13.8 (30.9) [0-183]	22.8 (153.7) [0-1622]
Patients with both scans on the same day	0/117	25/117	92/117

Supplementary Table 1. Interval between ¹⁸F-FDG, ¹⁸F-Flortaucipir (FTP) and ¹¹C-PIB PET scans





Supplementary Figure 1. (A) Distribution of ¹⁸F-FDG cerebellar IA in controls (n=76) and patients (n=197) (B) 2 controls that were excluded due to significant asymmetry in cerebellar metabolism (arrow) or basal ganglia (arrowhead), likely due to vascular disease.

Absolute cortical IA	¹⁸ F-FDG	¹¹ C-PIB	¹⁸ F-FTP
	(n=197)	(n=117)	(n=117)
Mean	4.9 %	3.1 %	6.4 %
SD	4.0 %	3.6 %	6.7 %
Min	0.0 %	0.0 %	0.0 %
Мах	18.0 %	19.4 %	38.6 %

Supplementary Table 2. Distribution of absolute cortical index of asymmetry (IA) for each modality

Patients (n=197)	Parietal	Frontal	Temporal	Occipital	Basal ganglia
Cerebellar	725*	743*	613*	506*	617*
Parietal		.827*	.876*	.788*	.655*
Frontal			.780*	.540*	.729*
Temporal				.760*	.648*
Occipital					.434*

Controls (n=74)	Parietal	Frontal	Temporal	Occipital	Basal ganglia
Cerebellar	161	.066	.146	.001	.005
Parietal		.691*	.570*	.488*	.397†
Frontal			.650*	.329†	.349 [†]
Temporal				.388†	.508*
Occipital					.289†

Supplementary Table 3. Relationship between regional ¹⁸F-FDG IA and cerebellar ¹⁸F-FDG IA in the whole patient cohort (top) and in controls (bottom)

Pearson's correlation coefficients are shown; * p< .001

, † p< .01



Supplementary Figure 2. Relationship between ¹⁸F-FDG cerebellar IA, CDR-SB (left) and MMSE (right) by clinical diagnosis.

Relationship between disease severity (CDR-SB or MMSE) and cerebellar asymmetry on ¹⁸F-FDG was still significant when controlling for clinical diagnosis (coded as typical AD, atypical AD and non-AD). No interaction was seen between disease severity and clinical group.





Indirect path: p=0.01*



Direct path: p=0.45

Supplementary Figure 3. Mediation analyses between $^{18}\mbox{F-FDG}$ cerebellar IA, MMSE (A) and CDR-SB (B) (n=197)

	CCD (n=47)	No CCD (n=146)	p value
Act. tremor UL	15/46 (33%)	41/141 (29%)	p= .65
Asymmetry	5/46 (11%)	13/141 (9%)	p= .74
Act. tremor LL	0/46 (0%)	0/141 (0%)	p= 1.0
Asymmetry	0/46 (0%)	0/141 (0%)	p= 1.0
Pron. Sup.	14/46 (30%)	39/140 (28%)	p= .74
Asymmetry	7/46 (15%)	18/140 (13%)	p= .69
Fing. Nose	5/46 (11%)	11/141 (8%)	p= .56
Asymmetry	4/46 (9%)	6/141 (4%)	p= .25
Heel to shin	2/21 (10%)	0/38 (0%)	p= .06
Asymmetry	0/21 (0%)	0/38 (0%)	p= 1.0
Tandem walk	16/45 (36%)	47/138 (34%)	p= .86
Ataxic gait	0/45 (0%)	0/141 (0%)	p= 1.0

Supplementary Table 4. Tests of cerebellar function on neurological examination in patients

Number of subjects with abnormal test are indicated with percentage (%). For bilateral tests, number of subjects with asymmetric findings (L>R or R>L) are indicated with percentage (%).

Act. Tremor: action or postural tremor. UL: upper limbs, LL: lower limbs *Pron. Sup.:* pronation/supination of hand *Fing. Nose:* Finger to Nose



Supplementary Figure 4. Analyses similar to Figure 6 but additionally including the 51 patients with significant cerebellar ¹⁸F-FDG asymmetry.