Supplemental Material: Manipulation of Majorana bound states in proximity to a quantum ring with Rashba coupling

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Quasiparticle spectra, Charge and Spin Currents For N = 5, 6.

The spectra and currents for N = 5, 6 are presented.



Figure 1: Quasiparticle spectra for $\lambda_1 = 0.1$ and $\lambda_2 = 0$. The number of sites, N, the coupling between MZMs, ξ_M , and the Rashba spin-orbit coupling, α , are indicated in the figure. Black curves represent the states in the quantum ring and the red curves correspond to the Majorana modes.



Figure 2: Charge and spin persistent currents, I_q and I_s respectively, for $\lambda_1 = 0.1, \lambda_2 = 0$. The number of sites, N, and the Rashba spin-orbit coupling, α , are indicated in the figures. The coupling between MZMs, ξ_M , is indicated by coloured lines, shown in the leftmost panels.



Figure 3: Quasiparticle spectra for $\lambda_1 = 0.1$ and $\lambda_2 = 0.15$. The number of sites, N, the coupling between MZMs, ξ_M , and the Rashba spin-orbit coupling, α , are indicated in the figure. Black curves represent the states in the quantum ring and the red curves correspond to the Majorana modes.



Figure 4: Charge and spin persistent currents, I_q and I_s respectively, for $\lambda_1 = 0.1, \lambda_2 = 0.15$. The number of sites, N, and the Rashba spin-orbit coupling, α , are indicated in the figures. The coupling between MZMs, ξ_M , is indicated by coloured lines, shown in the leftmost panels.

The spectra obtained for N = 5 show avoiding crossings between Majorana modes in panel (b) and (f) from Figure 3. In the spectra for N = 3 Majorana modes display zero energy crossing around 0.5 and -0.5, as we mention before, this does not happen for N > 5 as can be observed in panel (f) from Figure 6.

Quasiparticle Spectra for N = 11, 12.



Figure 5: Quasiparticle spectra for $\lambda_1 = 0.1$ and $\lambda_2 = 0$. The number of sites, N, the coupling between MZMs, ξ_M , and the Rashba spin-orbit coupling, α , are indicated in the figure. Black curves represent the states in the quantum ring and the red curves correspond to the Majorana modes.



Figure 6: Quasiparticle spectra for $\lambda_1 = 0.1$ and $\lambda_2 = 0.15$. The number of sites, N, the coupling between MZMs, ξ_M , and the Rashba spin-orbit coupling, α , are indicated in the figure. Black curves represent the states in the quantum ring and the red curves correspond to the Majorana modes.