

Supplementary Information: Systematic Optimization of Magnesium Force Field Parameters for Biomolecular Simulations with Accurate Solvation, Ion-pairing, and Water Exchange Properties in SPC/E, TIP3P-fb, TIP4P/2005, TIP4P-Ew, and TIP4P-D.

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Contents

S1 Supplementary methods	S3
S1.1 Literature values for central Mg ²⁺ properties	S3
S1.2 Water models	S3
S1.3 Simulation setups	S4
S1.4 Diffusion coefficient	S5
S1.5 Rate constant of water exchange	S5
S1.6 Calculation of activity derivatives	S6
S1.7 Calculation of free energy profiles	S7
S1.8 Binding affinity towards DMP	S9
S1.8.1 General strategies for computing binding affinities	S10
S1.8.2 Methods in this work for computing binding affinities	S11
S2 Supplementary results	S12
S2.1 Transferability	S12

S2.2 Isosurfaces	S13
S2.3 Lennard-Jones interaction potentials	S14
S2.4 One-dimensional free energy profiles for Mg^{2+} -water interactions	S15
S2.5 Two-dimensional free energy profiles for Mg^{2+} -water interactions	S16
S2.6 Binding affinities	S18
S3 Bibliography	S20

S1 Supplementary methods

S1.1 Literature values for central Mg^{2+} properties

Previous force fields for Mg^{2+} failed to provide a quantitative description of central properties of the ion. In Table S1 the central properties are listed for Mg^{2+} as obtained from the literature and compared to experiments.

Table S1: Values for Mg^{2+} models from the literature for central properties of the ion in comparison to experiments and one model of the current work.

	R_1 [nm]	ΔG_{solv} [kJ/mol]	k [s ⁻¹]	ΔG_{b}^0 [k _B T]
Mamatkulov-Schwierz (TIP3P) ¹	0.196 ¹	-2531.1 ¹	24 ± 9 ²	-14.53 ± 0.95 ³
Allner-Villa (TIP3P) ⁴	0.204 ⁴	-2397.3 ⁵	$\ll 2.39 \times 10^5$ ⁶	-12.17 ± 0.14 ⁶
Li-Merz (TIP3P) ⁷	0.194 ⁷	-2527.0 ⁷	$\ll 3.52 \times 10^4$ ⁶	n.a.
Li-Merz (TIP3P) [12-6-4] ⁸	0.208 ⁸	-2519.1 ⁸	$(1.44 \pm 0.03) \times 10^7$ ⁶	n.a.
Mamatkulov-Netz (SPC/E) ⁹	0.196 ⁹	-2532.0 ⁹	n.a.	-14.35 ± 0.48
Aquist (SPC/E) ¹⁰	0.199 ⁵	-2505.3 ⁵	n.a.	n.a.
Li-Merz (SPC/E) ⁷	0.195 ⁷	-2521.2 ⁷	n.a.	n.a.
Li-Merz (SPC/E) [12-6-4] ⁸	0.208 ⁸	-2524.9 ⁸	n.a.	n.a.
Li-Merz (TIP4P-Ew) ⁷	0.199 ⁷	-2520.3 ⁷	n.a.	n.a.
Li-Merz (TIP4P-Ew) [12-6-4] ⁸	0.208 ⁸	-2526.2 ⁸	n.a.	-7.65 ± 0.35 ⁶
<i>microMg</i> (SPC/E) [current work]	0.209	-2530.5	$(9.62 \pm 1) \times 10^5$	-1.266 ± 0.62
Exp.	0.209 ± 0.004 ¹¹	-2532 ¹²	$5.3 - 6.7 \times 10^5$ ^{13,14}	-1.036 ¹⁵

S1.2 Water models

We used five different rigid water models and listed their partial charges and Lennard-Jones parameters in Table S2. For SPC/E, the bond length is fixed at 0.1 nm and the bond angle at 109.47°. For TIP3P-fb, the bond length is fixed at about 0.10118 nm and the bond angle at about 108.15°. Otherwise, the bond length is 0.09572 nm and the bond angle is 104.52°.

Table S2: Parameters of different water models. The 3-site waters (SPC/E, TIP3P-fb) carry their negative partial charge ($q_{\text{Ow/Mw}}$) on the oxygen Ow, whereas for the 4-site waters (TIP4P/2005, TIP4P-Ew, and TIP4P-D), it is located on the slightly shifted additional site Mw. q_{H} is the partial charge of the hydrogen atoms and σ_{Ow} and ε_{Ow} the Lennard-Jones parameters of the water oxygen.

	$q_{\text{Ow/Mw}}$ [e]	q_{H} [e]	σ_{Ow} [nm]	ε_{Ow} [kJ/mol]
SPC/E	-0.8476	0.4238	0.3166	0.650
TIP3P-fb	-0.848448	0.424224	0.317796456355	0.652143528104
TIP4P/2005	-1.1128	0.5564	0.31589	0.774898
TIP4P-Ew	-1.04844	0.52422	0.316435	0.680946
TIP4P-D	-1.16	0.58	0.316508	0.936256

S1.3 Simulation setups

In all simulations long-range electrostatic forces were handled applying the particle-mesh Ewald method¹⁶ with periodic boundary conditions, a Fourier spacing of 0.12 nm and a grid interpolation up to order 4. Short-range Coulomb and Lennard-Jones interactions were cut off at 1.2 nm. In all simulations, a 2 fs timestep was used. In all simulations, ions and rigid water models are used, in those with AMBER we employed SETTLE,¹⁷ and in those with GROMACS we employed LINCS.¹⁸ Hydrogen bonds are constrained in all simulations containing DMP using LINCS. All the simulations started with an energy minimization by steepest decent, which was followed by two equilibration steps of 0.5 ns in NVT and 1 ns in NPT. The temperature was kept at 300 K and the pressure at 1 atm using thermostat and barostat of Berendsen.¹⁹ Position restraints were applied to all ions to ensure that no ions are pairing before hydration shells can properly form. The restraints were released in the production run. Lorentz-Berthelot combination rules were chosen for all simulations. The simulations to compute solvation free energy ΔG_{solv} , radius of the first hydration shell R_1 , and coordination number n_1 , were performed employing the thermostat and barostat of Berendsen¹⁹ with $\tau = 0.1$ and $\tau_p = 1.0$ to ensure a temperature of 300 K and roughly an atmospheric pressure of 1 bar. All other simulations were performed with the velocity rescaling thermostat by Bussi et al.²⁰ with $\tau = 0.1$. In case of the simulations in isothermal-isobaric ensemble (NPT in Table S3 and S4) the Parrinello-Rahman barostat²¹ with $\tau_p = 5.0$ was applied. Frames were written out every 0.2 ps if not stated otherwise. For both engines GROMACS and AMBER, the same setups were employed.

Table S3: This table shows all simulation setups of the 3-site water models SPC/E and TIP3P-fb. In 'Phys. property', the physical properties are listed that we obtained from the respective simulation using the respective 'Method' (FEP: free energy perturbation, unbiased: straight forward simulations without additional biases, US: umbrella sampling). 'System' lists all particles of the respective simulation and 'Duration' their duration (products show for FEP and US simulations the individual simulation windows). ' L ' indicates the simulation box size (edge length) for (cu) cubic and (do) rhombic dodecahedron box shapes. 'Ensemble' expresses if an canonical ensemble (with constant number of particles N , constant volume V , and constant temperature T), or an isobaric-isothermal ensemble (with constant pressure P and flexible simulation box size) was used. [GMX and AMBER specify the setup used for the 12-6 based (GMX) or the 12-6-4 based parameters (AMBER)].

Phys. property	Method	System	Duration	L	Ensemble
$\Delta G_{\text{solv}}, R_1, n_1$	FEP	1 Mg ²⁺ , 506 water	40 × 1 ns	2.5 nm (cu)	NPT
D_0	unbiased	1 Mg ²⁺ , 506 water	100 ns	2.5 nm (cu)	NVT
a_{cc}, k	unbiased	39 Mg ²⁺ , 78 Cl ⁻ , 2048 water (1 M)	1 μs	4 nm (cu)	NPT
a_{cc}	unbiased	73 Mg ²⁺ , 146 Cl ⁻ , 1961 water (2 M)	150 ns	4 nm (cu)	NPT
a_{cc}	unbiased	40 Mg ²⁺ , 20 Cl ⁻ , 2105 water (0.5 M)	150 ns	4 nm (cu)	NPT
a_{cc}	unbiased	20 Mg ²⁺ , 10 Cl ⁻ , 2135 water (0.25 M)	150 ns	4 nm (cu)	NPT
$F(r_{\text{MgOw}})$	US (GMX)	1 Mg ²⁺ , 505 water	68 × 3 ns	2.5 nm (cu)	NPT
$F(r_{\text{MgOw}})$	US (AMBER)	1 Mg ²⁺ , 500 water	68 × 3 ns	2.5 nm (cu)	NPT
$F(r_{\text{MgOw}_1}, r_{\text{MgOw}_2})$	US	1 Mg ²⁺ , 506 water	946 × 5 ns	2.5 nm (cu)	NVT
ΔG_{b}^0	FEP	1 DMP, 1 Mg ²⁺ , 1 Cl ⁻ , 1492 water	20 × 15 ns	4 nm (do)	NPT
$\Delta G_{\text{b}}^0, F(r_{\text{MgOP}})$	US	1 DMP, 1 Mg ²⁺ , 1 Cl ⁻ , 1492 water,	67 × 20 ns	4 nm (do)	NVT
$\Delta G_{\text{ref}}^0, F(r_{\text{ref-OP}})$	US	1 DMP, 1 ref atom, 1 Cl ⁻ , 1492 water	67 × 20 ns	4 nm (do)	NVT

Table S4: This table lists all simulation setups using the 4-site water models TIP4P/2005, TIP4P-Ew, and TIP4P-D that differ from Table S4. If the required 'Phys. property' is not listed here, the same setup is applied as in Table S3.

Phys. property	Method	System	Duration	L	Ensemble
a_{cc}, k	unbiased	39 Mg ²⁺ , 78 Cl ⁻ , 2055 water (1 M)	150 ns	4 nm (cu)	NPT
a_{cc}	unbiased	73 Mg ²⁺ , 146 Cl ⁻ , 1909 water (2 M)	150 ns	4 nm (cu)	NPT
a_{cc}	unbiased	20 Mg ²⁺ , 40 Cl ⁻ , 2135 water (0.5 M)	150 ns	4 nm (cu)	NPT
a_{cc}	unbiased	10 Mg ²⁺ , 20 Cl ⁻ , 2171 water (0.25 M)	150 ns	4 nm (cu)	NPT
ΔG_b^0	FEP	1 DMP, 1 Mg ²⁺ , 1 Cl ⁻ , 1536 water	20 × 15 ns	4 nm (do)	NPT
$\Delta G_b^0, F(r_{\text{MgOP}})$	US	1 DMP, 1 Mg ²⁺ , 1 Cl ⁻ , 1536 water	67 × 20 ns	4 nm (do)	NVT
$\Delta G_{\text{ref}}^0, F(r_{\text{ref-OP}})$	US	1 DMP, 1 ref atom, 1 Cl ⁻ , 1536 water	67 × 20 ns	4 nm (do)	NVT

S1.4 Diffusion coefficient

Diffusion coefficients D_0 were calculated from 10 ns long NVT simulations. The first 1 ns was excluded in each trajectory from the analysis. We calculated the coefficients $D_{\text{pbc}}(L)$ from a straight line fit of the slope of the mean-squared displacement of the single ion and took only the linear part into account. The obtained diffusion coefficient was size-corrected²² by

$$D_0 = \frac{\eta_W}{\eta_{\text{water}}} \left[D_{\text{pbc}}(L) + \frac{k_B T \zeta_{\text{ew}} \alpha}{6\pi\eta L} \right]. \quad (\text{S1})$$

We explicitly took the different viscosities η_W of the different water models W into account (Table S5).

Table S5: Viscosities η_W for each water model W . Values for SPC/E and TIP4P/2005 are taken from ref.,²³ the value for TIP4P-D is taken from ref.,²⁴ the other values are from their original publications (TIP3P-fb,²⁵ TIP4P-Ew²⁶).

	[kg m ⁻¹ s ⁻¹]
$\eta_{\text{SPC/E}}$	$7.29 \cdot 10^{-4}$
$\eta_{\text{TIP3P-fb}}$	$3.13 \cdot 10^{-4}$
$\eta_{\text{TIP4P/2005}}$	$8.55 \cdot 10^{-4}$
$\eta_{\text{TIP4P-Ew}}$	$7.2 \cdot 10^{-4}$
$\eta_{\text{TIP4P-D}}$	$9.37 \cdot 10^{-4}$

S1.5 Rate constant of water exchange

The most popular theory to calculate reaction rates is transition state theory (TST).^{27,28} In simple systems for which the reaction coordinate is exactly known, TST gives an accurate estimate of the rate. However, in complex many body systems as the ones presented here, TST can fail due to the violation of the non-recrossing hypothesis, one of the fundamentals of the theory. Therefore, in the following an alternative approach is presented (for more details see ref.⁶).

For the exchange of water from the first hydration shell of Mg^{2+} , the rate constant k is defined by¹³

$$\text{rate} = 6 \cdot k \cdot [\text{Mg}(\text{H}_2\text{O})_6^{2+}] , \quad (\text{S2})$$

where 6 is the coordination number of the first hydration shell and $[\text{Mg}(\text{H}_2\text{O})_6^{2+}]$ is the concentration of hexa-coordinated Mg^{2+} ions.

In this work, the water exchange rate constant k is calculated by counting the total number of transitions that are observed within a $1 \mu\text{s}$ long trajectories of a 1 M MgCl_2 solution. As a transition N , we regard the exchange of waters between the first and second hydration shell of Magnesium (the exchange from first to second hydration shell and the reverse transition are counted as individual events). The water exchange rate constant k is hence given by

$$k = \frac{1}{N_{\text{H}_2\text{O}}} \cdot \frac{N}{2 \cdot t_B} , \quad (\text{S3})$$

where $N_{\text{H}_2\text{O}}$ is the number of water molecules in the simulation box. $t_B = N_{\text{Mg}} \cdot p_B \cdot t_{\text{sim}}$ is the cumulative time the water molecule spends in the first hydration shell of any Mg^{2+} ion. N_{Mg} is the number of Mg^{2+} ions in the simulation box, $p_B = 6/(N_{\text{H}_2\text{O}} - 6)$ is the probability of water to be in the first hydration shell and t_{sim} is the total simulation time. Errors are calculated from block averaging²⁹ by dividing the trajectory into 2 blocks.

S1.6 Calculation of activity derivatives

The derivative a_{cc} of the activity $a_c = \rho_c y_c$ with activity coefficient y_c is defined via

$$a_{cc} = \left(\frac{\partial \ln a_c}{\partial \ln \rho_c} \right)_{P,T} = 1 - \left(\frac{\partial \ln y_c}{\partial \ln \rho_c} \right)_{P,T} = \frac{1}{1 + \rho_c (G_{cc} - G_{co})} , \quad (\text{S4})$$

with respect to the natural logarithm of the number density ρ_c . The expressions G_{cc} and G_{co} are for divalent cations obtained^{30,31} from

$$G_{cc} = \frac{1}{9} \left[G_{+++} + 4(G_{--} + G_{+-}) \right] \quad (\text{S5})$$

and

$$G_{co} = G_{oc} = \frac{1}{3} G_{+o} + \frac{2}{3} G_{-o} , \quad (\text{S6})$$

where G_{ij} are the Kirkwood-Buff (KB) integrals³¹⁻³³ (eq S7) with +, -, and o denoting the cation, anion, and water oxygen, respectively. To obtain these KB integrals we followed that same strategy as in ref.,⁶

$$G_{ij} = 4\pi \int_0^\infty [g_{ij}^{\mu\text{VT}}(r_{ij}) - 1] r_{ij}^2 dr_{ij}, \quad (\text{S7})$$

where $g_{ij}^{\mu\text{VT}}(r_{ij})$ is the radial distribution function of the two species in the grand canonical ensemble, with r_{ij} being the center of mass distance between the two. Note that the simulation were done in the NPT ensemble. Therefore, we introduce a correction factor such that the radial distribution function used in the calculations of the KB integrals shows the correct asymptotic behavior at large distances (for more details see refs.^{1,6,31,33}).

S1.7 Calculation of free energy profiles

We computed all free energy profiles $F(R)$ with umbrella sampling^{34,35} and the weighted histogram analysis method (WHAM)³⁶ to combine the individual umbrella windows.

1D Mg²⁺ - water: One dimensional free energy profiles as a function of the distance between Mg²⁺ and the oxygen atom of the leaving water molecule for the 12-6 type force fields were computed with GROMACS³⁷ (version 2020). The profile of the 12-6-4 type force field in SPC/E water was computed using AMBER³⁸ (version 2018) and PLUMED³⁹ (version 2.5). Force constants and window spacing were in both setups $k = 400,000$ kJ/(mol nm²) and 0.005 nm [$0.17 \leq R_{\text{MgOx}} < 0.4$ nm] and $k = 100,000$ kJ/(mol nm²) and 0.01 nm [$0.4 \leq R_{\text{MgOx}} < 0.6$ nm]. Frames for the analysis were considered every 0.5 ps. We took a bin width of 5.4×10^{-4} nm into account for WHAM.

To ensure convergence, windows of size 50 ns were obtained and subdivided into blocks of (A) 10 x 5 ns, (B) 5 x 10 ns, and (C) 2 x 25 ns for the Mamatkulov-Netz parameters in SPC/E water (Figure S1). Of each individual block a free energy profile is calculated. Afterwards, we transformed the free energy profiles into potentials of mean force $V^{\text{PMF}}(R)$ by applying a Jacobian correction,

$$V^{\text{PMF}}(R) = F(R) + 2k_{\text{B}}T \ln R, \quad (\text{S8})$$

to take radial distances rather the Cartesian coordinates into account. We find that with windows of duration (A) 5 ns and (B) 10 ns the individual profiles show deviations whereas with a duration of (C) 25 ns the results are converged.

All other water exchange free energy profiles were thus simulated for 25 ns (see Table S3 and S4 for more

details on the simulation setups).

As an additional validation step, we obtained the radial distribution function $g(R)$ from the 1 μ s 1 M MgCl₂ trajectory and the free energy profile via Boltzmann inversion. Note that the free energy profile from the radial distribution function is used only to validate the depth of the two minima. The barrier height cannot be derived from this method as the transitions of water exchange are too rare. Further insight into the quality of the umbrella sampling method is provided by the evenly spaced and overlapping histograms (Figure S1D).

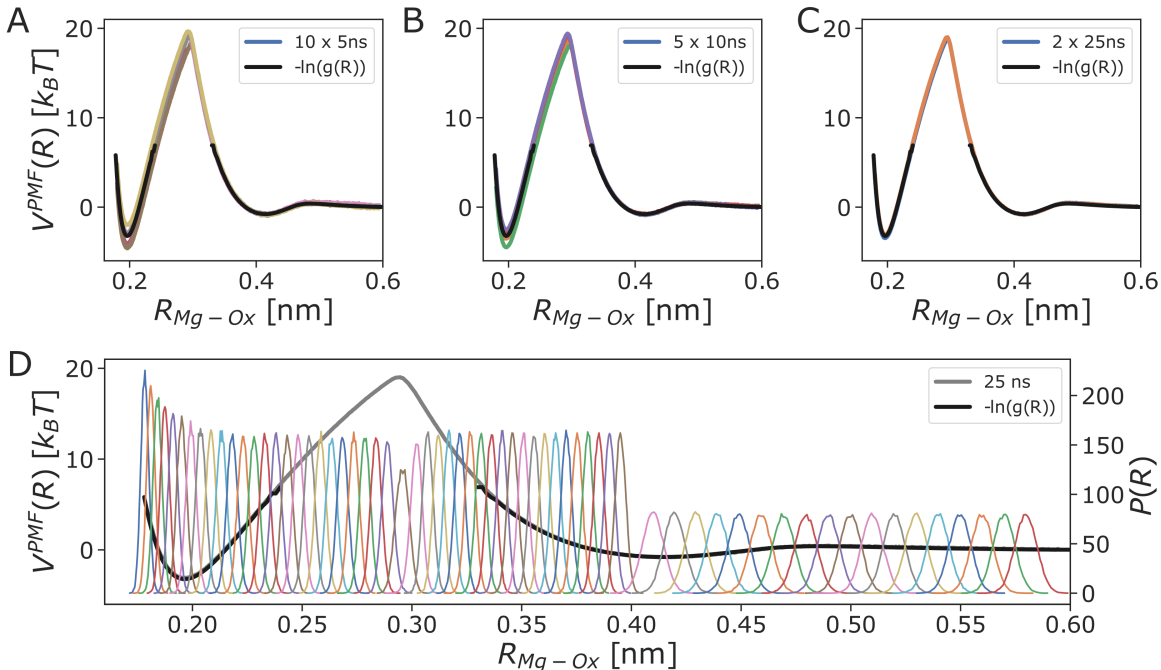


Figure S1: Convergence check. Potential of mean force $V^{\text{PMF}}(R)$ along the distance between a Mg²⁺ ion and the oxygen atom of the leaving water molecule, obtained from windows of 50 ns that are subdivided into blocks of (A) 10 x 5 ns, (B) 5 x 10 ns, and (C) 2 x 25 ns and $V^{\text{PMF}}(R)$ obtained from $-\ln g(R)$. In (D) additional to $V^{\text{PMF}}(R)$ obtained from 25 ns long windows, the histograms are shown. Parameters used are Mamatkulov-Netz and SPC/E water.

1D Mg²⁺ - phosphate oxygen: The free energy profile along the distance between Mg²⁺ and one of the two non-bridging phosphate oxygens of the dimethylphosphate (DMP) was obtained with force constants and window spacing of $k = 300,000$ kJ/(mol nm²) and 0.0075 nm [$0.15 \leq R_{\text{MgOP}} < 0.525$ nm] and $k = 5,000$ kJ/(mol nm²) and 0.02 nm [$0.525 \leq R_{\text{MgOP}} < 0.885$ nm], respectively, using GROMACS⁴⁰ (version 2020). PLUMED³⁹ was employed to include an additional bias avoiding any direct interaction with any of the DMP atoms but the selected phosphate oxygen (see ref. ⁶ for more details). Frames for the analysis were considered every 0.5 ps. For WHAM a bin width of 9.2×10^{-4} nm was considered.

To ensure convergence, windows of size 100 ns were obtained and subdivided into blocks of (A) 10 x 10

ns, (B) 5 x 20 ns, and (C) 2 x 50 ns for the Mamatkulov-Netz SPC/E parameters (Figure S2). The results show that 20 ns per window are sufficient to provide converged results. For all other profiles for DMP and Mg^{2+} , windows were simulated for 20 ns (see Table S3 and S4 for more details on the simulation setups). Additionally, Figure S2D shows the overlapping histograms of neighboring simulation windows.

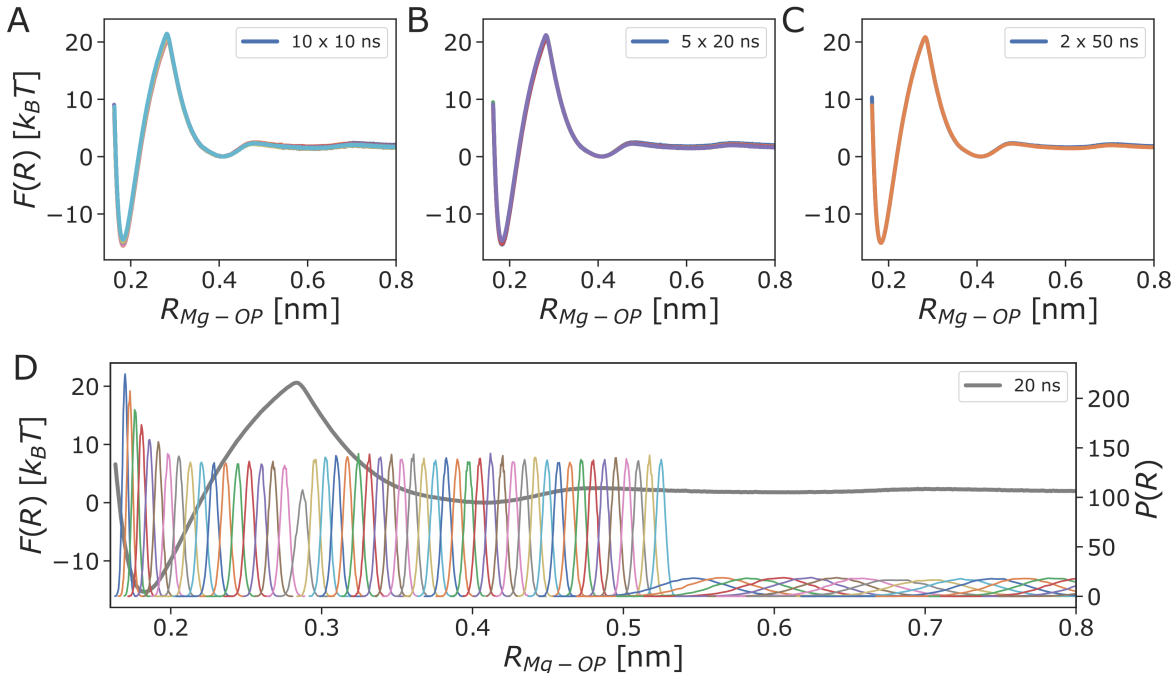


Figure S2: Convergence check. Free energy profile $F(R)$ along the distance between one of the non-bridging oxygens of the DMP and a Mg^{2+} ion, obtained from windows of 100 ns that are subdivided into blocks of (A) 10 x 10 ns, (B) 5 x 20 ns, and (C) 2 x 50 ns. In (D) additional to $F(R)$ obtained from 20 ns long windows, overlapping distance histograms are shown. Parameters used are Mamatkulov-Netz and SPC/E water.

S1.8 Binding affinity towards DMP

Calculating binding affinities from molecular dynamics simulations can be challenging since the results depend sensitively on accurate sampling. In principle, one can obtain the binding affinity of a metal cation toward the phosphate oxygen in three different ways: (i) Via association/dissociation rates, (ii) via free energy perturbation calculations, or (iii) via integrating potentials of mean force (PMFs). All three methods yield consistent results if accurately sampled (see Table S6 for results for Ca^{2+} from previous works). To avoid possible pitfalls, we strongly recommend to use different methods to verify binding affinities obtained by computer simulations.

S1.8.1 General strategies for computing binding affinities

Association/dissociation rates If association k_{on} and dissociation k_{off} rates are available, the free energy of binding can be calculated from

$$\Delta G_{\text{b}}^0 = -k_{\text{B}}T \cdot \ln \left(\frac{c^0}{[M]} \cdot \frac{k_{\text{on}}}{k_{\text{off}}} \right), \quad (\text{S9})$$

with respect to the standard concentration $c^0 = 1$ M. For Ca^{2+} , the rates were calculated in our previous work⁴¹ and the results for the resulting free energy are shown in Table S6.

Free energy perturbation The binding free energy can be obtained from free energy perturbation using the double decoupling method (DDM)⁴² or alchemical transformation calculations.^{43,44} In the former (eq S10), both van der Waals as well as electrostatic interactions are decoupled for the ion in solution ($\Delta G_{\text{elec+vdW}}^{\text{solv}}$) and turned back on for an ion at the binding site ($\Delta G_{\text{elec+vdW}}^{\text{BS}}$). The effect of the restraints to keep the ion in the binding site during the decoupling in bulk ($\Delta G_{\text{rest}}^{\text{solv}}$) and in the binding site ($\Delta G_{\text{rest}}^{\text{BS}}$) has to be included⁴²

$$\Delta G_{\text{b}}^0 = \Delta G_{\text{elec+vdW}}^{\text{solv}} + \Delta G_{\text{elec+vdW}}^{\text{BS}} + \Delta G_{\text{rest}}^{\text{solv}} + \Delta G_{\text{rest}}^{\text{BS}} \quad (\text{S10})$$

In the alchemical transformation (eq S11), a reference ion of the same valency is used. The ion of interest is alchemically transformed into the reference ion, both in bulk ($\Delta G_{\text{ion} \rightarrow \text{ref}}^{\text{solv}}$) as well as at the binding site ($\Delta G_{\text{ref} \rightarrow \text{ion}}^{\text{B}}$)

$$\Delta G_{\text{b}}^0 = \Delta G_{\text{ion} \rightarrow \text{ref}}^{\text{solv}} + \Delta G_{\text{ref}}^0 + \Delta G_{\text{ref} \rightarrow \text{ion}}^{\text{BS}} \quad (\text{S11})$$

where ΔG_{ref}^0 is the binding affinity of the reference ion. To check the convergence, the transformation is done in opposite directions (i.e. forward and backward). For Ca^{2+} , the values for both methods were obtained from our previous works^{3,41} and are listed in Table S6.

Integration of a potential of mean force Here, the binding affinity is obtained by integrating the potential of mean force $V^{\text{PMF}}(r)$ (eq S8) along the distance r between the binding site and the ion of interest,

$$\Delta G_{\text{b}}^0 = -k_{\text{B}}T \cdot \ln \left(\frac{c^0}{[M]} \cdot \frac{\int_0^{r^\dagger} r^2 e^{-V^{\text{PMF}}(r)/k_{\text{B}}T} dr}{\int_{r^\dagger}^{r_{\text{L}}} r^2 e^{-V^{\text{PMF}}(r)/k_{\text{B}}T} dr} \right), \quad (\text{S12})$$

where $[M]$ is the ion concentration of the simulation box, r_{L} is the radius of a sphere that contains the same number of water molecules as the simulation box and r^\dagger is the position of the maximum of the PMF. Note that both $[M]$ and r_{L} are dependent on the number of waters in the simulation such that eq S12 becomes

independent of the box size used. The value for Ca^{2+} listed in Table S6 is taken from our previous work.⁶

As shown in Table S6 the results for Ca^{2+} for all four methods match within error. This demonstrates that the methods are converged and that all of these setups to obtain the binding free energy for Ca^{2+} (which is used as reference ion in this current work) are sufficiently accurate.

Table S6: Comparison of different methods to compute the free binding energy of Ca^{2+} to a non-bridging phosphate oxygen using the parameters by Mamatkulov-Schwierz in TIP3P.¹

Method	Formula	$\Delta G_{\text{Ca}^{2+}}^0$ [k _B T]
Rates (TREMMD)	(S9)	-4.51 ± 1.27 ⁴¹
FEP DDM	(S10)	-4.57 ± 0.90 ⁴¹
FEP alchem. trafo.	(S11)	-4.86 ± 0.85 ³
PMF	(S12)	-4.84 ± 0.18 ⁶

S1.8.2 Methods in this work for computing binding affinities

In this present work, to fine-tune the interaction and find scaling factors between the different Mg^{2+} models and the phosphate oxygen, we primarily computed the binding affinities via integration of PMFs (eq S12), as this strategy also includes a more mechanistic picture due to the obtained energetic profiles. The free energy profiles (most of which are shown in Figure 6B,C in the main text) were obtained using umbrella sampling. Details on all the simulation parameters are given in Section S1.2 and all parameters for the umbrella sampling in Section S1.6. (All simulation parameters are exactly the same as in our previous work before.⁶)

The concentrations of Mg^{2+} in the simulation boxes used in eq S12 are $[M] = 0.037$ M and 0.036 M for the 3-site and 4-site waters, respectively. Errors are calculated by dividing the 20 ns long windows into 4 blocks, and subsequent calculation of PMFs and thus ΔG_b^0 from each block and block averaging.

As an independent validation step, we selected a second method to obtain the binding affinities. Association/dissociation rates are very difficult to obtain for Mg^{2+} due to the long timescales involved. Therefore, we chose alchemical transformation calculations (eq S11), as their accuracy is comparable to other methods (Table S6), while they are computationally more efficient than the double decoupling method (eq S10) as fewer steps are involved. Employing the final scaling factors (Table 1, main text), we calculate Mg^{2+} binding affinities toward the DMP by transforming the Mg^{2+} ion for each water models into a reference ion (eq S11) and using forward and backward transformations. For the reference ion, we chose the parameters by Mamatkulov-Schwierz for Ca^{2+} in TIP3P water¹ since we already had well converged results based on our previous work (Table S6).

The transformation was performed in 20 iterative steps gradually switching the Lennard-Jones parameters from the respective Mg^{2+} model to the reference ion and vice versa both in solution as well as at its binding site (yielding $\Delta G_{\text{ion} \rightarrow \text{ref}}^{\text{solv}}$ and $\Delta G_{\text{ref} \rightarrow \text{ion}}^{\text{BS}}$ from eq S11).

ΔG_{ref}^0 for each water model was obtained from integration of the potentials of mean force (Figure S8) using eq S12 (simulation parameters are again given in Section S1.2 and Section S1.6) and the values are listed in Table S8.

Employing the respective reference binding affinities, we check for convergence by performing the transformation for each Mg^{2+} model corresponding to one of the five waters both in forward as well as in backward direction (Tables S9 and S10).

Both methods yielded identical results within error (Tables S8, S9, and S10). Errors were calculated from block averaging by dividing the trajectory of the alchemical transformation into 5 blocks.

S2 Supplementary results

S2.1 Transferability

Table S7: Parameters and single-ion properties after converting *microMg*(TIP3P) and *nanoMg*(TIP3P) into *microMg*(TIP3P|W) and *nanoMg*(TIP3P|W) using Lorentz-Berthelot combination rules (eq 2, main text, unscaled). σ_{ii} , ε_{ii} , σ_{io} , ε_{io} are the ion-ion and ion-water LJ parameters single-ion properties. ΔG_{solv} , R_1 , and n_1 are the solvation free energy of the neutral MgCl_2 ion-pair, the radius of the first hydration shell, and the coordination number of the first hydration shell, respectively.

	σ_{ii} [nm]	ε_{ii} [kJ/mol]	σ_{io} [nm]	ε_{io} [kJ/mol]	ΔG_{solv} [kJ/mol]	R_1 [nm]	n_1
<i>microMg</i> (TIP3P SPC/E)	0.1019	235.80	0.2101	13.75	-2534.9 ± 1	0.206 ± 0.004	6
<i>nanoMg</i> (TIP3P SPC/E)	0.1025	389.80	0.2106	17.50	-2535.0 ± 1	0.210 ± 0.004	6
<i>microMg</i> (TIP3P TIP3P-fb)	0.1019	235.80	0.2107	13.77	-2536.1 ± 1	0.208 ± 0.004	6
<i>nanoMg</i> (TIP3P TIP3P-fb)	0.1025	389.80	0.2112	17.52	-2535.5 ± 1	0.211 ± 0.004	6
<i>microMg</i> (TIP3P TIP4P/2005)	0.1019	235.80	0.2097	15.01	-2451.2 ± 1	0.210 ± 0.004	6
<i>nanoMg</i> (TIP3P TIP4P/2005)	0.1025	389.80	0.2102	19.10	-2455.8 ± 1	0.213 ± 0.004	6
<i>microMg</i> (TIP3P TIP4P-D)	0.1019	235.80	0.2101	14.49	-2474.7 ± 1	0.211 ± 0.004	6
<i>nanoMg</i> (TIP3P TIP4P-D)	0.1025	389.80	0.2106	20.99	-2483.1 ± 1	0.214 ± 0.004	6
<i>microMg</i> (TIP3P TIP4P-Ew)	0.1019	235.80	0.2100	14.07	-2462.9 ± 1	0.208 ± 0.004	6
<i>nanoMg</i> (TIP3P TIP4P-Ew)	0.1025	389.80	0.2105	17.90	-2465.4 ± 1	0.212 ± 0.004	6
exp.					-2532^{12}	0.209 ± 0.004^{11}	6 ¹¹

S2.2 Isosurfaces

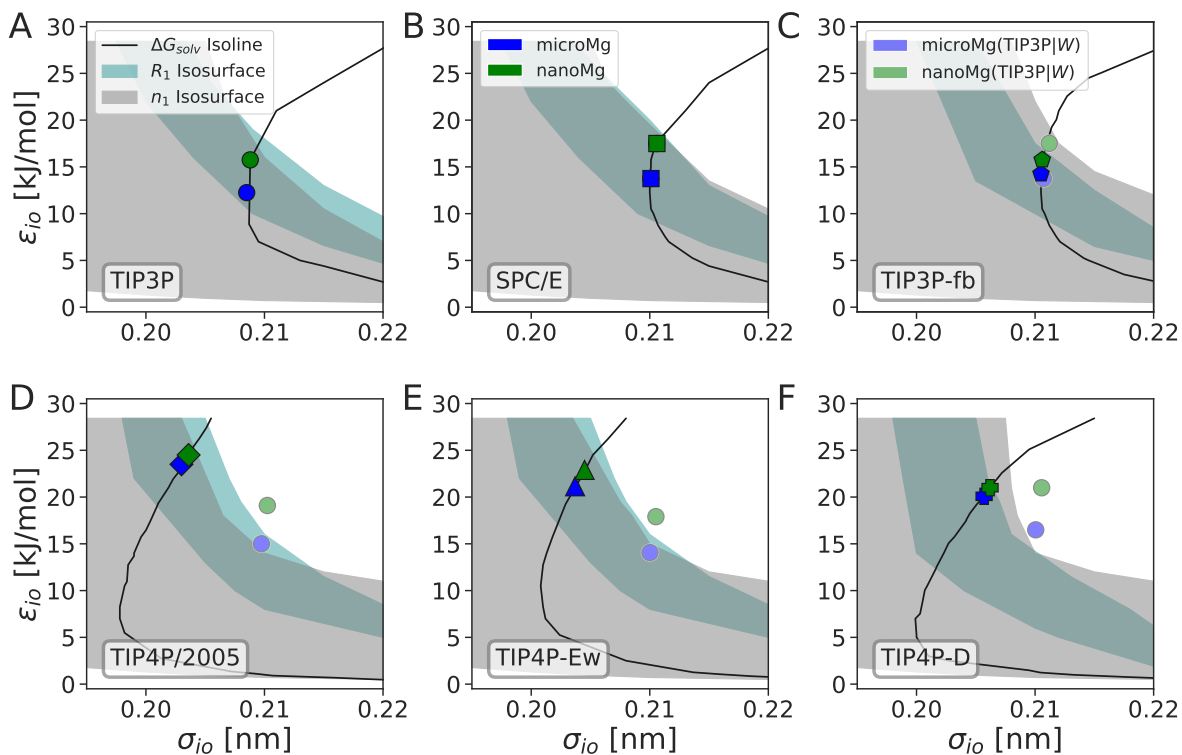


Figure S3: Solvation free energy ΔG_{solv} , radius of the first hydration shell R_1 , and coordination number n_1 isosurfaces in $\sigma_{\text{io}} - \epsilon_{\text{io}}$ space for the interaction of the *microMg* and *nanoMg* parameters of various water models, including the force fields for (A) TIP3P⁴⁵ from the literature,⁶ (B) SPC/E,⁴⁶ (C) TIP3P-fb,²⁵ (D) TIP4P/2005,⁴⁷ (E) TIP4P-Ew,²⁶ and (F) TIP4P-D.⁴⁸ Transparent circles indicate converted *microMg*(TIP3P|*W*) and *nanoMg*(TIP3P|*W*) parameters, using the ion-ion parameter sets, σ_{ii} and ϵ_{ii} , of TIP3P water⁶ and Lorentz-Berthelot combination rules (eq 2, main text, unscaled) to gain the effective water-ion parameter sets, σ_{io} and ϵ_{io} , of the respective water model *W* (Table S7). In parameter regions far off the ΔG_{solv} isolines, grid points are sparser. Therefore, the R_1 and n_1 surfaces are less accurate in those regions.

S2.3 Lennard-Jones interaction potentials

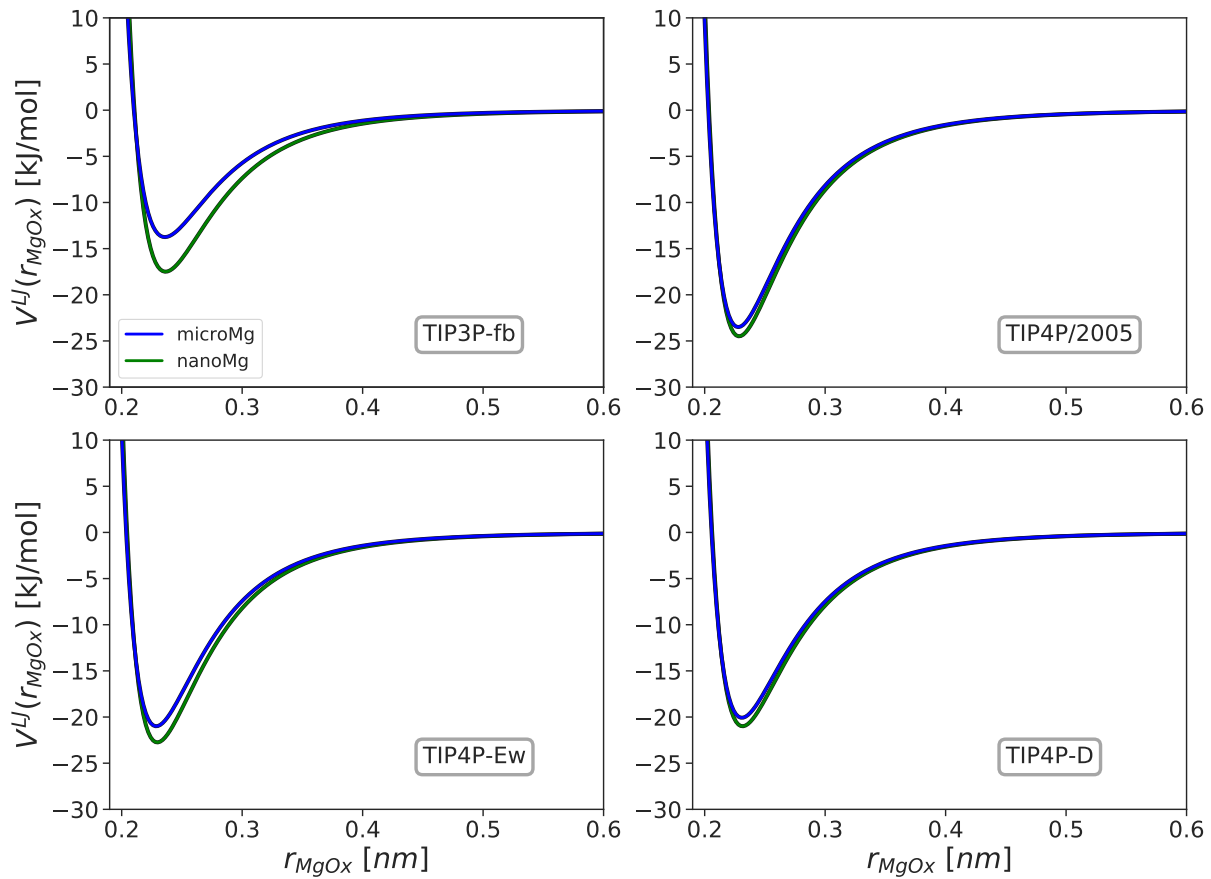


Figure S4: Lennard-Jones interaction potential V^{LJ} as function of the Mg²⁺-oxygen distance r_{MgOx} for different Mg²⁺ force fields and (A) TIP3P-fb,²⁵ (B) TIP4P/2005,⁴⁷ (C) TIP4P-Ew,²⁶ and (D) TIP4P-D⁴⁸ water models.

S2.4 One-dimensional free energy profiles for Mg^{2+} -water interactions

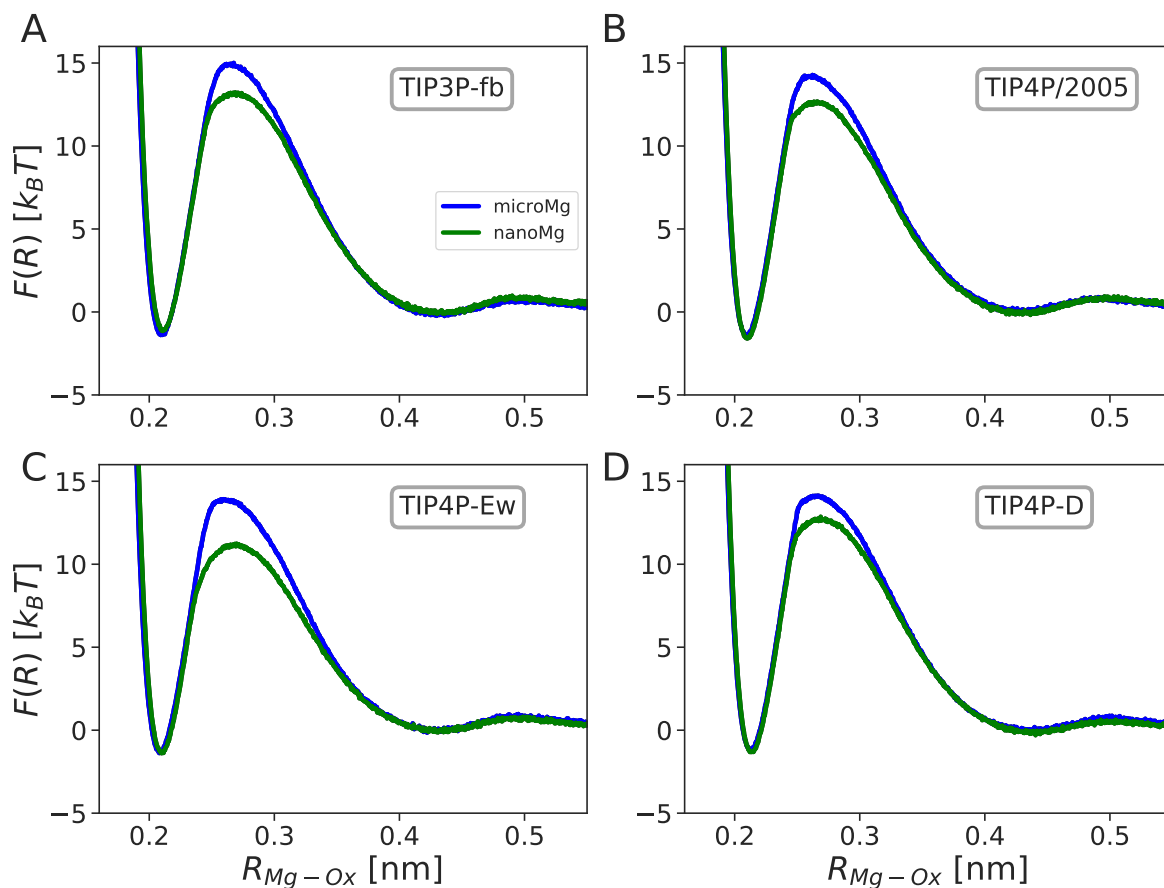


Figure S5: One-dimensional free energy profiles as a function of the distance between Mg^{2+} and the leaving water molecule $R_{\text{Mg}-\text{Ox}}$ for different force fields in combination with (A) TIP3P-fb,²⁵ (B) TIP4P/2005,⁴⁷ (C) TIP4P-Ew,²⁶ and (D) TIP4P-D⁴⁸ water models.

S2.5 Two-dimensional free energy profiles for Mg^{2+} -water interactions

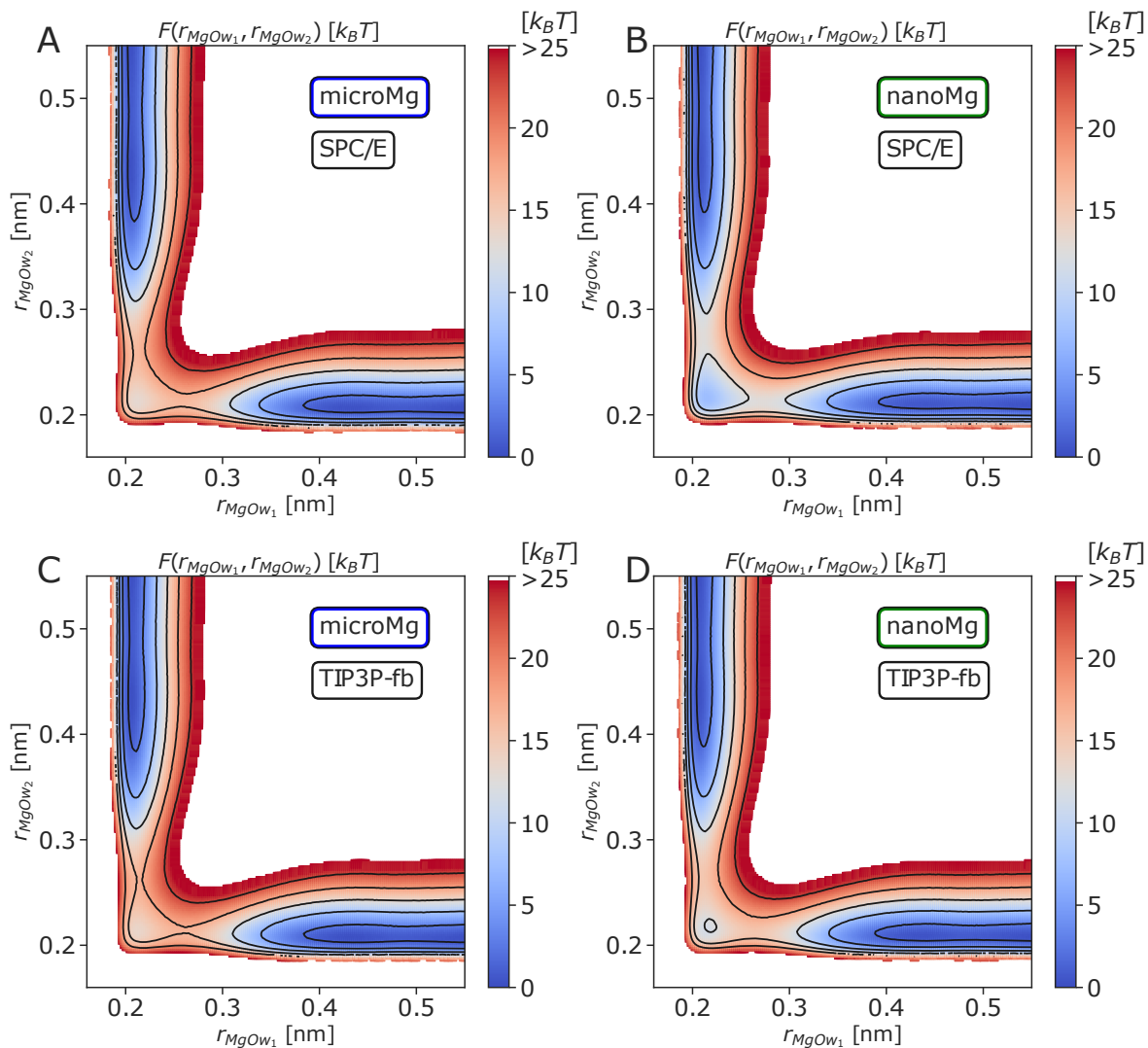


Figure S6: Two-dimensional free energy profiles as a function of the distance between Mg^{2+} and the leaving water molecule r_{MgOw_1} and Mg^{2+} and the entering water molecule r_{MgOw_2} for different force fields in combination with (A,B) SPC/E and (C,D) TIP3P-fb water models. The free energy profiles were calculated via umbrella sampling using additional restraints (see ref. ⁶ for more details).

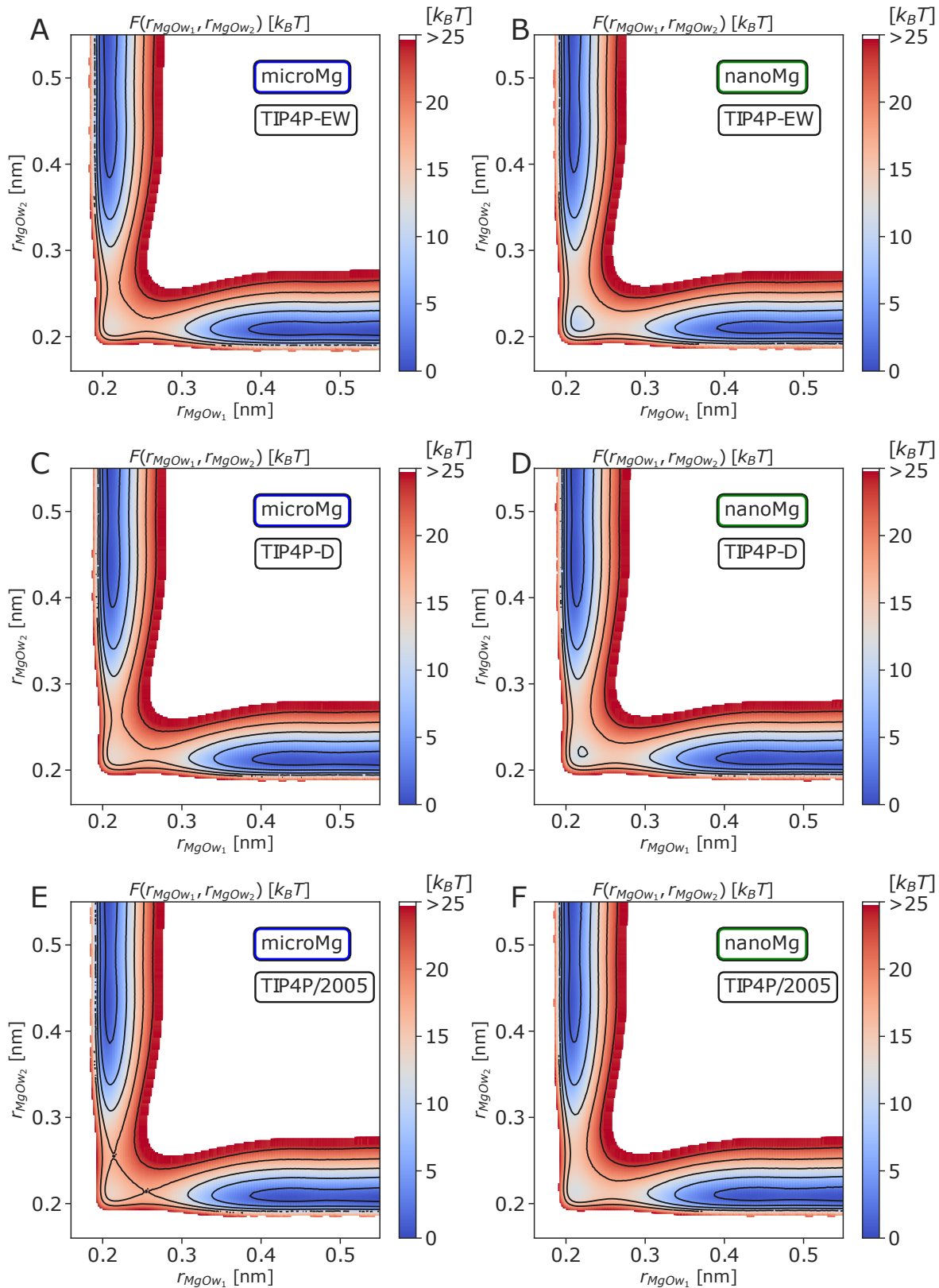


Figure S7: Two-dimensional free energy profiles as a function of the distances between Mg^{2+} and the leaving water molecule r_{MgOW_1} and Mg^{2+} and the entering water molecule r_{MgOW_2} for different force fields in combination with (A,B) TIP4P-Ew, (C,D) TIP4P-D and (E,F) TIP4P/2005 water models. The free energy profiles were calculated via umbrella sampling using additional restraints (see ref. ⁶ for more details).

S2.6 Binding affinities

Two strategies were proceeded to validate binding affinities values, as the calculation of binding affinities is prone to errors even for small systems, like the one we are using here. Both methods yielded nearly identical results within error (Tables 5, main text, S9, and S10).

First strategy to calculate binding affinities: Integration of the free energy profiles along the distance between the Mg^{2+} ion and the dimethylphosphate (DMP) molecule. Resulting properties are listed in Table 5 in the main text.

Second strategy to calculate binding affinities: Alchemical transformation between Mg^{2+} and an divalent reference atom of known binding affinity. As reference ion (Table S8), we choose the parameters of Ca^{2+} in TIP3P water obtained earlier.¹

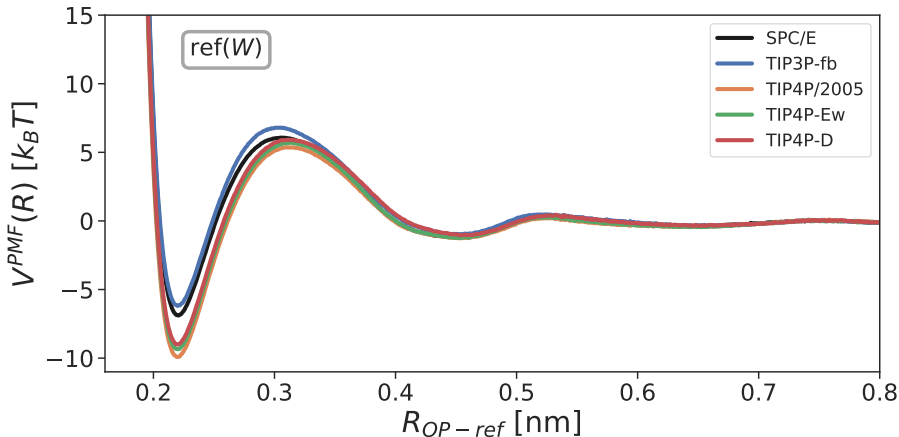


Figure S8: One-dimensional potential of mean force V^{PMF} as a function of the distance $R_{\text{OP-ref}}$ between the divalent reference ion and one of the non-bridging phosphate oxygens of the DMP in different water models. The free energy profile was calculated via umbrella sampling using additional restraints (see ref.⁶ for more details). Afterwards a Jacobian correction was applied (eq S8).

Table S8: Binding affinity ΔG_{ref}^0 obtained for the divalent reference ion (parameters for Ca^{2+} from Mamatkulov-Schwierz in TIP3P¹) in the different water models via integration of their potentials of mean force (Figure S8).

water model	ΔG_{ref}^0 [$k_B T$]
SPC/E	-4.561 ± 0.174
TIP3P-fb	-3.881 ± 0.132
TIP4P/2005	-7.591 ± 0.065
TIP4P-Ew	-7.057 ± 0.090
TIP4P-D	-6.703 ± 0.210

Table S9: Binding affinity ΔG_b^0 obtained from forward alchemical transformation. The values given for $\Delta G_{\text{Mg}^{2+} \rightarrow \text{ref}}^{\text{solv}}$ and $\Delta G_{\text{ref} \rightarrow \text{Mg}^{2+}}^{\text{bind}}$ are obtained from block averaging for 5 blocks of 3 ns long windows each. $\Delta G_{\text{ref} \rightarrow \text{Mg}^{2+}}^{\text{bind}}$, $\Delta G_{\text{Mg}^{2+} \rightarrow \text{ref}}^{\text{bind}}$ and hence ΔG_b^0 are shown for the final scaling factor combination $\lambda_{\sigma, \epsilon}^{\text{RNA}}$ (Table 2, main text). R_b is obtained from the last 15 ns window of the alchemical transformation calculation, the error here indicates the standard deviation of the distribution.

	ΔG_b^0 [k _B T]	$\Delta G_{\text{Mg}^{2+} \rightarrow \text{ref}}^{\text{solv}}$ [k _B T]	$\Delta G_{\text{ref} \rightarrow \text{Mg}^{2+}}^{\text{bind}}$ [k _B T]	R_b [nm]
<i>microMg</i> (SPC/E)	-0.873 ± 0.4	131.776 ± 0.003	-128.088 ± 0.003	0.209 ± 0.004
<i>nanoMg</i> (SPC/E)	-1.033 ± 0.4	131.766 ± 0.003	-128.238 ± 0.003	0.208 ± 0.004
<i>microMg</i> (TIP3P-fb)	-0.789 ± 0.4	133.557 ± 0.006	-130.465 ± 0.003	0.208 ± 0.004
<i>nanoMg</i> (TIP3P-fb)	-0.976 ± 0.4	133.674 ± 0.006	-130.770 ± 0.006	0.208 ± 0.004
<i>microMg</i> (TIP4P/2005)	0.138 ± 0.4	161.893 ± 0.008	-154.165 ± 0.007	0.207 ± 0.004
<i>nanoMg</i> (TIP4P/2005)	-0.632 ± 0.4	161.396 ± 0.007	-154.437 ± 0.007	0.207 ± 0.004
<i>microMg</i> (TIP4P-Ew)	-0.897 ± 0.4	154.691 ± 0.007	-148.532 ± 0.007	0.208 ± 0.004
<i>nanoMg</i> (TIP4P-Ew)	-0.945 ± 0.4	154.497 ± 0.003	-148.384 ± 0.006	0.208 ± 0.004
<i>microMg</i> (TIP4P-D)	-0.677 ± 0.4	158.560 ± 0.007	-152.535 ± 0.006	0.207 ± 0.004
<i>nanoMg</i> (TIP4P-D)	-0.775 ± 0.4	158.550 ± 0.006	-152.622 ± 0.006	0.207 ± 0.004
exp.	-1.036 ¹⁵	n.a.	n.a.	0.206 - 0.208 ⁴⁹

Table S10: Binding affinity ΔG_b^0 obtained from backward alchemical transformation. The values given for $\Delta G_{\text{ref} \rightarrow \text{Mg}^{2+}}^{\text{solv}}$ and $\Delta G_{\text{Mg}^{2+} \rightarrow \text{ref}}^{\text{bind}}$ are obtained from block averaging for 5 blocks of 3 ns long windows each. $\Delta G_{\text{Mg}^{2+} \rightarrow \text{ref}}^{\text{bind}}$ and hence ΔG_b^0 are shown for the final scaling factor combination $\lambda_{\sigma, \epsilon}^{\text{RNA}}$ (Table 2, main text). R_b is obtained from the first 15 ns window of the alchemical transformation calculation, the error here indicates the standard deviation of the distribution.

	ΔG_b^0 [k _B T]	$\Delta G_{\text{ref} \rightarrow \text{Mg}^{2+}}^{\text{solv}}$ [k _B T]	$\Delta G_{\text{Mg}^{2+} \rightarrow \text{ref}}^{\text{bind}}$ [k _B T]	R_b [nm]
<i>microMg</i> (SPC/E)	-0.987 ± 0.4	-131.606 ± 0.003	128.032 ± 0.003	0.209 ± 0.004
<i>nanoMg</i> (SPC/E)	-1.097 ± 0.4	-131.867 ± 0.003	128.403 ± 0.003	0.208 ± 0.004
<i>microMg</i> (TIP3P-fb)	-0.953 ± 0.4	-133.431 ± 0.006	130.503 ± 0.003	0.208 ± 0.004
<i>nanoMg</i> (TIP3P-fb)	-0.821 ± 0.4	-133.687 ± 0.006	130.627 ± 0.003	0.209 ± 0.004
<i>microMg</i> (TIP4P/2005)	-0.435 ± 0.4	-161.357 ± 0.008	154.200 ± 0.007	0.207 ± 0.004
<i>nanoMg</i> (TIP4P/2005)	-0.974 ± 0.4	-161.162 ± 0.007	154.544 ± 0.007	0.207 ± 0.004
<i>microMg</i> (TIP4P-Ew)	-0.770 ± 0.4	-154.764 ± 0.003	148.478 ± 0.003	0.208 ± 0.004
<i>nanoMg</i> (TIP4P-Ew)	-0.589 ± 0.4	-154.582 ± 0.003	148.114 ± 0.006	0.208 ± 0.004
<i>microMg</i> (TIP4P-D)	-0.444 ± 0.4	-158.512 ± 0.007	152.254 ± 0.006	0.207 ± 0.004
<i>nanoMg</i> (TIP4P-D)	-0.687 ± 0.4	-158.678 ± 0.006	152.662 ± 0.006	0.207 ± 0.004
exp.	-1.036 ¹⁵	n.a.	n.a.	0.206 - 0.208 ⁴⁹

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