- ¹ Supplementary Information:
- ² Coexistence of structural and magnetic phases in van der
- ³ Waals magnet Crl₃
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25 1 CrI₃ bulk crystal growth

Chromium triiodide crystals were grown using the chemical vapour transport technique. Chromium 26 powder (99.5% Sigma-Aldrich) and anhydrous iodine beads (99.999% Sigma-Aldrich) were mixed 27 in a 1:3 ratio in an argon atmosphere inside a glovebox. 972 mg of the mixture were loaded into 28 a silica ampoule with a length, inner diameter and outer diameter of 500 mm, 15 mm and 16 mm 29 respectively (Supplementary Figure 1a). The ampoule was extracted from the glovebox with a ball 30 valve covering the open end to prevent air exposure and then it was immediately was evacuated 31 using a turbo-molecular pump down to 6×10^{-6} . Once the pressure stabilised, the closed end was 32 dipped in liquid nitrogen to prevent the sublimation of the iodide beads. The ampoule was then 33 flame sealed and introduced into a three-zone furnace. An initial inverted gradient step was used 34 to minimize nucleation sites in the growth zone. The gradient was then inverted so that the source 35

zone would remain at 650 °C, the middle growth zone at 550 °C and the third zone at 600 °C for 36 3 days. Crystal growth takes place in the centre and source zones. The single crystals and the 37 microcrystalline powder were both extracted from the ampoule and stored in an argon atmosphere 38 inside the glovebox to prevent oxidation and hydration. A sample of the bigger single crystals was 39 ground into a powder using a razor blade. X-Rays diffraction analysis was performed on samples 40 of the powder and single crystalline CrI₃ by loading the material into a capillary and flame-sealing 41 it inside the glove box. The powder pattern of both samples were consistent with the monoclinic 42 AlCl₃-type structure (C2/m) reported for CrI₃ (Supplementary Figure 1b). 43



Supplementary Figure 1: CrI_3 samples. a, Picture of the ampoule used for sample fabrication. b, X-Ray diffraction pattern of the CrI_3 microcrystalline powder studied in the μ -SR experiment. The most prominent peaks of the orange trace (experiment) have been labelled (Miller indices) and marked (grey lines) with peaks positions of the monoclinic (room temperature) crystalline phase of CrI_3 .

44 **2** μ -SR experiment and analysis

The μ -SR method is based on the observation of the time evolution of the spin polarization $\vec{P}(t)$ 45 of the muon ensemble. In μ -SR experiments an intense beam ($p_{\mu} = 29$ MeV/c) of 100 % spin-46 polarized muons is stopped in the sample. Currently available instruments allow essentially a back-47 ground free μ -SR measurement at ambient conditions¹. The positively charged muons thermalize 48 in the sample at interstitial lattice sites, where they act as magnetic microprobes. In a magnetic 49 material the muons spin precess in the local field B_{μ} at the muon site with the Larmor frequency 50 $v_{\mu} = \gamma_{\mu}/(2\pi)B_{\mu}$ (muon gyromagnetic ratio $\gamma_{\mu}/(2\pi) = 135.5$ MHz T⁻¹). The muons μ^+ implanted 51 into the sample will decay after a mean life time of $\tau_{\mu} = 2.2 \ \mu s$, emitting a fast positron e^+ prefer-52 entially along their spin direction. Various detectors placed around the sample track the incoming 53 μ^+ and the outgoing e^+ . When the muon detector records the arrival of a μ in the specimen, the 54 electronic clock starts. The clock is stopped when the decay positron e^+ is registered in one of the 55 e^+ detectors, and the measured time interval is stored in a histogramming memory. In this way a 56 positron-count versus time histogram is formed. A muon decay event requires that within a certain 57 time interval after a μ^+ has stopped in the sample a e^+ is detected. This time interval extends 58 usually over several muon lifetimes (e.g. 10μ s). 59

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The GPS (π M3 beamline) μ -SR instrument at the Paul Scherrer Institute, Switzerland, was used to study the CrI₃ sample. The specimen was mounted in a He gas-flow cryostat and the temperature was varied between 5 and 200 K. Analysis of Weak TF- μ SR data The weak TF asymmetry spectra were analyzed ^{2,3} using the function:

$$A_{S}(t) = A_{p} \exp(-\lambda t) \cos(\omega t + \phi).$$
⁽¹⁾

where t is the time after muon implantation, A(t) is the time-dependent asymmetry, A_p is the ampli-67 tude of the oscillating component (related to the paramagnetic volume fraction), λ is an exponential 68 damping rate due to paramagnetic spin fluctuations and/or nuclear dipolar moments, $\omega = 2\pi v_{\mu}$ is 69 the Larmor precession frequency set by the strength of the transverse magnetic field, and ϕ is a 70 phase offset. The zero for A(t) was allowed to vary for each temperature to deal with the asymmetry 71 baseline shift occurring for magnetically ordered samples. From these refinements, the magneti-72 cally ordered volume fraction at each temperature T was obtained by $V_M = 1 - A_p(T)/A_p(T_{max})$, 73 where $A_p(T_{max})$ is the amplitude in the paramagnetic phase at high temperature. 74

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⁷⁶ Analysis of ZF μ -SR data In the paramagnetic state, the μ -SR spectra are described by the com-⁷⁷ bination of Lorentzian and Gaussian Kubo-Toyabe depolarization function:

$$A_{\text{ZF,PM}}(t) = (1 - V_M) A_0 \left(\frac{1}{3} + \frac{2}{3} \left(1 - (\sigma t)^2 - \Lambda t\right) e^{-\frac{1}{2}(\sigma t)^2 - \Lambda t}\right)$$
(2)

⁷⁸ Here, the depolarisation rates σ and Λ are due to the nuclear dipole moments and randomly ⁷⁹ oriented diluted local electronic moments, respectively. A_0 is the initial asymmetry. $V_{PM} = 1 - V_M$ ⁸⁰ is the paramagnetic fraction, which acquires maximum value of 1 above 60 K.

In the ordered state, the response of the sample consists of three magnetic components, depending on temperature:

$$A_{\text{ZF,M}}(t) = V_M A_0 \omega_1 \left(f_{T1} \cos(\gamma_\mu B_{\mu 1} t + \phi) e^{-\lambda_{T1} t} + f_{L1} e^{-\lambda_{L1} t} \right) + \cdots$$
(3)

$$V_{M}A_{0}\omega_{2}\left(f_{T2}\cos(\gamma_{\mu}B_{\mu2}t+\phi)e^{-\lambda_{T2}t}+f_{L2}e^{-\lambda_{L2}t}\right)+\cdots$$
(4)

$$V_M A_0 \omega_3 \left(f_{T3} e^{-\lambda_{T3}t} + f_{L3} e^{-\lambda_{L3}t} \right) \tag{5}$$

⁸³ Here, ω_1 , ω_2 , and ω_3 are the relative fractions of the magnetic components. The first and ⁸⁴ second terms describe the high and low frequency magnetic components, respectively. The com-⁸⁵ ponents are characterised by an oscillating "transverse" component and a slowly relaxing "lon-⁸⁶ gitudinal" component. The longitudinal component arises due to muons experiencing local field

components which are parallel to the initial muon spin polarization. In polycrystalline samples 87 with randomly oriented fields the orientational averaging results in a so-called "one-third tail" 88 with $f_L = \frac{1}{3}$ $(f_T = \frac{2}{3})$. For single crystals, f_L varies between zero and unity as the orientation 89 between field and polarization changes from being perpendicular to parallel. λ_T and λ_L are the 90 transverse and longitudinal depolarisation rates of the μ -SR signals, respectively. $B_{\mu 1}$ and $B_{\mu 2}$ 91 are the internal magnetic fields at the muon site, corresponding to high and low frequency com-92 ponents, respectively. The third term describes the strongly damped magnetic component, which 93 occurs below 30 K only. We note that it is not possible to separate λ_{L3} from λ_{L1} and λ_{L2} and thus 94 it is fixed to 0 in the analysis. 95

96 **3** SQUID magnetometry

Magnetization curves and zero-field-cooled/field-cooled susceptibility sweeps were carried out in 97 a SQUID magnetomoter (Quantum Design MPMS-XL-7) on single crystals of CrI₃ were the rel-98 ative orientation of the basal plane of the sample with the external magnetic field (both AC and 99 DC) is controlled. In order to measure the magnetization of CrI₃ in the presence of in-plane and 100 out-of-plane external magnetic fields, two different samples were prepared. For the out-of-plane 101 orientation, various single crystals were stacked one on top of the other and placed onto the surface 102 on the end of a polyethylene rod. This was carefully placed inside a silica tube with the crystals 103 facing upwards and another polyethylene rod placed on top trapping the crystal in between. For 104 the in-plane orientation, a polyethylene rod was cut longitudinally and a single crystal was glued 105 to the flat using Apiezon-N grease. These preparations were performed in an argon atmosphere 106 to avoid crystal degradation. The samples were then inserted inside an outer silica tube and flame 107 sealed at a pressure lower than 10^{-3} mbar. 108

109 4 Synchrotron X-ray diffraction measurements

Synchrotron X-ray powder diffraction (SXRPD) measurements were performed on the BL04-110 MSPD beam-line of the ALBA Synchrotron Light Facility (Barcelona, Spain) using the multi-111 crystal analyser MAD detector system. The wavelength, $\lambda = 0.38670(3)$ Å, was determined by 112 measuring a NIST standard silicon. This energy (32 KeV) was selected in order to avoid the flu-113 orescence from iodine ions (33 KeV). The sample was loaded in a borosilicate glass capillary of 114 0.3 mm diameter to keep the absorption below 1, and was kept spinning during data acquisition. 115 Patterns between 10 and 300 K were collected using a Dynaflow liquid He cryostat. Measurements 116 were performed at fix temperatures in warming conditions, after a first cooling down to 10 K. 117



Supplementary Figure 2: **Temperature dependent X-ray diffraction. a-c,** Temperature evolution of selected monoclinic reflections below 80 K (MSPD Alba). Panels show the persistence of the monoclinic phase even at low temperatures. Notice the wide Lorentzian shape of the $(\pm 1L1)$ family of planes.

118 5 Additional analysis on X-ray data

To illustrate the coupling between structures and magnetic phases in a different way, Supplementary Figures S3–4 show the SXRPD intensity profiles of some R-peaks at the following selected temperatures: 80, 65, 55, 40, 25 and 10 K. In Supplementary Figure S3 we compare the thermal evolution of $(003)_R$ and $(116)_R$ profiles. Firstly, a sudden increase in the intensity is apparent in both below 55 K. Secondly, and more interestingly, there is a remarkable intensity drop in $(003)_R$ below 25 K, which concurs with a large increase of the intensity of $(116)_R$. These small but reliable changes strongly suggest a coupling between the structure and the magnetic transitions in CrI₃.



Supplementary Figure 3: **Temperature dependent X-ray diffraction.** Anomalous temperature evolution close to the magnetic transition temperatures of the $(003)_R$ (left) and $(116)_R$ (right) rhombohedral peaks (MSPD Alba). Left: Sudden $(003)_R$ intensity increase below 55 K and sharp drop below 25 K. Right: Prominent $(116)_R$ intensity increase below 55 K and additional increase below 25 K, concurrent with the drop in $(003)_R$.

Similar intensity changes were observed in most of the R-peaks. As a further example, 126 Supplementary Figure S4 shows the changes at low temperatures in the intensity of six additional 127 diffraction peaks. A marked intensity raise below 55 K is apparent in $(327)_R$, $(416)_R$, $(238)_R$, 128 $(051)_R$. The highest intensity is reached at 25 K for $(101)_R$, $(300)_R$, $(238)_R$, $(051)_R$ whereas 129 a substantial intensity drop occurs at 10 K. The evolution of these peaks is reminiscent of that in 130 Supplementary Figure S3, and it is in contrast with reflections (327)_R or (416)_R in which (mirroring 131 the peak (116)_R in Fig. S3) keeps growing also below 25 K. Therefore, this anomalous evolution 132 is consistent with small structural changes causing certain relative intensity variations within the 133 low-temperature range. 134



Supplementary Figure 4: **Temperature dependent X-ray diffraction.** Temperature evolution of some rhombohedral peaks of CrI3 (MSPD Alba) showing different trends in the temperature dependence below 80 K.

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