1	Machine learning-informed and synthetic biology-enabled semi-continuous algal
2	cultivation to unleash renewable fuel productivity
3	Long <i>et al</i> .

4 Supplementary Method 1. Training data collection and processing for light pattern

5 prediction

6 In order to access real-time light availability inside algal culture, we first developed a light 7 distribution pattern prediction model (LDPM) to predict light distribution patterns (LDPs) in a cuboid photobioreactor (PBR). We collected 138 LDPs in the PBR (19.6 cm in length \times 9.6 cm 8 9 in width \times 20 cm in height) with 23 different cell concentrations and 6 different light intensities as training samples for the machine-learning model. The LDPs were captured by a camera fixed 10 on top of a PBR containing different cell concentrations and illuminated with different light 11 intensities. A LED light bar (4000K, CRI =80) placed on one side of the photobioreactor was 12 used as a light source (Figure 1A). The illuminance was monitored by a sensor on the surface 13 of the photobioreactor and converted to photosynthetic photon flux density (PPFD) with a 14 coefficient of 56. The twenty-three cell concentration gradients were set to 0.11973, 0.21294, 15 0.40872, 0.45162, 0.54405, 0.62712, 0.74256, 0.82056, 0.90948, 0.96915, 1.10604, 1.2246, 16 1.3026, 1.3923, 1.443, 1.5444, 1.7901, 1.9188, 2.0241, 2.3556, 2.535, 2.9601, 3.6777 g/L, 17 while the six light intensity gradients were set to 107, 178, 267, 357, 570, 714 μ mol m⁻² s⁻¹. 18 The camera was set to manual mode and all parameters were locked throughout the 19 20 photographing process to ensure consistency. After acquiring all LDPs, raw pictures were cropped, converted to grayscale, and compressed to 40×18 pixels in Photoshop 2020 (Figure 21 1A). The compressed images were used to represent the light distribution pattern inside the 22 photobioreactor with grayscale values (GSVs) representing light intensities. The GSVs were 23 extracted from the grayscale images with the CV2 module in Python. To evaluate the accuracy 24 of GSVs representing light intensities, we extracted GSVs at (0, 20) (row 0, column 20) from 25

LDPs over a wide range of cell concentrations and assessed the linearity between GSV and lightintensity.

28 The training sample collection for pond LDPM is shown in Figure S10A. LDP images were 29 captured from a simplified pond setup (Figure S10A) and the collected LDP images were converted to 208×10 -pixel grayscale images as mentioned above. The light intensities for the 30 31 pond LDP training samples were set to 196, 268, 357, 446, 536, 625, 714, 804, 964, 1071, 1161, 1250, 1339, 1429, 1518, 1607, 1696, 1786, 1875 µmol m⁻² s⁻¹, and cell concentrations were set 32 to 0.062, 0.140, 0.228, 0.337, 0.466, 0.620, 0.871, 0.999, 1.177, 1.254, 1.396, 1.482, 1.553, 33 34 2.007, 2.320, 2.814, 3.199, 3.694, 4.577, 5.519 g/L. The LDP for the pond system was set to be one-dimensional and represented with the 208 pixels in the middle column (column 5) of the 35 LDP image. 36

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Supplementary Method 2. LDPM training and evaluation

Due to the high complexity of the LDP inside algal culture and limited training samples, we 38 39 believe that predicting LDPs pixel by pixel is the best method for accurate prediction. Pixel-by-40 pixel prediction means that individual pixels in LDP images are treated as individual models and then combined, rather than treating the whole image as one model. Thus, we trained 720 models 41 42 for a 40×18 -pixel LDP prediction. Cell concentrations and light intensities, two major factors shaping LDP, were set as features in training with the corresponding GSVs at each pixel as labels. 43 Both features and labels were normalized by subtracting their average and dividing by their 44 standard deviation. Around 10% of the training samples were randomly selected as testing samples. 45 We chose Support Vector Regression with a Radial Basis Function kernel (SVR-RBF) as the 46 algorithm and kernel for the prediction in this study. SVR-RBF from an open-source machine 47 learning library, scikit-learn¹, was used for training and prediction. We selected the best models at 48 each pixel by selecting the combinations of parameters (C:1, 10, 100, 1000, 3000; gamma: 0.003, 49 0.01, 0.03, 0.1, 0.3, 1.) returning the highest R^2 score. Prediction accuracy was determined by 50 overall evaluation and by pixel-by-pixel evaluation. The overall evaluation calculated an R² value 51 by comparing all predicted GSVs with measured GSVs in the testing data set to assess the overall 52 prediction accuracy of the model. Pixel-by-pixel evaluation calculated the R² value at each pixel 53 to assess the prediction accuracy at different positions on LDPs. Accuracy percentages were 54 calculated by counting pixels with an \mathbb{R}^2 score larger than 0.90 (or between 0.79 and 0.85), and 55 dividing by 720. The R^2 evaluation was performed with the metrics module on scikit-learn. The 56 matplotlib module in Python was used for visualization of evaluation results and predicted images². 57

58 Supplementary Method 3. Dark area calculation

59 In the machine-learning training process, we collected LDPs from a larger cuboid 60 photobioreactor (19.6 cm in length \times 9.6 cm in width \times 20 cm in height) in order to get more 61 information from a single image. However, the photobioreactor used for cultivation was a smaller photobioreactor 10 cm long and 5 cm wide. To adapt the pre-trained models to the 62 smaller photobioreactor, we selected the 10 left-most columns (column 0-9) and 10 right-most 63 columns (column 30-39) in the 9 rows (row 0-8) closest to the light source in the LDP of the 64 larger photobioreactor to represent the LDP of the smaller photobioreactor. Thus, LDPs in small 65 photobioreactors were represented by images with $180(20 \times 9)$ pixels. For dark area calculation, 66 grayscale values less than 25.5 (1/10 of the maximum grayscale value) were counted (n) and 67 normalized as percentages of LDP pixels ($n/180 \times 100\%$). The dark area with double light sources 68 was estimated with the following equation (1), assuming no interference between light from 69 two sources: 70

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$$A_{2} = \begin{cases} (1 - (1 - A_{1}) \times 2) \times 100\% & if A_{1} > 50\%; \\ 0 & if A_{1} < 50\%; \end{cases}$$
(1)

Where A₁ and A₂ refer to dark areas with one and two light sources at given light intensities,
respectively.

74 Supplementary Method 4. Growth curve fitting, growth rate calculation, and biomass

75 productivity prediction

To generate a growth curve, we collected cell concentration under given light intensities at different time points by measuring OD₇₃₀. Variables were normalized by subtracting their average and dividing by their standard deviation. The logistic curve was defined as the equation (2):

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$$f(x) = \frac{a}{(1 + e^{-c(x-d)})} + b$$
 (2)

81 Where x represents the variable here, representing time and a, b, c, d are parameters that 82 determine the shape of the growth curve. The fitting and prediction were processed by the 83 Optimize module in the SciPy library in Python³. Growth rates at specific time points were 84 estimated by the slope of the corresponding curve at that point.

85 Supplementary Method 5. Growth Rate Prediction Model (GRM) training and evaluation

The GRM was trained to predict cyanobacterial growth rates based on the LDPs (Figure 86 87 2B). In order to collect training data, we cultivated cyanobacteria under different light intensities (107, 178, 267, 357, 570, 714 μ mol m⁻² s⁻¹) in the smaller PBR. The concentration 88 of the cyanobacteria was monitored and fitted with sigmoid curves for growth rate calculations 89 90 mentioned above. Vectors extracted from the first 9 rows in the middle column of the LDP were used as features, and the corresponding (at the same time points) calculated growth rates were 91 set as labels in the training. The features were normalized by subtracting their averages and 92 93 dividing by their standard deviations. The random forest algorithm was used for the GRM model and the performance of the model was evaluated by calculating an R^2 value between the 94 predicted and measured growth rates in the reserved testing set (20% of the training samples). 95 The GRM was adapted to predict growth rates under a double-light condition based on the 96 assumption that there are no interferences between light from two sources. In this way, vectors 97 extracted from the first 5 rows of the middle columns of LDPs were used as features for the 98 GRM training. 99

Similar to the GRM for PBR, we grew several batches of cyanobacteria in a pond system to acquire the growth data for pond GRM training. The growth data were then fitted with sigmoid curves for growth rate calculation. The normalized 208-length vectors predicted from the pond LDPM and the calculated growth rates were set as features and labels, respectively, for the pond GRM training. The training and evaluation of the pond GRM were the same as the PBR GRM described above.

106 Supplementary Method 6. Growth simulation

Cyanobacterial growth simulation was performed as shown in Figure 2A. An initial cell 107 108 concentration and light program are required inputs and the simulation process contains a loop 109 with four steps: 1) predict the LDP based on the initial cell concentration and initial light intensity with the LDPM; 2) predict the growth rate based on the LDP from step 1 with the 110 GRM; 3) calculate the new cell concentration from the initial cell concentration and the 111 predicted growth rate; 4) update the newly calculated cell concentration and current light 112 intensity as inputs for the next round of LDP prediction. The light programs were specified in 113 the main text. The initial cell concentration used for PBR growth simulation ranged from 0.2 to 114 4.8, with a 0.2 increment. The initial concentration used for pond growth simulation was set to 115 0.1, 0.4, 0.6, and 0.8. To ensure accurate growth simulation, the bubbling rate, temperature, 116 surface area, and light conditions were tightly controlled in a way that no severe sedimentation 117 happens during cultivation in PBRs, while these conditions were controlled to achieve 118 sedimentation in collection vessel. 119





121 Supplementary Figure 1. Pixel-by-pixel evaluation of LDPM prediction over testing

samples. 94.4% of pixels achieved R^2 values higher than 0.90, and only 0.8% of pixels had R^2

123 values in the range of 0.79 to 0.85.



Supplementary Figure 2. Light intensity (represented by GSV) changes over the length of 125 the light path. GSVs in the middle column (column 20, row 1 - 18) of LDPs were extracted to 126 127 represent light intensities over light paths and plotted against distances from light sources (a-d). Different colors in the figures represent different intensities of light sources (107, 178, 267, 357, 128 570, 714 μ mol m⁻² s⁻¹). Light intensity decreased only slightly over the path when cell 129 concentration was low (a). But significant decreases were observed when cell concentration 130 increased (b, c), and light intensity dropped sharply (GSV below 20 within 1 cm) when cell 131 concentration reached 2.9601 g/L (d). The results suggest intensified mutual shading at higher cell 132 concentration. Source data are provided as a Source Data file. 133



Supplementary Figure 3. Relationship between cell concentration (OD₇₃₀), dark area derived 135 from LDP, and growth rate. Growth curves (blue) were generated by fitting cell concentration 136 (OD₇₃₀ and time) collected from cultivations under light intensities at 107 (a), 178 (b), 267 (c), 357 137 (d), 570 (e), 714 (f) µmol m⁻² s⁻¹. Slopes of growth curves were calculated to represent growth 138 rates at these light intensities (green, a-f). LDPs over the growth at given light conditions were 139 predicted by LDPM and dark areas were defined as LDP pixels with GSVs less than 25.5 (magenta, 140 a-f). Growth rates peaked at 36.8 ± 4.7 hours and dark areas reached $43.1 \pm 4.9\%$ regardless of 141 light intensity (green, magenta, a-f). Overall, dark areas experienced three stages: zeros stage (left 142 of the first dashed line), increasing stage (in between the first and second dashed lines), and plateau 143 stage (right of the second dashed line) (magenta, a-f). The increasing stage (between dashed lines) 144 overlapped significantly with the fastest growth period of cyanobacteria (green, magenta, a-f). 145 146 Source data are provided as a Source Data file.



Supplementary Figure 4. Validation of growth simulation by machine-learning models under different growth conditions and comparison between semi-continuous algal cultivation (SAC) and fed-batch. The growth simulation achieved R² scores of 0.996 (a), 0.999 (b), 0.996 (c), 0.998 (d), 0.996 (e), 0.997 (f), and 0.978 (g) under light intensities of 107, 178, 267, 357, 570, 714, and 178-714-178 µmol m⁻² s⁻¹, indicating high prediction accuracy. (h) Growth comparison of UTEX 2973 with SAC and fed-batch cultivation Data are presented as mean values +/- standard deviations (n = 3 independent samples). Source data are provided as a Source Data file.



Supplementary Figure 5. GRM adapted for growth rate prediction with double light sources.
a, validation of the growth rate prediction by the GRM adapted for double light. b, Growth
simulation suggests setting initial OD₇₃₀ at 2.3 delivers highest biomass productivity. Source data
are provided as a Source Data file.



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161 Supplementary Figure 6. Transmission electron microscopy reveals cell surface differences

162 between *Synechococcus elongatus* PCC 7942 and UTEX 2973. UTEX 2973 showed relatively

smooth cell surface compared to PCC 7942, where lots of pili formed. Similar results were found

164 in two independents observations. Original images are provided as a Source Data File.



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166 Supplementary Figure 7. Comparison of growth between UTEX 2973 WT and L524. No

significant growth differences were found between WT and L524 in the given growth conditions.

168 Data are presented as mean values +/- standard deviations (n = 3 independent samples). Source

169 data are provided as a Source Data file.





Supplementary Figure 8. Standard curve used to normalize limonene productivity with recovery rate. Limonene concentrations of 250, 500, 750, 1000 μ g/mL were used to spike the UTEX 2973 wildtype cells. Limonene was collected and measure as described in the Methods of the main text. Data are presented as mean values +/- standard deviations (n = 3 independent samples). Source data are provided as a Source Data file.



178 Supplementary Figure 9. Techno-economic analysis of the pond SAC platform. The NREL

algae farm model projects a MBSP of approximately \$281 per ton based on the outdoor trial yield.

180 Cost breakdown suggests the dewatering process accounts for \$24.50 per ton.



Supplementary Figure 10. LDP prediction for open pond system and conversion between turbidity and OD₇₃₀. The process of adapting LDPM for pond system prediction (a) and the calibration curve for OD-turbidity (Attenuation Unit, AU) conversion (b). Source data are provided as a Source Data file.

Primer name	Sequence	Note
NS-DS-F	cacgaggccctttcgtcttcaagaaATGGATCTGACCAACATG	Building L524
NS-US-R	atcgatgataagctgtcaaacatgagaaAAACGCGCGAGGCAGGAT	Building L524
NSI-F	TCAGCTGCTTTAGGCCCACCAGTTTGAAG	Segregation
NSI-R	TTATCTCTCGGCTAGTGGACGCAAGCAGCG	Segregation
petB1-F	CGACTGGTTCGAGGAGCGTC	qRT-PCR, IS
petB1-R	TTGCAAAGCCGGTGGCAAAC	qRT-PCR, IS
LS1-F	CTCGAATCTGCCCGCGAGTT	qRT-PCR, LS
LS1-R	GATCCAGACCGGGGGCATTGG	qRT-PCR, LS

188 IS, internal standard; LS, limonene synthase.

189 Supplementary references

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195 196 197	3.	Virtanen P, et al. SciPy 1.0: fundamental algorithms for scientific computing in Python. <i>Nat Methods</i> 17 , 261-272 (2020).