

## Supplementary Information

Inferences on a Multidimensional Social Hierarchy Use a Grid-like Code

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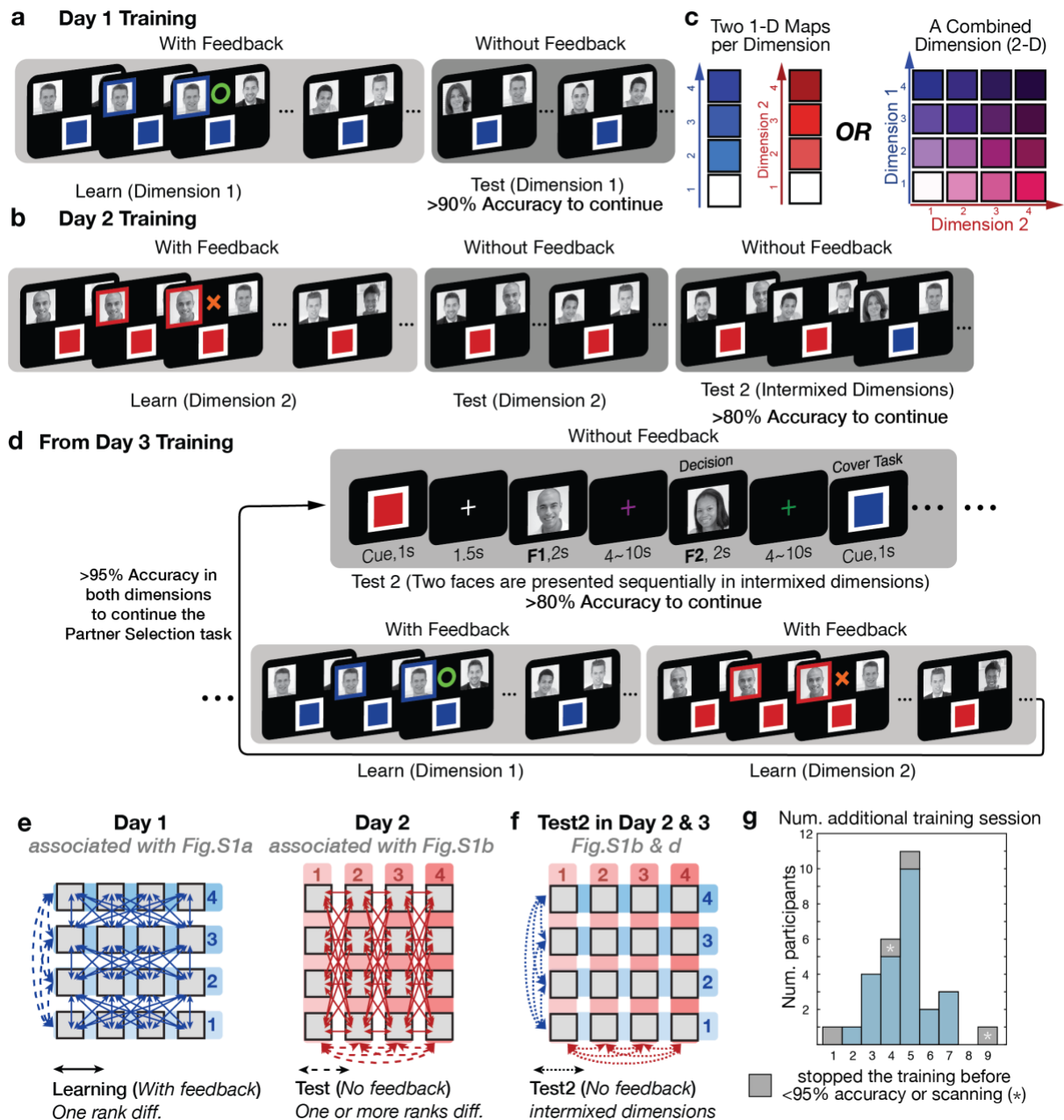
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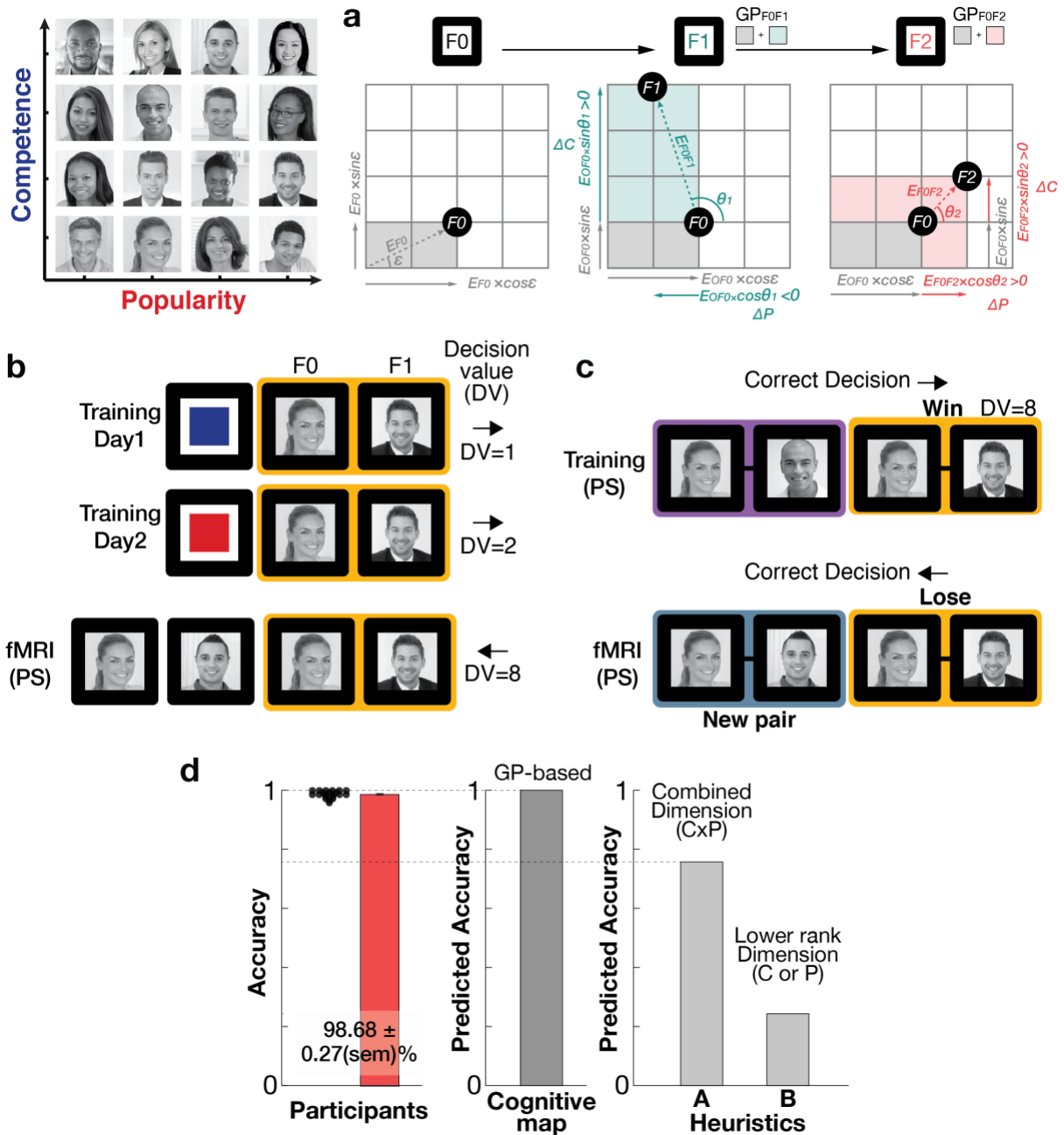
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### References



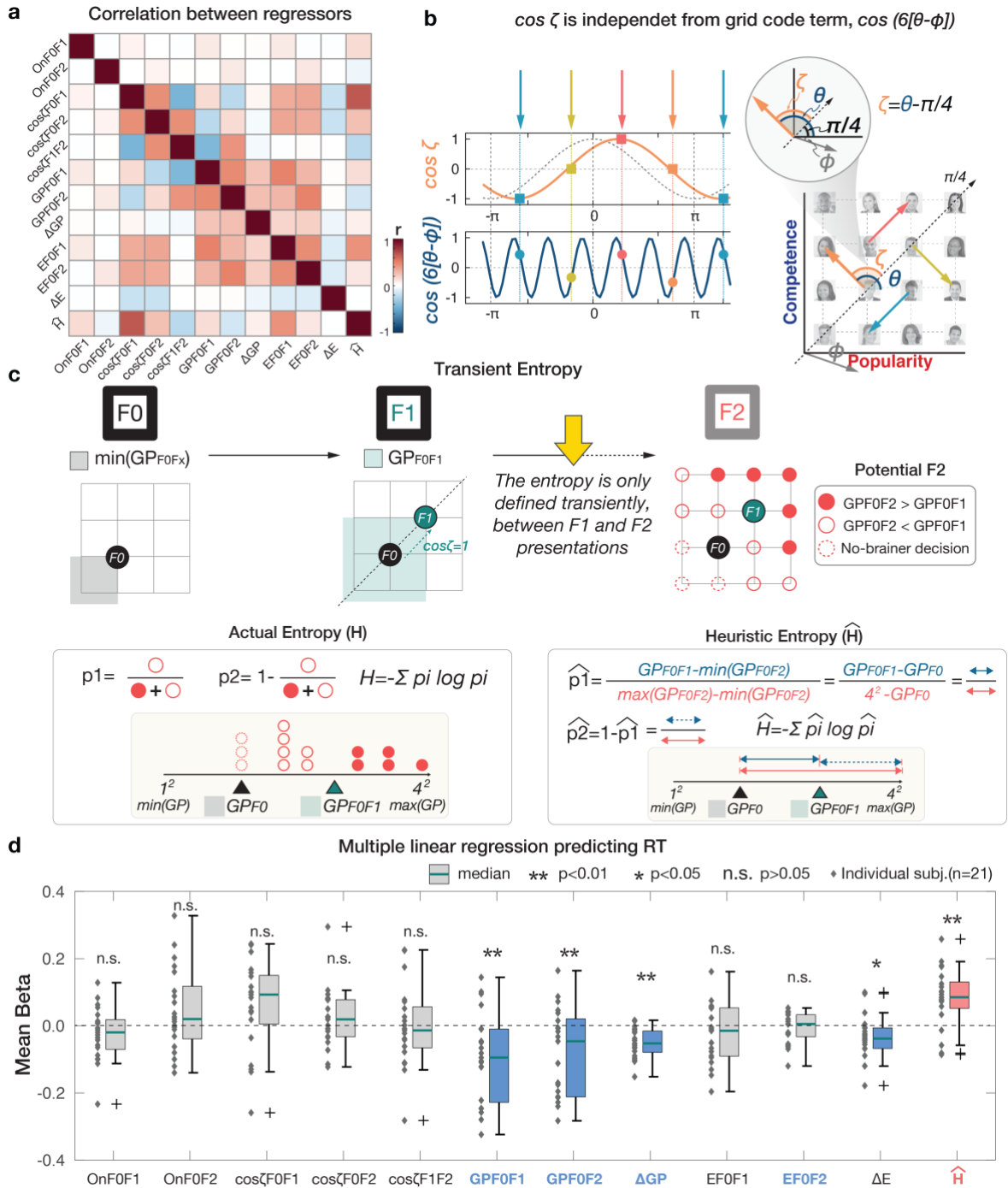
**Supplementary Figure 1. Behavioral training before the fMRI partner selection task.** **a.** During the Learn phase on day 1, participants learned the relative rank of 16 individuals in one of two social hierarchy dimensions (indicated by cue color) based on feedback from binary comparisons. Participants were asked to choose the higher rank individual between two who differed by one level only in the given social hierarchy dimension. During the test phase on day 1, participants were asked to infer the relationship of people who were never paired during the Learn phase through transitive inferences. No feedback was given during the test phase. **b.** During the Learn phase on day 2, participants learned the relative status of the same 16 individuals in the unlearned dimension by comparing people who differed by one level only in the corresponding dimension. During the Test phase on day 2, participants were asked to infer the relative status of unlearned pairs through transitive inference. As before, no feedback was given during the test phase. At the end of day 2 training, participants' knowledge about both 1-D social hierarchies was tested (test 2). During the Test 2 phase, participants were asked to infer the relative status of two individuals while both dimensions were intermixed across trials. **c.** After day 1 training, participants

could have built a hierarchical structure in one dimension. After training on day 2, participants could build two structures of social hierarchy per each dimension (left panel), or they could in principle have built a combined hierarchical structure in two dimensions (Right panel). **d.** The Test 2 phase and the two Learn phases per dimension were repeated until participants could make inferences correctly during the Test 2 phase with an accuracy higher than 90% in both dimensions to continue to the partner selection task. From day 3 training, during the Test 2 phase, stimuli were presented sequentially (top). While presenting F2, participants were asked to make an inference of the relative status of two individuals and indicate their decision. For the Test 2 phase, both dimensions were intermixed across trials and feedback was not given for participants' decisions. **e.** The squares indicate the position of individuals in the 4x4 social hierarchy. The arrows between individuals indicates the pairs that were presented to participants in learning block trials in which participants got feedback on their decision. As shown here, the paired individuals' ranks differ by 1 level in either the competence (left) or popularity (right) dimensions. Participants learned the relative status of those pairs in the left panel in the competence dimension (**Supplementary Figure 1a**) and the relative status of those pairs in the right panel in the popularity dimension (**Supplementary Figure 1b**) on different days. A learning block was followed by a test block. During the test block, all possible pairs except for oneself and those who are at the same rank in the given dimension were presented to participants. The dotted lines indicate the pairs presented during the test blocks that include pairs whose ranks differed by 1,2, and 3 ranks. **f.** After two days of training, Test2 blocks followed at the end of Day2 (the right panel in **Supplementary Figure 1b**) and at the beginning of Day3 (the top panel in **Supplementary Figure 1d**). The dotted lines indicate the pairs presented in Test2 block. The pairs presented in Test2 block comprise the pairs presented during the test blocks in both dimensions. **g.** The bar graph shows the number of additional sessions that each of 29 subjects participated in. 2 among 29 participants stopped the training before reaching 95% accuracy, and 2 who reached >95% stopped the experiment before scanning (marked with \*).



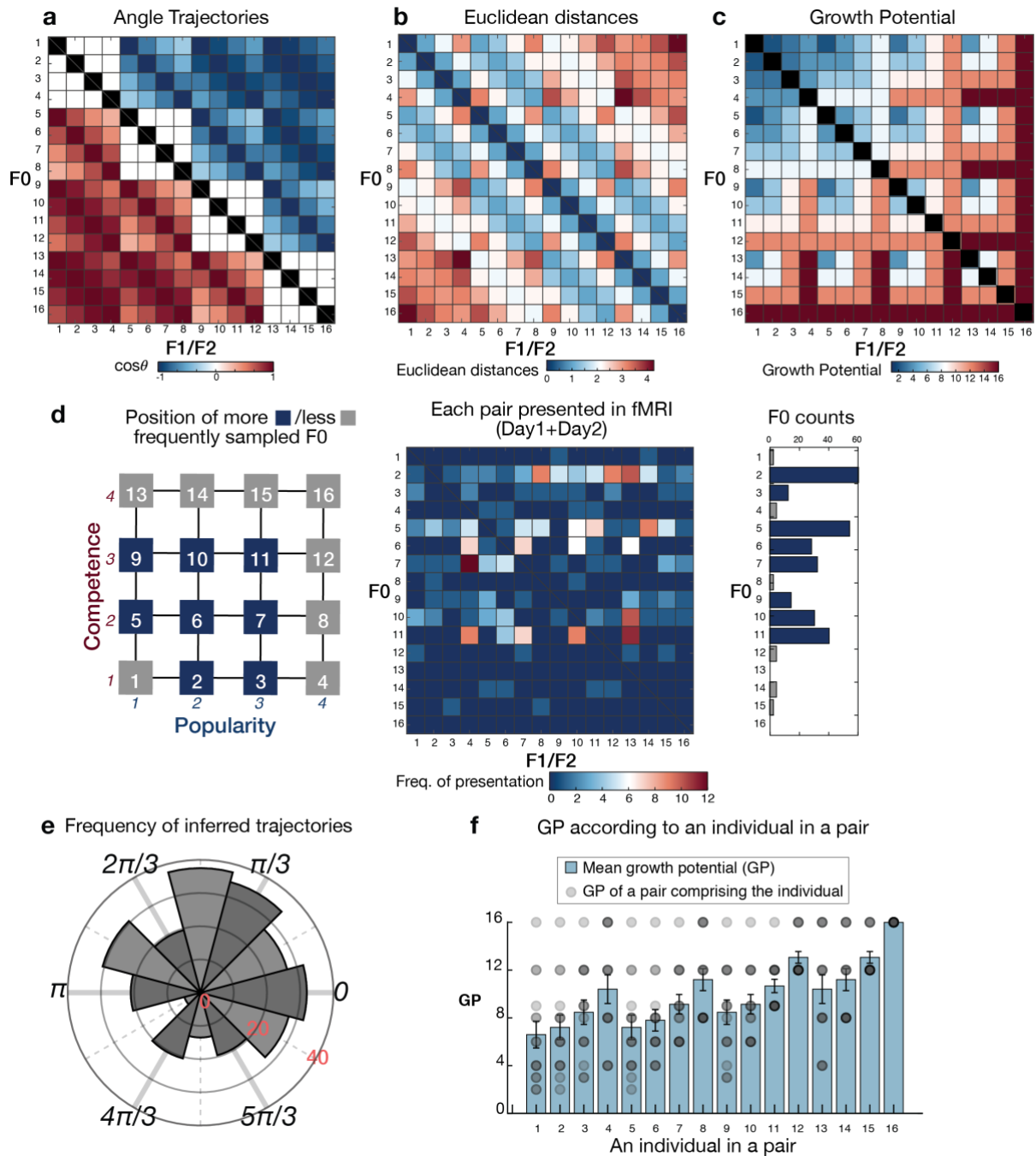
**Supplementary Figure 2. Decision values in behavioral training cannot be generalized for partner selection decisions.** **a.** The computation of growth potential (GP) based on the Euclidean distance and the angle of the inferred trajectories using the polar coordinate system. At the time of  $F_0$  presentation (left panel), the ranks of  $F_0$  in the competence and popularity dimensions are  $E_{F_0} \times \sin(\varepsilon)$  and  $E_{F_0} \times \cos(\varepsilon)$ , respectively, where  $E_{F_0}$  indicates the Euclidean distance of  $\vec{F_0}$  vector from the origin,  $[0,0]$  and their angle is  $\varepsilon$ . At the time of  $F_1$  presentation, participants can compute the  $GP_{F_0F_1}$  based on the non-negative relative rank difference between  $F_1$  and  $F_0$ . The rank difference in the popularity dimension is computed as  $\Delta P = E_{F_0F_1} \times \cos(\theta)$ , while the rank difference in the competence dimension is computed as  $\Delta C = E_{F_0F_1} \times \sin(\theta)$ . Therefore,  $GP_{F_0F_1}$  is computed as  $(C_0 + \Delta C) \times (P_0 + \Delta P)$ , while  $\Delta C$  and  $\Delta P \geq 0$ . Last,  $GP_{F_0F_2}$  is also computed in the same way when  $F_2$  is presented. **b.** An example showing that when the same  $F_0F_1$  pair is presented, the decision value (DV) in a trial during behavioral training (DV=1 for day 1 training; DV=2 for day 2 training) cannot be generalized for the DV for the partner selection decision (DV=8). **c** An example showing

that remembering the winning pair in a trial of the partner selection task during behavioral training (F0F1 pair here) does not help participants to make a correct decision in the partner selection task in fMRI since they are compared with other pairs that participants had never compared them with. These examples (**b** and **c**) illustrate that on most trials, participants needed to make inferences to compute the decision value (GP) in order to be accurate in the partner selection task, though they had been trained extensively to learn the ranks differences in each one-dimensional social hierarchy during behavioral training. **d.** Participants ( $n=21$ ) were able to choose the better partners during the partner selection task (mean accuracy  $\pm$  sem =  $98.68 \pm 0.27\%$ ; left panel; a black dot indicates the accuracy of each participant). We examined whether the decisions were better explained by the difference between GPs of two pairs (GP1-GP2), which in principle may require participants to use the cognitive map (middle panel), or other alternative heuristics (right panel). As the first alternative way to make a decision, we tested whether participants used a rank assigned to each individual in a combined dimension (such as, rank in competence dimension (C)  $\times$  rank in popularity dimension (P)), rather than using ranks of each of the two dimensions, and chose the one who had greater overall rank between F1 and F2 (Heuristic A). As the second alternative model, we tested whether participants only use the ranks of F1 and F2 in the dimension in which the rank of F0 was relatively deficient (Heuristic B). We found that both heuristics cannot explain the high accuracy that participants achieved during partner selection, suggesting that participants use the cognitive map to compute GP to guide correct decisions.



**Supplementary Figure 3. Results of a multiple linear regression on reaction times (RTs) of partner selection decisions.** **a.** The correlation matrix shows the correlation ( $r$ ) between 12 regressors. The 12 regressors include the Euclidean distance between  $F0F1$  and  $F0F2$  pairs, the absolute difference between them ( $E_{F0F1}$ ,  $E_{F0F2}$ , and  $\Delta E = |E_{F0F1} - E_{F0F2}|$ ), the GP of  $F0F1$  and  $F0F2$  pairs, and their absolute difference ( $GP_{F0F1}$ ,  $GP_{F0F2}$ , and  $\Delta GP = |GP_{F0F1} - GP_{F0F2}|$ ), the cosine angles of the trajectories ( $\cos \zeta_{F0F1}$ ,  $\cos \zeta_{F0F2}$ , and  $\cos \zeta_{F1F2}$ ), whether the  $F0F1$  and  $F0F2$  vector was aligned to the EC grid orientation or not ( $On_{F0F1}$  and  $On_{F0F2}$ ) and the transient heuristic entropy ( $\hat{H}$ ). **b.** In this analysis, we compute the angle ( $\cos \zeta$ ) aligned to the diagonal since ranks in both dimensions are equally important in the partner selection task. Therefore,  $\cos \zeta = \cos(\theta - \pi/4)$  was inputted into the regressors. Importantly, the vector angles of each pair ( $\cos \zeta$ ) are defined independently from the hexadirectional modulations in the grid-like code

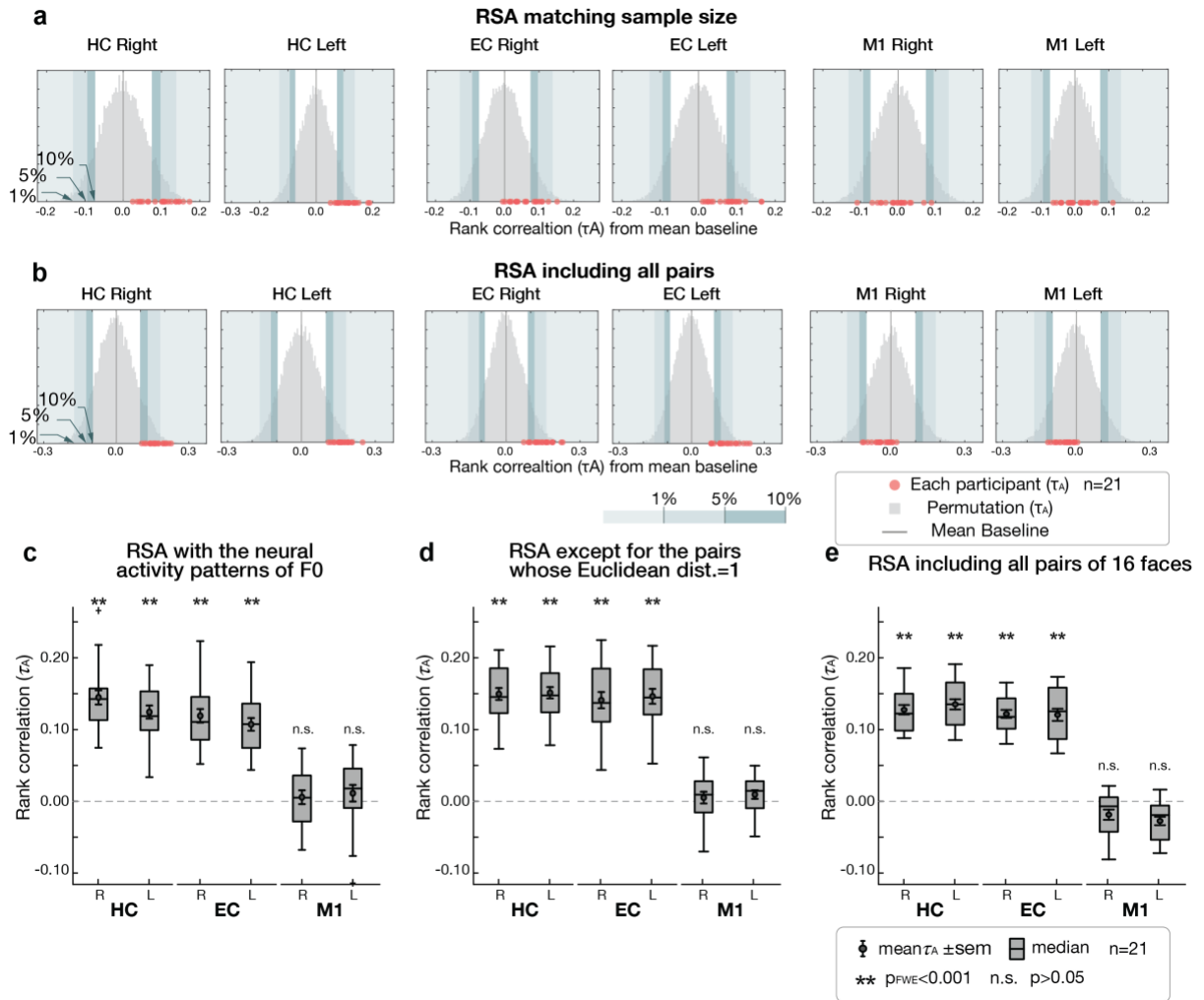
( $\cos(6[\theta - \phi])$ ). As shown in **a**.  $\cos \zeta$  (including  $\cos \zeta_{F_0F_1}$ ,  $\cos \zeta_{F_0F_2}$ , and  $\cos \zeta_{F_1F_2}$ ) did not predict whether the corresponding vector was aligned or misaligned to the EC grid orientation ( $On_{F_0F_1}$  and  $On_{F_0F_2}$ ). **c**. The RT can increase with levels of the ‘transient entropy’ of the partner selection decision. While the entropy indicates the level of uncertainty, there is no uncertainty in the partner selection task itself. This entropy is only defined under a specific condition where the stimuli are sequentially sampled. That is, the uncertainty occurs temporarily when participants know F0 and F1 but wait for the F2 presentation (Yellow arrow period; This transient entropy is resolved (no uncertainty) with the F2 presentation). While F2 is not known, participants who have the representation of the social hierarchy, in practice, are able to conjecture the probability that F1 wins against other potential F2 candidates in the social hierarchy. For example, if the  $GP_{F_0F_1}$  is greater than the average expected GP of F0, F1 is more likely to be a better partner. Subsequently, participants could prepare their decisions even before knowing F2. The actual entropy ( $H$ ) can be computed based on the true GP distribution of all possible 15 pairs (excluding F0 herself). Specifically, participants can estimate the probability that the F0F1 pair wins by counting the number of pairs who generate greater GP than  $GP_{F_0F_1}$ . However, it is extremely hard to compute the GP of 15 pairs during the brief ISI (2~5 s) in every trial (as the GP distribution changes every trial according to F0). As an alternative heuristic, we tested the idea that participants might use a uniform distribution to compute the probability that F1 wins (heuristic entropy,  $\hat{H}$ ; right panel). Specifically, the heuristic entropy ( $\hat{H}$ ) assumes that participants use how high the  $GP_{F_0F_1}$  was in the possible range of the GP that F0 could expect as the approximated probability that F0F1 will win. The rank of  $GP_{F_0F_1}$  is approximated as  $[GP_{F_0F_1} - \min(GP_{F_0})]$  over the possible GP range of F0 which is  $[\max(GP_{F_0}) - \min(GP_{F_0})] = [4^2 - GP_{F_0}]$  (where  $4^2$  is the  $\max(GP_{F_0F_2})$  when F2 is the face16, the highest ranks in both dimensions and  $GP_{F_0}$  is corresponding to the grey area,  $C_{F_0} \times P_{F_0}$ ). To take into account the effects of transient entropy on the RTs, we inputted  $\hat{H}$  as an additional regressor. **d**. The mean beta (regression coefficients) across participants ( $n=21$ ). Each dot indicates an individual subject. We found significant negative effects of the  $GP_{F_0F_1}$ ,  $GP_{F_0F_2}$ ,  $\Delta GP$ , and  $\Delta E$  on RT (indicating faster RT) and a positive significant effect of  $\hat{H}$  on RT (indicating slower RT). The effect sizes of this regression are reported in **Supplementary Table 1**.  $**p < 0.01$ ,  $*p < 0.05$ , n.s.  $p > 0.05$ . The distances of trajectory ( $E$ ) have a moderate correlation level with the decision values ( $GP_s$ ) ( $r=0.47$ ). When we include  $E_{F_0F_1}$  and  $E_{F_0F_2}$  after partialling out their covariance with  $GP_{F_0F_1}$  and  $GP_{F_0F_2}$ , the GP effects ( $GP_{F_0F_1}$  and  $GP_{F_0F_2}$ ) get a little stronger ( $t_{20}=-4.69$  and  $p=1.42e-04$ ; and  $t_{20}=-4.86$  and  $p=9.51e-05$  respectively) while no notable changes were found for effects of the other regressors. Data distribution follows normality and equal variance (Shapiro-Wilk test <sup>1</sup>,  $p < 0.05$  for all except for one subject  $p=0.062$ ). Box, lower and upper quartiles; line, median; whiskers, range of the data excluding outliers; +, the whiskers’ range of outliers.



**Supplementary Figure 4. The angles, distances, and GP of pairs during the partner selection task.** **a.** The 16 x 16 matrix which includes all possible pairs of F0 and F1/F2 shows the values of the cosine angle ( $\cos\theta$ ) of the trajectories of all possible 240 pairs (except for the pairs in black where F0 and F1/F2 are the same). **b.** Euclidean distance of the trajectories of all possible pairs. **c.** Growth potential (GP) of the trajectories of all possible pairs. The pairwise Euclidean distance and the GP differ from each other, suggesting participants cannot use the Euclidean distance but should compute the GP of each pair to be accurate in the partner selection task. **d.** Among the 240 possible pairs shown in **Supplementary Figure 4a**, we carefully chose specific pairs for the partner selection task. The less sampled F0 positions are shown in gray (left panel). For the pairs where F0 is at the highest rank in one social hierarchy dimension, participants could make partner selection decisions by comparing the ranks in one dimension only. Similarly, position 1 and 16 always lose and win, respectively. Because we hypothesized the grid code may only be utilized

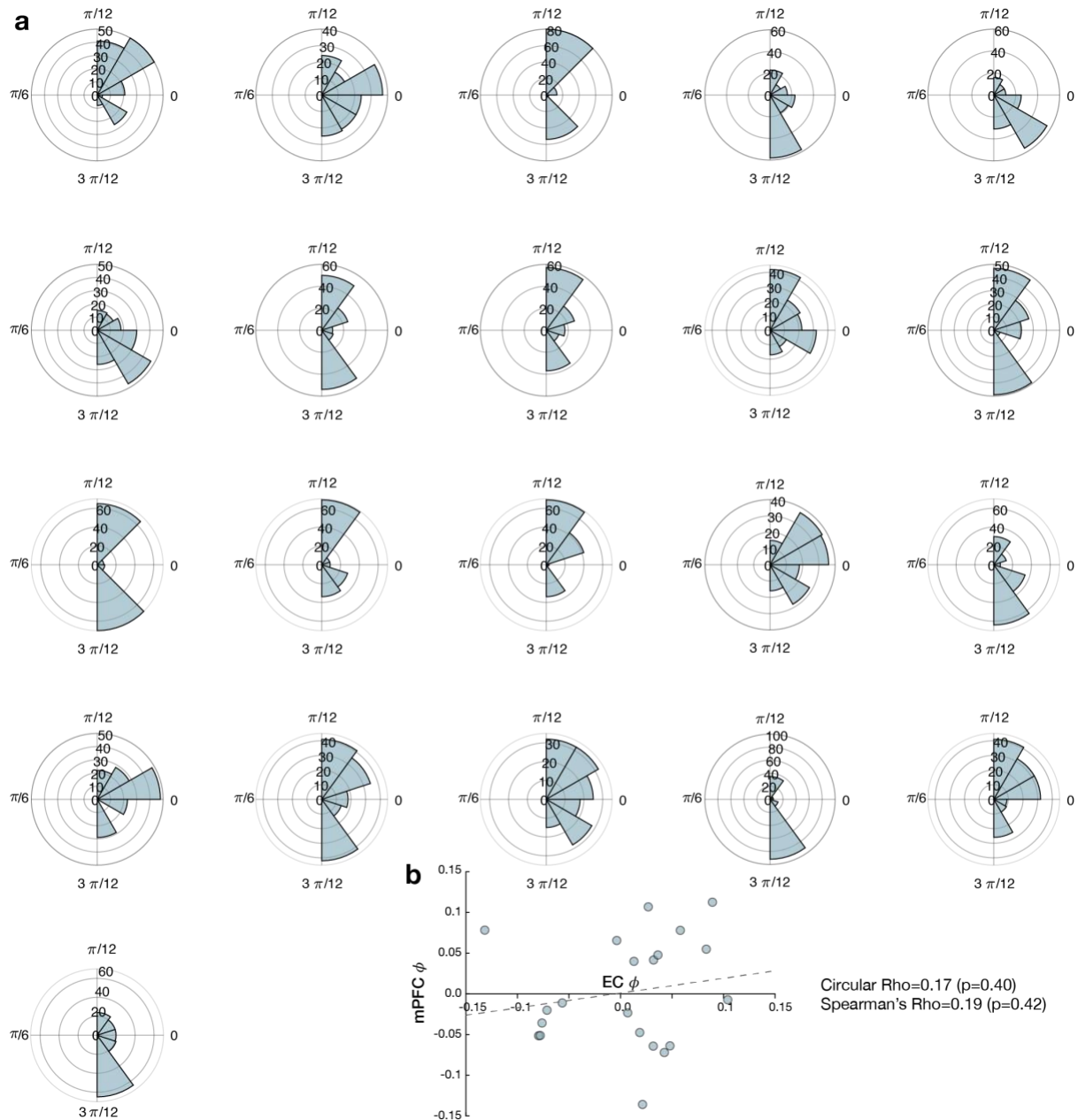


when subjects have to integrate both dimensions and simulate a relationship in 2D, rather than rely on simple choice heuristics, we only minimally sampled those F0 positions. The middle panel shows the number of presentations of each pair during the fMRI partner selection task, and the right panel shows the number of pairs according to their F0 face. **e.** The frequency of decision trajectories in the experiment, categorized into 12 equal bins of  $30^\circ$  according to the direction of inferred trajectories,  $\theta$ . **f.** The dots indicate the possible GP an individual can have according to whom they are paired with. The bars indicate the mean  $GP \pm SEM$  of possible GP values for that individual. It shows that the GP cannot be predicted by only one individual in a pair, but instead participants need to take both individuals in a pair into account to compute the GP. Moreover, the mean GP cannot be well accounted for by a linear function of the rank in one dimension but by the ranks in both dimensions. This implies that participants cannot utilize a separate 1-D cognitive map of the GP to make accurate decisions, but need to use the ranks of both individuals in a pair in both social hierarchy dimensions.

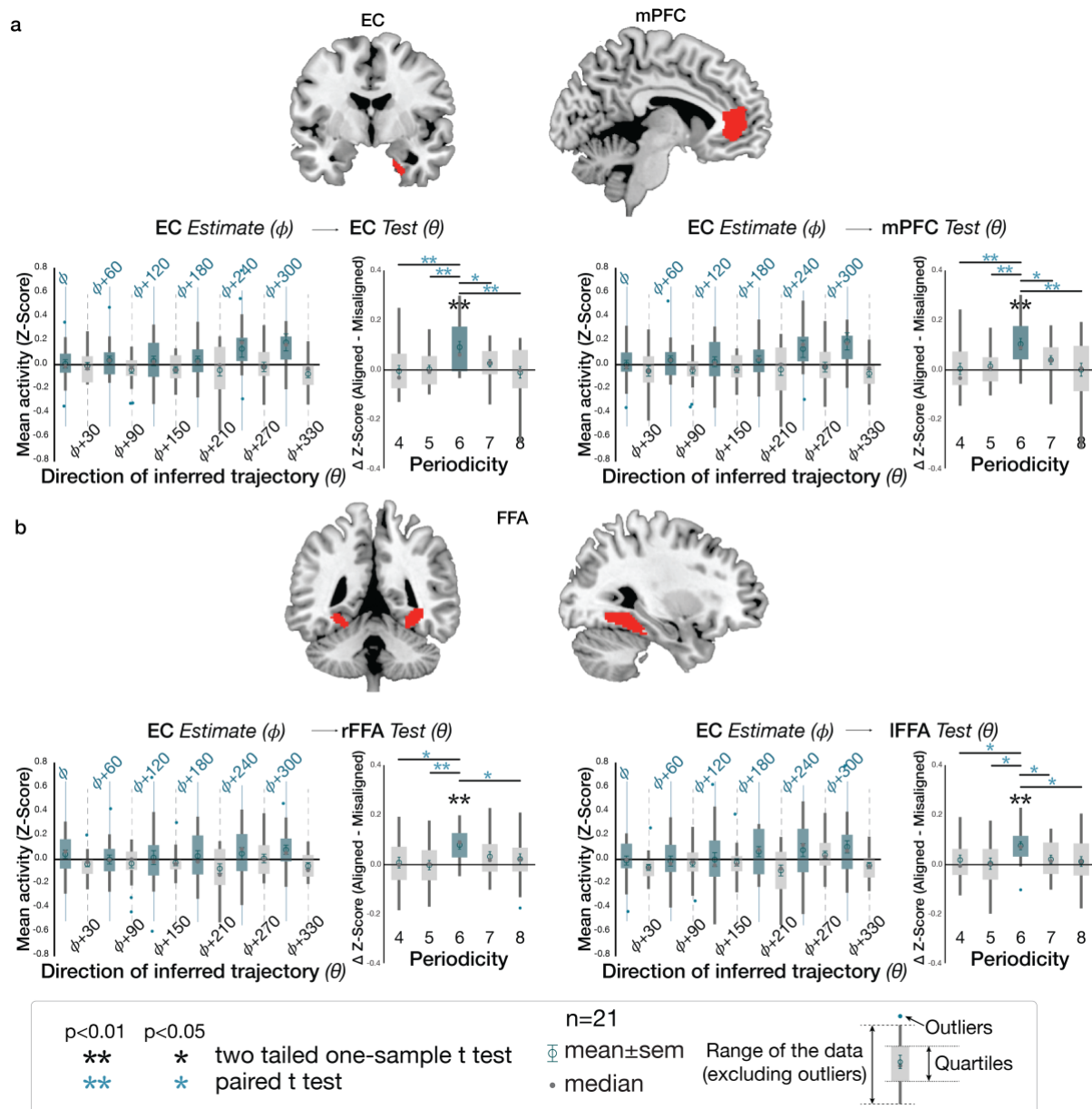


**Supplementary Figure 5. Representational similarity analysis (RSA).** **a** and **b**. The rank correlation (Kendall's  $\tau_A$ ) of each of the participants corrected from the baseline ( $n=21$ ) are shown as red dots on the  $x$ -axis.  $\tau_A$  indicates to what extent the pairwise Euclidean distance in the 2-D social hierarchy explains the neural activity patterns of the ROIs. The gray histogram shows the baseline distribution of  $\tau_A$  which was acquired from 1000 permutations while randomly shuffling the positions of the 14 individuals in the 2-D space. Based on the distribution, the thresholds of  $p=0.01$ ,  $p=0.05$ , and  $p=0.1$  are marked for two-tailed tests. The  $\tau_A$  of most participants are within the range of 0~10% in the bilateral HC and EC, whereas most are within the range of 10~90% in bilateral M1. We performed RSA while down-sampling the observations to match the same sample size of each face presentation to be the same (**a**) and while including all observed samples (**b**). **c**. To examine activity patterns in our ROIs while the activity was minimally modulated by other task-relevant cognitive processes, we performed a control RSA in which the neural activity only acquired at the time of F0 presentation (but not F1 or F2 presentation) was included. Since some faces were selected less frequently as F0 during partner selection, we only include 8 individuals at the positions in the social hierarchy for the control RSA. The dissimilarity between activity patterns associated with F0 presentation estimated in bilateral HC and EC increases in proportion to the pairwise Euclidean distance between individuals in the 2-D abstract social space. The rank correlation (Kendall's  $\tau_A$ ) shows robust effects of Euclidean distance on the pattern dissimilarity estimated in the HC and EC compared to the permuted baseline (1000 iterations), but not in our control region (M1) **d**. After excluding the pairs with Euclidean distance of 1, we still found robust effects of Euclidean distance on the increases in the pattern dissimilarity estimated in the HC and

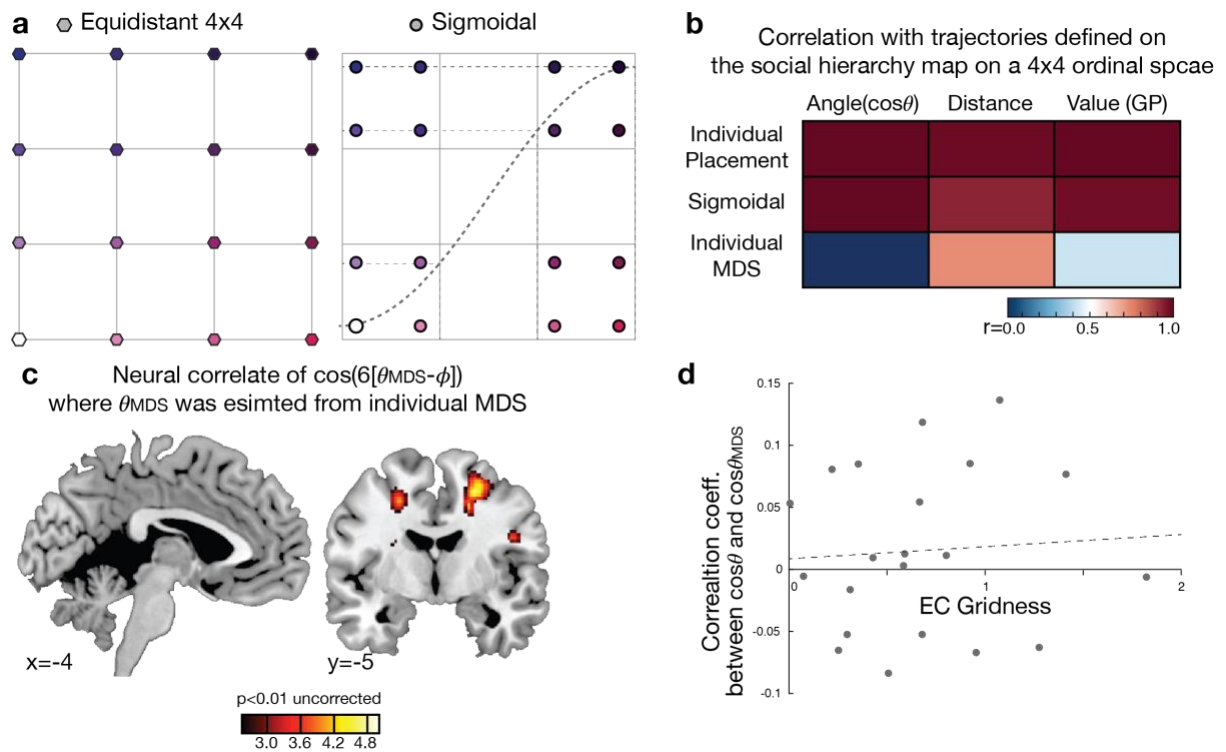
EC compared to the permuted baseline (1000 iterations), but not in a control region (M1). **e.** After including all the pairs between 16 individuals, we found robust effects of Euclidean distance on the increases in the pattern dissimilarity estimated in the HC and EC compared to the permuted baseline (1000 iterations) but not in M1. \*\*,  $p_{FWE} < 0.001$  Bonferroni-Holm method; n.s.,  $p > 0.05$ , uncorrected. **c. d., and e.** The rank correlation of each of the participants corrected from the baseline ( $n=21$ ). These results are consistent with the finding shown in **Figure 3** and **Extended Data Figure 2** using faces at all events (F0, F1 and F2 presentations). See **Supplementary Table 2e** for effect sizes. Box, lower and upper quartiles; line, median; whiskers, range of the data excluding outliers; +, the whiskers' range of outliers.



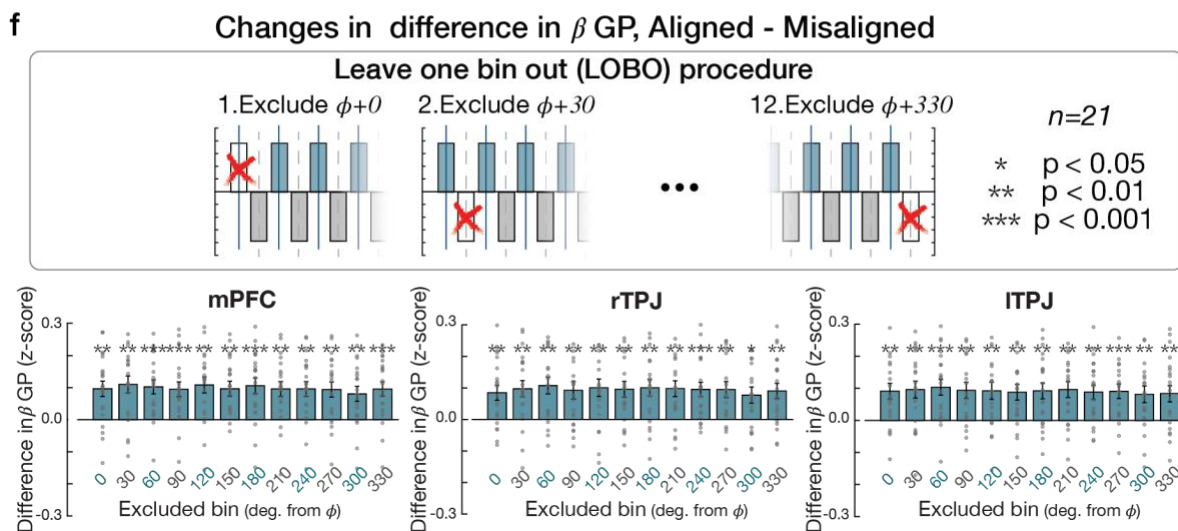
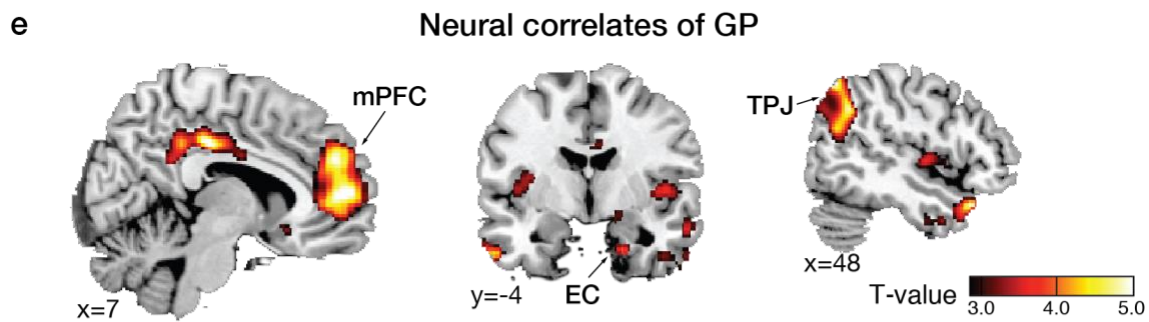
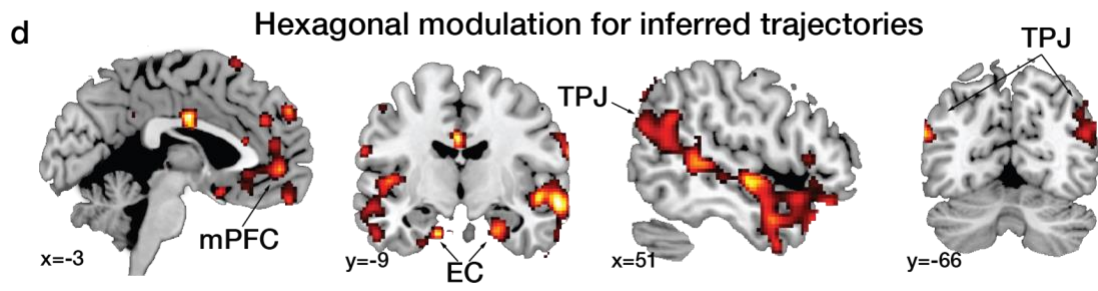
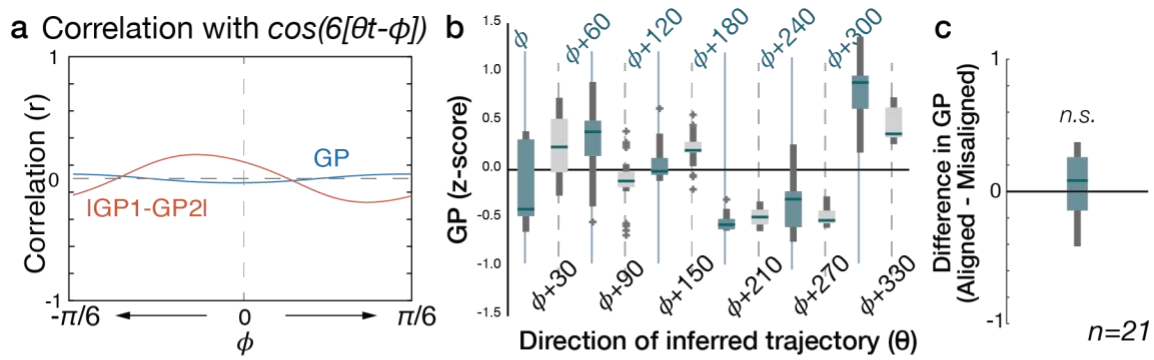
**Supplementary Figure 6. Nonuniform distributions of EC grid orientation. a.** Clustering of putative EC grid orientations within each participant ( $n=21$ ). Polar histograms show potential grid orientations (in the range  $0$  and  $\pi/3$ ) of each participant estimated from the sessions acquired for the day1 scan for all voxels in the EC ROI. Grid orientations were significantly clustered in all participants ( $p<0.01$ , Rayleigh's tests for nonuniformity; mean  $\pm$ SEM= $50.98\pm 4.14$  for the first day scan and  $58.66\pm 4.23$  for the second day scan). **b.** While the EC grid orientations (EC  $\phi$ ) correlate with the mPFC grid orientations (mPFC  $\phi$ ) minimally across participants ( $p>0.05$ ), we found that  $80.19\pm 1.66\%$  (SEM) of total pairs were classified as the same category (aligned or misaligned) when aligned to the EC and when aligned to the mPFC grid orientations.



**Supplementary Figure 7. Hexadirectional modulation on anatomically defined ROIs. a.** Confirmatory analyses of hexadirectional modulation on independent anatomically defined EC<sup>2,3</sup> and mPFC<sup>4</sup> ROIs in alignment with the EC grid angle ( $n=21$ ). Consistent with our functionally defined ROI-based analyses (**Figure 4b and 4c**), this effect in anatomically defined EC and mPFC was also specific to six-fold periodicity (one-tailed t-test,  $p < 0.01$ ), as it was not seen for four-, five-, seven-, or eightfold periodicities (all  $p > 0.05$ ). The effect at six-fold was significantly greater than those of the control periodicities (paired t-test). **b.** Hexadirectional modulation was also tested on independent, functionally-defined FFA ROIs. The FFA ROIs were identified by a contrast analysis between presentations of face stimuli and the fixation cross (within a mask defined at the threshold  $p < 0.001$ , uncorrected). We found that this effect in bilateral FFA was also specific to a six-fold periodicity ( $p < 0.01$ ), as it was not present for other control periodicities (all  $p > 0.05$ , uncorrected). \*\*,  $p < 0.01$  and \*,  $p < 0.05$ . The effect at six-fold was significantly greater than those of the control periodicities for all but one comparison in rFFA (paired t-test). **a and b.** Box, lower and upper quartiles; line, median; whiskers, range of the data excluding outliers; +, the whiskers' range of outliers.



**Supplementary Figure 8. Inferred trajectories defined on cognitive maps based on alternative geometries.** **a.** The positions of 16 individuals computed using non-linear monotonic dimensions using a sigmoid function to test the effects of deformation of the cognitive map. **b.** The level of correlation between the properties of inferred trajectories (angles, distances, and decision value [GP]) computed in a 4x4 ordinal space and those computed from other cognitive maps defined on alternative dimensions (placement, sigmoidal and MDS estimated from the hippocampus (HC) of individual participants). **c.** The effects of hexadirectional grid-like coding modulated by the angles of trajectories estimated from the coordinates of each individual MDS ( $\theta_{\text{MDS}}$ ), rather than angles in the true hierarchy space, were tested. We found only the motor cortex showed significant effects at a reduced threshold ( $p<0.005$ , uncorrected) when estimating  $\theta$  from the individual MDS. **d.** In addition to the within-subject analyses, we further performed a between-subject analysis to test whether those participants who had greater grid effects in the EC were more likely to have an MDS close to the true social hierarchy structure. The EC gridness indicates to what extent the EC activity of each participant is hexagonally modulated. The level of similarity between the MDS of each participant and the true structure was estimated from the correlation coefficient between cosine angle trajectories estimated from each of two spaces. We find that the EC gridness does not correlate with to what extent the MDS closely reflects the true social hierarchy structure ( $r=0.07$ ).

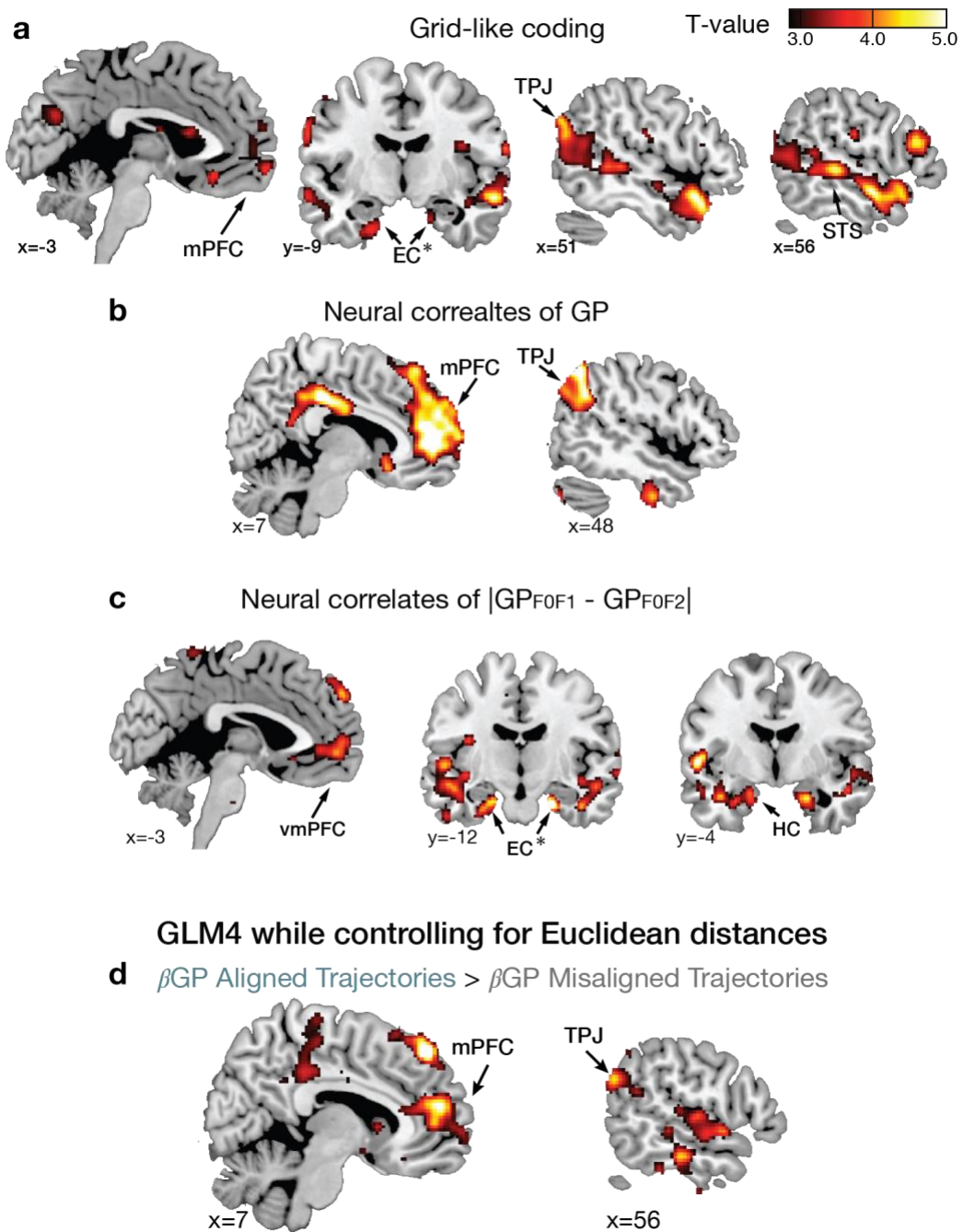


**Supplementary Figure 9. Grid-like coding while controlling for the growth potential of inferred trajectories.** **a.** To make optimal decisions in the partner selection task, we hypothesized that participants could make inferences along direct trajectories between two individuals which guide the computation of GP and subsequently the two option's GP comparison,  $|GP1-GP2|$ . We confirmed that both GP and  $|GP1-GP2|$  were not explained by a function of the direction of the inferred trajectory,  $\cos(6[\theta - \phi])$  regardless of the grid orientation,  $\phi$ . This low correlation indicates

that it is statistically possible to identify the neural encoding of GP while controlling for the neural modulation of the direction of inferred trajectories. **b.** The z-scored GP within each block categorized into 12 equally distributed bins of 30° according to the direction of the inferred trajectories ( $\theta$ ), aligned to each participant's (n=21) EC grid orientation ( $\phi$ ) shows that the distribution of GP did not show the hexagonally symmetrical pattern. This pattern shows that the hexadirectional modulations of  $\beta$  GP in TPJ and mPFC (**Figure 5b**) were not caused by difference in GP itself but were specific for the inferred trajectories in alignment with the EC grid orientation, **c.** We further tested whether there was a significant difference in GP between aligned and misaligned trajectories, which was not present (one-tailed t test;  $t=-0.34$ ,  $p=0.63$ ,  $n=21$ ). **b and c.** Box, lower and upper quartiles; line, median; whiskers, range of the data excluding outliers; +, the whiskers' range of outliers. **d and e.** We found that the effects of hexagonal modulation ( $\cos(6[\theta_t - \phi])$ ) (**Figure 4a**) and the GP (**Figure 5a**) remained when including both regressors in the same GLM, indicating each of the regressors explained independent variance in these regions. **f.** Leave-one-bin-out (LOBO) test. The average differences in z-scored GP effects ( $\pm$ SE) across participants between aligned and misaligned trajectories. The positive z-score differences (aligned > misaligned) suggesting hexadirectional modulations in the activity encoding GP in mPFC and bilateral TPJ were found when they were computed based on the activity of 11 bins while excluding the activity in one of 12 bins (all  $p<0.05$ ; see **Supplementary Table 8b**). This result shows that the effects of hexadirectional modulation were not driven by the activity in any single direction but prevalent across directions. \*\*,  $p<0.01$ ; \*\*,  $p<0.01$ . Error bars indicate the standard error mean (SE).

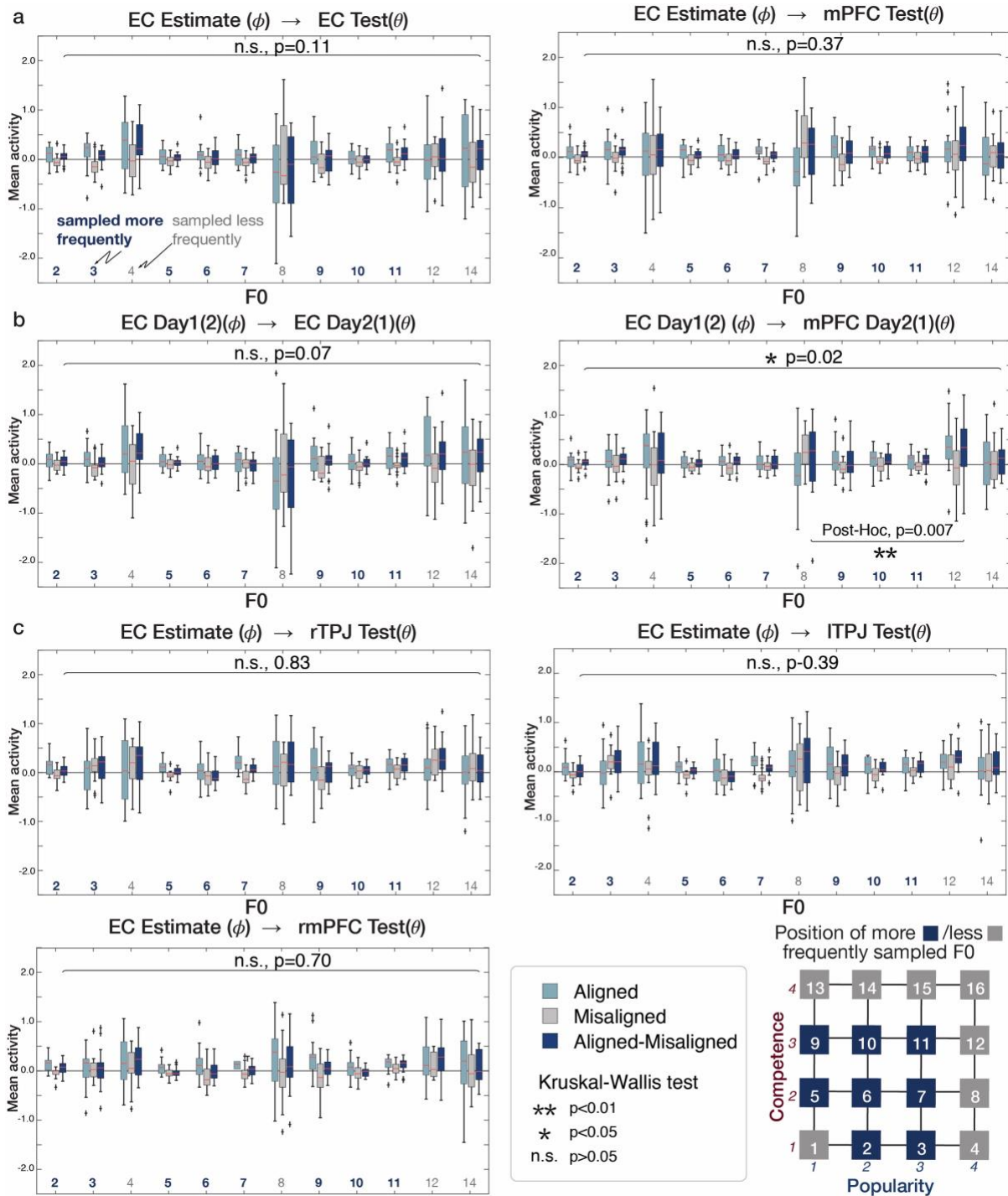


### GLM3 while controlling for Euclidean distances



**Supplementary Figure 10. Grid-like coding and GP effects while controlling for the Euclidean distances of inferred trajectories.** Associated with Figure 5. **a.** The hexadirectional grid-like effect ( $\cos(6[\theta - \phi])$ ) is shown, while controlling for the Euclidean distance of trajectories ( $E_{F0F1}$  and  $E_{F0F2}$ ) (GLM3). The effects of grid-like coding were significant in mPFC, TPJ, and STS ( $p_{FWE} < 0.05$  whole brain TFCE correction) and EC ( $p_{FWE} < 0.05$  corrected in the anatomically defined EC ROI [marked with \*]). **b.** Whole-brain map showing effects of the neural correlates of growth potential (GP), while controlling for the Euclidean distance of trajectories ( $E_{F0F1}$  and  $E_{F0F2}$ ). The neural correlates of GP were significant in mPFC and TPJ ( $p_{FWE} < 0.05$  whole brain TFCE correction). **c.** Whole-brain map showing effects of value comparison ( $|GP_{F0F1} - GP_{F0F2}|$ ). The neural correlates of value comparison were significant in vmPFC and HC ( $p_{FWE} < 0.05$  whole brain TFCE correction) and EC ( $p_{FWE} < 0.05$  corrected in the anatomically defined EC ROI), while controlling for

the Euclidean distance of trajectories ( $E_{F0F1}$  and  $E_{F0F2}$ ). **d.** Whole-brain map contrasting the effects of GP ( $\beta$  GP) for trajectories aligned with the EC grid orientation,  $\phi$ , compared to those misaligned trajectories ( $\beta$  GP aligned  $>$   $\beta$  GP misaligned) (GLM4). The contrast effects of GP were significant in mPFC, and TPJ ( $p_{FWE} < 0.05$  whole brain TFCE correction), while controlling for the Euclidean distance of trajectories ( $E_{F0F1}$  and  $E_{F0F2}$ ). For visualization purposes, the whole-brain maps are thresholded at  $p < 0.005$  uncorrected.



**Supplementary Figure 11. Grid effects of the inferred trajectories were tested separately according to F0 of the pairs. a.** The mean activity in the EC and mPFC when the trajectories are aligned and misaligned to the EC grid orientation estimated from different blocks of the same day scan (Associated with **Figure 4b**). The blue bars indicate their differences (aligned - misaligned). \*\* $<0.01$ , \* $<0.05$  in Wilcoxon signed rank test. This effect was not different across pairs according to the F0 position ( $p>0.05$  in Kruskal-Wallis test). Note that the statistical analysis is not always reliable for some F0 positions since the sample sizes are significantly reduced for this analysis. **b.** The mean activity in the EC and mPFC when the trajectories are aligned and misaligned to the EC grid orientation estimated from the scan acquired from a different day (associated with **Figure 4c**). This effect was not different across pairs according to the F0 position in EC ( $p>0.05$  in Kruskal-

Wallis test; Since the number of samples was limited for some F0 positions (See **Supplementary Figure 4d**), we used non-parametric statistics that do not assume normality). In mPFC, the effects did not differ across the F0 positions ( $p>0.05$ ) except for the pair between face8 and face12 ( $p<0.01$ ), although this difference is likely unreliable given their small number of samples. **c.** The GP effects ( $\beta_{GP}$ ) in the mPFC and bilateral TPJ when the trajectories are aligned and misaligned to the EC grid orientation (associated with **Figure 5b**). This effect was not different across pairs according to the F0 position ( $p>0.05$  in Kruskal-Wallis test). **a, b and c.** Box, lower and upper quartiles; red line, median; whiskers, range of the data excluding outliers; +, the whiskers' range of outliers.

	$On_{F0F1}$	$On_{F0F2}$	$\cos \zeta_{F0F1}$	$\cos \zeta_{F0F2}$	$\cos \zeta_{F1F2}$	$GP_{F0F1}$
$T_{20}$	-1.389	1.623	2.06	1.035	-0.167	-3.262 **
p	0.180	0.120	0.053	0.313	0.869	0.004
	$GP_{F0F2}$	$\Delta GP$	$E_{F0F1}$	$E_{F0F2}$	$\Delta E$	$\hat{H}$
$T_{20}$	-2.887 **	-5.452 **	-1.429	-0.666	-2.474 *	4.293 **
p	0.009	2.46e-05	0.168	0.513	0.022	3.55e-04

**Supplementary Table 1. Multiple linear regression predicting reaction times.** Mean effect sizes (group T-values; one-sample t test, two-tailed) of each regressor included in the multiple linear regression predicting reaction times (RT) in the partner selection task. Associated with **Supplementary Figure 3**.

**a.**

	HC		EC		M1 (Control)	
	right	left	right	left	right	left
	p <sub>FWE</sub> (Bonferroni-Holm)				p (Uncorrected)	
E	1.91e-06	1.43e-06	9.54e-07	4.77e-07	<i>0.4324</i>	<i>0.0735</i>
D1	0.0024	3.81e-06	0.0036	0.0016	<i>0.3289</i>	<i>0.6460</i>
D2	1.91e-06	6.68e-05	3.34e-05	1.43e-05	0.0786	0.0597

**b.**

		HC right	HC left	EC right	EC left
$\tau$ E vs. $\tau$ D1	Z <sub>20</sub>	4.01	4.01	3.91	3.63
	p <sub>FWE</sub>	0.0002	0.0002	0.0003	0.0002
$\tau$ E vs. $\tau$ D2	Z <sub>20</sub>	4.01	4.01	3.28	3.42
	p <sub>FWE</sub>	0.0002	0.0002	0.0012	0.001
$\beta$ E vs. $\beta$ D1	T <sub>20</sub>	36.74	34.17	23.25	22.26
	p <sub>FWE</sub>	7.8E-20	3.3E-19	0.00009	0.00028
$\beta$ E vs. $\beta$ D2	T <sub>20</sub>	50.08	37.48	21.27	25.18
	p <sub>FWE</sub>	0.00006	0.00006	0.001	0.00061

**c.**

	HC		EC		M1 (Control)	
	right	left	right	left	right	left
	p <sub>FWE</sub> (Bonferroni-Holm)				p (Uncorrected)	
E	1.91e-06	1.43e-06	9.54e-07	4.77e-07	<i>1.0000</i>	<i>1.0000</i>
D1	1.91e-06	1.43e-06	2.86e-06	3.34e-06	<i>0.9649</i>	<i>0.9976</i>
D2	1.91e-06	1.43e-06	9.54e-07	4.77e-07	<i>1.0000</i>	<i>1.0000</i>

**d.**

		HC right	HC left	EC right	EC left
$\tau$ E vs. $\tau$ D1	Z <sub>20</sub>	3.91	4.01	3.84	3.32
	p <sub>FWE</sub>	2.77E-04	2.38E-04	2.45E-04	9.02E-04
$\tau$ E vs. $\tau$ D2	Z <sub>20</sub>	4.01	4.01	3.53	3.60
	p <sub>FWE</sub>	2.38E-04	1.79E-04	4.19E-04	6.43E-04

**e.**

	HC		EC		M1 (Control)	
	right	left	right	left	right	left
	p <sub>FWE</sub> (Bonferroni-Holm)				p (Uncorrected)	
Supplementary Fig. 5c	1.91e-06	1.43e-06	9.54e-07	4.77e-07	<i>0.2367</i>	<i>0.0953</i>
Supplementary Fig. 5d	1.91e-06	9.06e-06	1.34e-05	2.86e-06	<i>0.5942</i>	<i>0.1145</i>
Supplementary Fig. 5e	1.91e-06	1.43e-06	9.54e-07	4.77e-07	<i>0.9999</i>	<i>0.9868</i>

**Supplementary Table 2. Representational similarity analysis (RSA) results. a and b. Associated with Figure 3c.** **a.** The one-tailed Wilcoxon signed rank test (p values) of the rank correlation between the pattern dissimilarity based on equal sampling of 14 individuals at all events (F0, F1, and F2 presentations) and the pairwise Euclidean distance (E) ( $\tau$ E, Kendall's  $\tau_A$ ), and the 1-D rank difference in the competence dimension ( $\tau$ D1) and the 1-D rank difference in the popularity dimension ( $\tau$ D2). The p values (p<sub>FWE</sub>) are reported after correction for the number of bilateral ROIs (n=4) with the Bonferroni-Holm method (except for the control region, M1 that we reported uncorrected p values (italicized)). **b.** The pattern similarity in the HC and EC activity is

better accounted for by the 2-D Euclidean distance (E) than either 1-D distance alone. First, we compared the rank correlation of E ( $\tau_E$ , Kendall's  $\tau_A$ ) with the rank correlation of the 1-D rank difference in the competence dimension ( $\tau_{D1}$ ) and the rank correlation of the 1-D rank difference in the popularity dimension ( $\tau_{D2}$ ) (top rows). The z-values of the two-tailed Wilcoxon signed-rank test are reported in the table (\*\*  $p_{FWE} < 0.001$  in all 4 ROIs, Holm-Bonferroni correction;  $p_{FWE}$  values are in parenthesis). Second, we inputted the z-scored 2-D distance (E) and 1-D rank distance in one of two social hierarchy dimensions (D1 or D2) into the same general linear model (GLM) to pit them against one another to explain the pattern dissimilarity in the HC and EC (bottom rows). As regressors, we inputted E and D1 into one GLM, and E and D2 as regressors in another GLM. We further compared the regression coefficients  $\beta$  with the paired t-test. Consistent with the Wilcoxon signed-rank test, we found that E explains the pattern dissimilarity in bilateral HC and bilateral EC significantly better than D1 or D2 alone ( $p_{FWE} < 0.001$  in all 4 ROIs, Holm-Bonferroni correction). The t-values are reported in the table and the p-values are in parenthesis. **c and d.** In association with **Extended Figure 2a. c.** is the same as **a.**, and **d.** is the same as **b.** except that the pattern dissimilarity was estimated from the neural responses associated with all presentations of 14 individuals at all events (F0, F1, and F2 presentations). **e.** In association with **Supplementary Figure 5c, d, and e.** The one-tailed Wilcoxon signed rank test (p values) of the rank correlation of the pairwise E across participants (n=21).

a.

Brain areas	Laterality	k	T	Peak coordinate (MNI)		
				x	y	z
Supramarginal Gyrus	L	271	5.74	-42	-46	26
Caudate	L	829	5.7	-14	4	18
Hippocampus	R	1704	5.35	42	-20	-6
Medial Prefrontal Cortex/ Rostral Anterior Cingulate Cortex	R/L	658	4.66	0	30	10
Orbitofrontal cortex (BA11)	R		3.54	26	48	-10
Hippocampus *	L	49	3.79	-30	-36	-6
Retrosplenial Cortex	R/L	265	3.95	0	-36	26
Medial Prefrontal Cortex	L	153	3.86	-18	30	-2
Entorhinal Cortex *	L	24	3.81	-18	-10	-26
Entorhinal Cortex *	R	6	3.69	26	-8	-44

b.

Brain areas	Laterality	k	T	Peak coordinate (MNI)		
				x	y	z
Hippocampus *	R	370	6.86	30	-12	-24
Hippocampus *	L	164	4.44	-26	-10	-28
Posterior Cingulate Cortex/ Precuneus/ Retrosplenial cortex	R/L	5301	6.33	22	-68	38
			5.28	10	-50	48
Medial Prefrontal Cortex/ Rostral Anterior Cingulate Cortex/ Orbitofrontal cortex	L		2063	4.5	12	56
Superior Frontal Sulcus	L	32	4.65	-24	0	44
Inferior Parietal Lobule/ Temporoparietal Junction	R	324	4.58	56	-62	36
Caudate	R	75	4.44	14	22	-2
Entorhinal Cortex *	R	47	4.69	28	-12	-30
Entorhinal Cortex *	L	53	4.32	-28	-14	-32

**Supplementary Table 3. Whole-brain searchlight representational similarity analysis (RSA).**

**a.** Associated with **Figure 3f**. Brain areas in which its pattern dissimilarity was significantly explained by the pairwise Euclidean distances of 14 individuals on the 2-D social hierarchy (**Figure 3a**). The dissimilarity between activity patterns associated with each of 14 individuals from all events (F0, F1, and F2 presentations) was estimated from each searchlight while matching the number of observations of each individual (down-sampling). **b.** Associated with **Figure 3g**. Same as in (a.) except RSA is based on all observations acquired from all events (F0, F1, and F2 presentations). Results are reported at the threshold,  $p_{FWE} < 0.05$  whole-brain TFCE correction except for the HC and EC (marked with \*) which was tested at the threshold,  $p_{FWE} < 0.05$  TFCE corrected in the independently defined *a priori* ROI.



Brain areas	Laterality	k	Z	Peak coordinate (MNI)		
				x	y	z
Medial prefrontal cortex (mPFC)	R/L	768	5.58	2	66	-4
Posterior cingulate cortex (PCC) /Precuneus	R/L	181	3.19	2	-50	36
Posterior parietal cortex (PPC)	R	149	4.27	36	-46	62
Posterior parietal cortex (PPC)	L	289	3.81	-38	-50	50
Lateral orbitofrontal cortex (IOFC)	L	65	3.79	-42	44	-8
Retrosplenial cortex (RSC)	R/L	49	3.45	2	-54	28
Entorhinal cortex (EC)*	R	21	2.80	26	-10	-40

**Supplementary Table 4. Whole brain analysis showing hexagonally symmetric signals.**

Associated with **Extended Data Figure 3a**. All  $p_{TFCE} < 0.05$  within whole brain Threshold-Free Cluster Enhancement (TFCE) correction<sup>5</sup> except with \* which indicates the correction within *a priori* regions of interest (ROI). The ROI was anatomically defined in the EC<sup>2,3</sup>. Cluster size (k) was reported at  $Z > 3.1$  which corresponded to  $p < 0.001$  for all regions except for the *a priori* hypothesized effect in EC, in which we reported the cluster size at the threshold,  $Z > 2.3$  ( $p < 0.01$ ). R/L: the cluster extended across bilateral hemispheres. R, right hemisphere; L, left hemisphere.

**a. Hexadirectional modulations aligned to EC grid orientation**

(Cross-validation (CV) between sessions acquired within the same day)

Brain areas	Laterality	k	T	Peak coordinate (MNI)		
				x	y	z
Medial prefrontal cortex (mPFC)	R/L	114	4.72	-6	48	-4
Temporoparietal junction (TPJ)	R	238	3.67	46	-58	20
Temporoparietal junction (TPJ)	L	39	5.71	-56	-68	24
Superior temporal sulcus (STS)	R	794	4.05	50	-40	4
Superior temporal sulcus (STS)	L	251	4.29	-60	-24	-6
Entorhinal cortex (EC)	R	75	4.11	22	-10	-28

**b. Hexadirectional modulations aligned to EC grid orientation**

(CV between sessions acquired from a different day after more than a week)

Brain areas	Laterality	k	T	Peak coordinate (MNI)		
				x	y	z
Medial prefrontal cortex (mPFC)	R/L	278	5.04	-2	36	-8
Posterior cingulate cortex (PCC)	R/L	36	3.68	6	-58	30
Temporoparietal junction (TPJ)	L	480	4.06	-36	-64	22
Inferior temporal cortex (STS)	L	106	4.20	-52	-64	-4
Fusiform gyrus (FFA)	R	32	3.82	44	-40	-16
Fusiform gyrus (FFA)	L	106	4.00	-48	-54	-6
Entorhinal cortex (EC) *	R	30	4.21	36	-10	-38

**Supplementary Table 5. Brain areas showing hexadirectional grid-like coding.** **a.** In association with **Figure 4a**. Whole brain analysis showing hexadirectional modulations according to the direction of inferred trajectories aligned with the EC grid orientation consistently across sessions acquired within the same day. **b.** In association with **Extended Data Figure 3e**. Whole brain analysis showing hexadirectional modulations according to the direction of inferred trajectories aligned with the EC grid orientation consistently across sessions acquired from a different day after more than a week. All  $p_{TFCE} < 0.05$ , whole-brain cluster corrected using TFCE<sup>5</sup> except with \* which indicates the correction within *a priori* regions of interest (ROI). The ROI was anatomically defined in the EC<sup>2,3</sup>.

Periodicity		6	4 vs. 6	5 vs. 6	7 vs. 6	8 vs. 6
<b>Associated with Figure 4b</b>						
EC	T <sub>20</sub>	5.60	3.58	3.04	4.66	3.30
	p	1.76e-05	1.88e-03	6.50e-03	1.49e-04	3.59e-03
mPFC	T <sub>20</sub>	11.52	5.99	5.40	6.03	4.45
	p	2.78e-10	7.45e-06	2.74e-05	6.81e-06	2.48e-04
<b>Associated with Figure 4c</b>						
EC	T <sub>20</sub>	4.16	3.19	3.46	2.66	2.73
	p	4.89e-04	4.57e-03	2.48e-03	1.50e-02	1.28e-02
mPFC	T <sub>20</sub>	6.23	3.20	3.65	4.45	3.19
	p	4.38e-06	4.53e-03	1.60e-03	2.44e-04	4.58e-03
<b>Associated with Figure 5b</b>						
mPFC	T <sub>20</sub>	6.51	5.14	3.52	4.04	4.69
	p	2.42e-06	5.02e-05	2.16e-03	6.44e-04	1.41e-04
rTPJ	T <sub>20</sub>	6.26	4.57	4.78	4.30	4.57
	p	4.08e-06	1.85e-04	1.13e-04	3.45e-04	1.85e-04
ITPJ	T <sub>20</sub>	7.00	4.14	5.58	6.10	4.81
	p	8.63e-07	5.03e-04	1.85e-05	5.76e-06	1.06e-04
<b>Associated with Supplementary Figure 7</b>						
EC	T <sub>20</sub>	4.00	3.28	4.01	2.26	3.45
	p	7.00e-04	3.70e-03	7.00e-04	3.54e-02	2.50e-03
mPFC	T <sub>20</sub>	4.75	3.44	3.98	2.17	3.48
	p	1.00e-04	2.60e-03	7.00e-04	4.27e-02	2.40e-03
rFFA	T <sub>20</sub>	4.81	2.42	3.27	1.85	2.16
	p	1.00e-04	2.50e-02	3.90e-03	7.90e-02	4.28e-02
IFFA	T <sub>20</sub>	4.86	2.12	2.63	2.09	2.41
	p	1.00e-04	4.67e-02	1.60e-03	4.93e-02	2.58e-02

**Supplementary Table 6. Hexagonal modulation for inferred trajectories in the regions of interests (ROIs).** The mean z-scored activity difference between aligned and misaligned trajectories was larger than zero for six-fold periodicity (two-tailed one-sample t test), and the activity difference is greater for six-fold compared to the other periodicities (paired t test).

**a. Neural correlates of GP**

Brain areas	Laterality	k	T	Peak coordinate (MNI)		
				x	y	z
Medial prefrontal cortex (mPFC)	R/L	1460	5.55	10	52	6
Temporoparietal junction (TPJ)	R	870	5.45	54	-56	34
Temporoparietal junction (TPJ)	L	276	5.18	-54	-60	28
Posterior cingulate cortex (PCC)	R/L	246	5.76	0	-24	36
Entorhinal cortex (EC)*	R	10	3.88	20	-4	-32

**b. Neural correlates of |GP1-GP2|**

Brain areas	Laterality	k	T	Peak coordinate (MNI)		
				x	y	z
Ventromedial prefrontal cortex (vmPFC)	R/L	484	5.07	-8	54	-6
Supramarginal cortex (SMC)	L	1723	5.68	-62	-62	8
Fusiform face area (FFA)	L	14	4.10	-32	-30	-24
Hippocampus (HC)/ Entorhinal cortex (EC)	L	79	4.53	-28	-4	-26
Entorhinal cortex (EC)*	R	140	5.10	22	-12	-26
Entorhinal cortex (EC)*	L	14	4.00	-26	-16	-32

**c. Contrasts of neural correlates of GP between aligned and misaligned trajectories**

Brain areas	Laterality	k	T	Peak coordinate (MNI)		
				x	y	z
Medial prefrontal cortex (mPFC)	R/L	398	4.97	8	46	8
Medial frontal gyrus (mFG)	R	280	5.28	8	42	50
Medial frontal gyrus (mFG)	L	27	4.16	-20	36	50
Inferior orbitofrontal cortex (iOFC)/ Anterior insula	R	339	5.83	30	12	-22
Temporoparietal junction (TPJ)	R	78	4.92	56	-66	28

**d. Difference in the GP effects in anatomically defined region of interests (paired t test)**

$\beta_{GP}$ [Aligned - Misaligned]	$T_{20}$	p
mPFC	4.33	3.26e-04
Right TPJ	5.81	1.11e-05
Left TPJ	3.45	0.0026

**Supplementary Table 7. Neural encoding of decision variables.** **a.** Whole brain analysis showing neural correlates of decision variables including growth potential (GP, in association with **Figure 5a**). **b.** Neural correlates of differences between GPs ( $|GP1-GP2|$ , in association with **Figure 5f**). **c.** The contrast map of neural correlates of GP between aligned and misaligned trajectories (Aligned > Misaligned, in association with **Figure 5d**). \* indicates correction within a *priori* regions of interest (ROIs). The ROI was anatomically defined in the EC <sup>2,3</sup>. All other brain areas were significant at the threshold,  $p_{TFCE} < 0.05$ , whole-brain cluster corrected using TFCE <sup>5</sup>. Cluster size (k) was reported at  $p < 0.001$ . **d.** Associated with **Figure 5e**. Difference in the GP effects between trials in which the inferred trajectory is aligned compared to misaligned trials in anatomically defined ROIs (paired t test).

**a.**

	ROIs	One-sample t test (First 6 30° bins)		Paired t test (Novel pairs only) (First 6 vs. last 6 30° bins)			
		$\phi \pm 15^\circ$	$\sim [\phi + \frac{5\pi}{6}] \pm 15^\circ$	$T_{20}$	$p$	$T_{20}$	$p$
CV across blocks (Associated with <b>Figure 4b</b> )	EC	2.35	0.03*	-0.96	0.35		
	mPFC	3.84	0.00**	-1.48	0.16		
CV across days (Associated with <b>Figure 4c</b> )	EC	2.35	0.03*	-0.72	0.48		
	mPFC	2.72	0.01*	-0.33	0.75		
GP effects (Associated with <b>Figure 5b</b> )	mPFC	5.07	0.00**	-0.20	0.85		
	GP						
	rTPJ GP	3.61	0.00**	-1.08	0.29		
	ITPJ GP	4.98	0.00**	-1.06	0.30		

**b.**

Excluded Bin	$\phi+0$	$\phi+30$	$\phi+60$	$\phi+90$	$\phi+120$	$\phi+150$
	$\phi+180$	$\phi+210$	$\phi+240$	$\phi+270$	$\phi+300$	$\phi+330$
ROIs	p value					
mPFC	1.87e-03	1.15e-03	4.19e-04	7.96e-04	1.02e-03	1.30e-03
	9.02e-04	1.15e-03	1.30e-03	1.87e-03	2.64e-03	9.02e-04
right TPJ	4.14e-03	2.10e-03	1.66e-03	6.36e-03	3.31e-03	1.30e-03
	2.36e-03	2.10e-03	7.02e-04	2.96e-03	1.17e-02	2.96e-03
left TPJ	2.10e-03	3.70e-03	6.18e-04	2.96e-03	3.31e-03	3.31e-03
	3.31e-03	2.36e-03	2.36e-03	7.96e-04	6.36e-03	8.69e-03

**Supplementary Table 8. Validation of Hexadirectional grid-like effects.** **a.** Hexadirectional grid-like effects restricted to the low angle space. The grid effects (aligned – misaligned) analysis including only the pairs in the first six 30° bins ( $\phi \pm 15^\circ \sim [\phi + 5\pi/6] \pm 15^\circ$ ). The mean activity of aligned pairs and GP effects ( $\beta$ GP) of aligned pairs are greater than those of the misaligned pairs (One-sample t test, two-tailed; \*\*  $p < 0.01$ , \*  $p < 0.05$ ; left column in the Table). This finding shows that the hexadirectional grid-like effect was not only driven by angles larger than 180°. The more frequent samples of inferred trajectories could influence the relatively weaker effects in first six bins. We further test whether the effect sizes differ between the first and the last six bins when the pairs were presented for the first time. Specifically, we tested the grid effects (aligned – misaligned) including only the pairs that were shown for the first time to the participants (novel pairs only). We further compared the grid effects of the first six 30° bins (lower angle bins;  $\phi \pm 15^\circ \sim [\phi + 5\pi/6] \pm 15^\circ$ ) to those of the last six 30° bins (higher angle bins;  $[\phi + \pi] \pm 15^\circ \sim [\phi + 11\pi/6] \pm 15^\circ$ ). We find that neither the mean activity nor the GP effects ( $\beta$ GP) of aligned compared to misaligned pairs differ between the first and the last six bins when the pairs are shown first time to the participants (Paired t test, all  $p > 0.05$ ; right column). **b.** Associated with **Supplementary Figure 9f**. Hexadirectional grid-like effects (z-scored mean activity differences in aligned – misaligned inferred trajectories) while leaving one bin out (LOBO) analysis. This shows that the hexadirectional grid-like effects are not dependent on the different activity in a single bin (all  $p < 0.05$ ).

Face 13 (42)	Face 14 (21)	Face 15 (16)	Face 16 (8)
Face 9 (23)	Face 10 (58)	Face 11 (58)	Face 12 (19)
Face 5 (69)	Face 6 (45)	Face 7 (57)	Face 8 (18)
Face 1 (12)	Face 2 (69)	Face 3 (18)	Face 4 (43)

**Supplementary Table 9. The numbers of each stimulus presentations.** The numbers of presentations of each of 16 faces during a single scan (three blocks of one day) were shown in brackets.

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