- ¹ **Supplementary Information:**
- ² **Coexistence of structural and magnetic phases in van der**
- ³ **Waals magnet CrI**³
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¹⁸ Contents

$19 \quad 1 \quad \text{CrI}_3 \text{ bulk crystal growth}$ $19 \quad 1 \quad \text{CrI}_3 \text{ bulk crystal growth}$ $19 \quad 1 \quad \text{CrI}_3 \text{ bulk crystal growth}$ 2

²⁴ [6 Supplementary References](#page-12-0) 13

$25 \quad 1 \quad \text{CrI}_3 \text{ bulk crystal growth}$

²⁶ Chromium triiodide crystals were grown using the chemical vapour transport technique. Chromium ²⁷ powder (99.5% Sigma-Aldrich) and anhydrous iodine beads (99.999% Sigma-Aldrich) were mixed ²⁸ in a 1:3 ratio in an argon atmosphere inside a glovebox. 972 mg of the mixture were loaded into ²⁹ a silica ampoule with a length, inner diameter and outer diameter of 500 mm, 15 mm and 16 mm ³⁰ respectively (Supplementary Figure [1](#page-2-0)a). The ampoule was extracted from the glovebox with a ball 31 valve covering the open end to prevent air exposure and then it was immediately was evacuated ³² using a turbo-molecular pump down to 6×10^{-6} . Once the pressure stabilised, the closed end was 33 dipped in liquid nitrogen to prevent the sublimation of the iodide beads. The ampoule was then ³⁴ flame sealed and introduced into a three-zone furnace. An initial inverted gradient step was used ³⁵ to minimize nucleation sites in the growth zone. The gradient was then inverted so that the source

 $_{36}$ zone would remain at 650 o C, the middle growth zone at 550 o C and the third zone at 600 o C for 37 3 days. Crystal growth takes place in the centre and source zones. The single crystals and the ³⁸ microcrystalline powder were both extracted from the ampoule and stored in an argon atmosphere ³⁹ inside the glovebox to prevent oxidation and hydration. A sample of the bigger single crystals was ⁴⁰ ground into a powder using a razor blade. X-Rays diffraction analysis was performed on samples ⁴¹ of the powder and single crystalline CrI₃ by loading the material into a capillary and flame-sealing ⁴² it inside the glove box. The powder pattern of both samples were consistent with the monoclinic 43 AlCl₃-type structure (C2/m) reported for CrI₃ (Supplementary Figure [1](#page-2-0)b).

Supplementary Figure 1: CrI_3 samples. a, Picture of the ampoule used for sample fabrication. b, X-Ray diffraction pattern of the CrI₃ microcrystalline powder studied in the μ -SR experiment. The most prominent peaks of the orange trace (experiment) have been labelled (Miller indices) and marked (grey lines) with peaks positions of the monoclinic (room temperature) crystalline phase of CrI3.

 44 2 μ -SR experiment and analysis

⁴⁵ The μ -SR method is based on the observation of the time evolution of the spin polarization $\dot{P}(t)$ ⁴⁶ of the muon ensemble. In μ -SR experiments an intense beam ($p_{\mu} = 29$ MeV/c) of 100 % spin-⁴⁷ polarized muons is stopped in the sample. Currently available instruments allow essentially a back-48 ground free μ -SR measurement at ambient conditions $\frac{1}{\mu}$ $\frac{1}{\mu}$ $\frac{1}{\mu}$. The positively charged muons thermalize ⁴⁹ in the sample at interstitial lattice sites, where they act as magnetic microprobes. In a magnetic 50 material the muons spin precess in the local field B_{μ} at the muon site with the Larmor frequency ⁵¹ $v_\mu = \gamma_\mu/(2\pi)B_\mu$ (muon gyromagnetic ratio $\gamma_\mu/(2\pi) = 135.5$ MHz T⁻¹). The muons μ^+ implanted ϵ ₅₂ into the sample will decay after a mean life time of τ _μ = 2.2 μs, emitting a fast positron e^+ prefer-⁵³ entially along their spin direction. Various detectors placed around the sample track the incoming ⁵⁴ μ^+ and the outgoing e^+ . When the muon detector records the arrival of a μ in the specimen, the 55 electronic clock starts. The clock is stopped when the decay positron e^+ is registered in one of the ⁵⁶ e⁺ detectors, and the measured time interval is stored in a histogramming memory. In this way a 57 positron-count versus time histogram is formed. A muon decay event requires that within a certain ⁵⁸ time interval after a μ^+ has stopped in the sample a e^+ is detected. This time interval extends ⁵⁹ usually over several muon lifetimes (*e*.*g*. 10µs).

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 61 The GPS (π M3 beamline) μ -SR instrument at the Paul Scherrer Institute, Switzerland, was 62 used to study the CrI₃ sample. The specimen was mounted in a He gas-flow cryostat and the tem-⁶³ perature was varied between 5 and 200 K.

65 **Analysis of Weak TF-** μ **SR data** The weak TF asymmetry spectra were analyzed ^{[2,](#page-12-2)3} using the ⁶⁶ function:

$$
A_S(t) = A_p \exp(-\lambda t) \cos(\omega t + \phi).
$$
 (1)

67 where *t* is the time after muon implantation, $A(t)$ is the time-dependent asymmetry, A_p is the ampli-68 tude of the oscillating component (related to the paramagnetic volume fraction), λ is an exponential 69 damping rate due to paramagnetic spin fluctuations and/or nuclear dipolar moments, $\omega = 2\pi v_\mu$ is 70 the Larmor precession frequency set by the strength of the transverse magnetic field, and ϕ is a 71 phase offset. The zero for $A(t)$ was allowed to vary for each temperature to deal with the asymmetry ⁷² baseline shift occurring for magnetically ordered samples. From these refinements, the magneti- 73 cally ordered volume fraction at each temperature *T* was obtained by $V_M = 1 - A_p(T)/A_p(T_{max})$, ⁷⁴ where $A_p(T_{max})$ is the amplitude in the paramagnetic phase at high temperature.

75

 76 Analysis of ZF μ -SR data In the paramagnetic state, the μ -SR spectra are described by the com- π bination of Lorentzian and Gaussian Kubo-Toyabe depolarization function:

$$
A_{\text{ZF,PM}}(t) = (1 - V_M)A_0 \left(\frac{1}{3} + \frac{2}{3} \left(1 - (\sigma t)^2 - \Lambda t \right) e^{-\frac{1}{2} (\sigma t)^2 - \Lambda t} \right) \tag{2}
$$

 78 Here, the depolarisation rates σ and Λ are due to the nuclear dipole moments and randomly 79 oriented diluted local electronic moments, respectively. A_0 is the initial asymmetry. $V_{PM} = 1 - V_M$ ⁸⁰ is the paramagnetic fraction, which acquires maximum value of 1 above 60 K.

81 In the ordered state, the response of the sample consists of three magnetic components, de-82 pending on temperature:

$$
A_{\text{ZF,M}}(t) = V_M A_0 \omega_1 \left(f_{T1} \cos(\gamma_\mu B_{\mu 1} t + \phi) e^{-\lambda_{T1} t} + f_{L1} e^{-\lambda_{L1} t} \right) + \cdots
$$
 (3)

$$
V_M A_0 \omega_2 \left(f_{T2} \cos(\gamma_\mu B_{\mu 2} t + \phi) e^{-\lambda_{T2} t} + f_{L2} e^{-\lambda_{L2} t} \right) + \cdots \tag{4}
$$

$$
V_M A_0 \omega_3 \left(f_{T3} e^{-\lambda_{T3}t} + f_{L3} e^{-\lambda_{L3}t} \right) \tag{5}
$$

Bere, $ω_1$, $ω_2$, and $ω_3$ are the relative fractions of the magnetic components. The first and 84 second terms describe the high and low frequency magnetic components, respectively. The com-⁸⁵ ponents are characterised by an oscillating "transverse" component and a slowly relaxing "lon-⁸⁶ gitudinal" component. The longitudinal component arises due to muons experiencing local field 87 components which are parallel to the initial muon spin polarization. In polycrystalline samples 88 with randomly oriented fields the orientational averaging results in a so-called "one-third tail" with $f_L = \frac{1}{3}$ $\frac{1}{3}$ ($f_T = \frac{2}{3}$ ³⁹ with $f_L = \frac{1}{3} (f_T = \frac{2}{3})$. For single crystals, f_L varies between zero and unity as the orientation 90 between field and polarization changes from being perpendicular to parallel. λ_T and λ_L are the 91 transverse and longitudinal depolarisation rates of the μ -SR signals, respectively. $B_{\mu 1}$ and $B_{\mu 2}$ ⁹² are the internal magnetic fields at the muon site, corresponding to high and low frequency com-93 ponents, respectively. The third term describes the strongly damped magnetic component, which 94 occurs below 30 K only. We note that it is not possible to separate λ_{L3} from λ_{L1} and λ_{L2} and thus ⁹⁵ it is fixed to 0 in the analysis.

96 3 SQUID magnetometry

 Magnetization curves and zero-field-cooled/field-cooled susceptibility sweeps were carried out in 98 a SQUID magnetomoter (Quantum Design MPMS-XL-7) on single crystals of CrI₃ were the rel- ative orientation of the basal plane of the sample with the external magnetic field (both AC and DC) is controlled. In order to measure the magnetization of CrI₃ in the presence of in-plane and out-of-plane external magnetic fields, two different samples were prepared. For the out-of-plane orientation, various single crystals were stacked one on top of the other and placed onto the surface on the end of a polyethylene rod. This was carefully placed inside a silica tube with the crystals facing upwards and another polyethylene rod placed on top trapping the crystal in between. For the in-plane orientation, a polyethylene rod was cut longitudinally and a single crystal was glued to the flat using Apiezon-N grease. These preparations were performed in an argon atmosphere to avoid crystal degradation. The samples were then inserted inside an outer silica tube and flame 108 sealed at a pressure lower than 10^{-3} mbar.

109 4 Synchrotron X-ray diffraction measurements

 Synchrotron X-ray powder diffraction (SXRPD) measurements were performed on the BL04- MSPD beam-line of the ALBA Synchrotron Light Facility (Barcelona, Spain) using the multi-112 crystal analyser MAD detector system. The wavelength, $\lambda = 0.38670(3)$ Å, was determined by measuring a NIST standard silicon. This energy (32 KeV) was selected in order to avoid the flu- orescence from iodine ions (33 KeV). The sample was loaded in a borosilicate glass capillary of 0.3 mm diameter to keep the absorption below 1, and was kept spinning during data acquisition. Patterns between 10 and 300 K were collected using a Dynaflow liquid He cryostat. Measurements ¹¹⁷ were performed at fix temperatures in warming conditions, after a first cooling down to 10 K.

Supplementary Figure 2: Temperature dependent X-ray diffraction. a-c, Temperature evolution of selected monoclinic reflections below 80 K (MSPD Alba). Panels show the persistence of the monoclinic phase even at low temperatures. Notice the wide Lorentzian shape of the $(\pm 1L1)$ family of planes.

¹¹⁸ 5 Additional analysis on X-ray data

¹¹⁹ To illustrate the coupling between structures and magnetic phases in a different way, Supplemen-¹²⁰ tary Figures [S3](#page-9-1)−[4](#page-11-0) show the SXRPD intensity profiles of some R-peaks at the following selected ¹²¹ temperatures: 80, 65, 55, 40, 25 and 10 K. In Supplementary Figure [S3](#page-9-1) we compare the thermal 122 evolution of $(003)_R$ and $(116)_R$ profiles. Firstly, a sudden increase in the intensity is apparent in 123 both below 55 K. Secondly, and more interestingly, there is a remarkable intensity drop in $(003)_R$ 124 below 25 K, which concurs with a large increase of the intensity of $(116)_R$. These small but reliable 125 changes strongly suggest a coupling between the structure and the magnetic transitions in CrI₃.

Supplementary Figure 3: Temperature dependent X-ray diffraction. Anomalous temperature evolution close to the magnetic transition temperatures of the $(003)_R$ (left) and $(116)_R$ (right) rhombohedral peaks (MSPD Alba). Left: Sudden $(003)_R$ intensity increase below 55 K and sharp drop below 25 K. Right: Prominent $(116)_R$ intensity increase below 55 K and additional increase below 25 K, concurrent with the drop in $(003)_R$.

¹²⁶ Similar intensity changes were observed in most of the R-peaks. As a further example, 127 Supplementary Figure [S4](#page-11-0) shows the changes at low temperatures in the intensity of six additional 128 diffraction peaks. A marked intensity raise below 55 K is apparent in $(327)_R$, $(416)_R$, $(238)_R$, 129 $(051)_R$. The highest intensity is reached at 25 K for $(101)_R$, $(300)_R$, $(238)_R$, $(051)_R$ whereas ¹³⁰ a substantial intensity drop occurs at 10 K. The evolution of these peaks is reminiscent of that in 131 Supplementary Figure [S3,](#page-9-1) and it is in contrast with reflections $(327)_R$ or $(416)_R$ in which (mirroring 132 the peak (116) _R in Fig. [S3\)](#page-9-1) keeps growing also below 25 K. Therefore, this anomalous evolution ¹³³ is consistent with small structural changes causing certain relative intensity variations within the ¹³⁴ low-temperature range.

Supplementary Figure 4: Temperature dependent X-ray diffraction. Temperature evolution of some rhombohedral peaks of CrI3 (MSPD Alba) showing different trends in the temperature dependence below 80 K.

6 Supplementary References

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