

# **Cross-Sections of Nanocellulose from Wood Analyzed by Quantized Polydispersity of Elementary Microfibrils**

## **Supplementary material**

Tomas Rosén<sup>a,b,c</sup>, HongRui He<sup>a</sup>, Ruifu Wang<sup>a</sup>, Chengbo Zhan<sup>a</sup>, Shirish Chodankar<sup>d</sup>, Andreas Fall<sup>e</sup>, Christian Aulin<sup>e</sup>, Per Tomas Larsson<sup>c,e</sup>, Tom Lindström<sup>a</sup>, and Benjamin S. Hsiao<sup>a,1</sup>

<sup>a</sup>Department of Chemistry, Stony Brook University, Stony Brook, NY 11794-3400, USA

<sup>b</sup>Fiber and Polymer Technology, KTH Royal Institute of Technology, SE-100 44, Stockholm, Sweden

<sup>c</sup>Wallenberg Wood Science Center, KTH Royal Institute of Technology, SE-100 44, Stockholm, Sweden

<sup>d</sup>National Synchrotron Light Source II, Brookhaven National Lab, Upton, NY 11793, USA

<sup>e</sup>RISE, Box 5604, 114 86, Stockholm, Sweden

<sup>1</sup>To whom correspondence should be addressed

**Contents:**

- TEM images of the 18 CNF samples in the study
- Assessment of isotropy in WAXD experiments
- Results from WAXD simulations

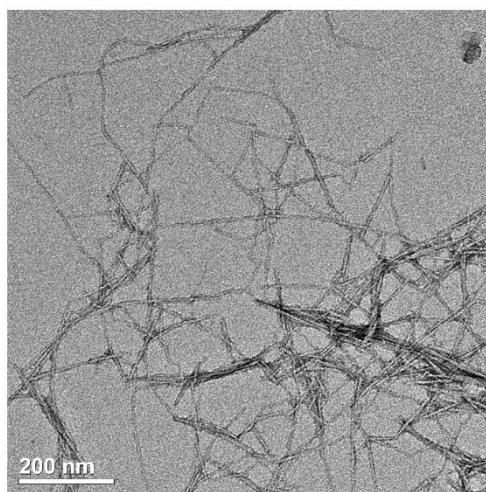
Additionally, a supplementary movie is provided to illustrate the principle of the WAXD simulations.

## **TEM images of CNF samples**

## TEMPO-oxidized CNF (low charge)

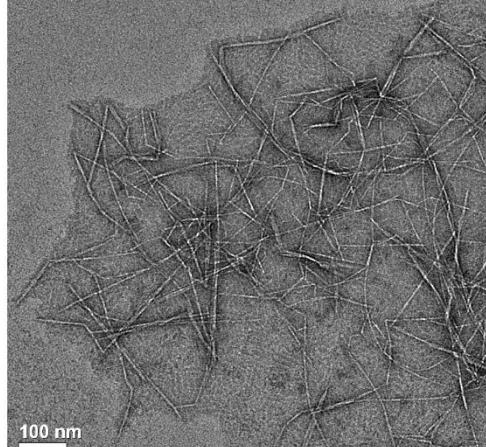
Sample #

1



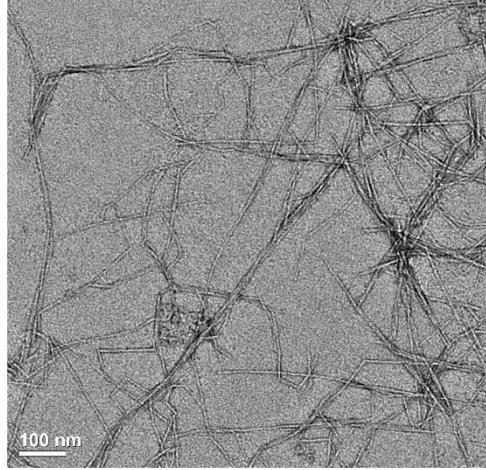
Average width based on  
>60 nanofibrils: 6.9 nm  
Standard deviation: 1.4 nm

2



Average width based on  
>60 nanofibrils: 6.3 nm  
Standard deviation: 1.3 nm

3

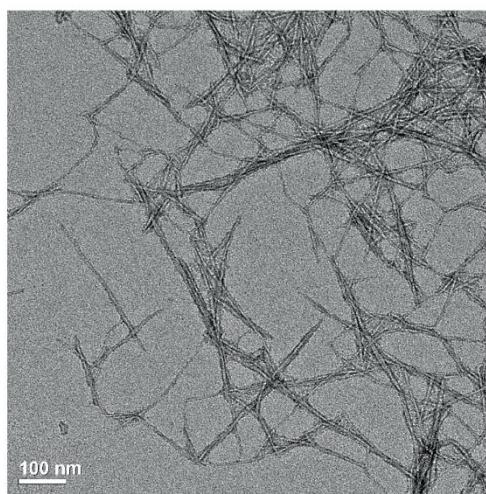


Average width based on  
>60 nanofibrils: 7.4 nm  
Standard deviation: 2.5 nm

## TEMPO-oxidized CNF (high charge)

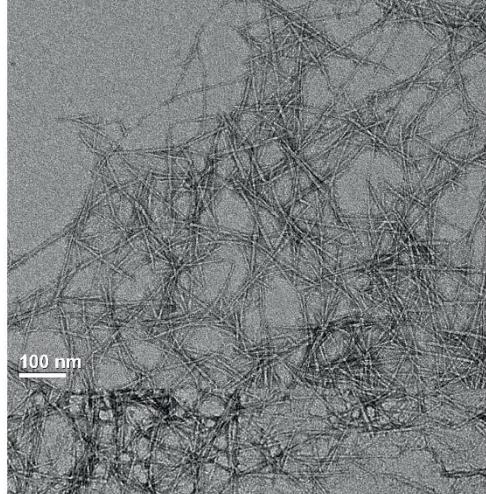
Sample #

4



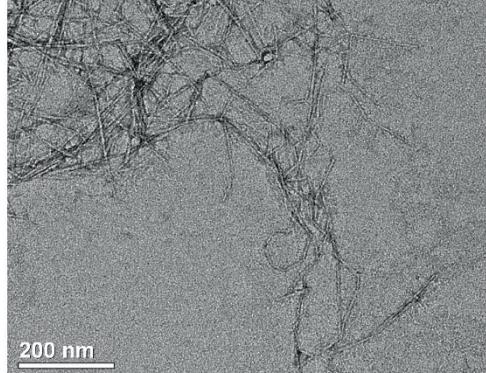
Average width based on  
>60 nanofibrils: 6.9 nm  
Standard deviation: 2.3 nm

5



Average width based on  
>60 nanofibrils: 6.0 nm  
Standard deviation: 2.4 nm

6

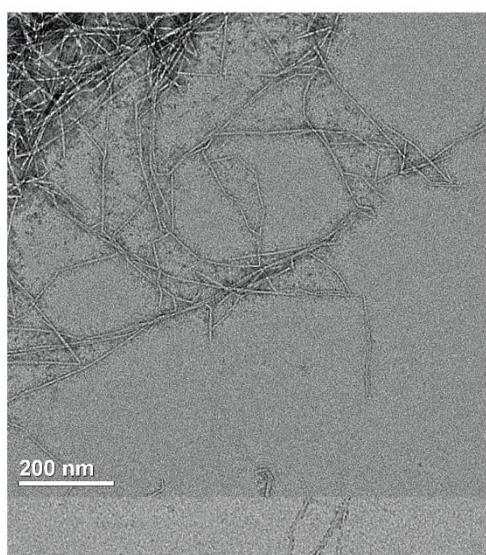


Average width based on  
>60 nanofibrils: 7.1 nm  
Standard deviation: 1.5 nm

## Carboxymethylated CNF (lowest charge)

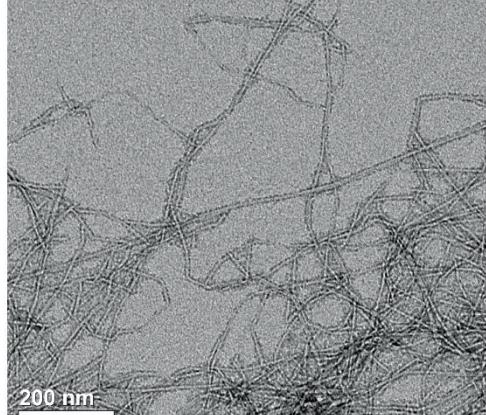
Sample #

7



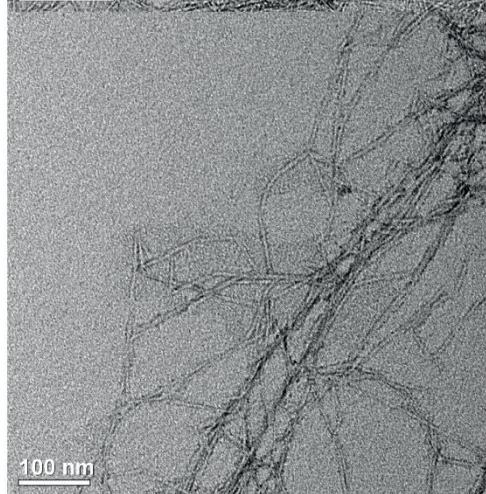
Average width based on  
>60 nanofibrils: 6.2 nm  
Standard deviation: 1.1 nm

8



Average width based on  
>60 nanofibrils: 5.9 nm  
Standard deviation: 1.1 nm

9

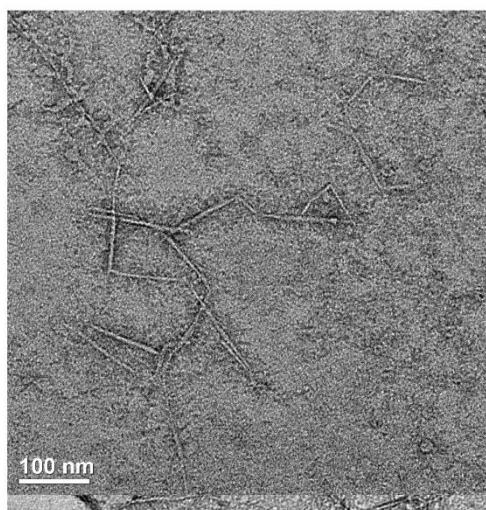


Average width based on  
>60 nanofibrils: 6.1 nm  
Standard deviation: 1.2 nm

## Carboxymethylated CNF (low charge)

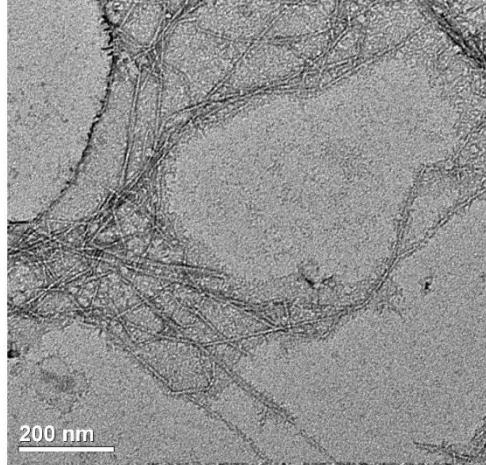
Sample #

10



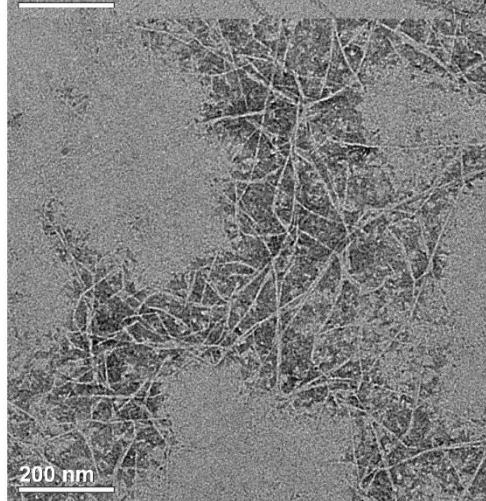
Average width based on  
>60 nanofibrils: 6.3 nm  
Standard deviation: 1.3 nm

11



Average width based on  
>60 nanofibrils: 5.8 nm  
Standard deviation: 1.2 nm

12

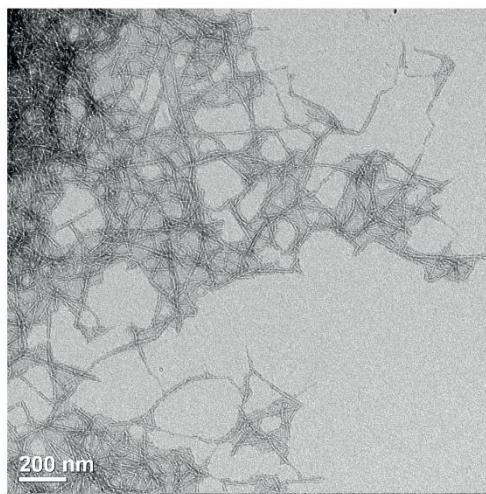


Average width based on  
>60 nanofibrils: 5.9 nm  
Standard deviation: 1.2 nm

## Carboxymethylated CNF (high charge)

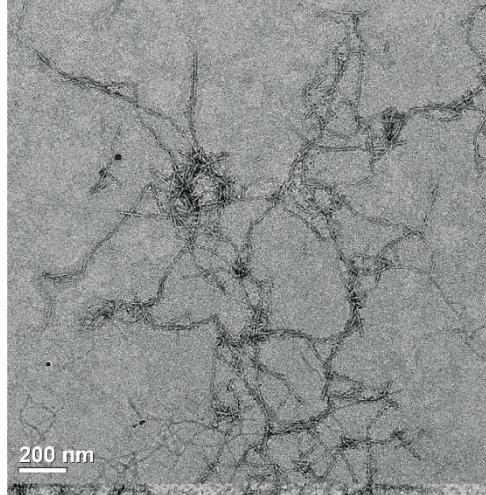
Sample #

13



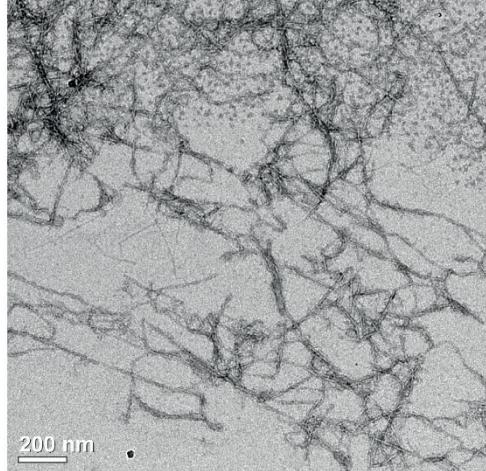
Average width based on  
>60 nanofibrils: 8.2 nm  
Standard deviation: 2.0 nm

14



Average width based on  
>60 nanofibrils: 5.0 nm  
Standard deviation: 1.0 nm

15

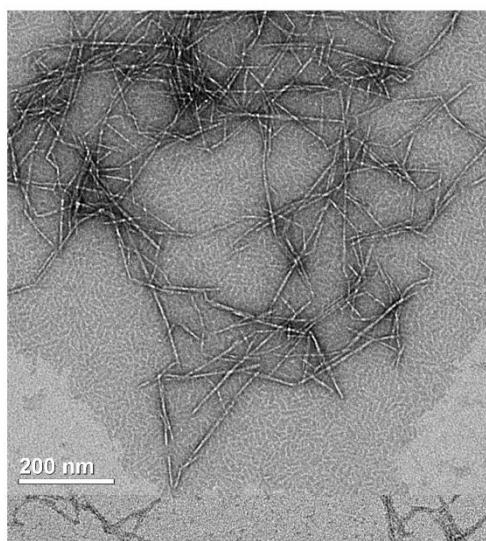


Average width based on  
>60 nanofibrils: 6.9 nm  
Standard deviation: 1.3 nm

## Carboxymethylated CNF (highest charge)

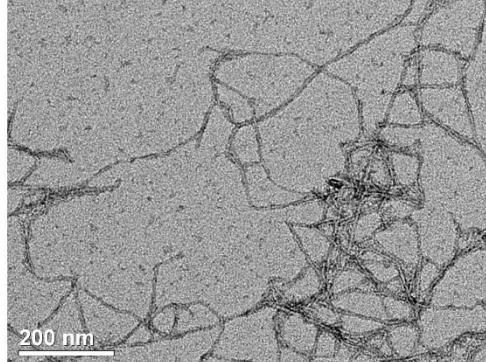
Sample #

16



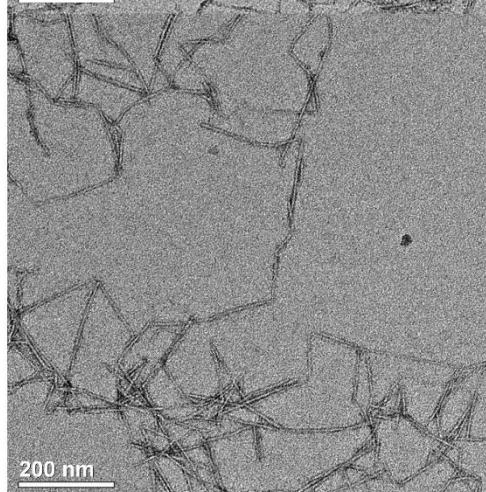
Average width based on  
>60 nanofibrils: 7.7 nm  
Standard deviation: 1.8 nm

17



Average width based on  
>60 nanofibrils: 6.8 nm  
Standard deviation: 2.0 nm

18

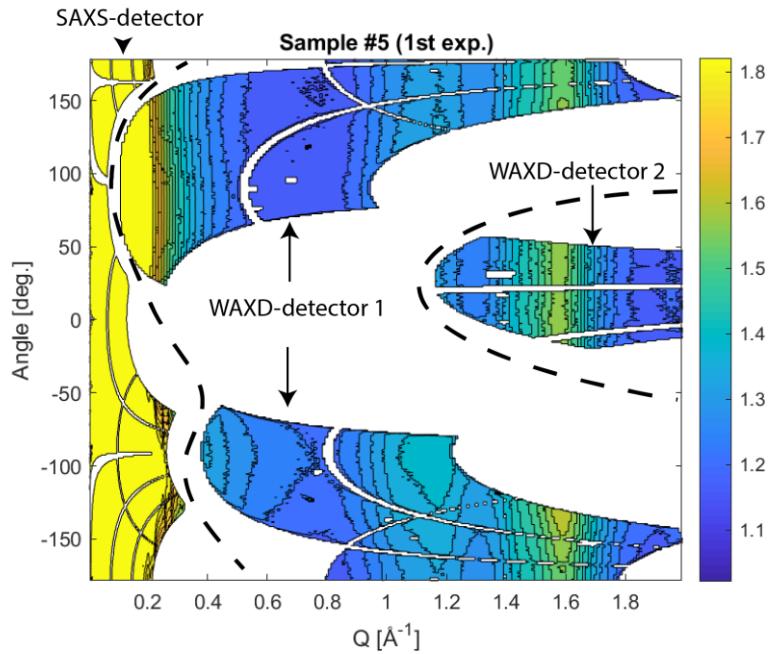


Average width based on  
>60 nanofibrils: 6.1 nm  
Standard deviation: 1.2 nm

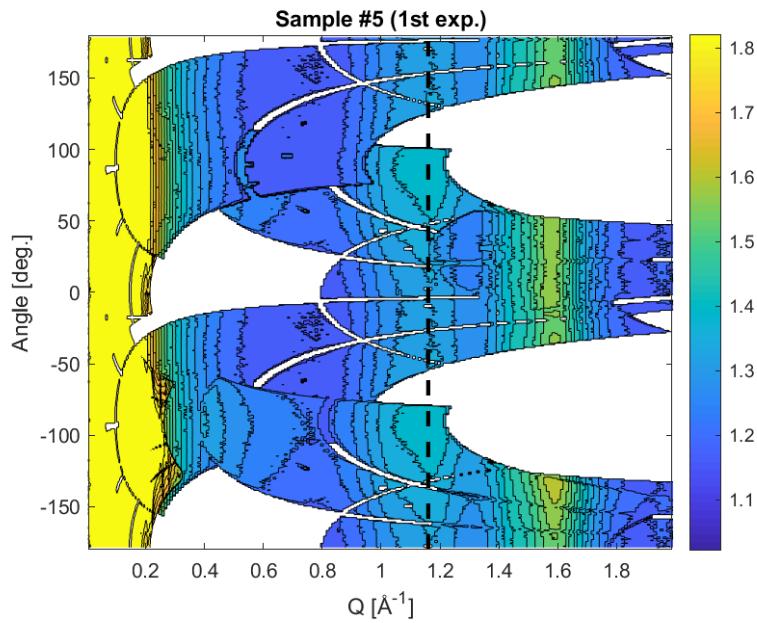
## **WAXD experiments: ensuring isotropy of samples**

## Procedure:

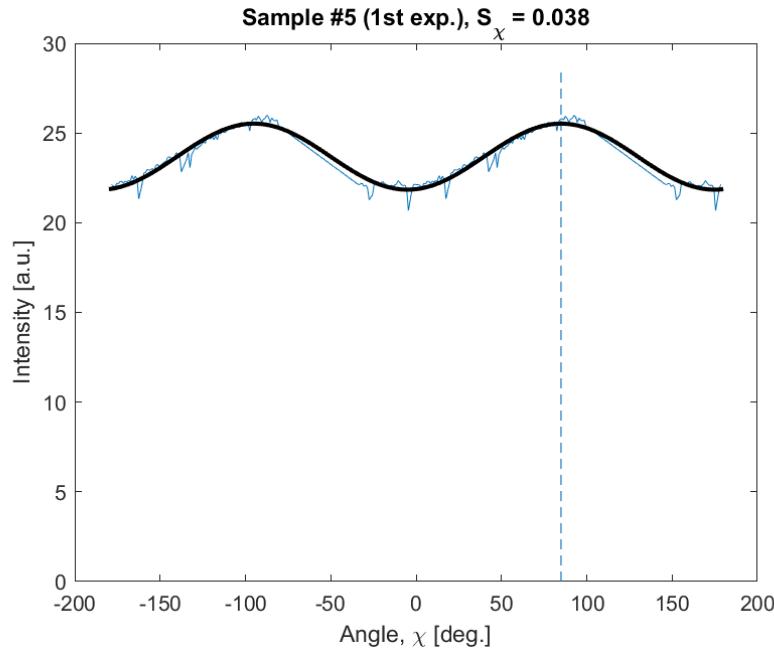
Simultaneous SAXS and WAXD signals were recorded on 3 different detectors (average of 5 different measurement locations, each with 1 s exposure):



The in-accessible (zero) pixels at an angle  $\chi$  are corrected with data from the corresponding mirror-pixel (if accessible) at  $\chi \pm 180^\circ$ , due to symmetry:



Note that this mirror-correction does not lead to a perfect matching owing to differences in the intensity due to slight detector tilt. The orientation distribution is evaluated at the location of the (110)-peak at  $q = 1.16 \text{ Å}^{-1}$  (thick dashed black line; note that the data at this  $q$ -value is only taken from one detector, *i.e.* WAXD-detector 1):



The raw intensity  $I(\chi)$  is fitted to a function of form:

$$I_{fit}(\chi) = A \cos(2(\chi - \chi_{tilt})) + B,$$

where  $\chi_{tilt}$  indicates the tilt angle (dashed blue line in figure). The order parameter  $S_\chi$  is calculated through:

$$S_\chi = \int_{-180^\circ}^{180^\circ} I_{fit}(\chi)(2 \cos^2(\chi - \chi_{tilt}) - 1) d\chi,$$

Where  $I_{fit}(\chi)$  initially is normalized according to:

$$1 = \int_{-180^\circ}^{180^\circ} I_{fit}(\chi) d\chi.$$

## Results:

The order parameter of all samples in the study are presented in the table below. Note that every sample was measured in two separate experiments (at different locations).

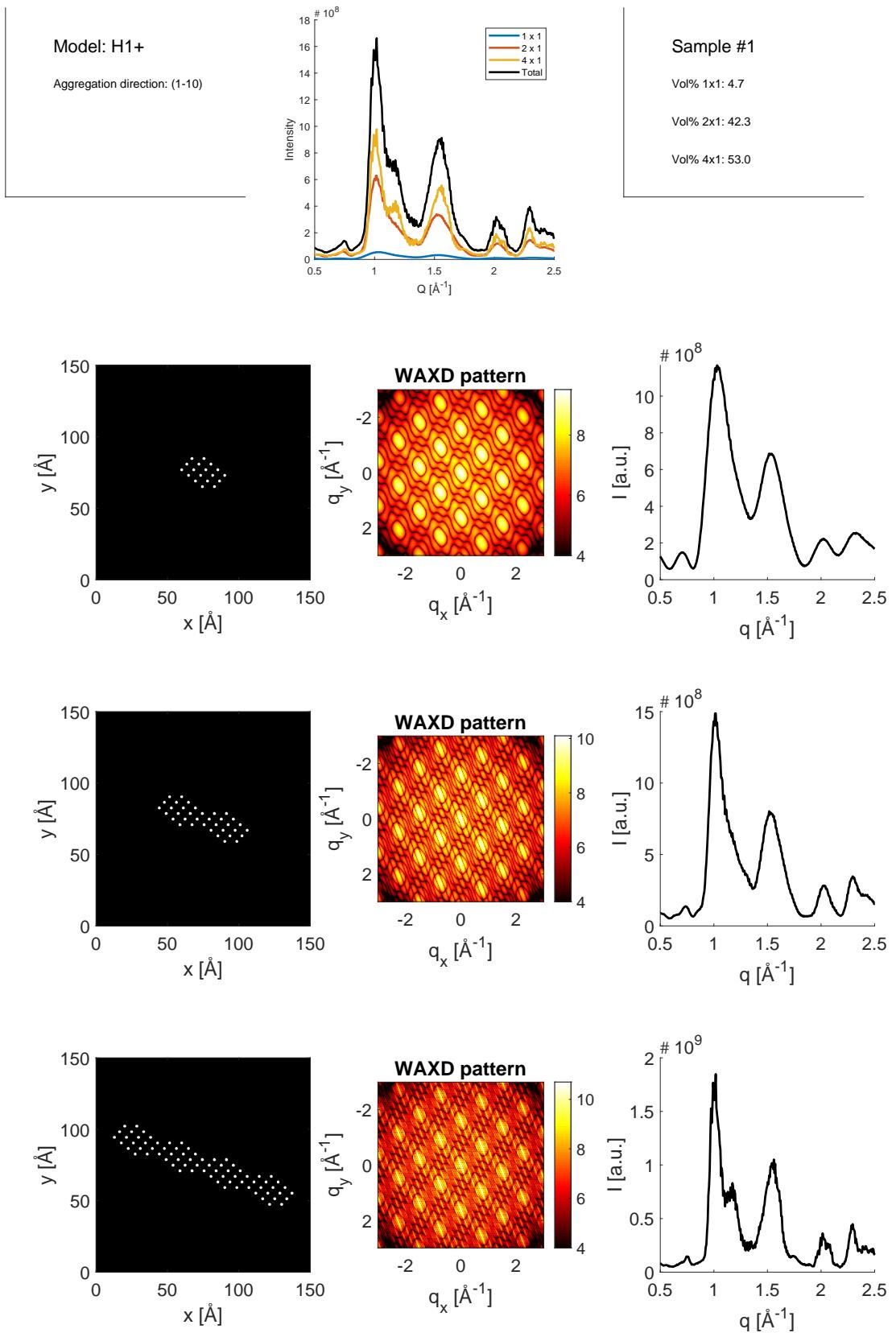
Sample #	$S_\chi$ (1 <sup>st</sup> exp.)	$S_\chi$ (2 <sup>nd</sup> exp.)
1	0.023	0.014
2	0.029	0.022
3	0.008	0.016
4	0.016	0.042
5	0.038	0.020
6	0.007	0.009
7	0.002	0.039
8	0.027	0.024
9	0.014	0.016
10	0.006	0.011
11	0.018	0.051
12	0.016	0.029
13	0.025	0.025
14	0.008	0.046
15	0.015	0.015
16	0.032	0.037
17	0.012	0.018
18	0.004	0.008

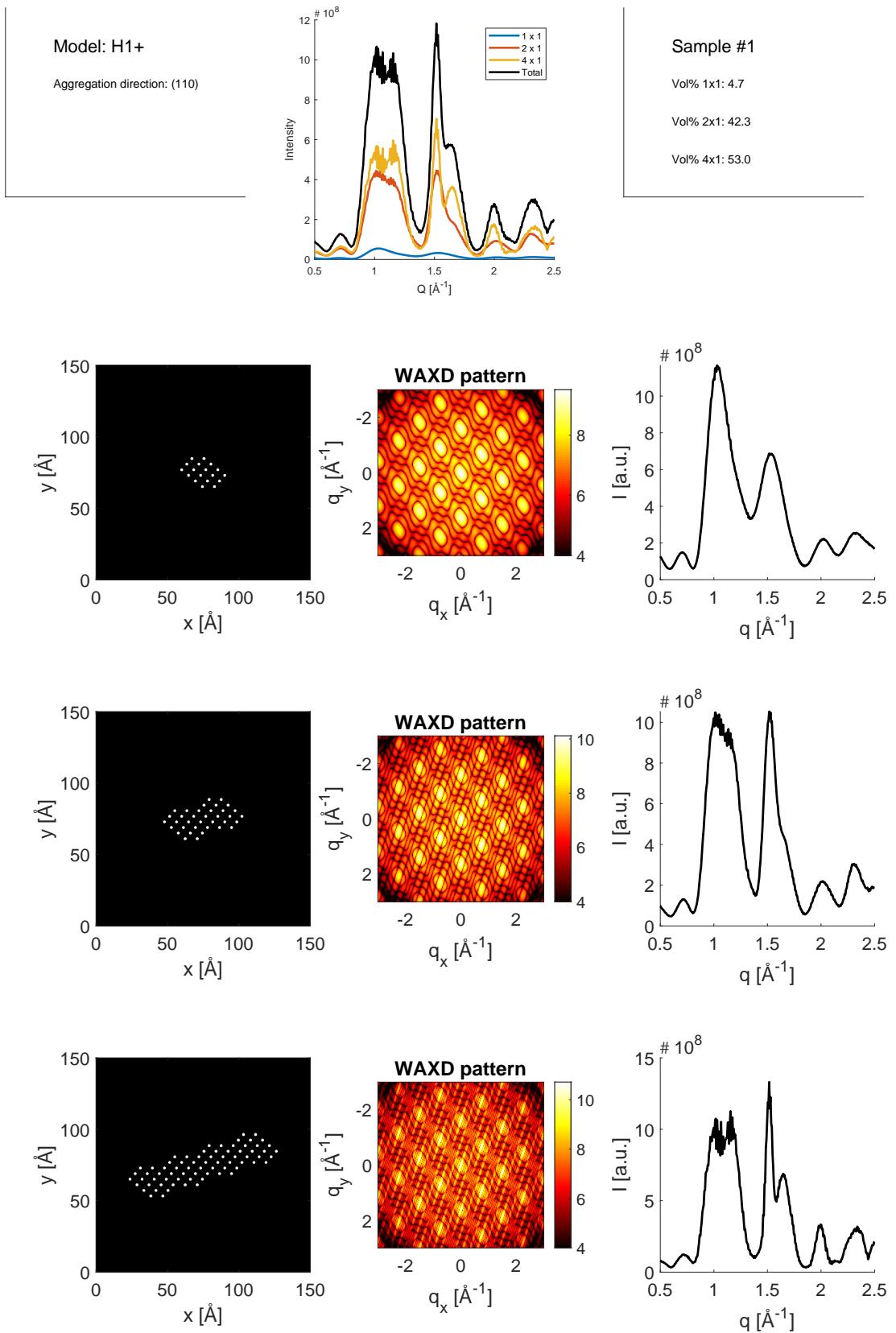
Since all the samples have an order parameter that fulfill  $S_\chi \ll 0.1$ , we can safely assume the samples to be isotropic.

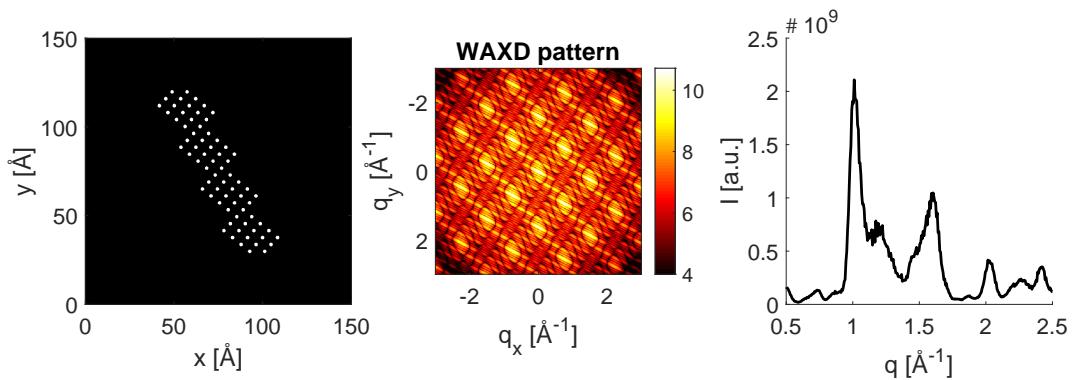
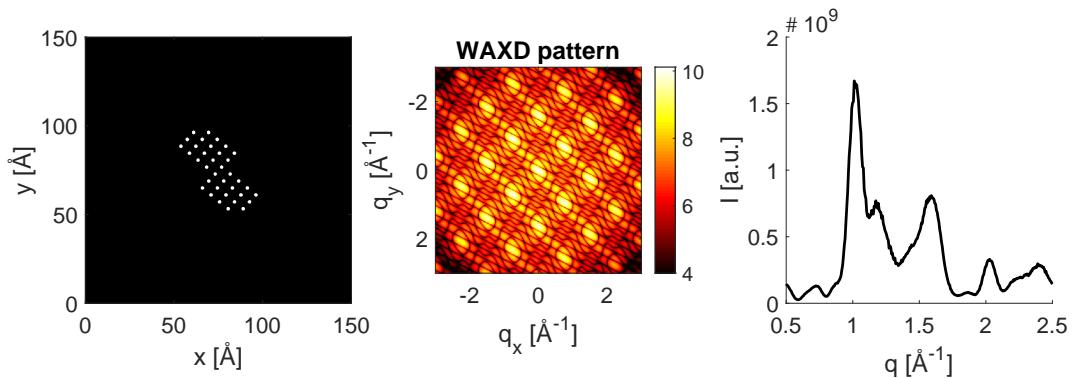
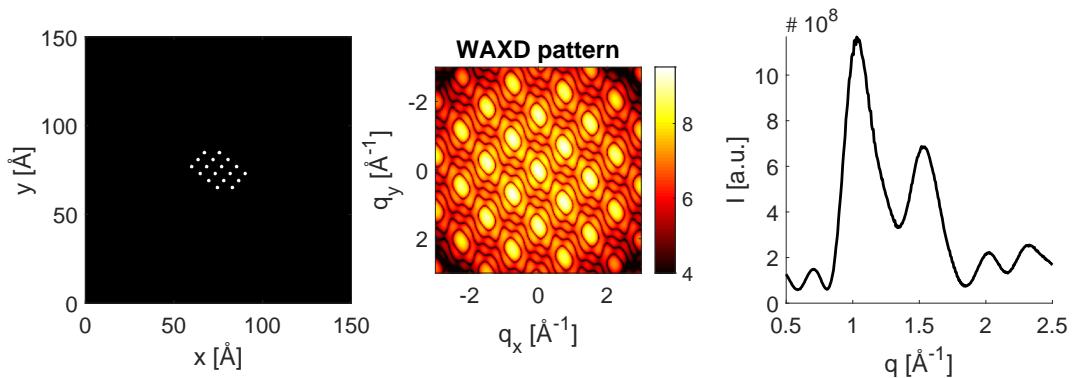
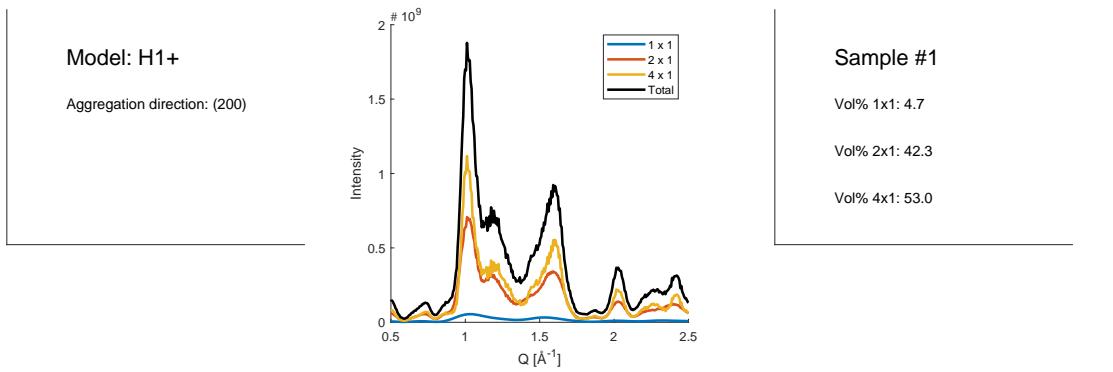
**WAXD simulations: Results**

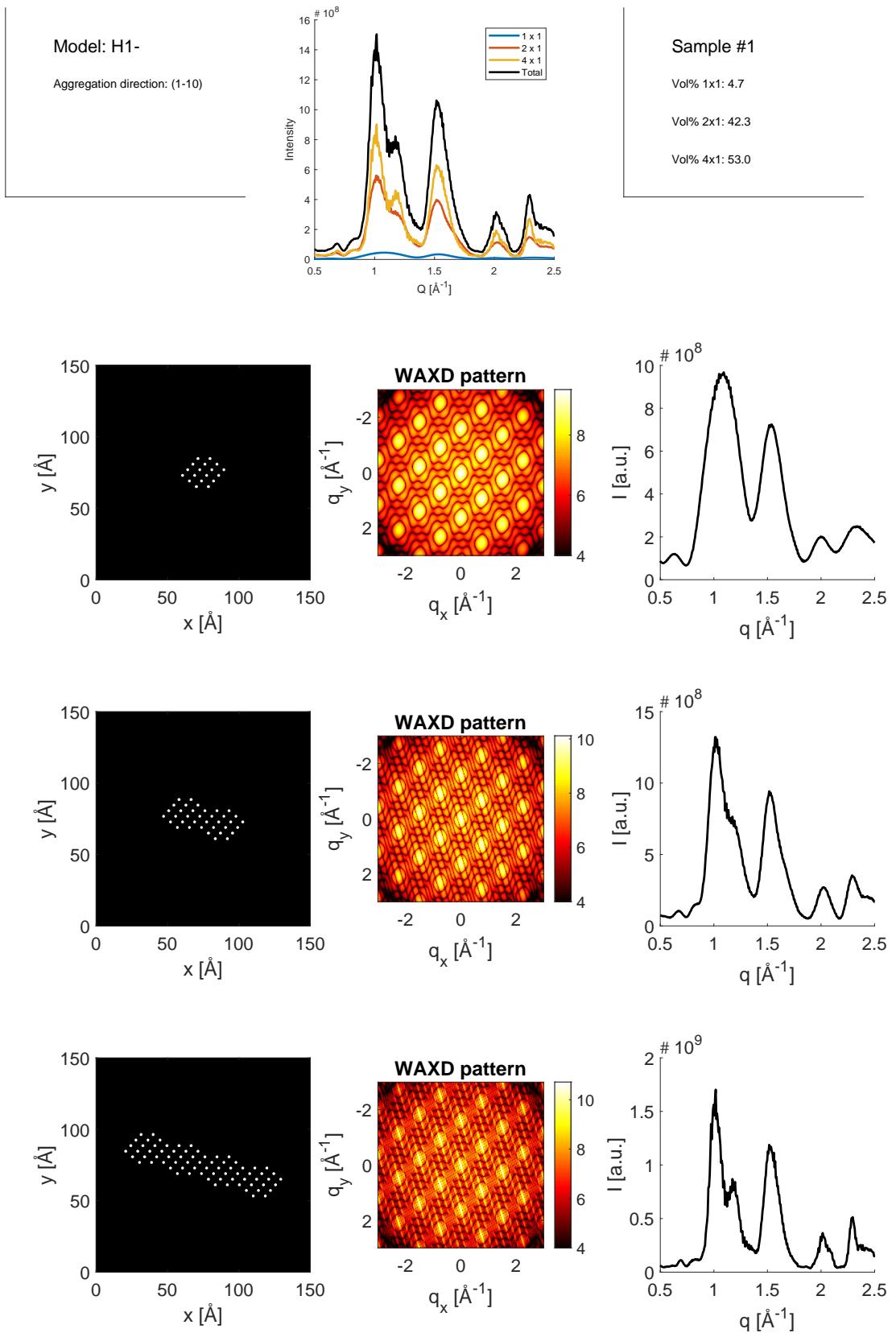
**Form factor of a CNF chain with semi-axes**

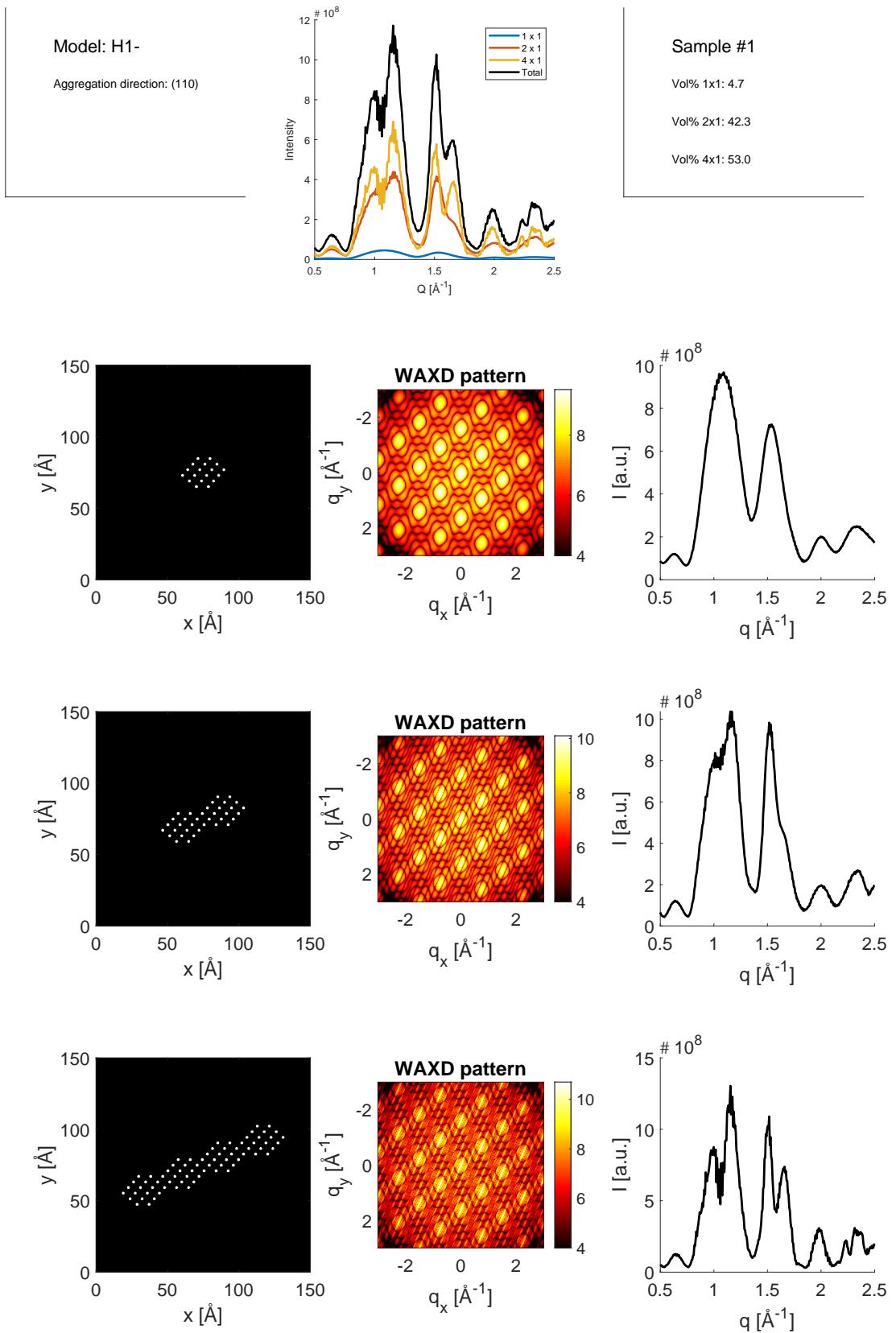
**1 Å x 1 Å**

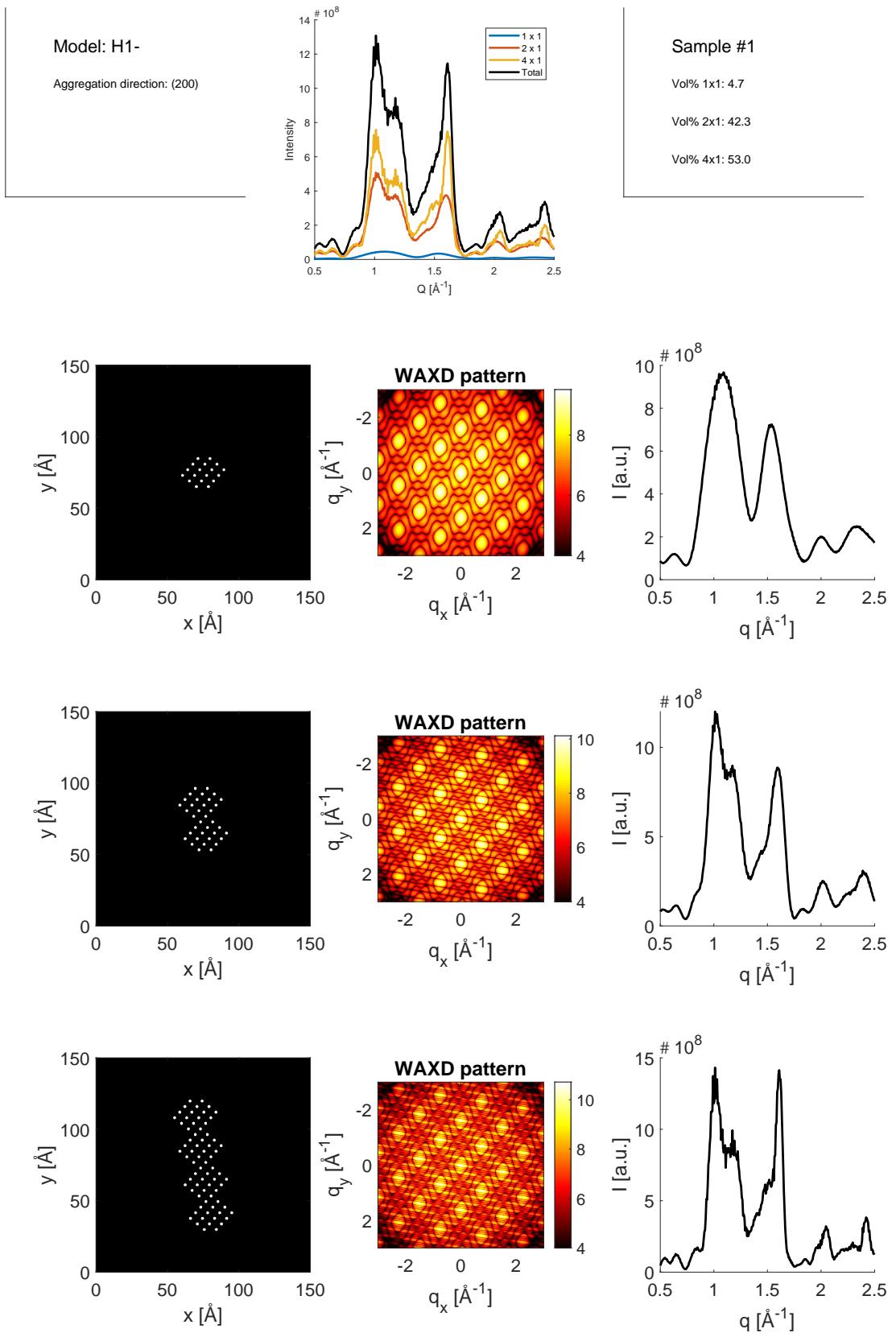


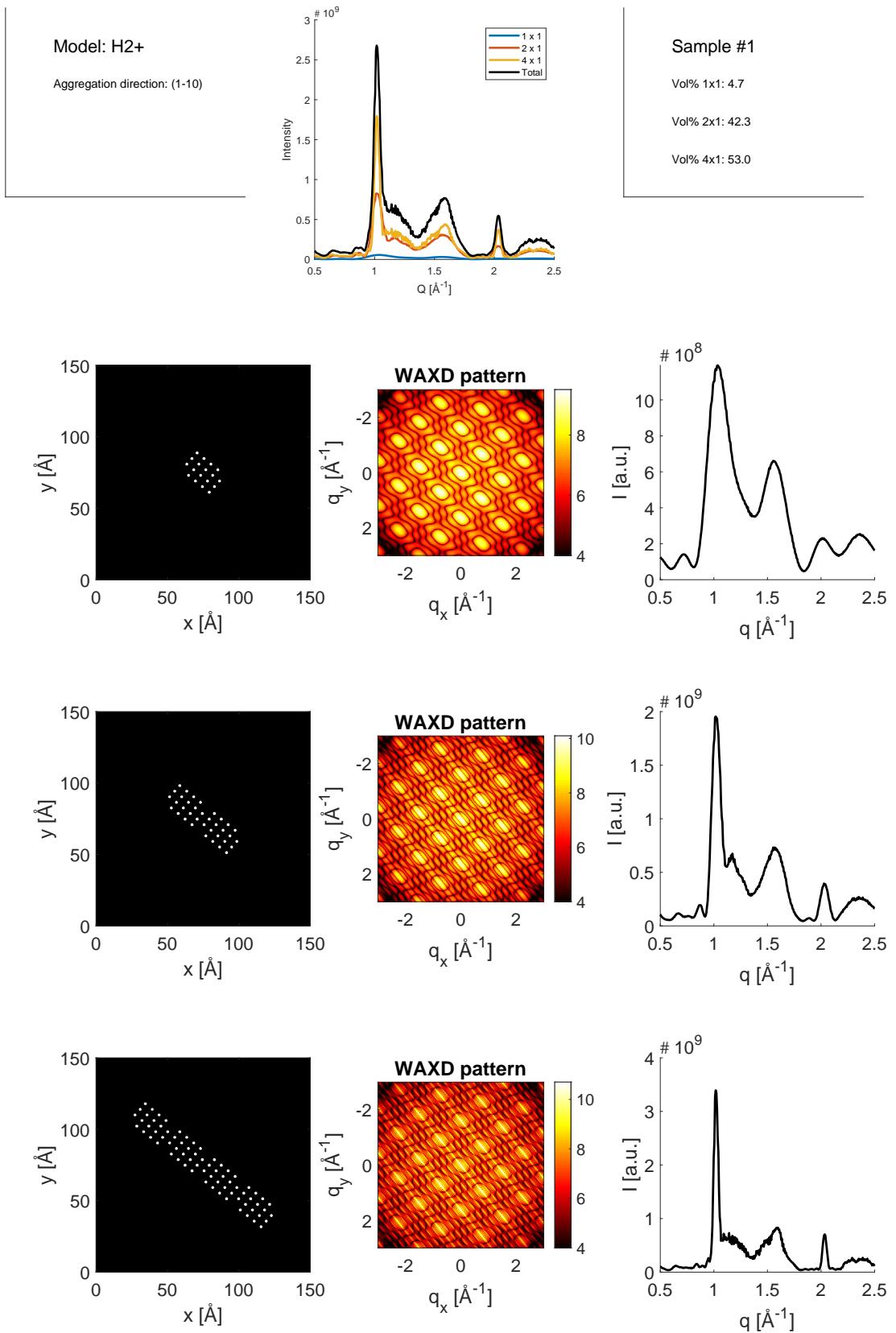


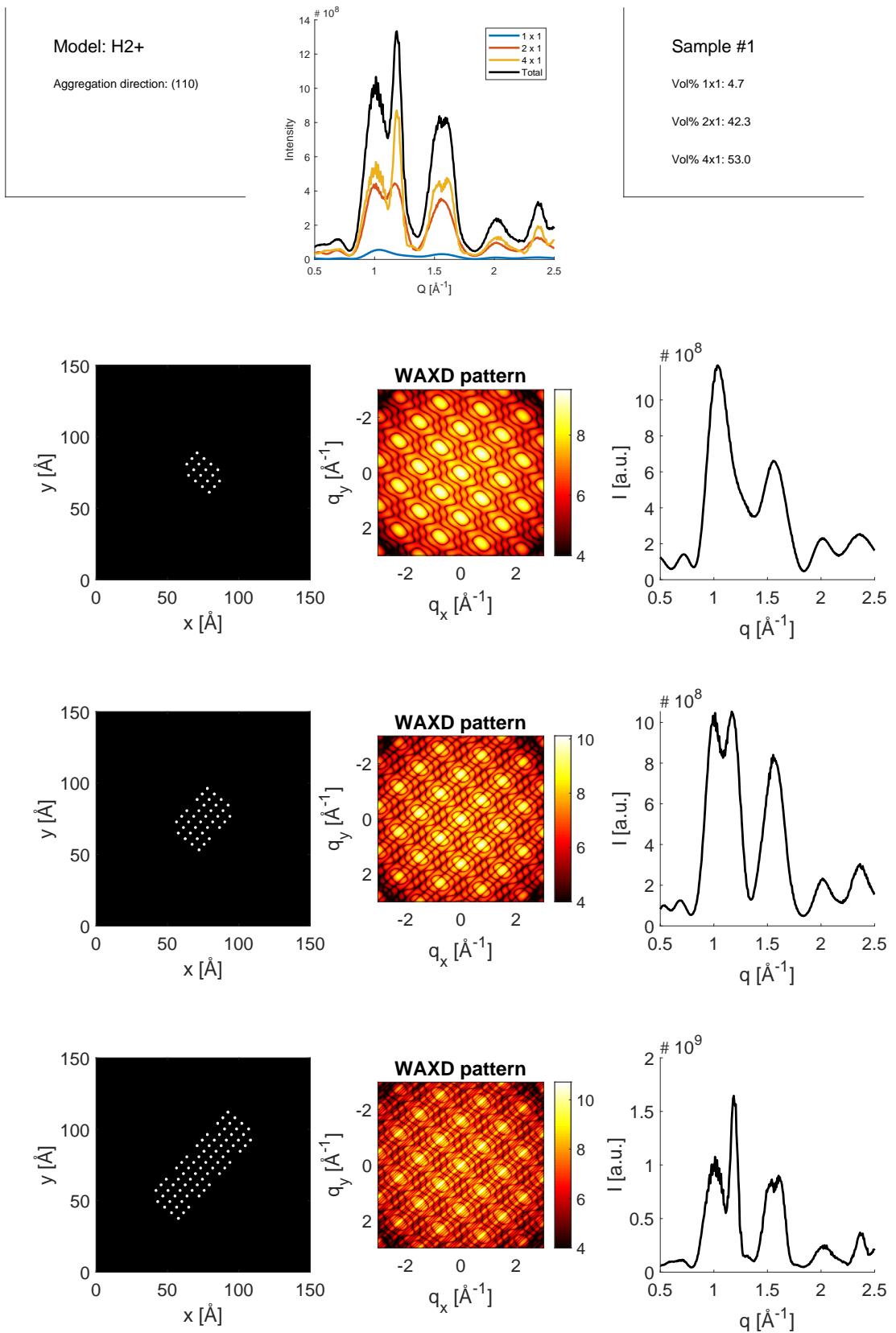


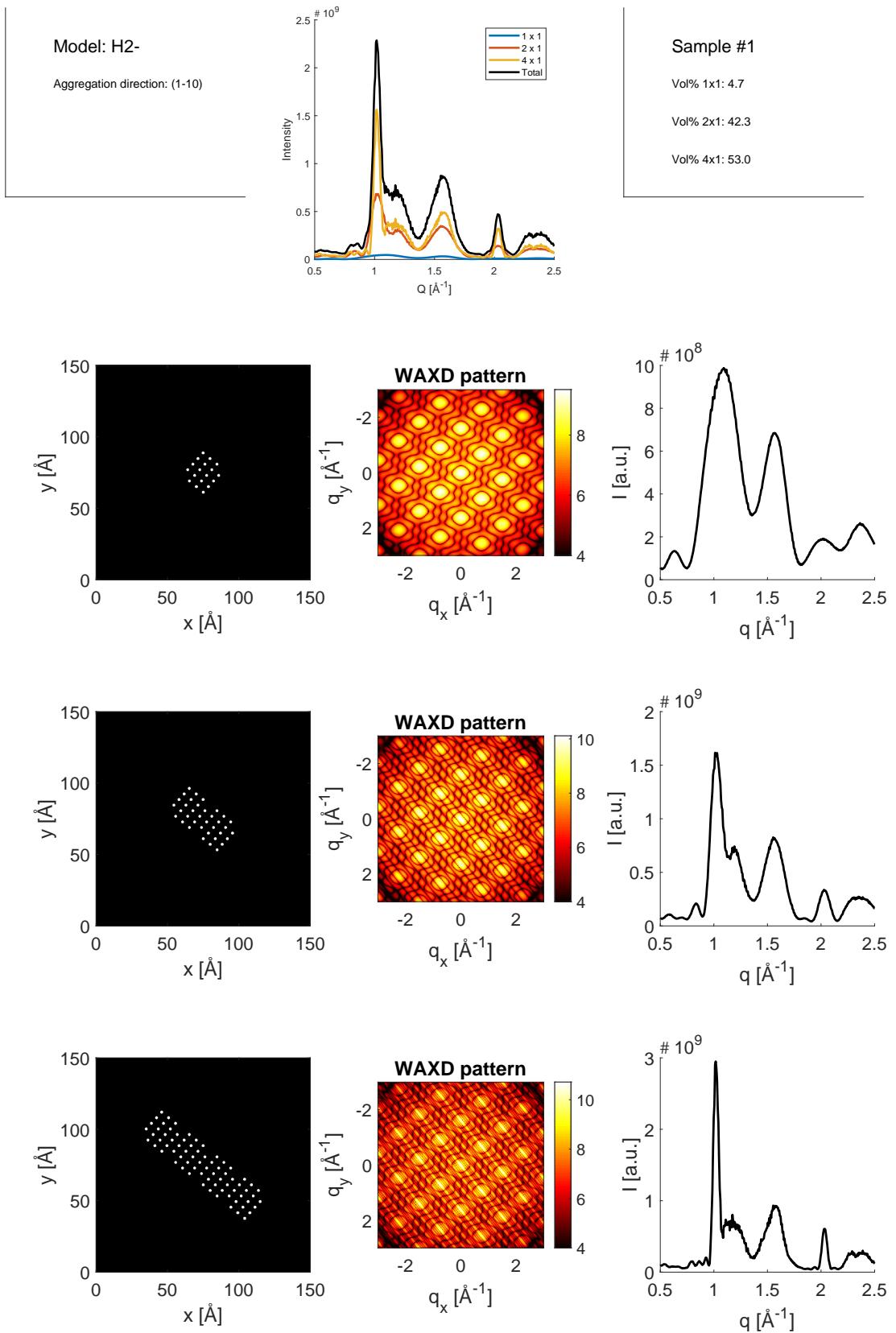


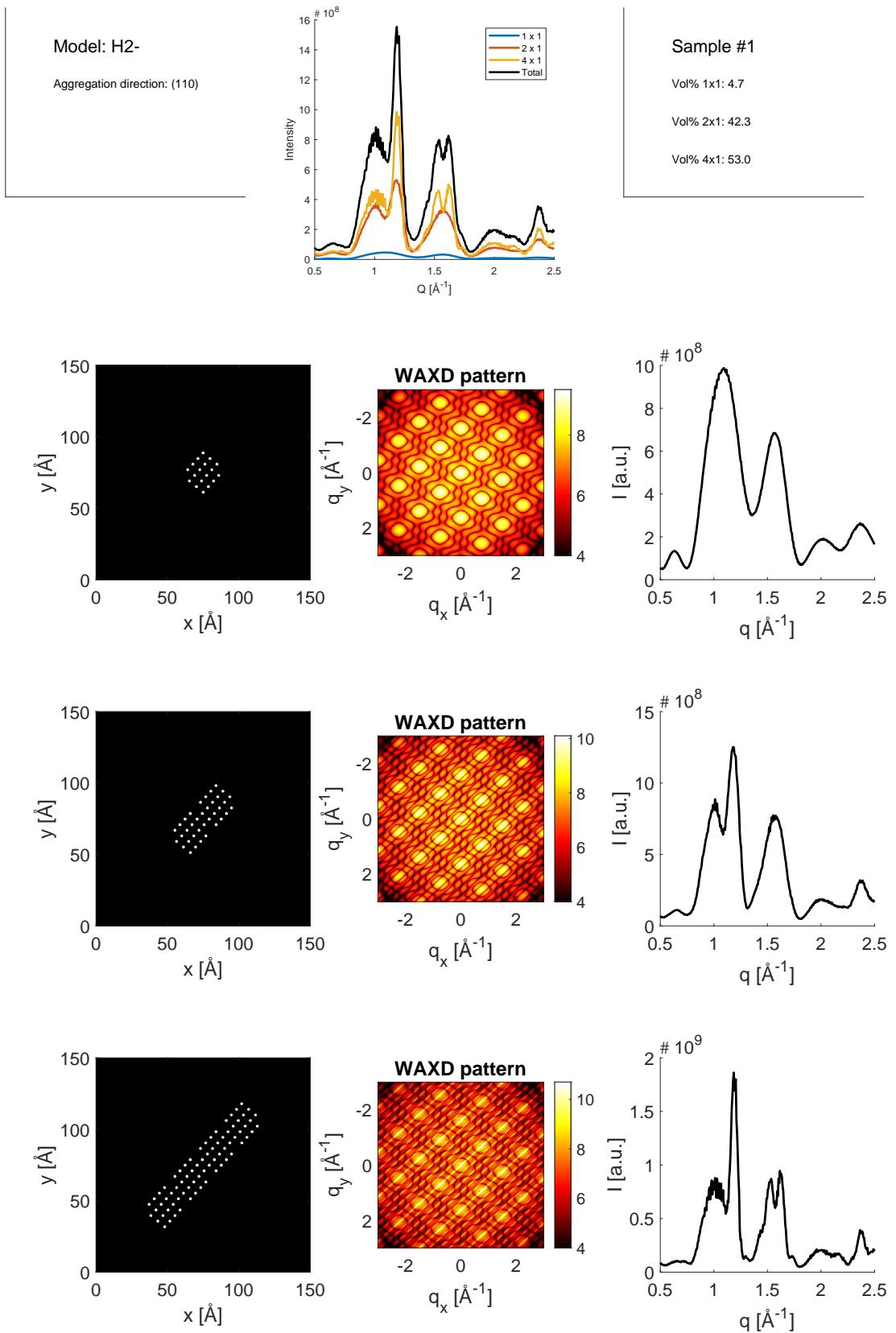


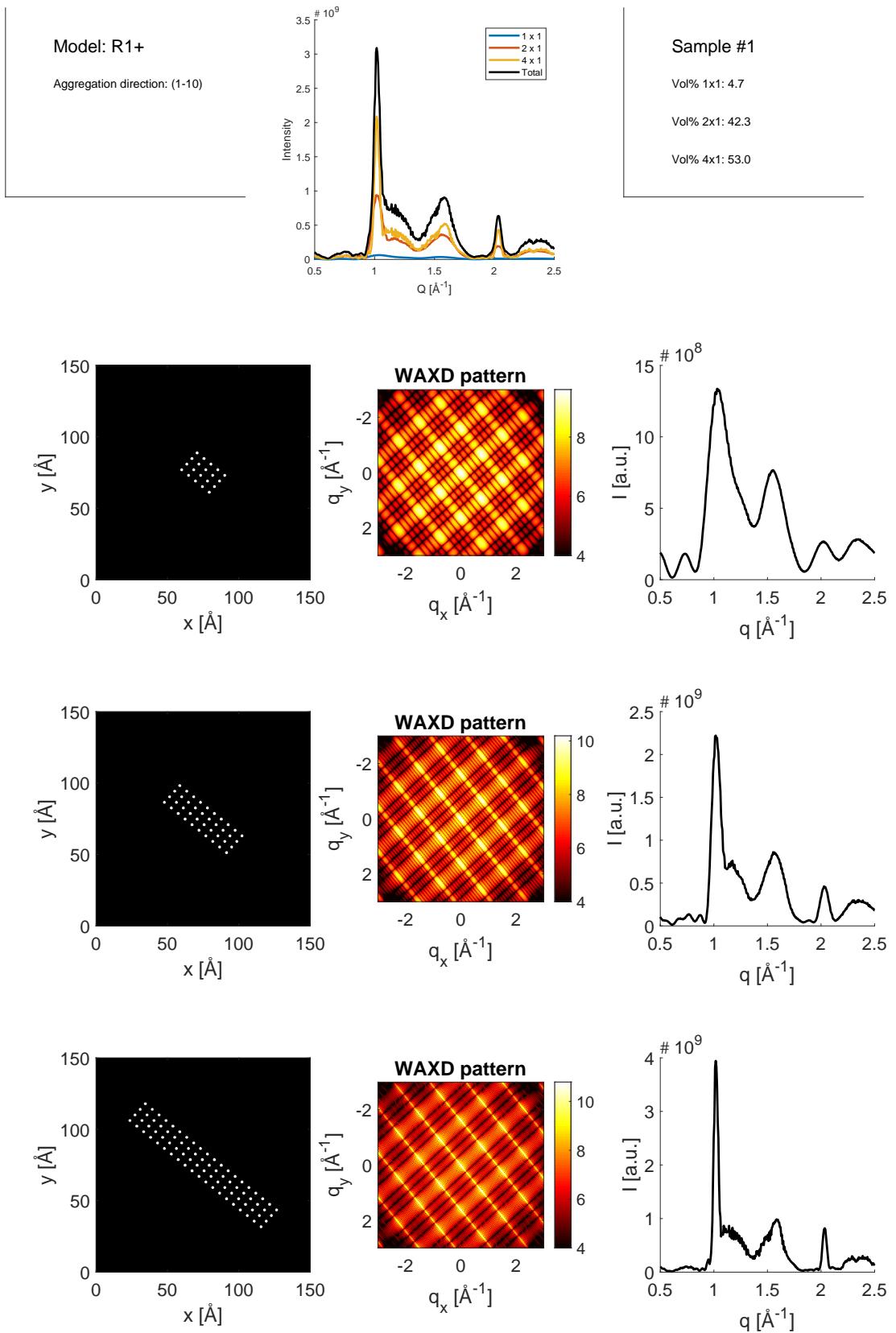


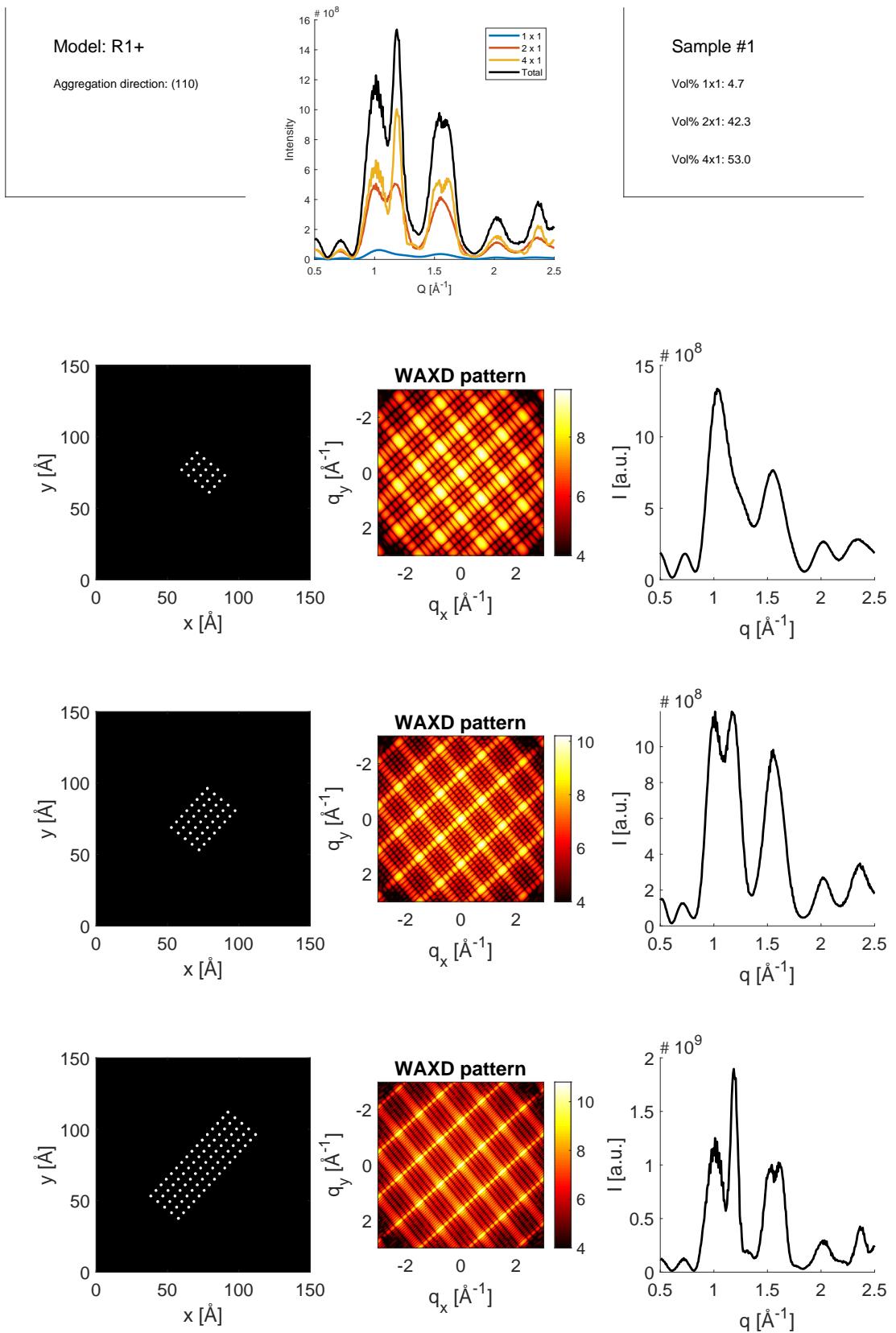


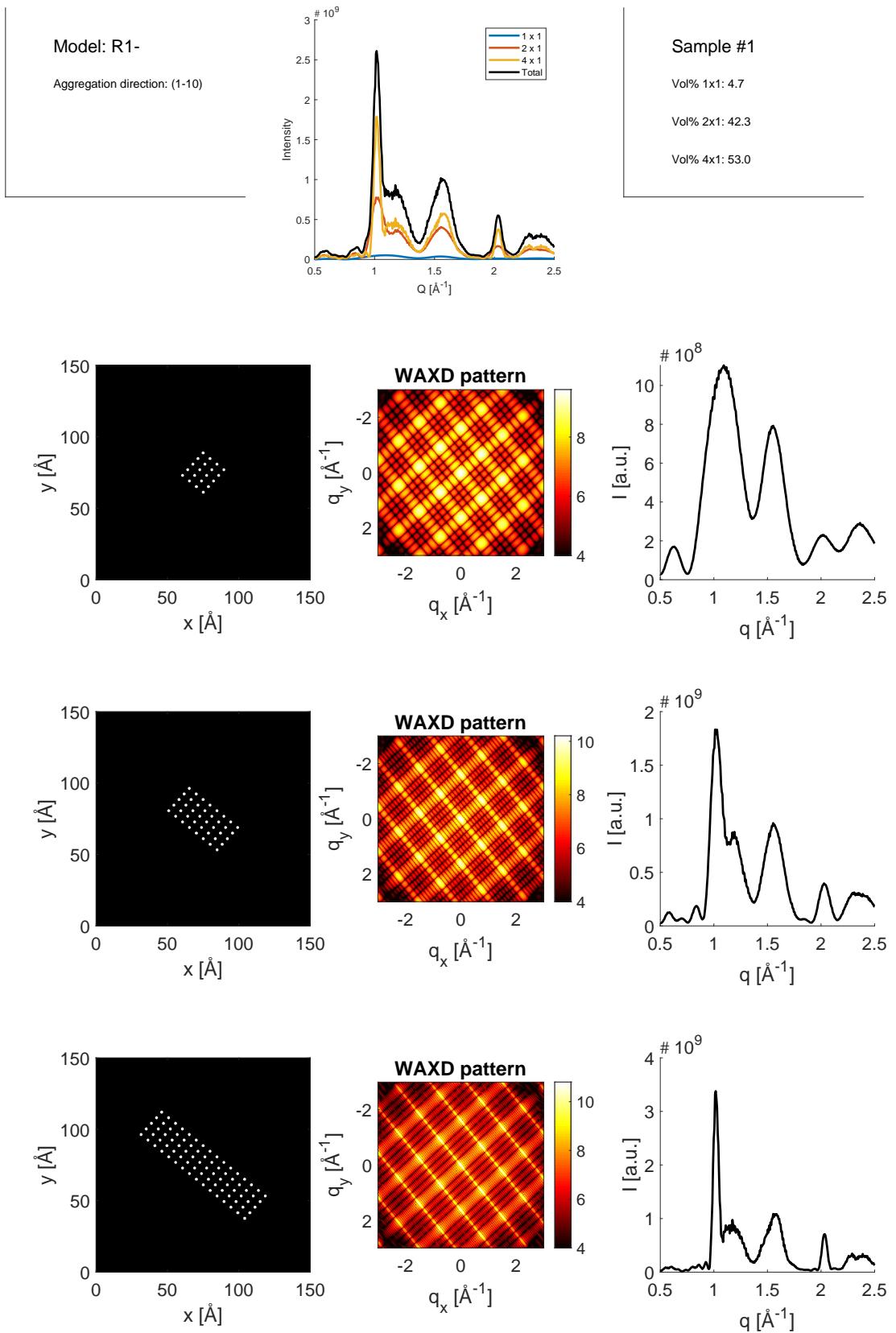


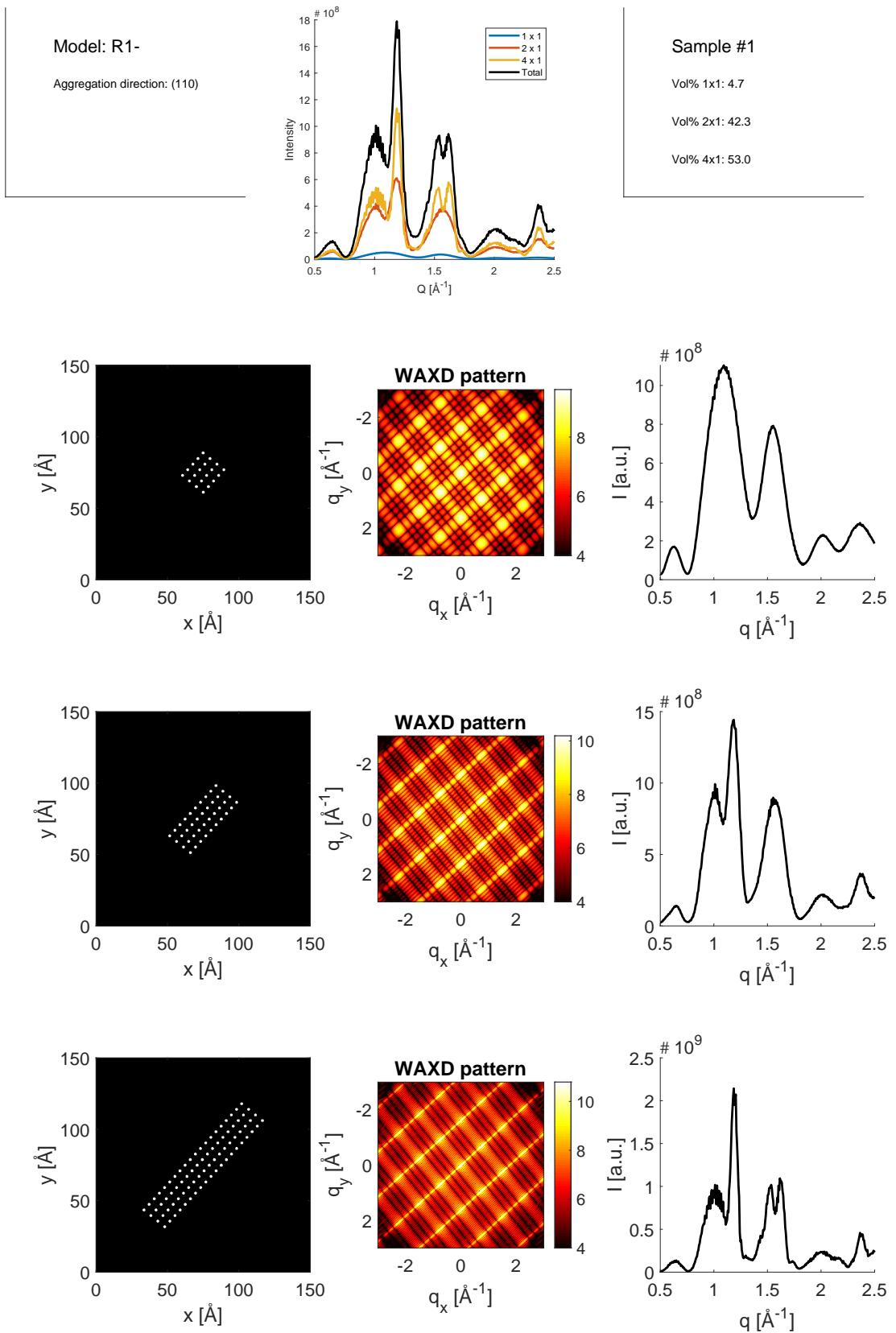


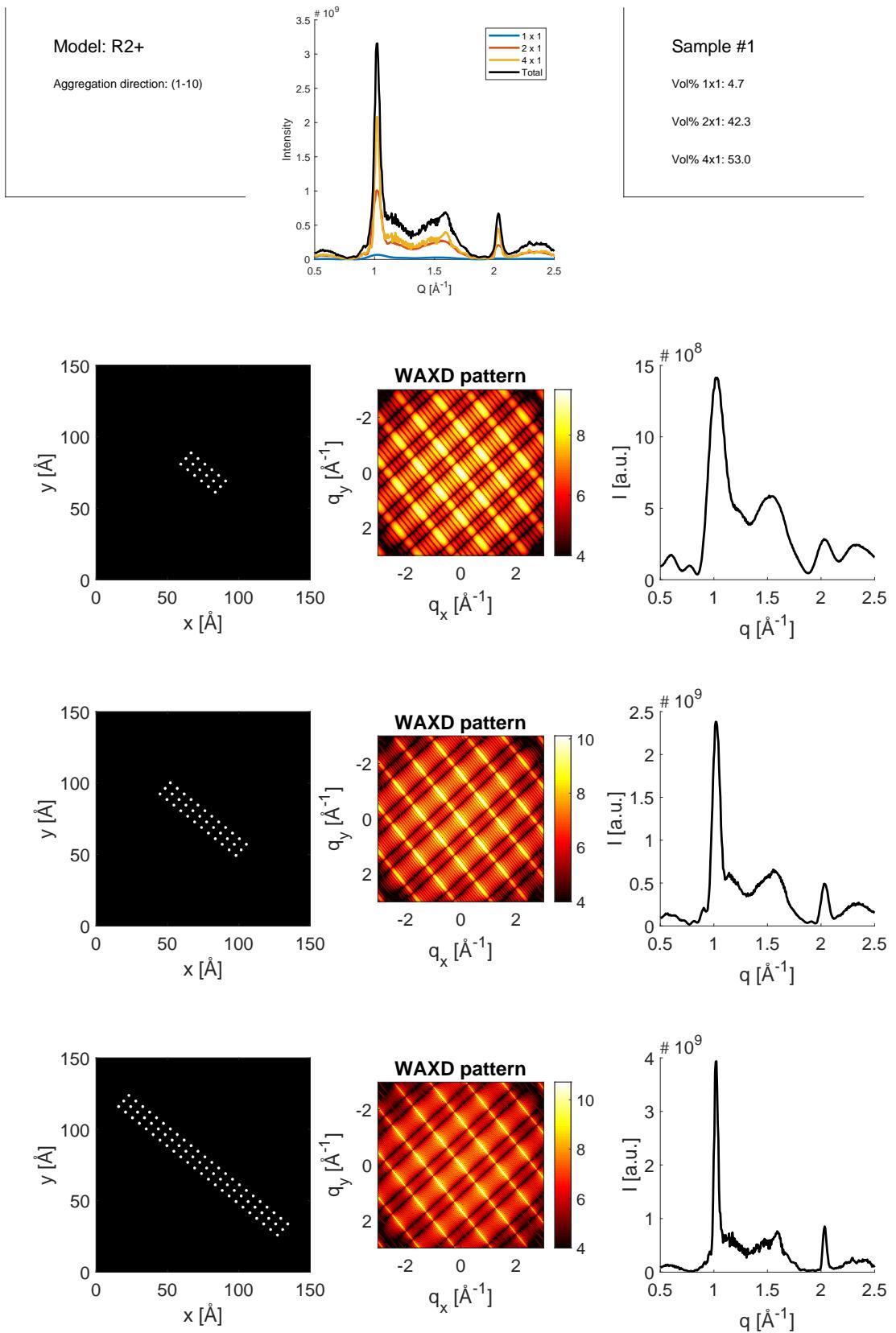


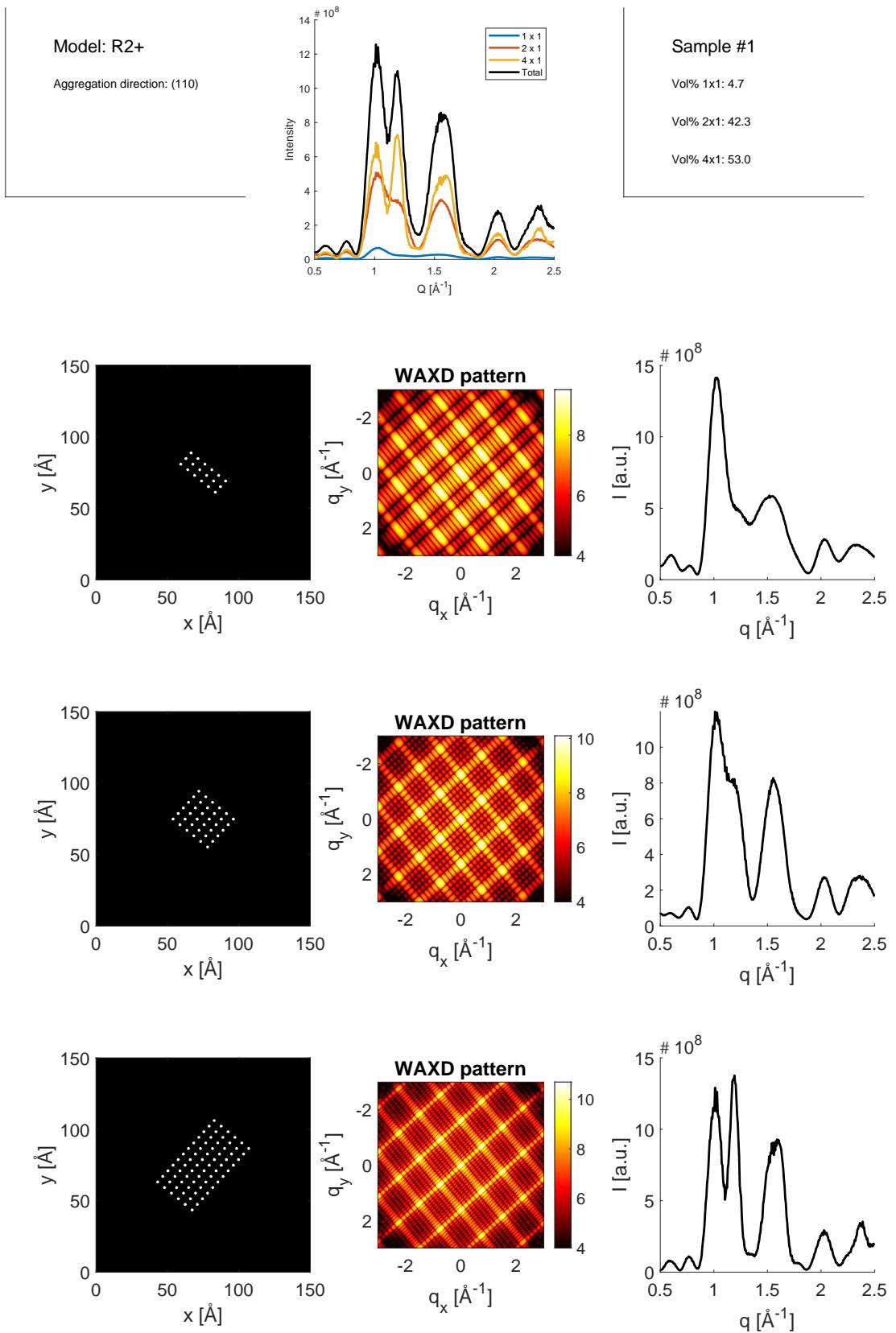


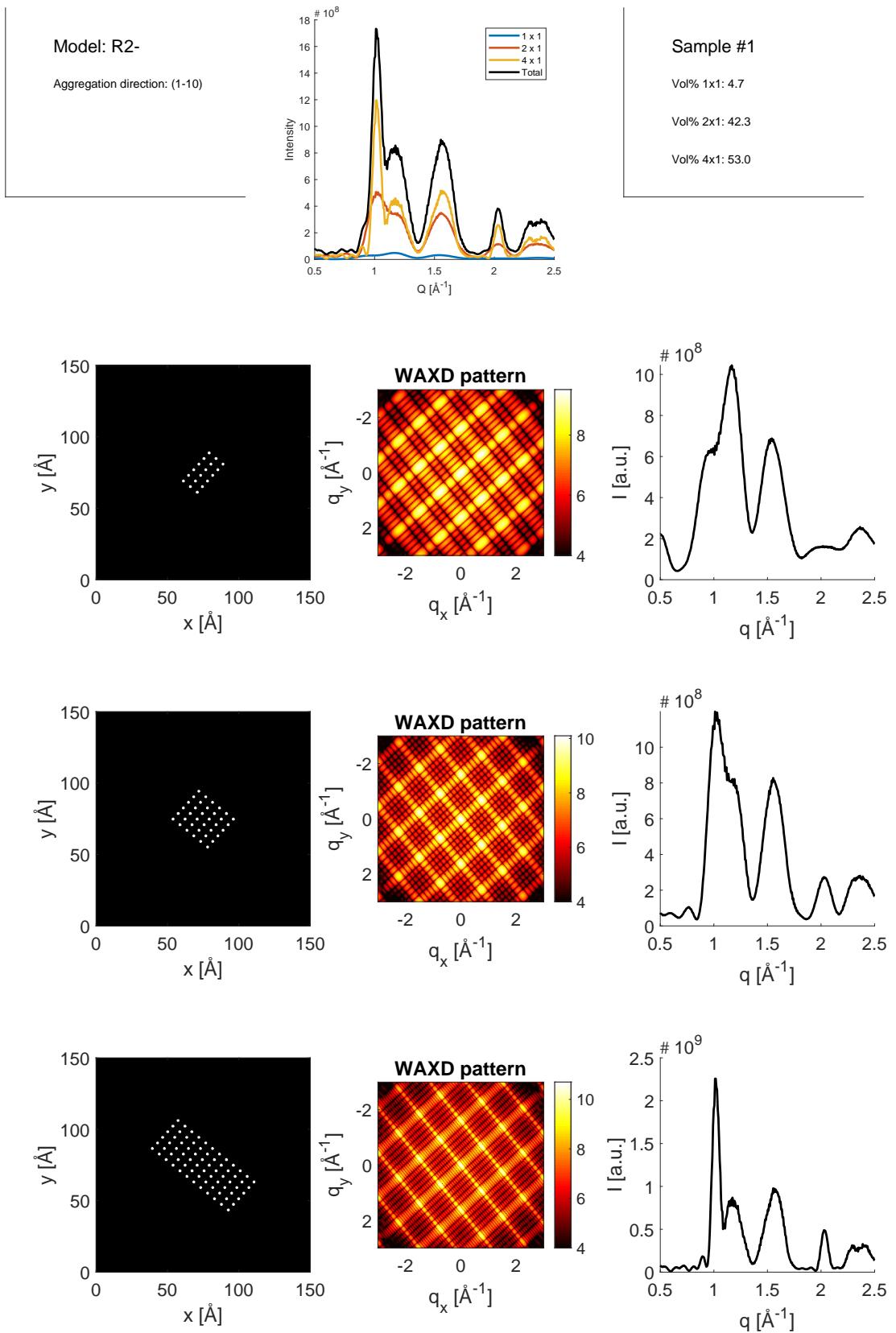


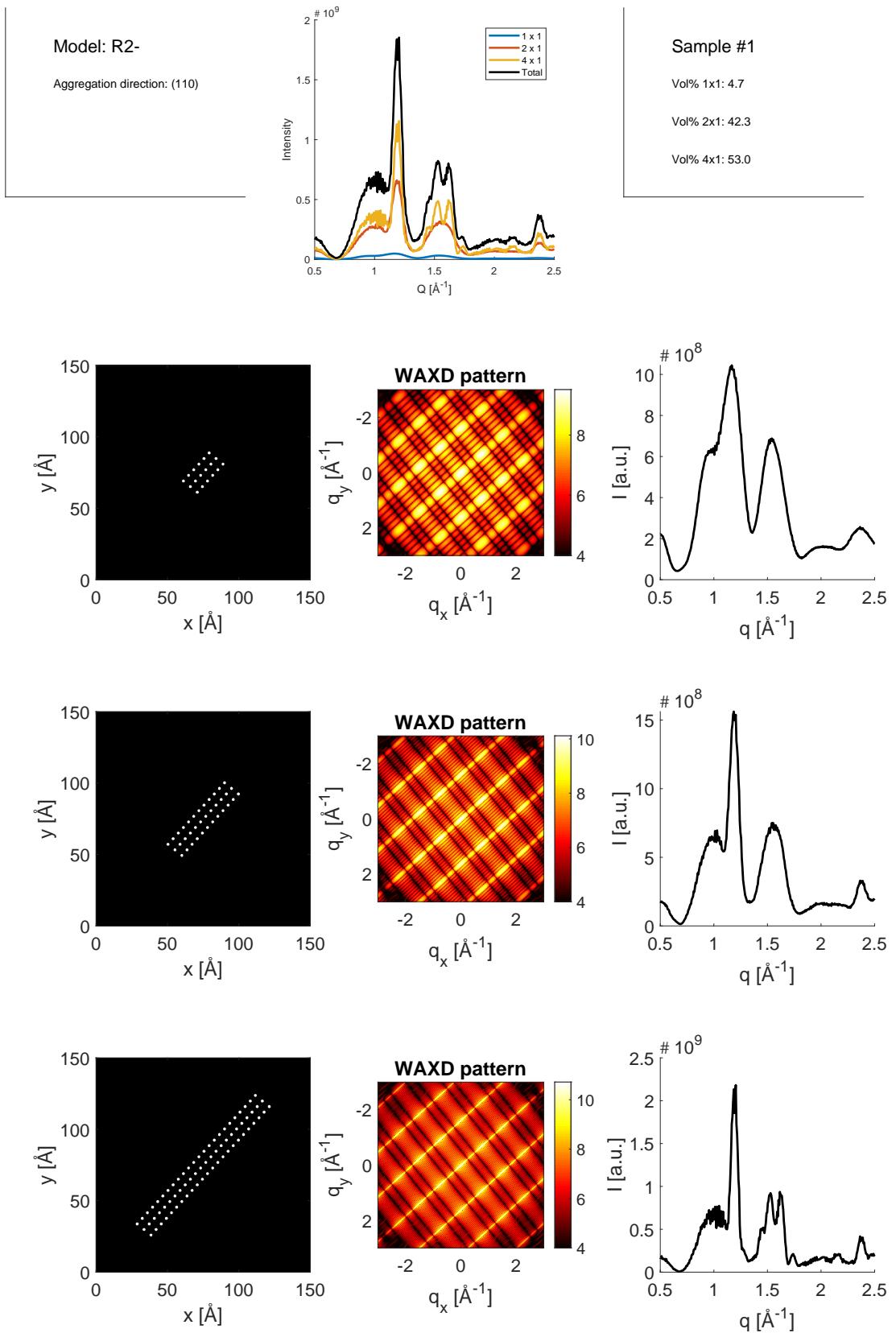


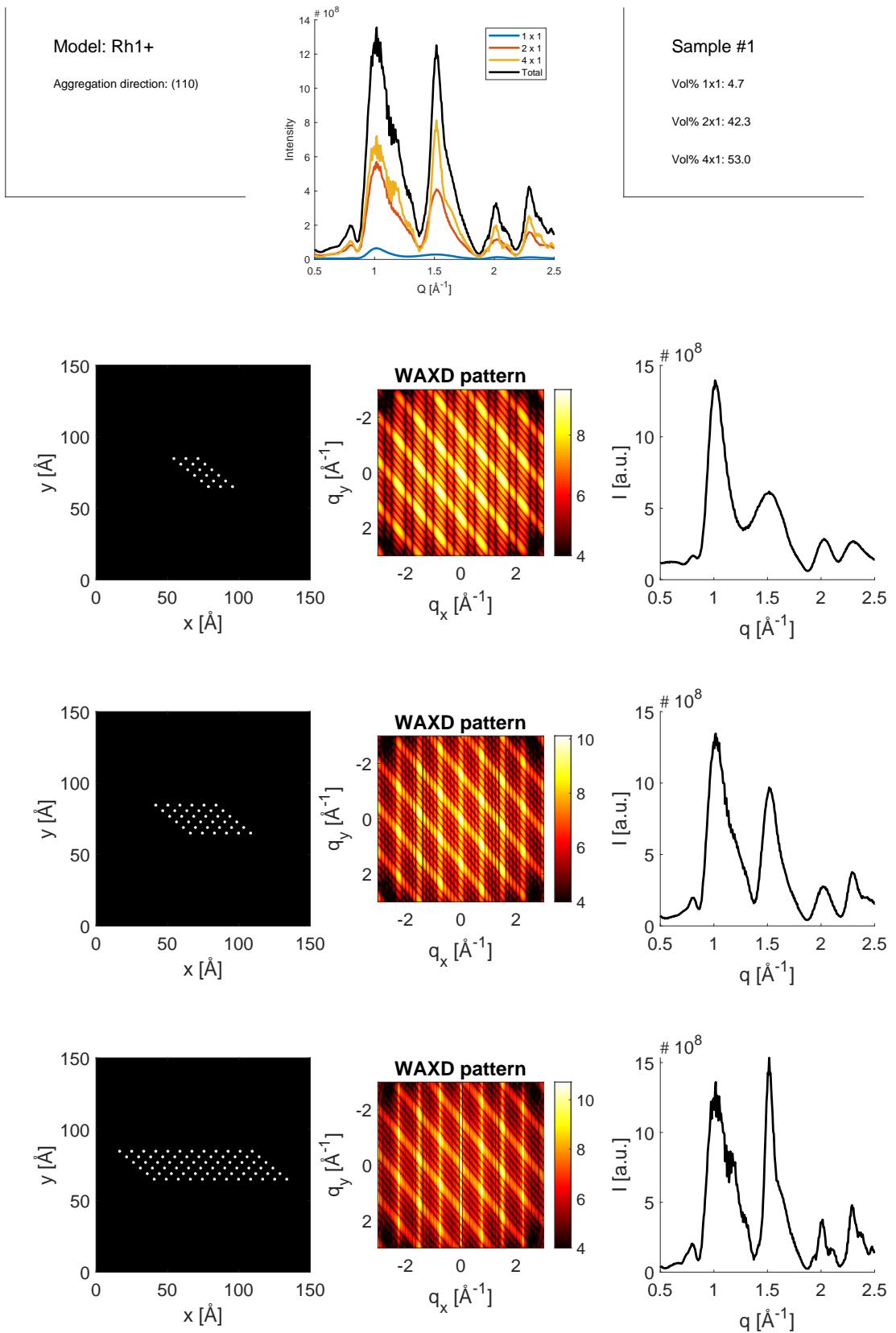


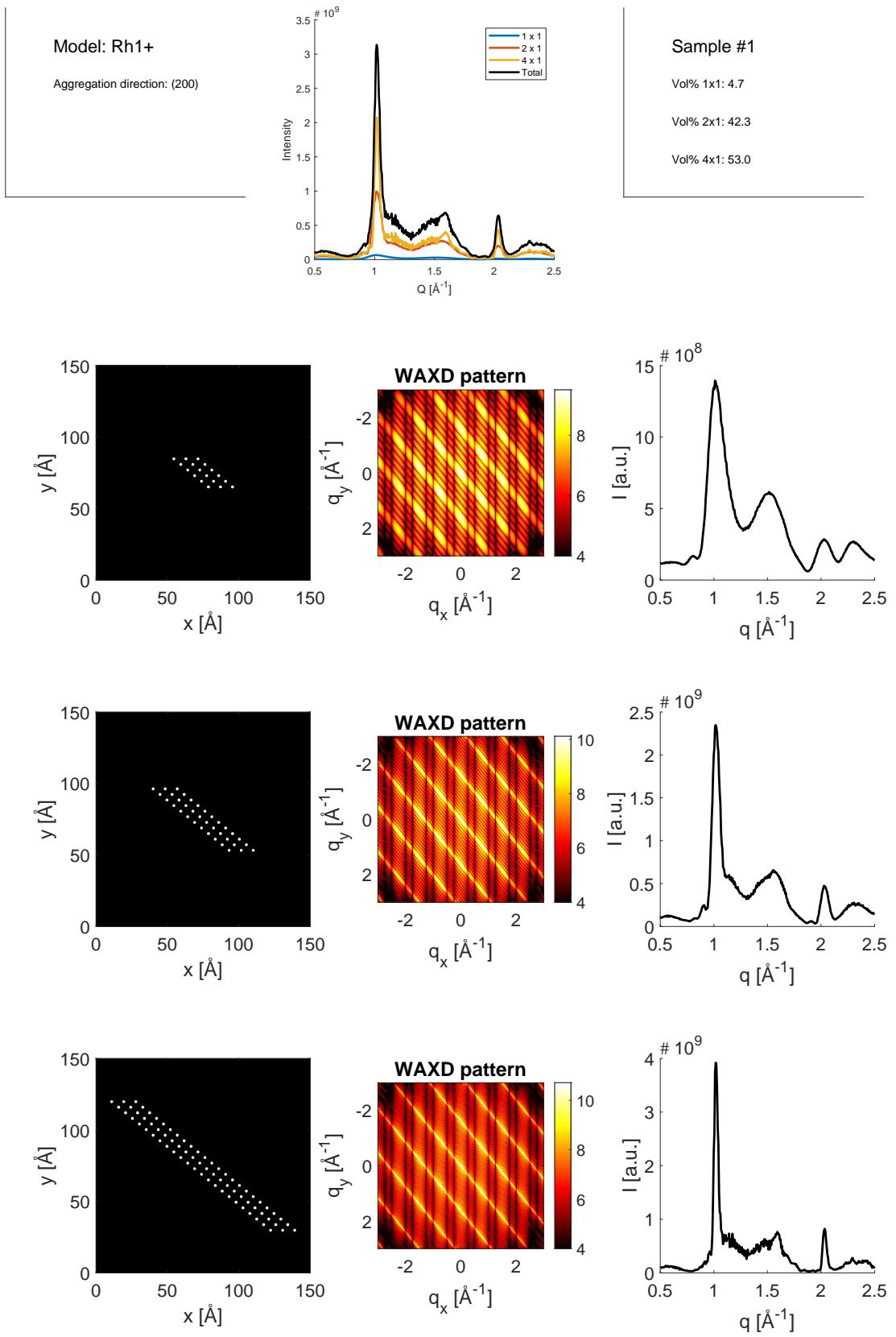


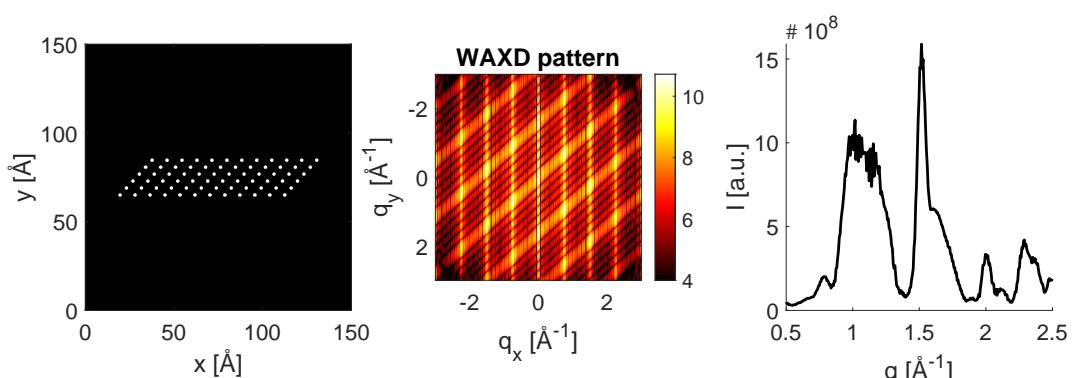
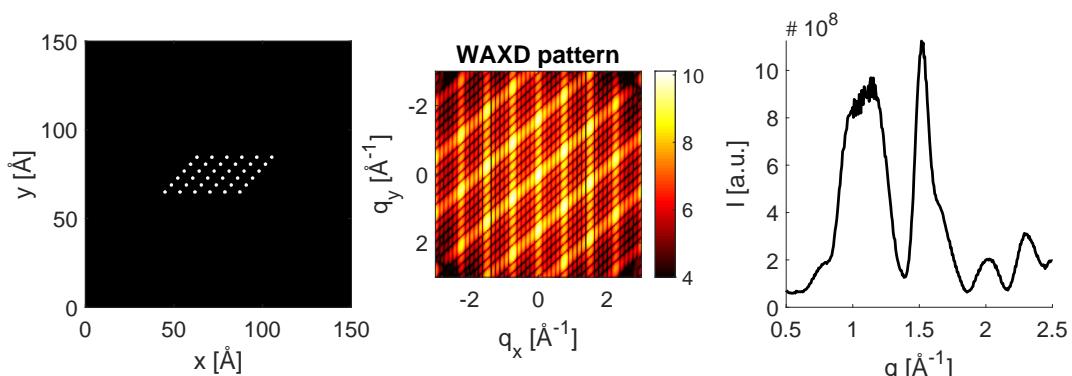
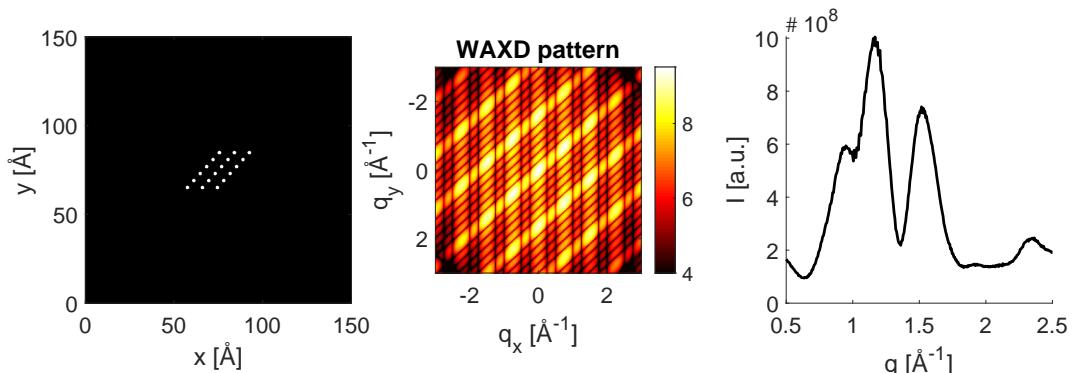
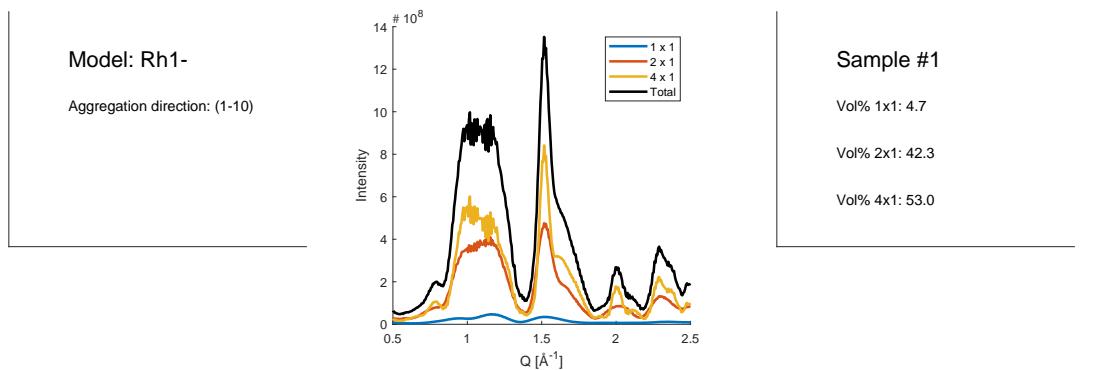


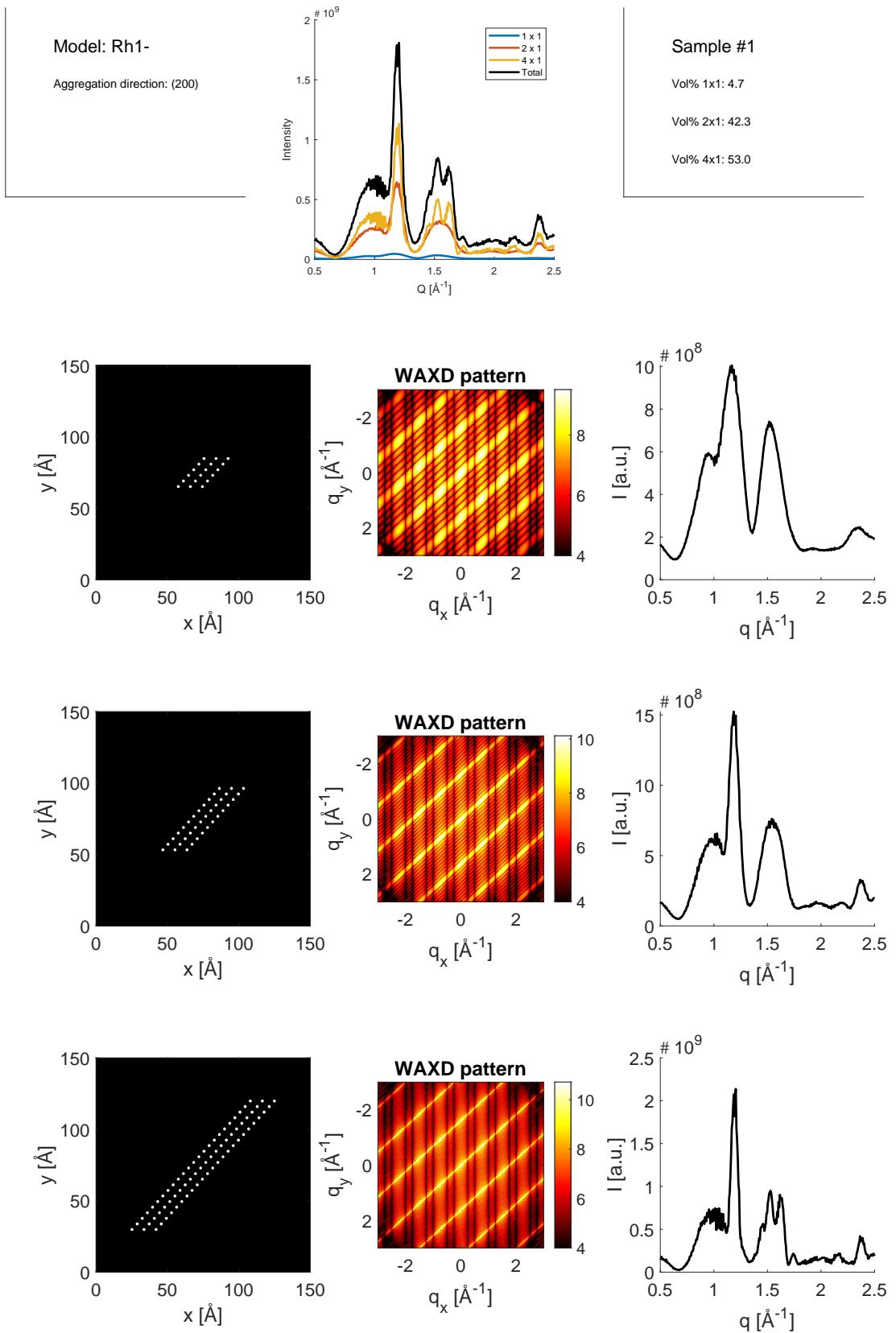


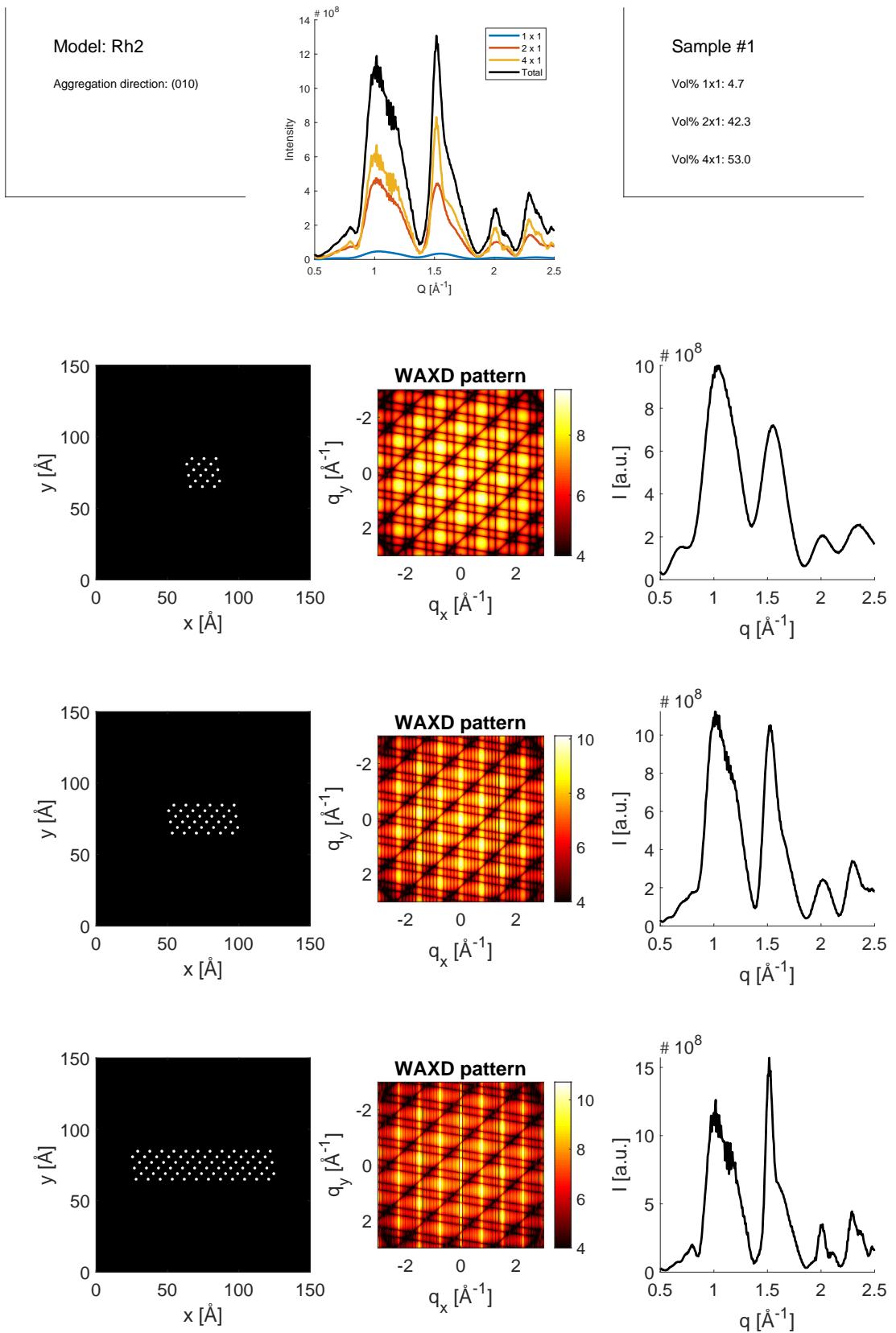


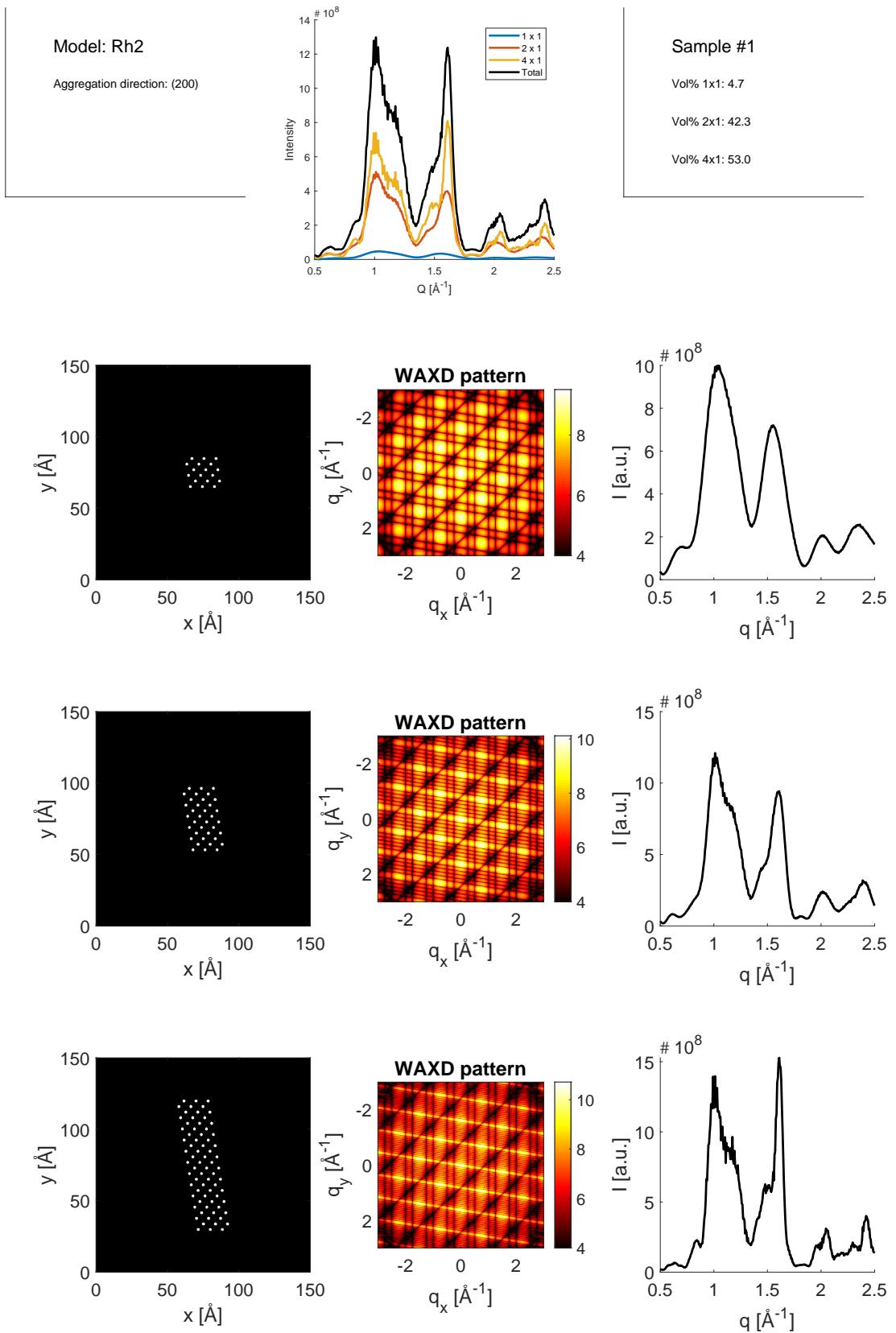


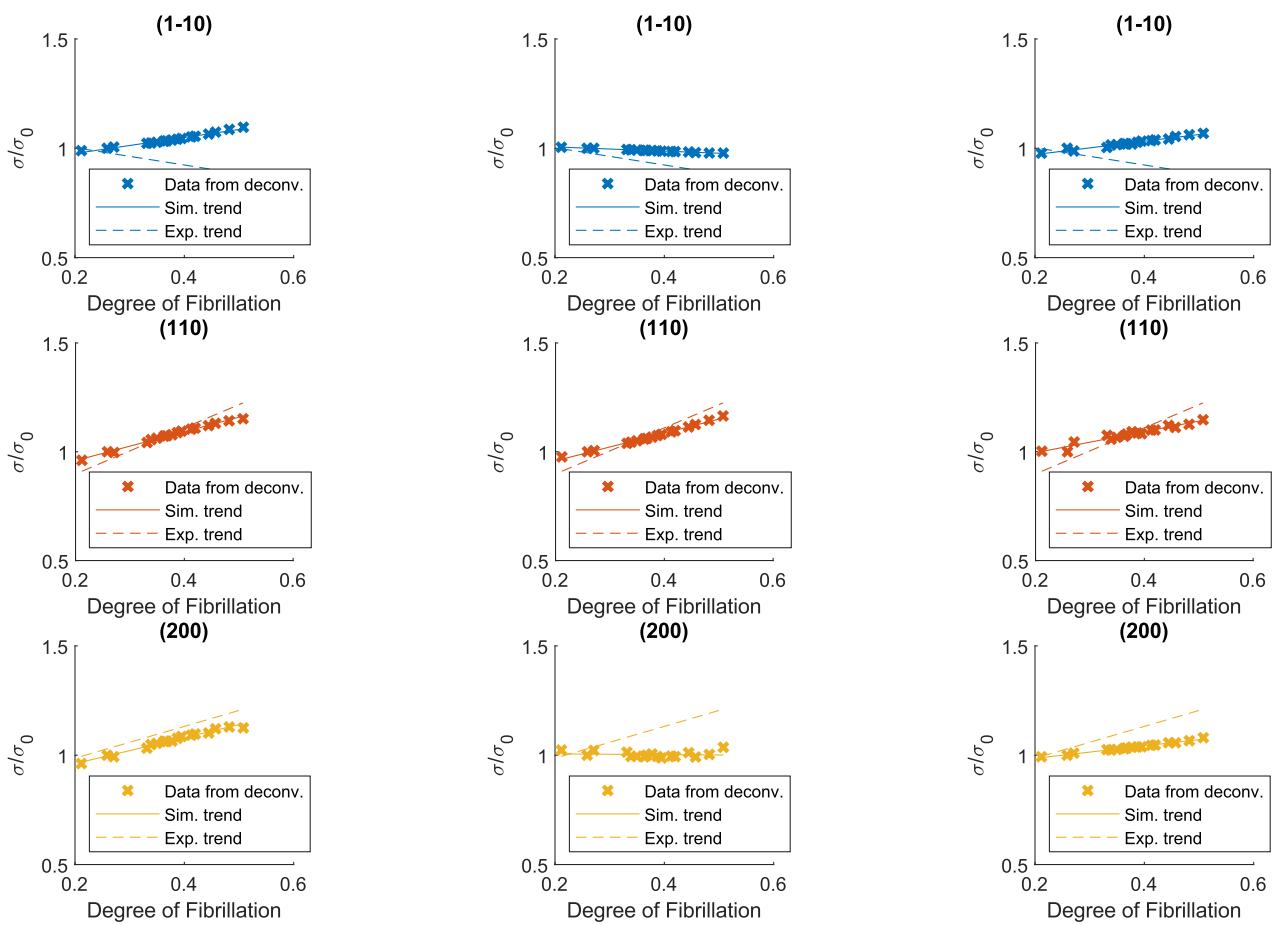
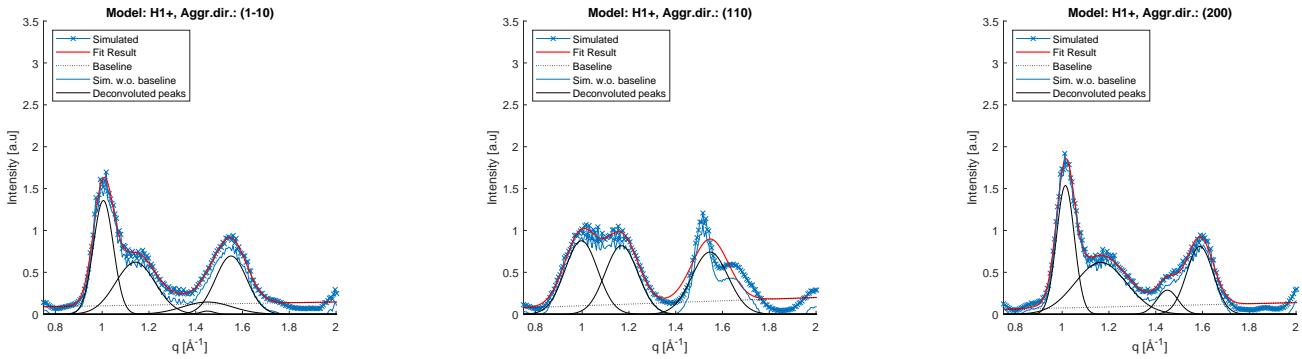


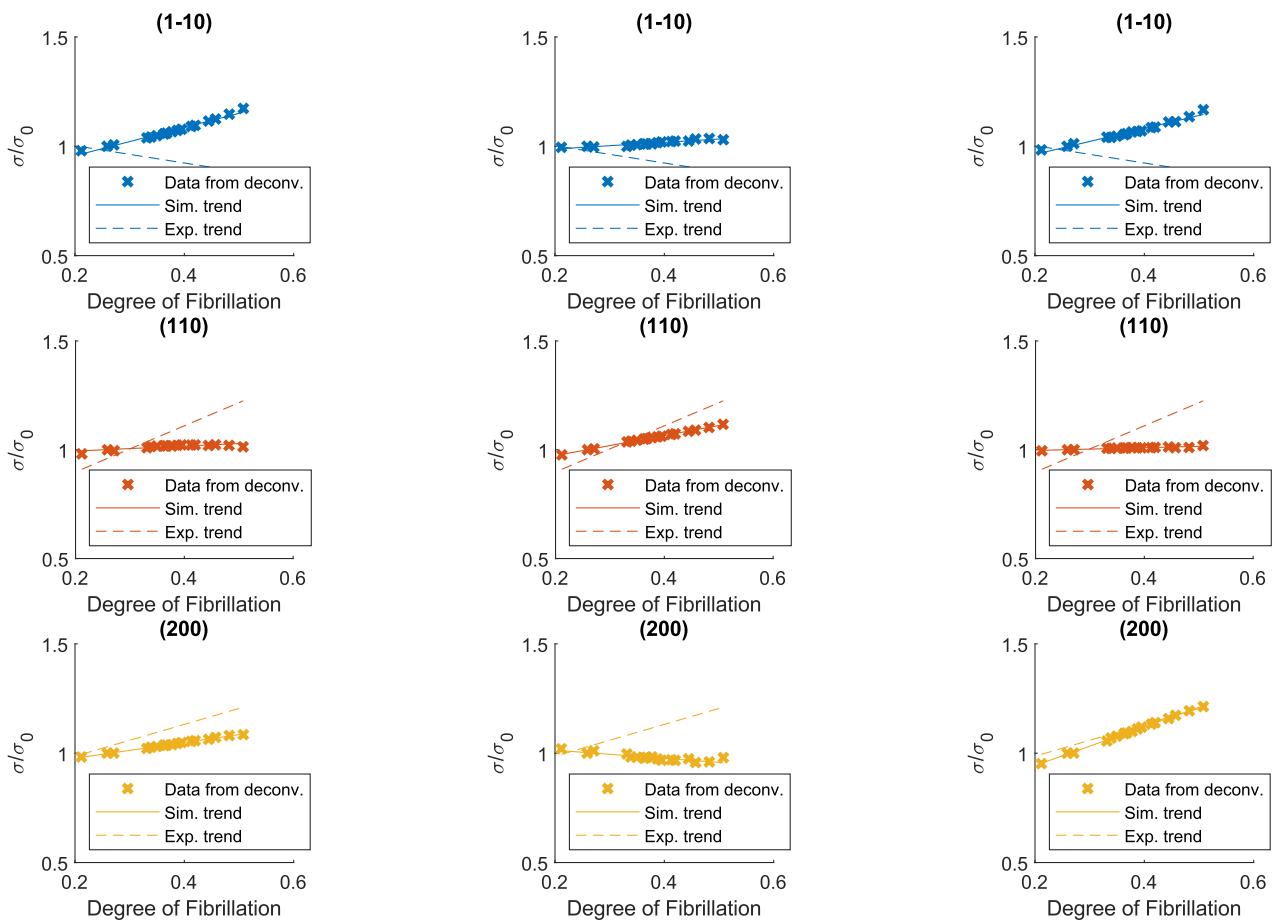
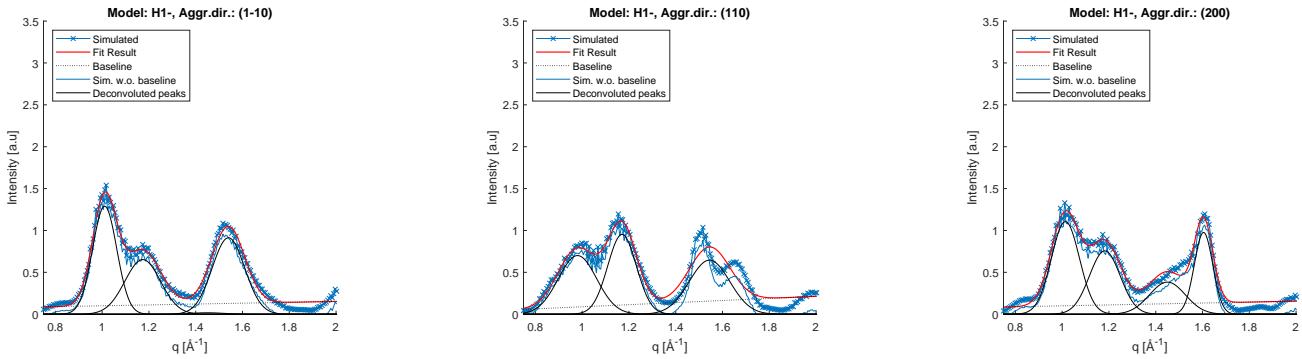


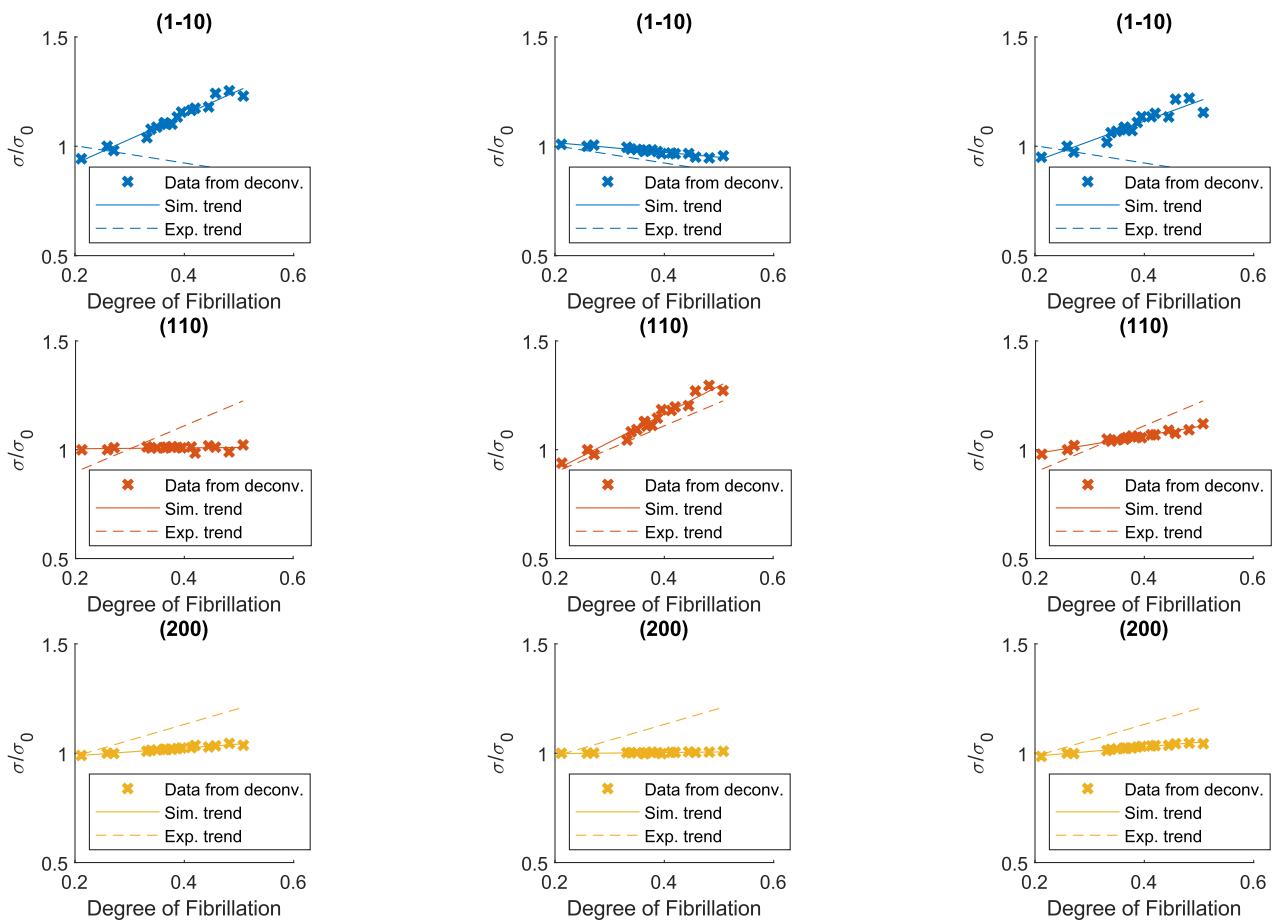
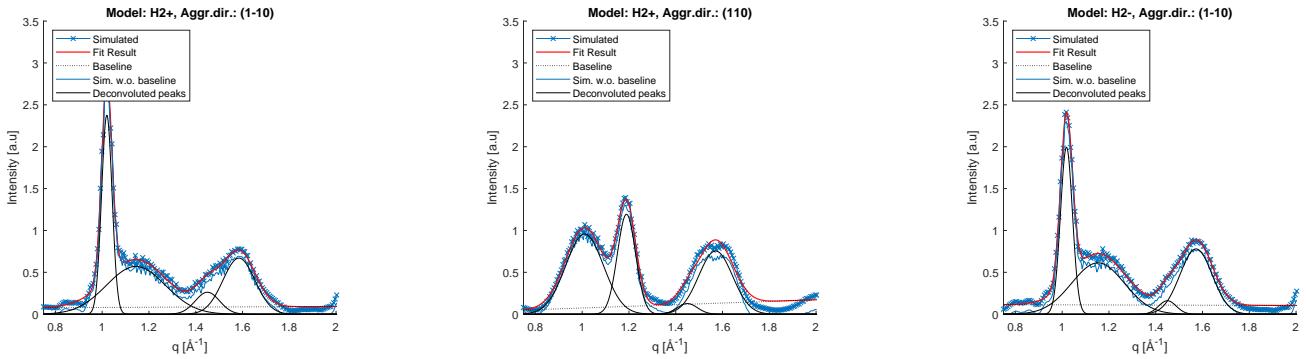


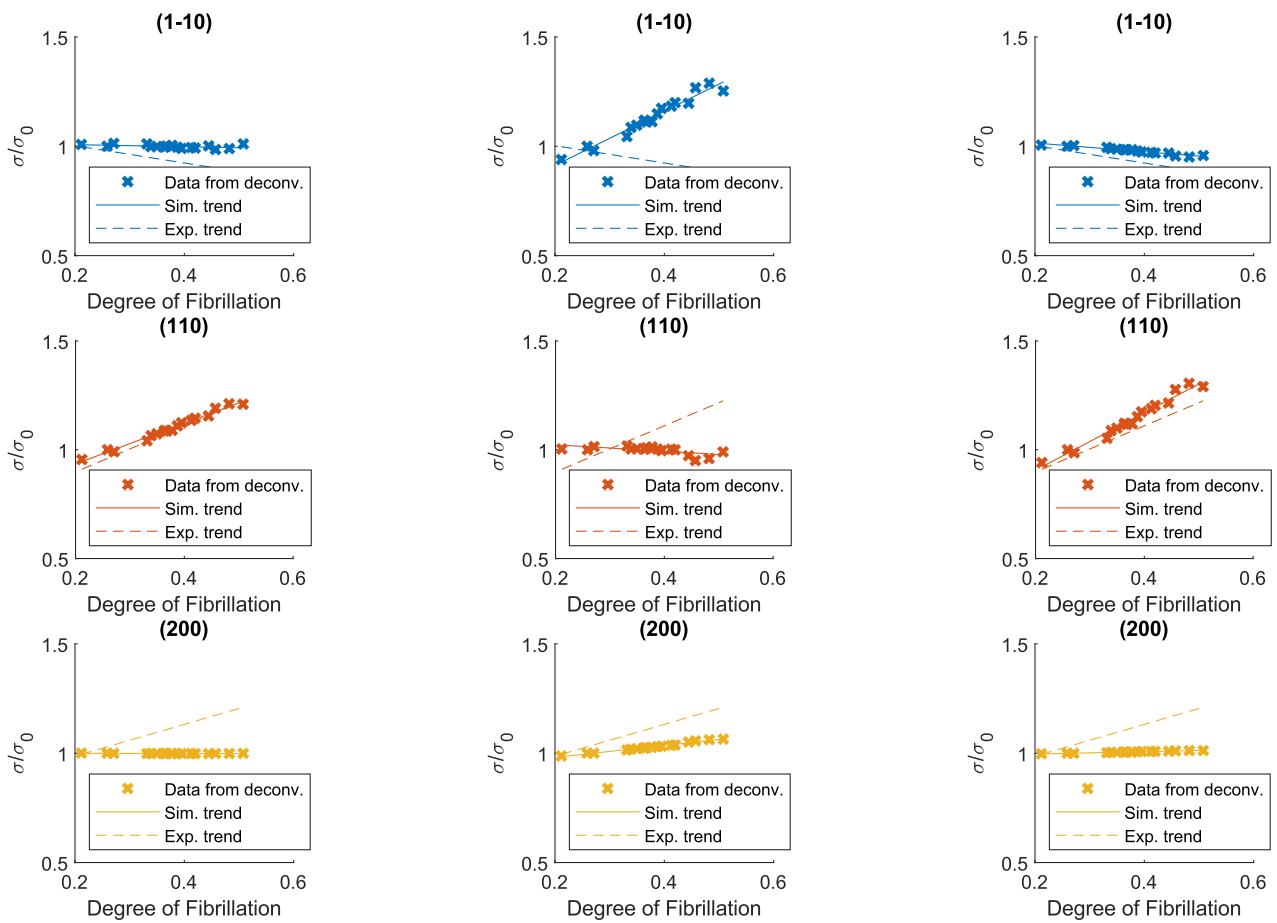
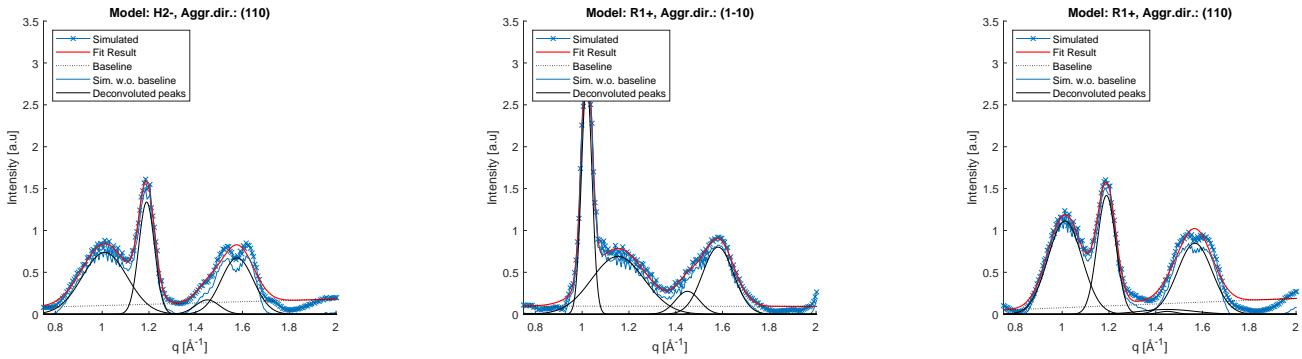


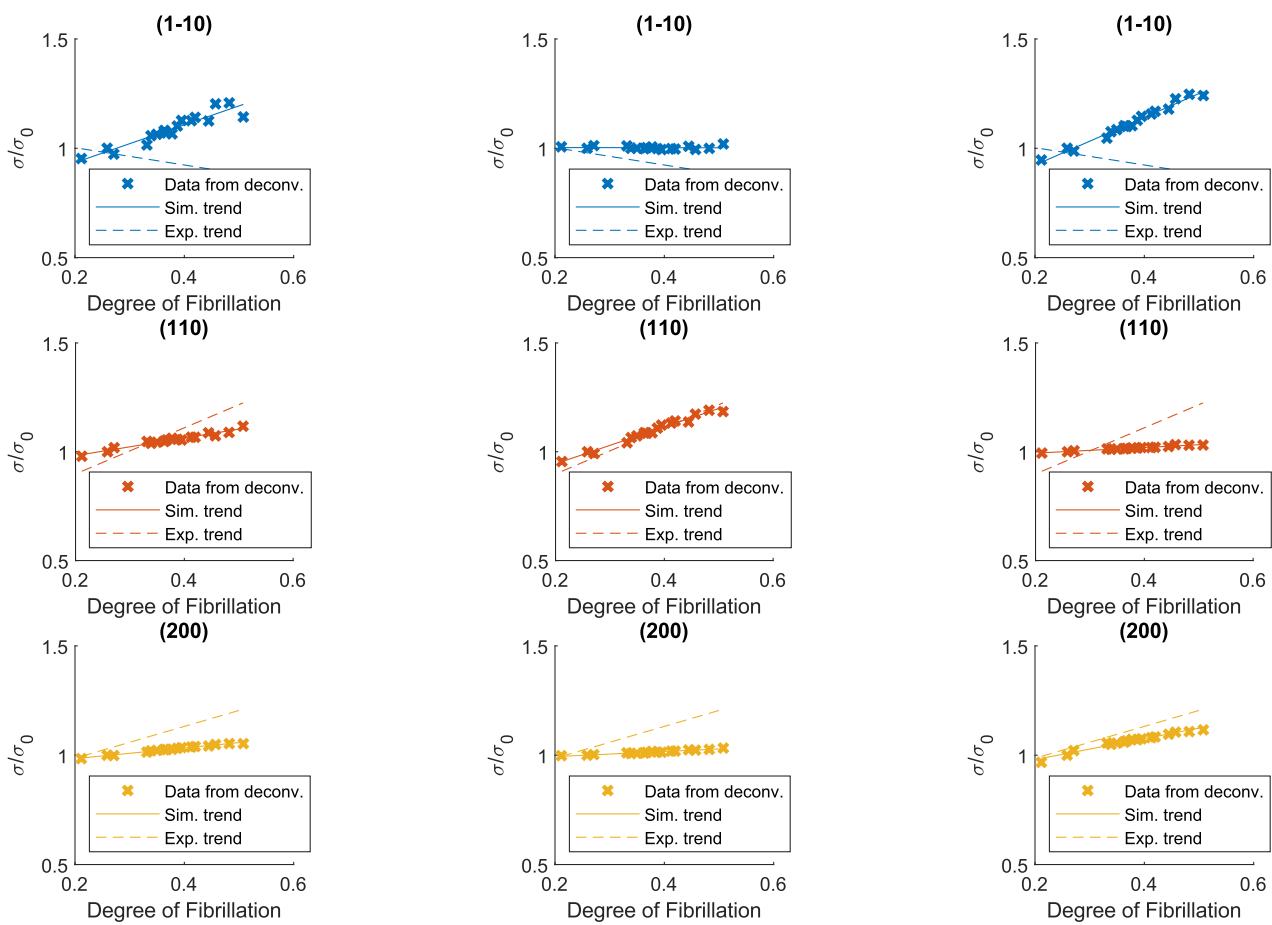
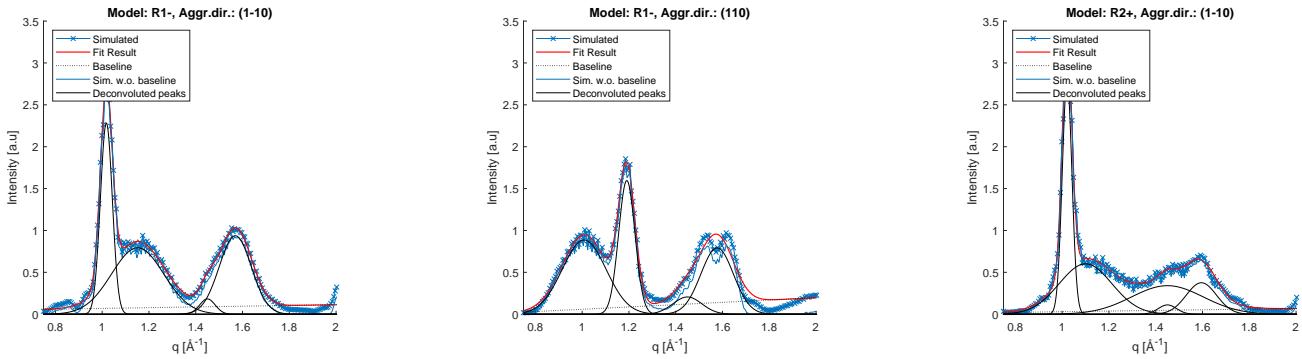


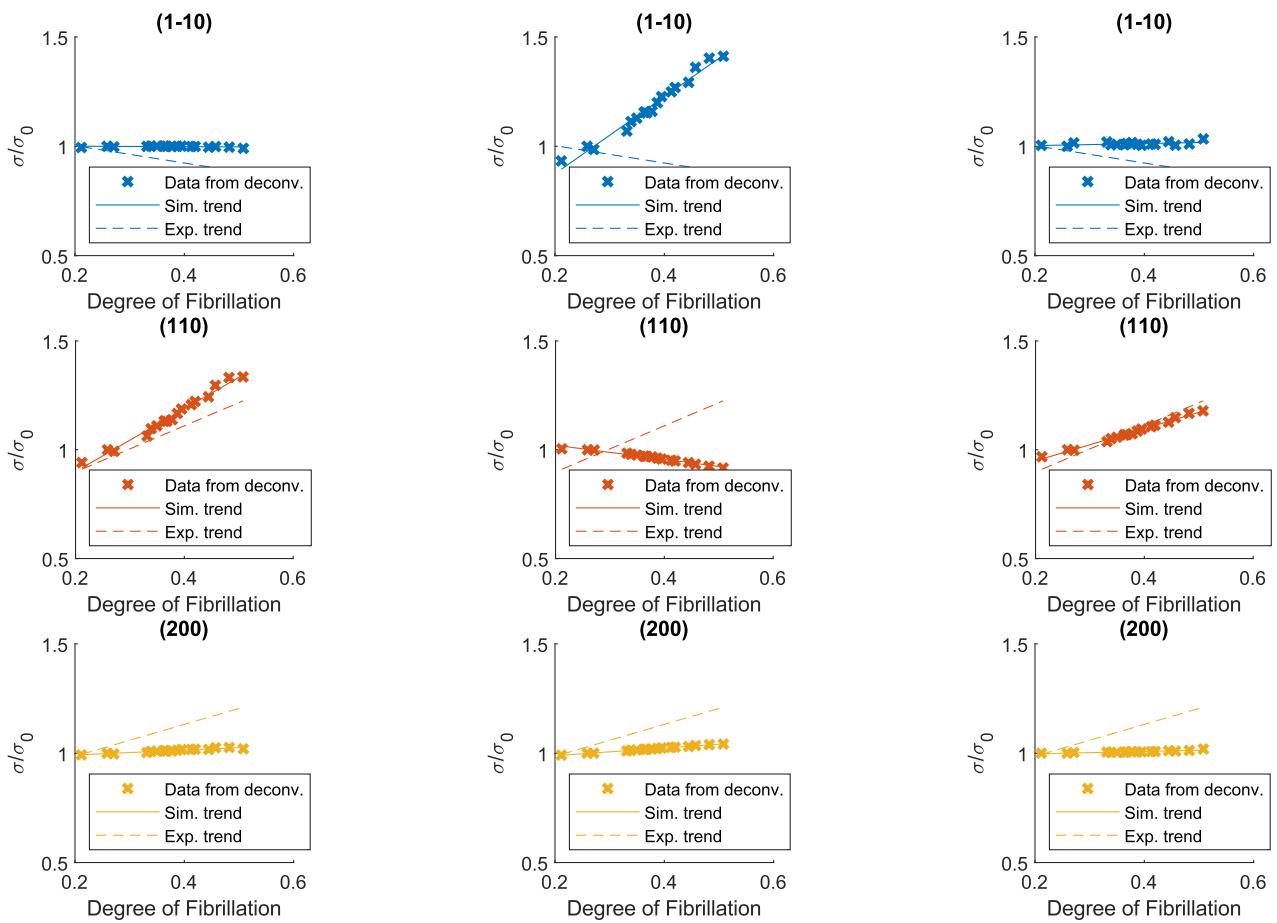
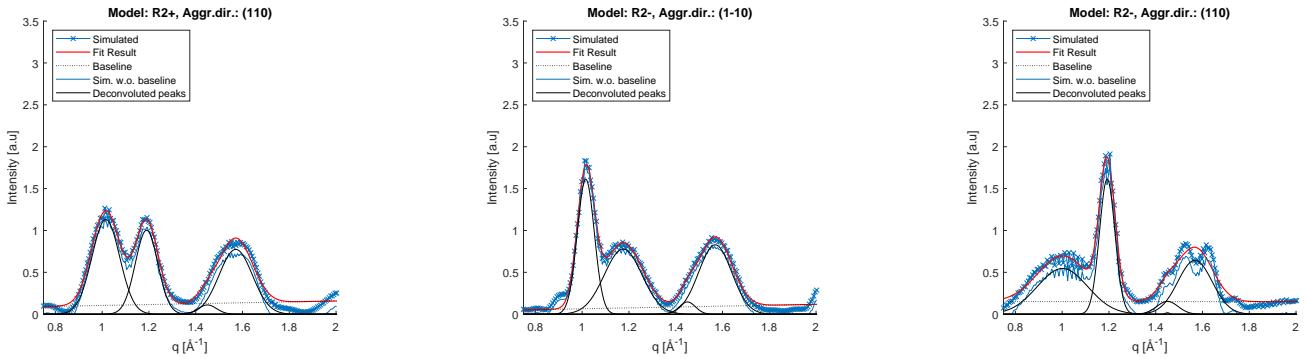


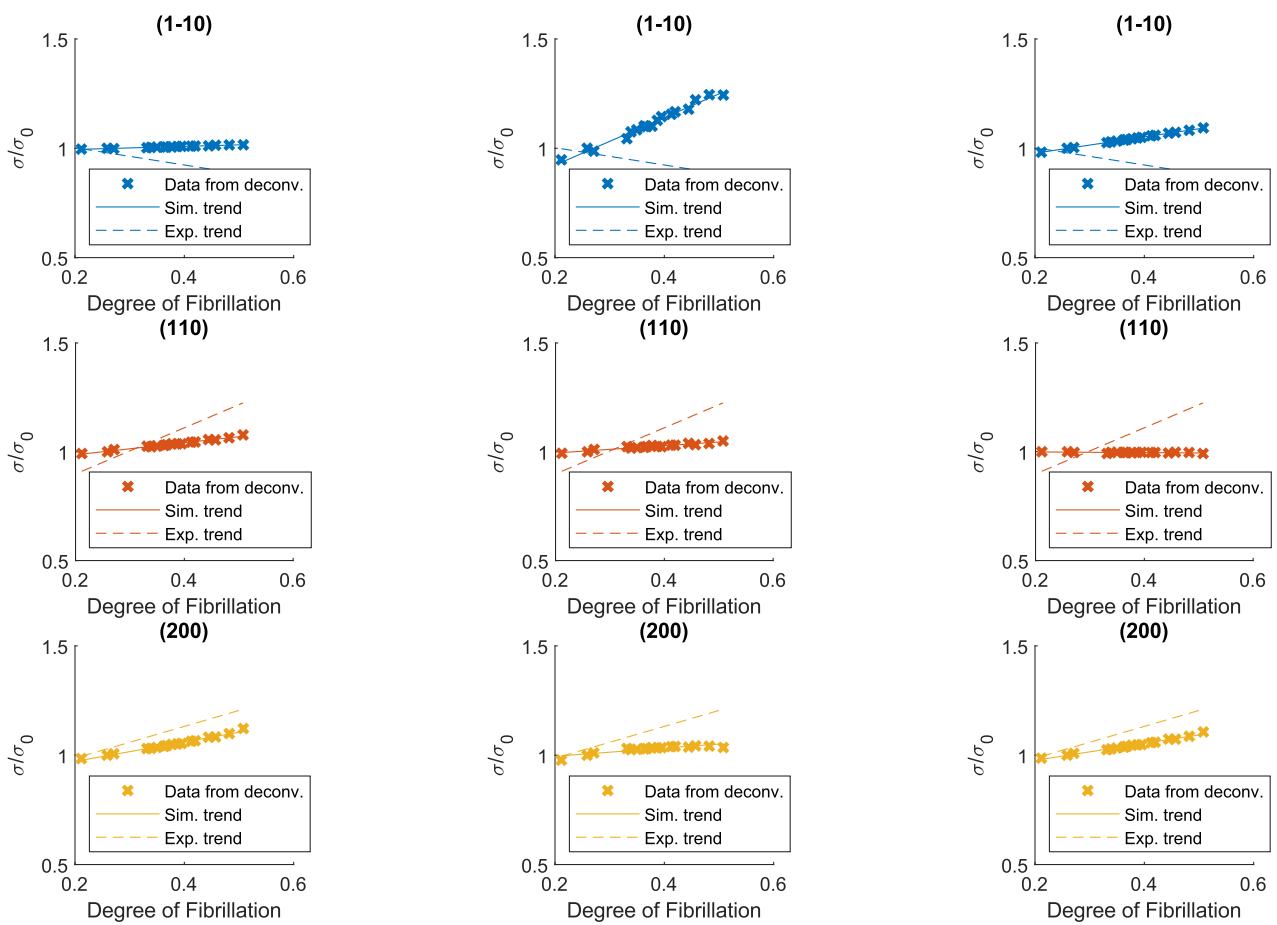
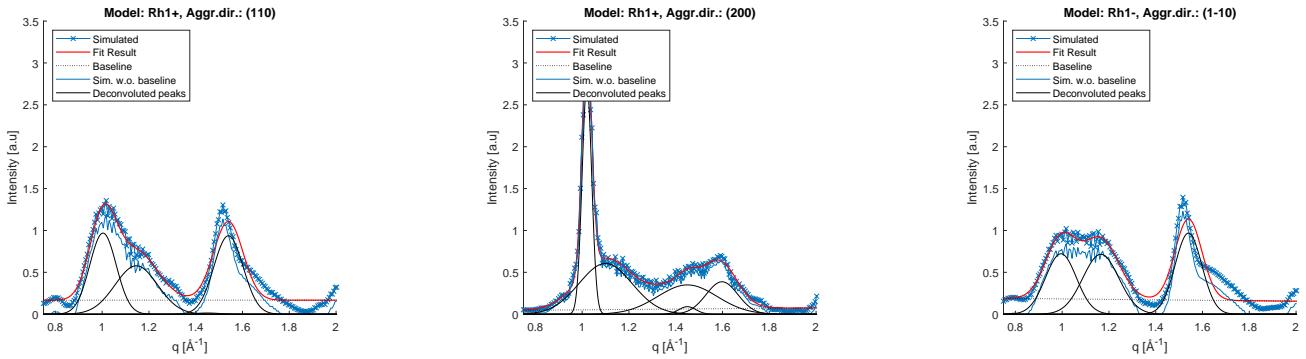


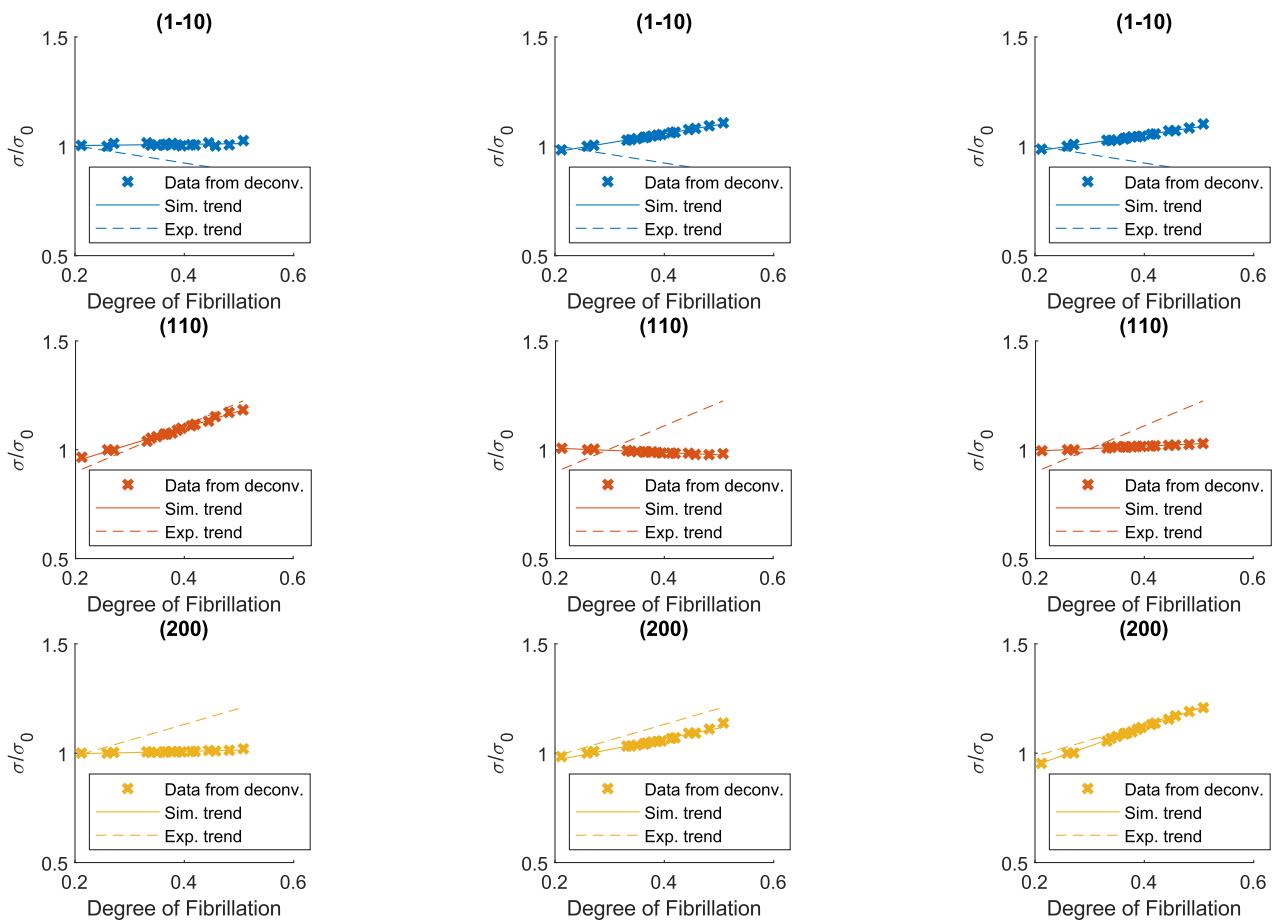
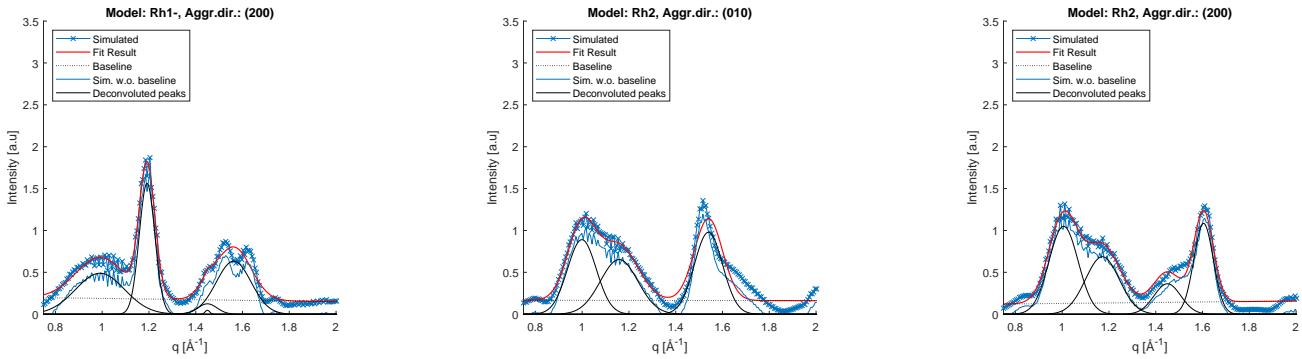




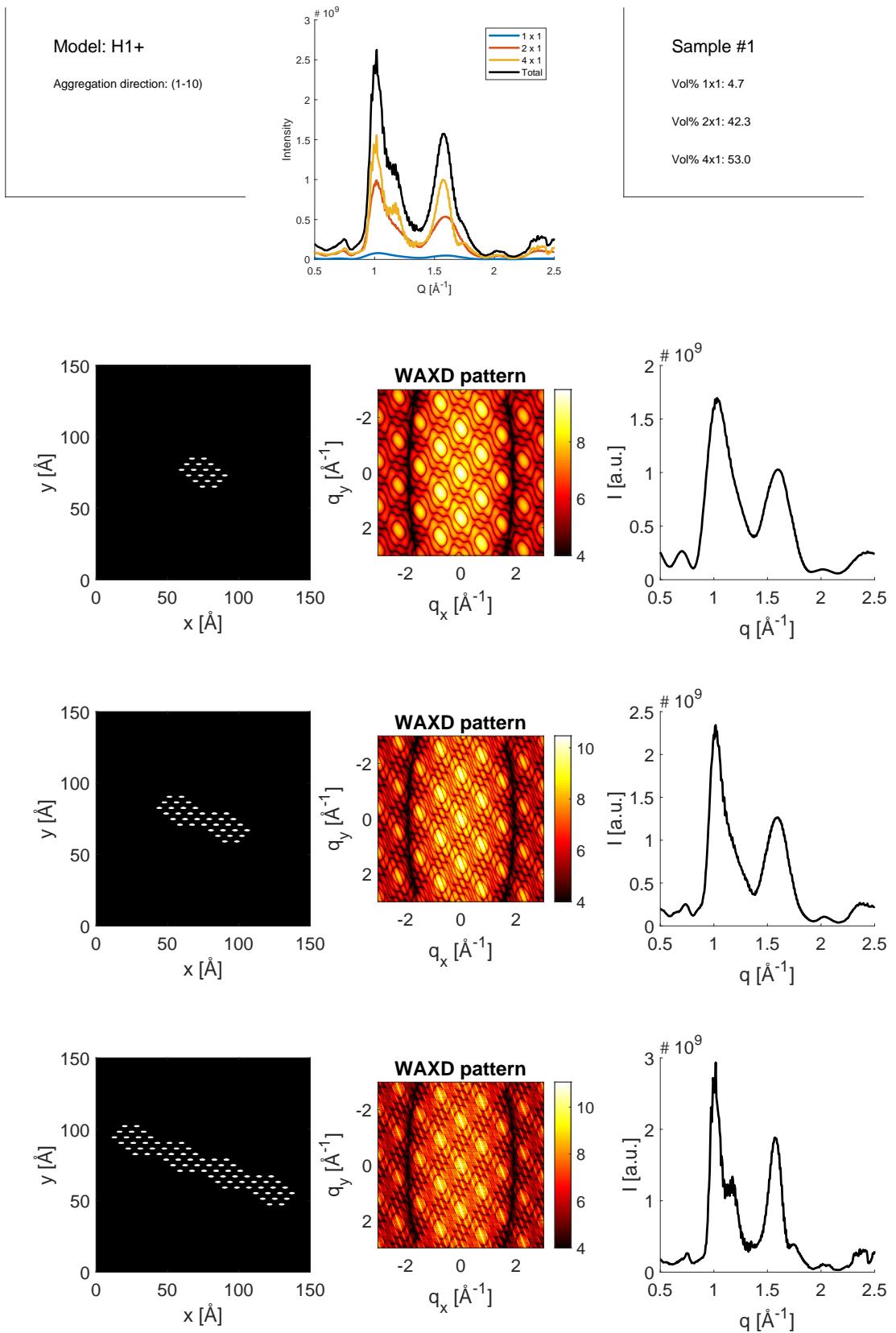


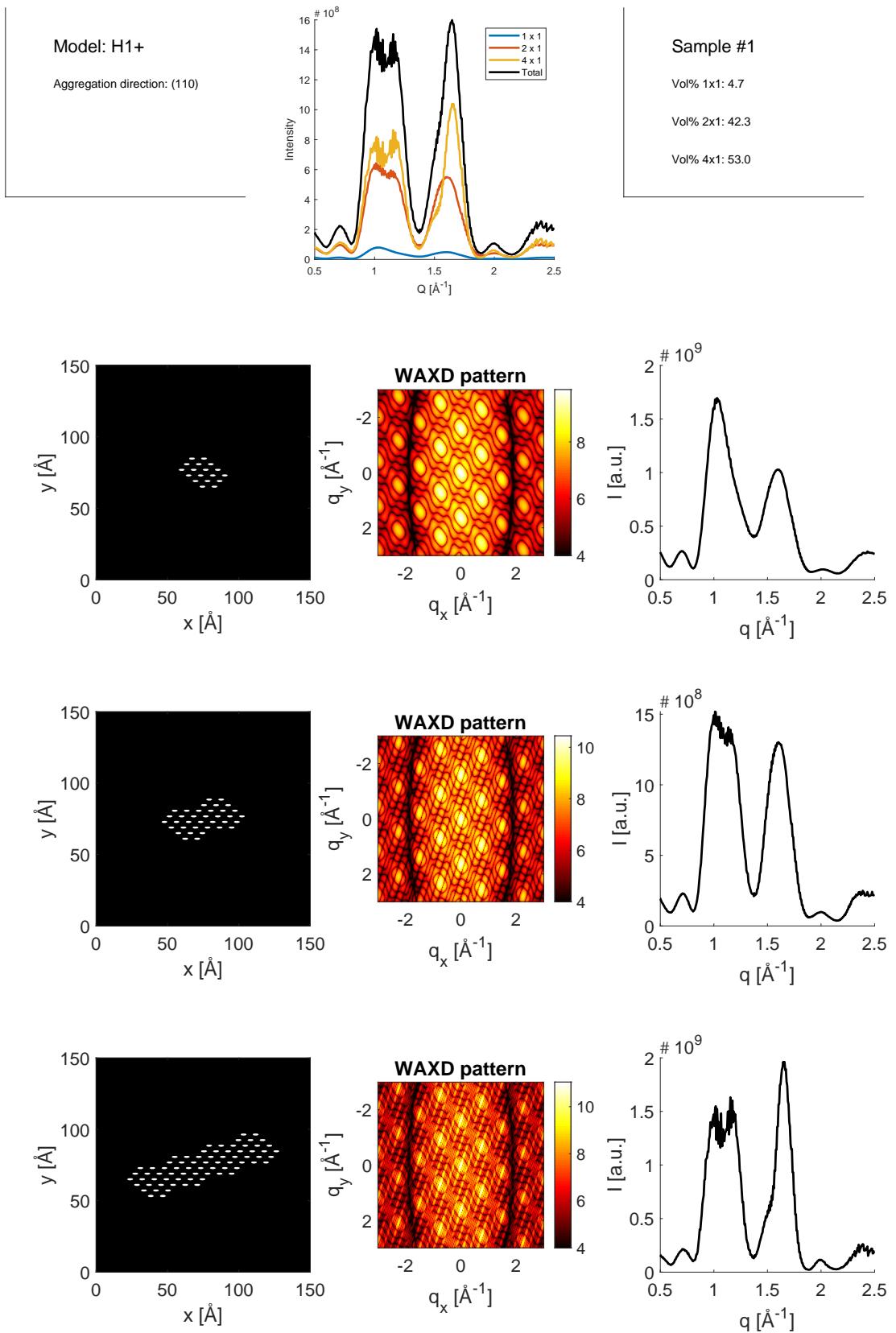


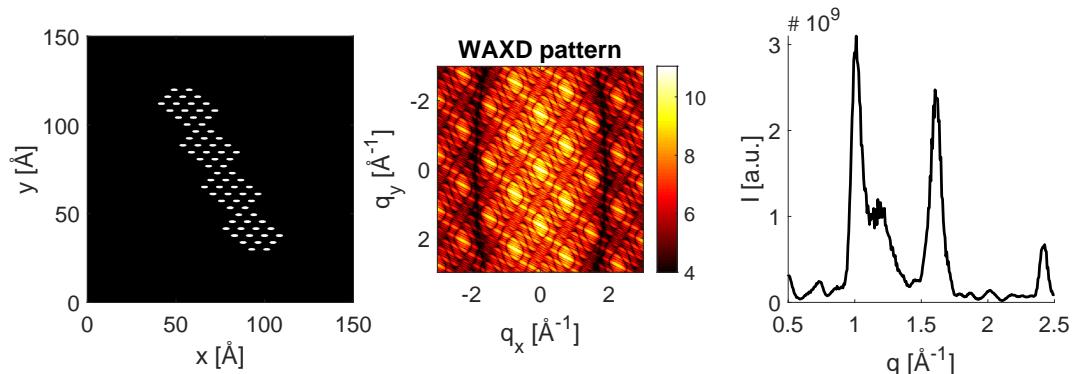
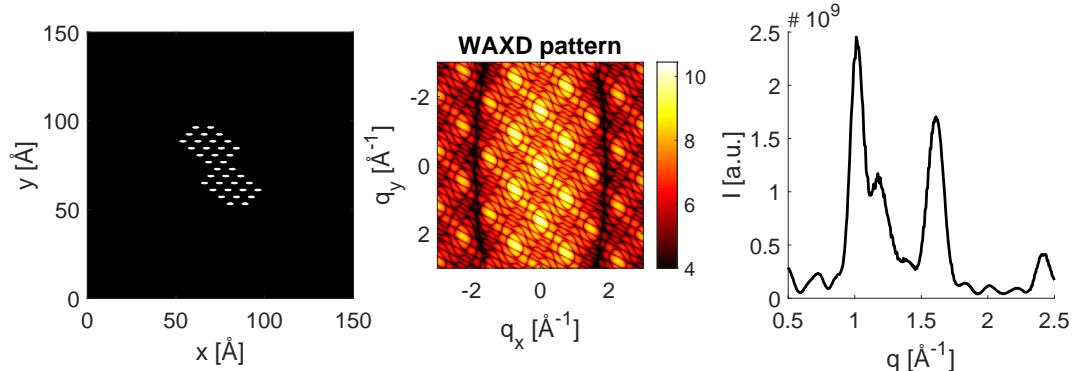
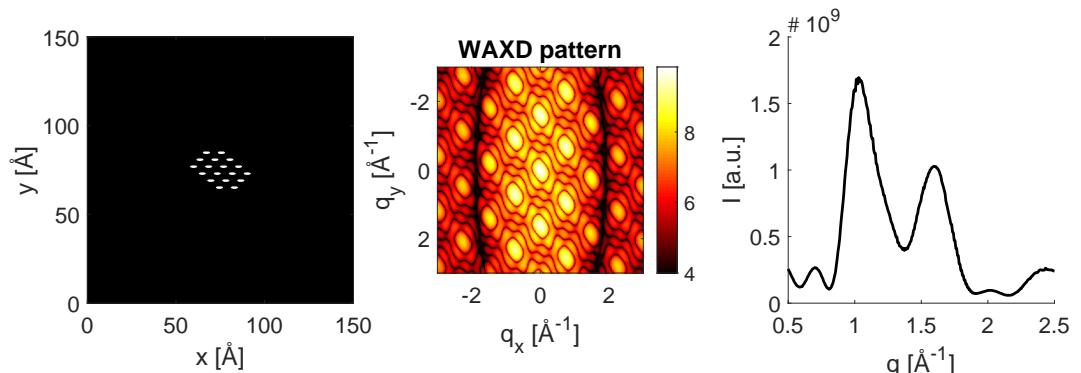
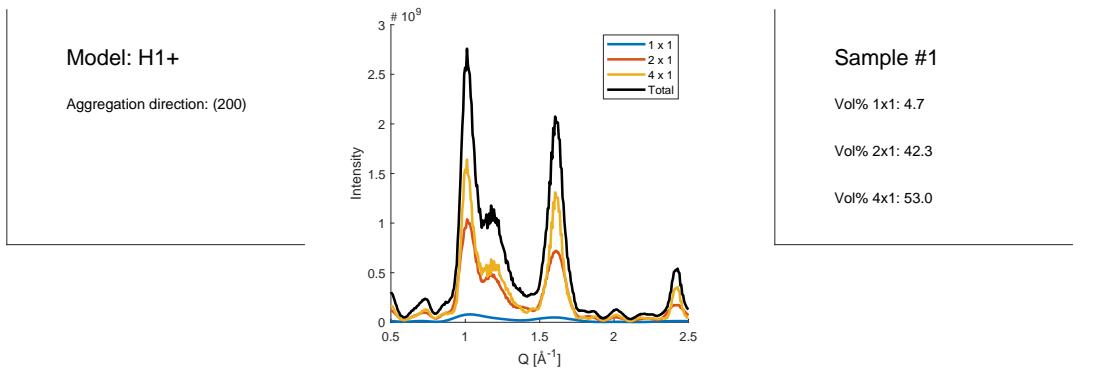


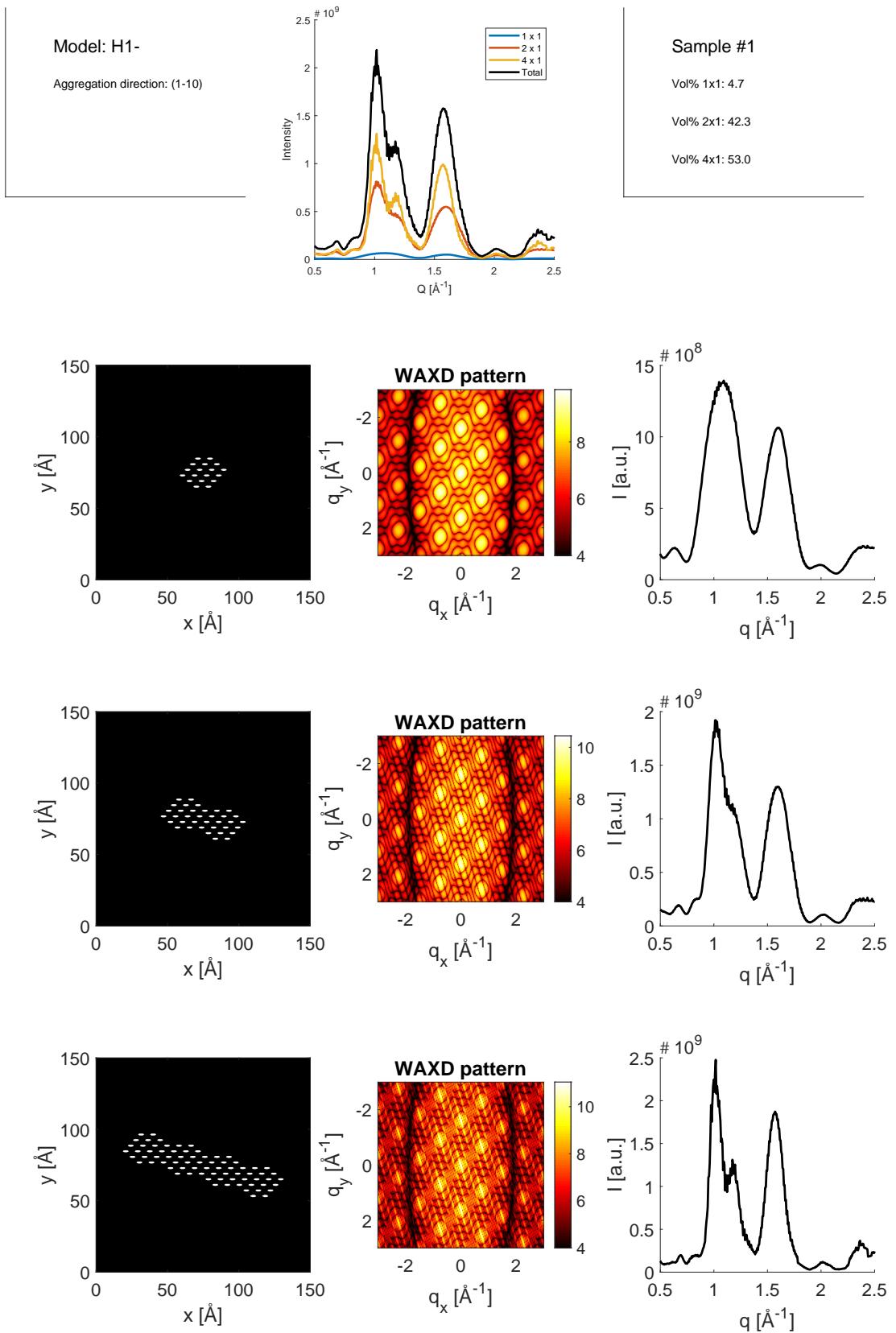


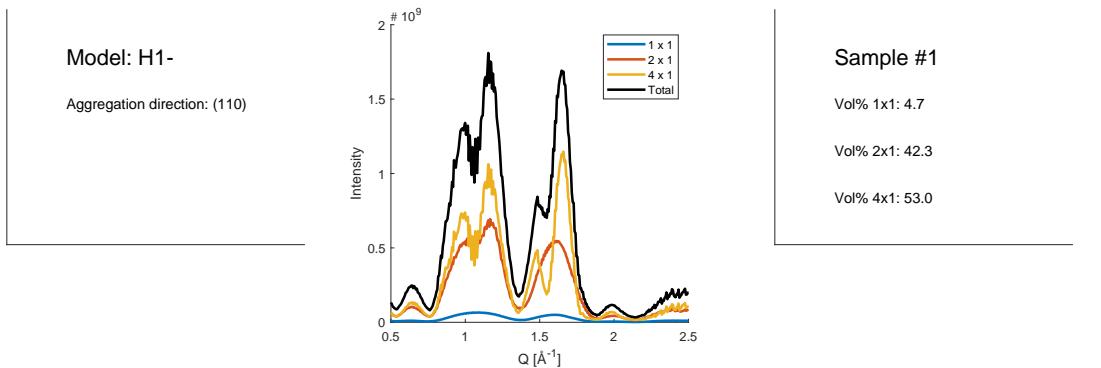
**WAXD simulations: Results**  
**Form factor of a CNF chain with semi-axes**  
**2 Å x 0.75 Å**



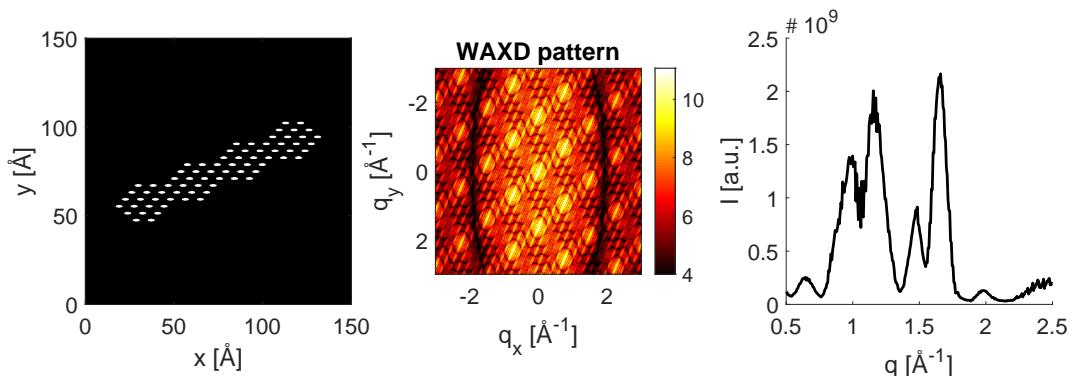
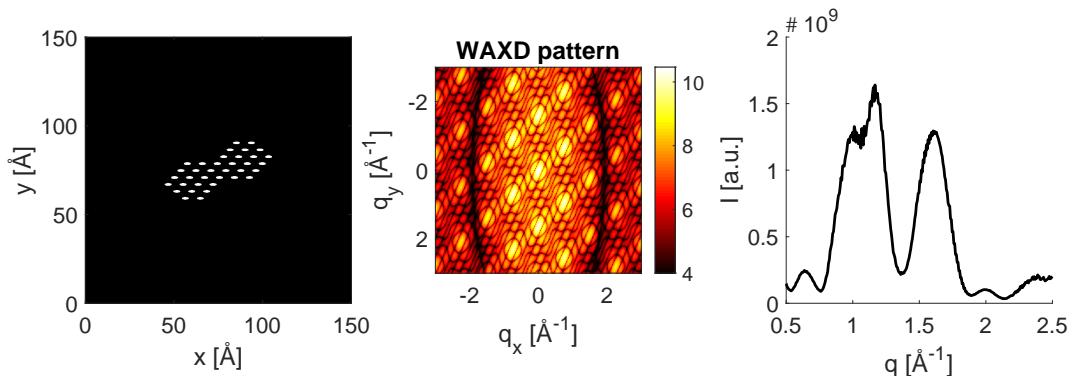
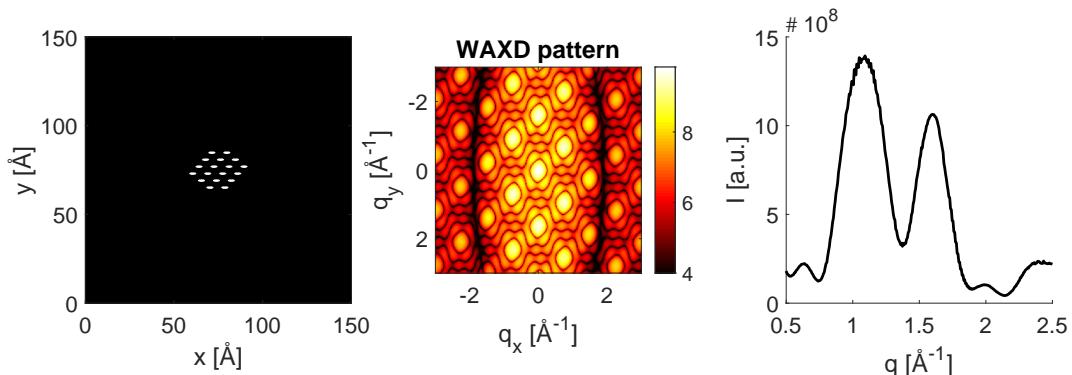


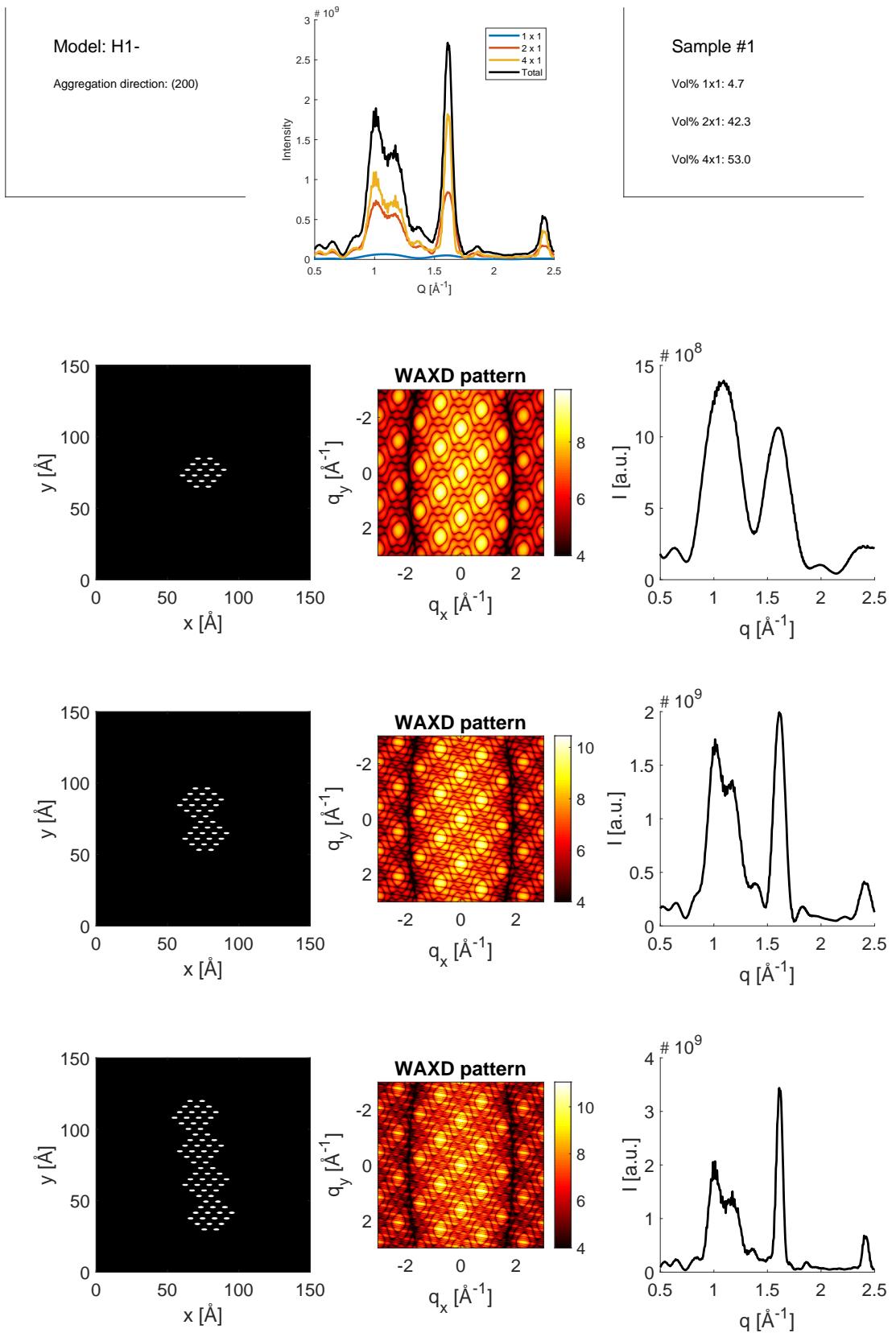


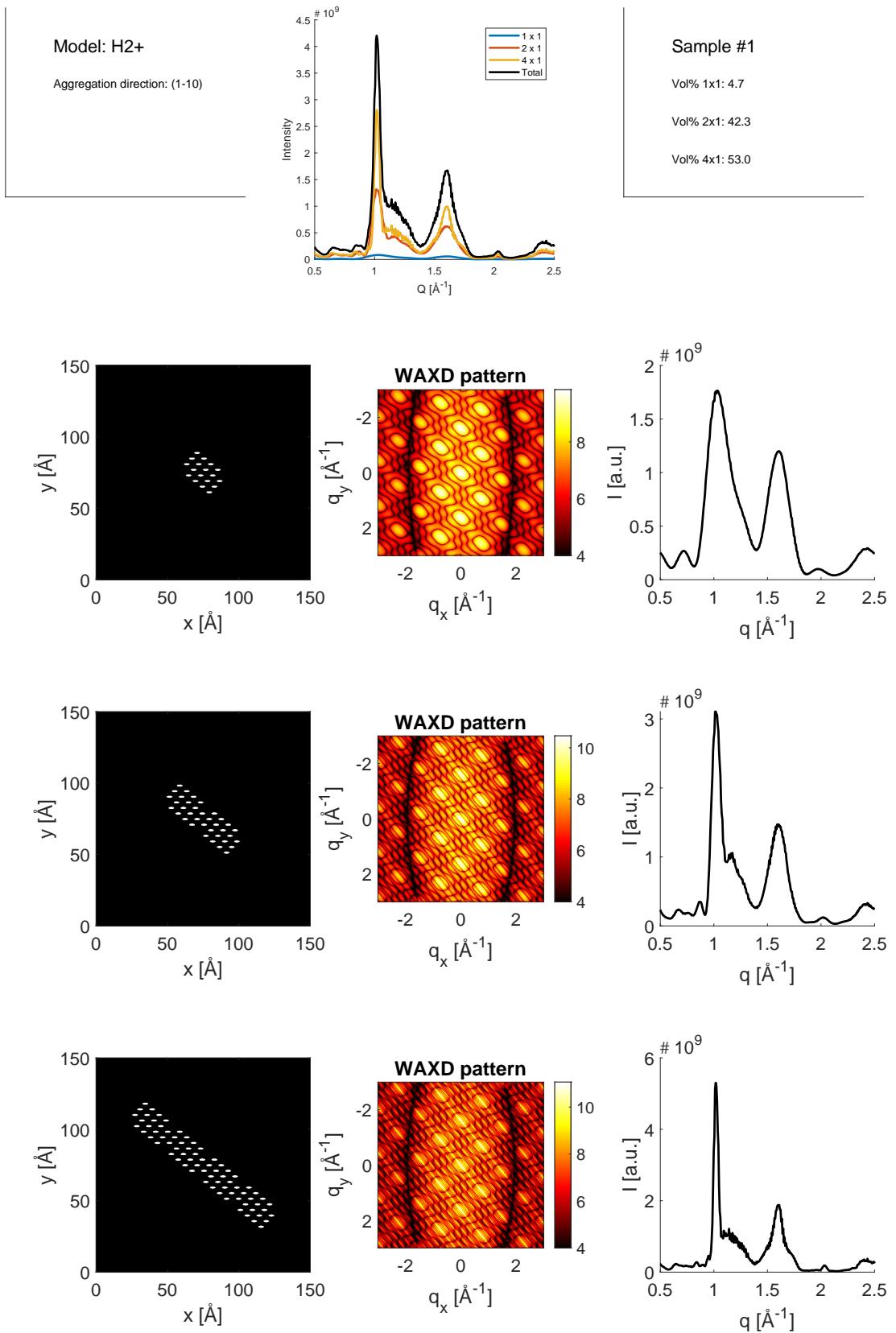


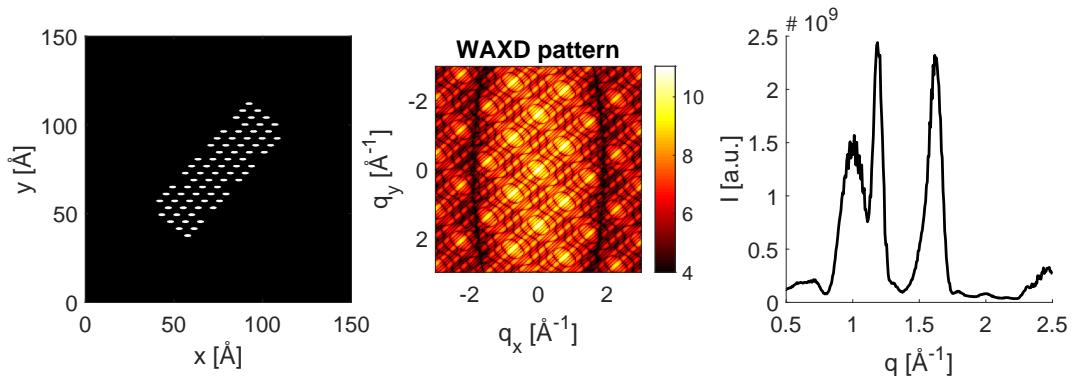
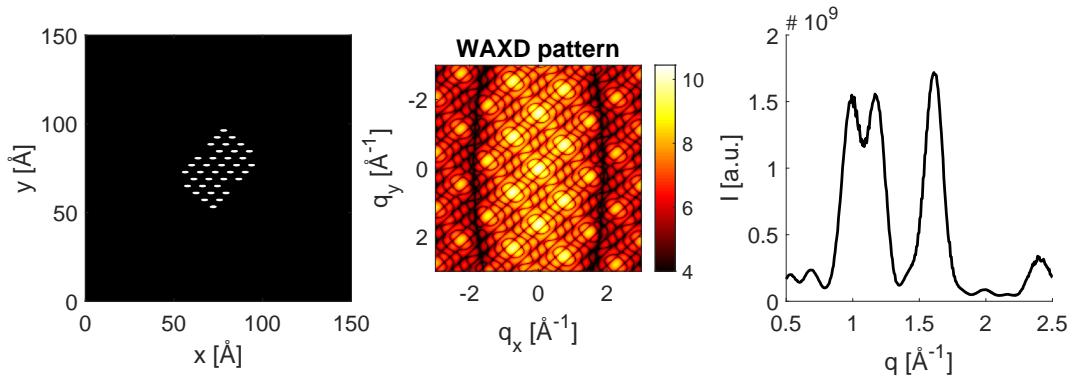
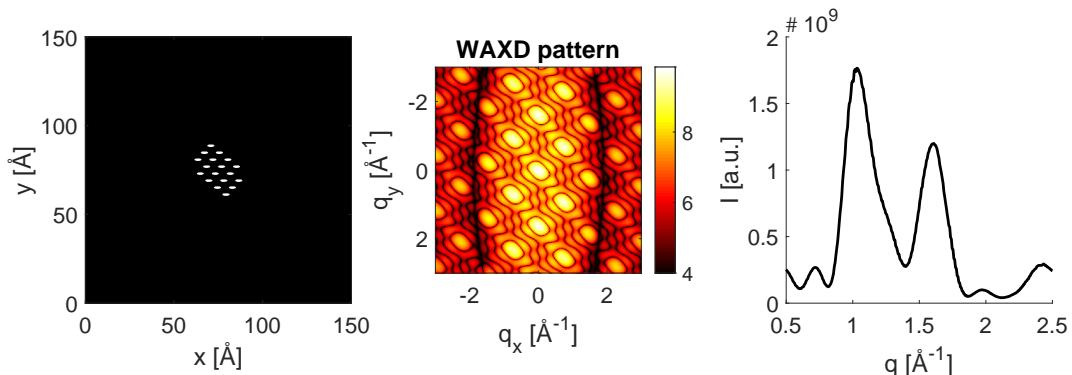
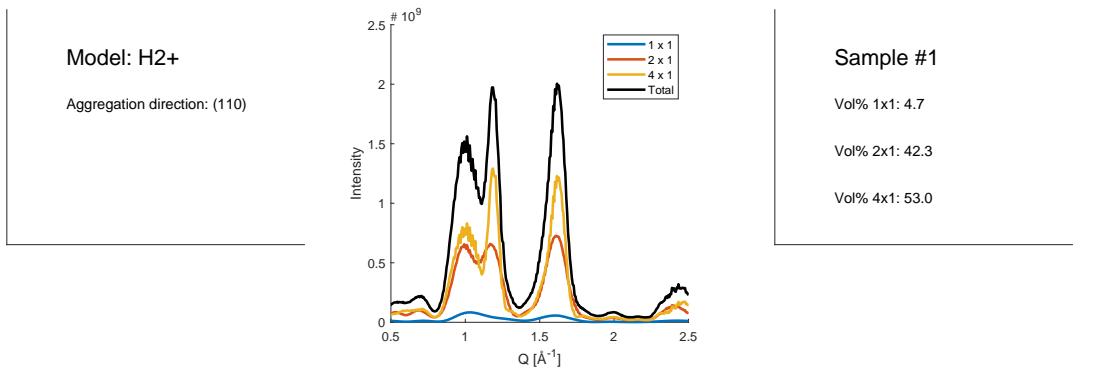


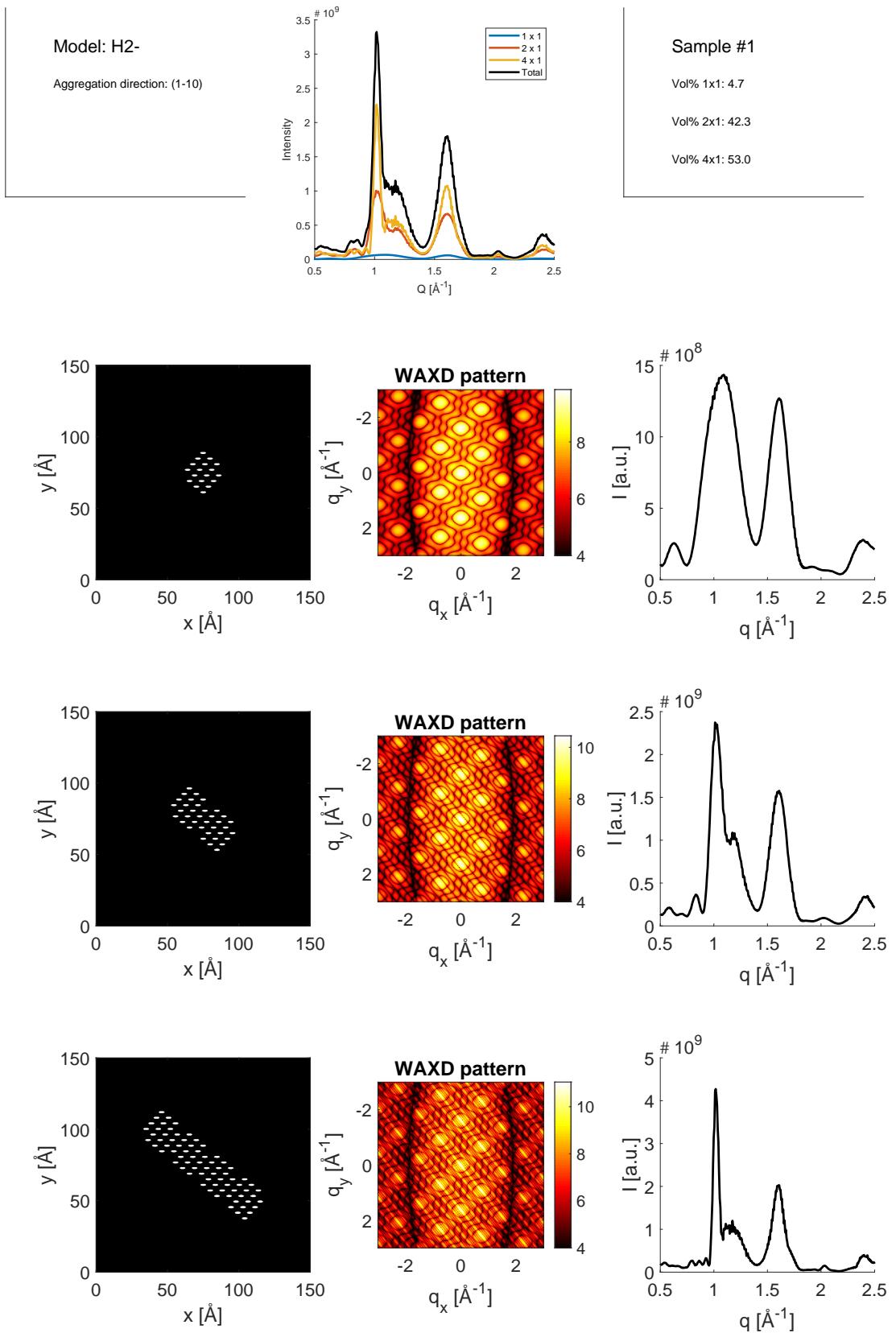
**Sample #1**  
Vol% 1x1: 4.7  
Vol% 2x1: 42.3  
Vol% 4x1: 53.0

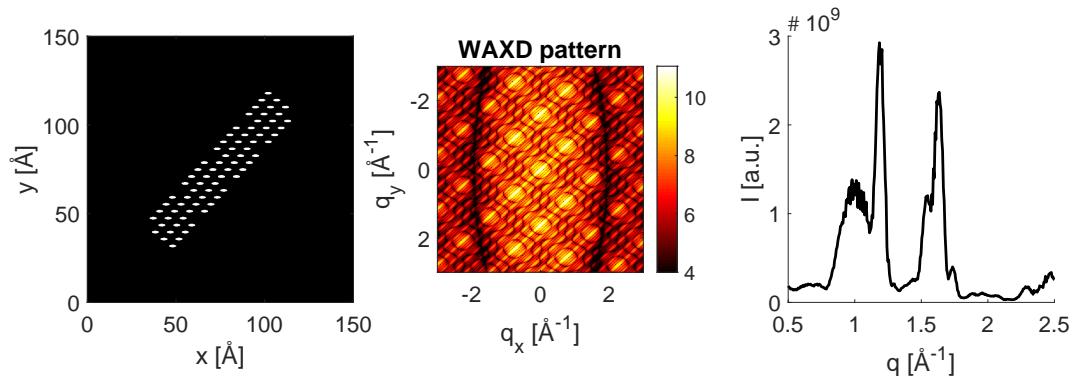
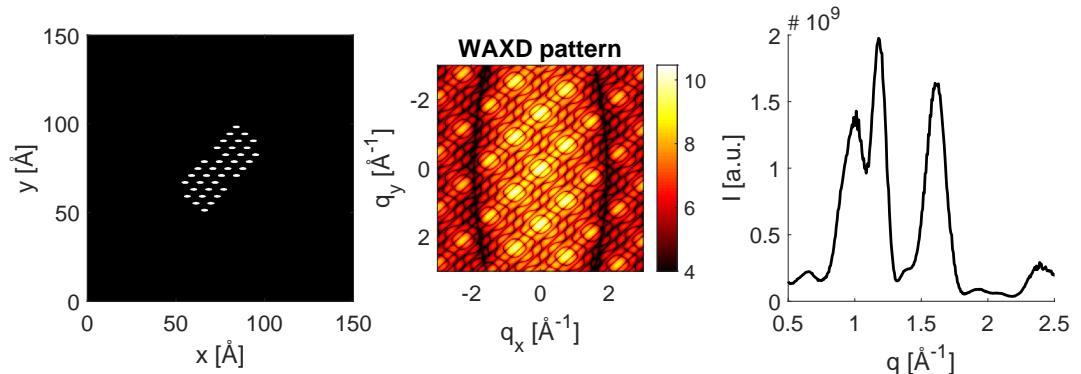
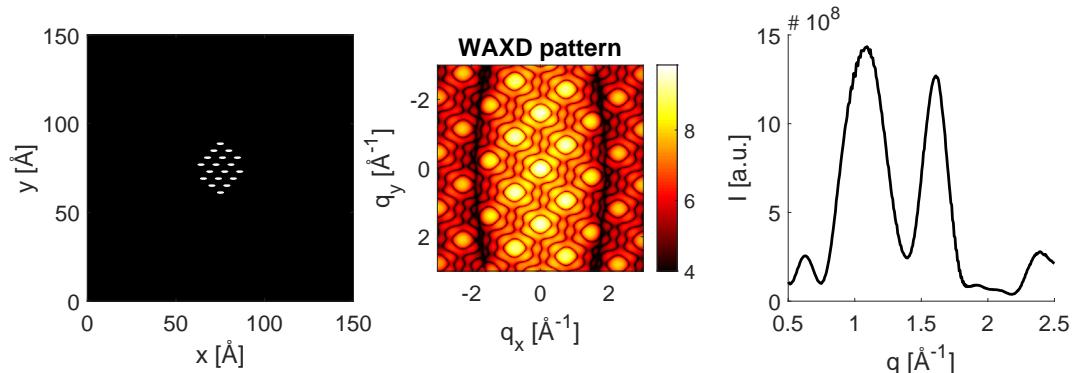
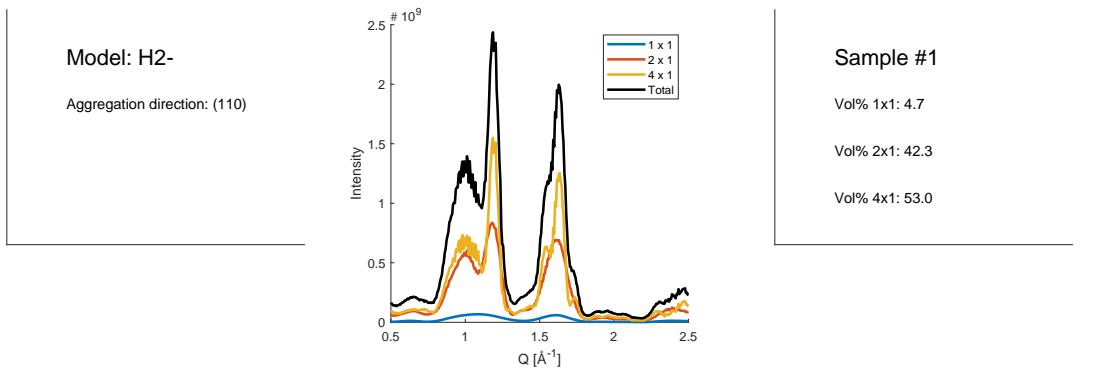


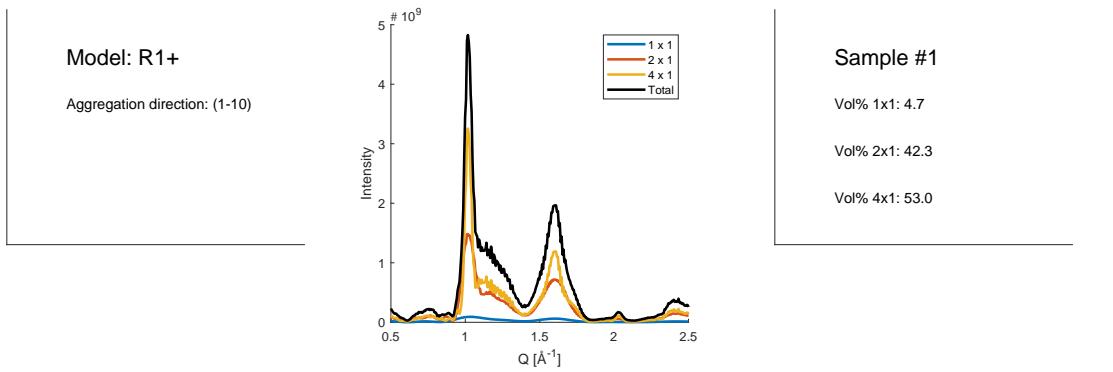










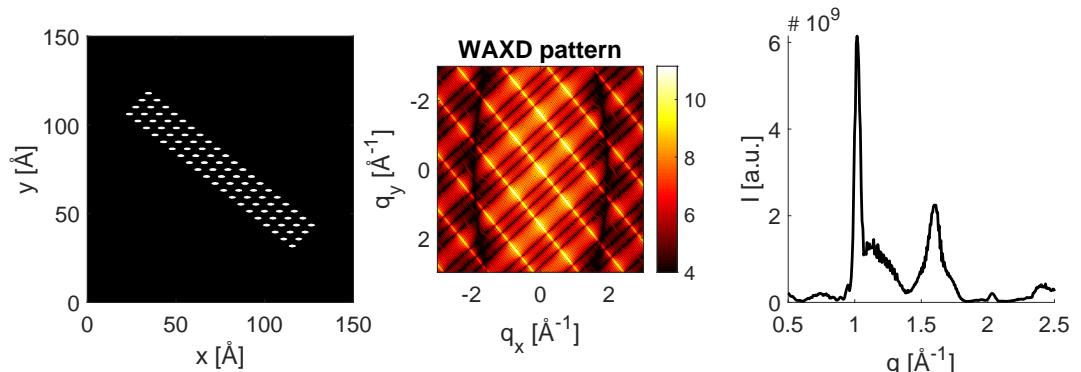
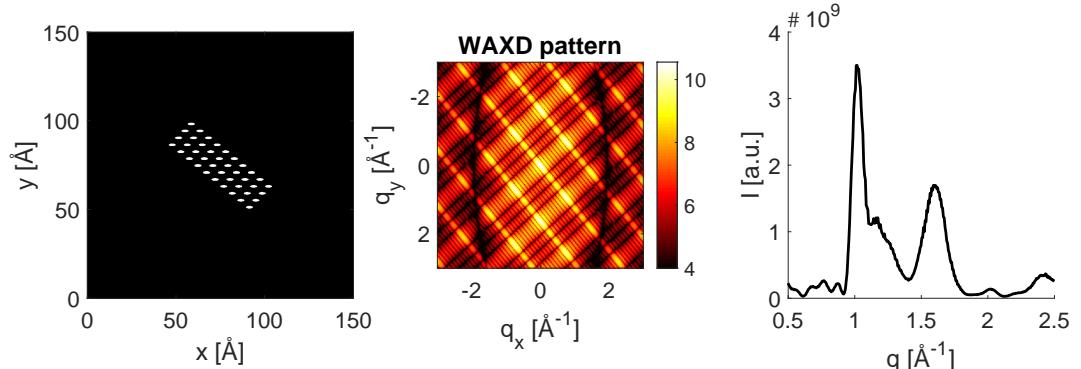
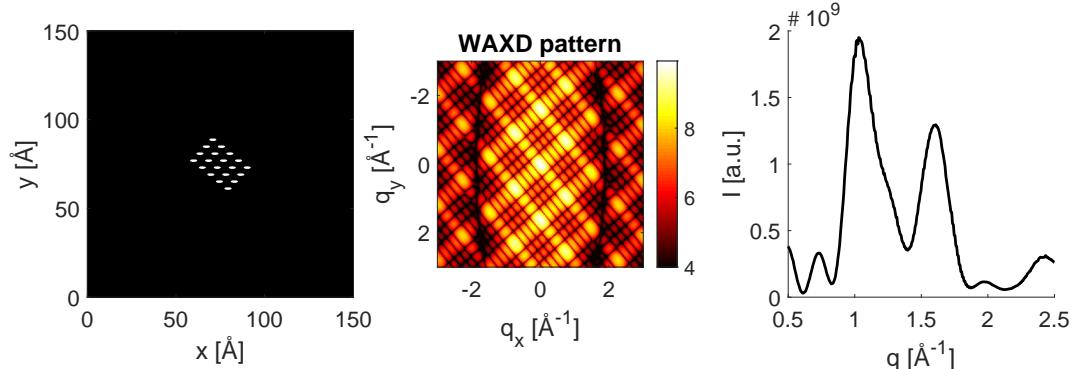


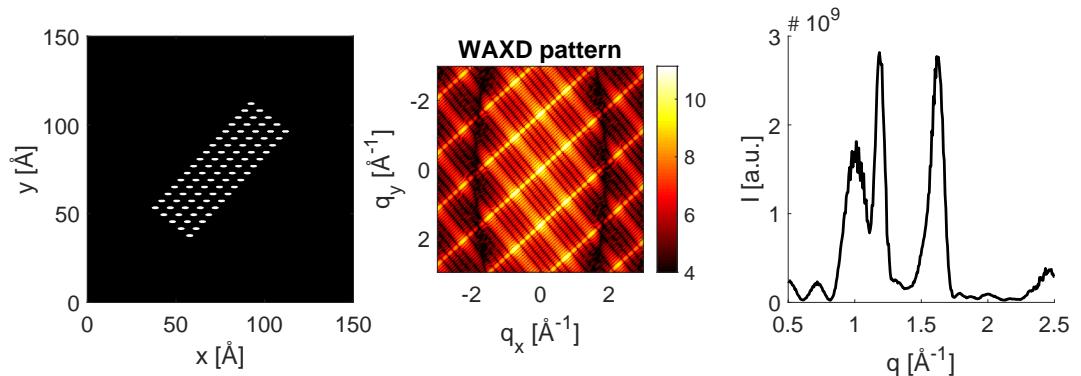
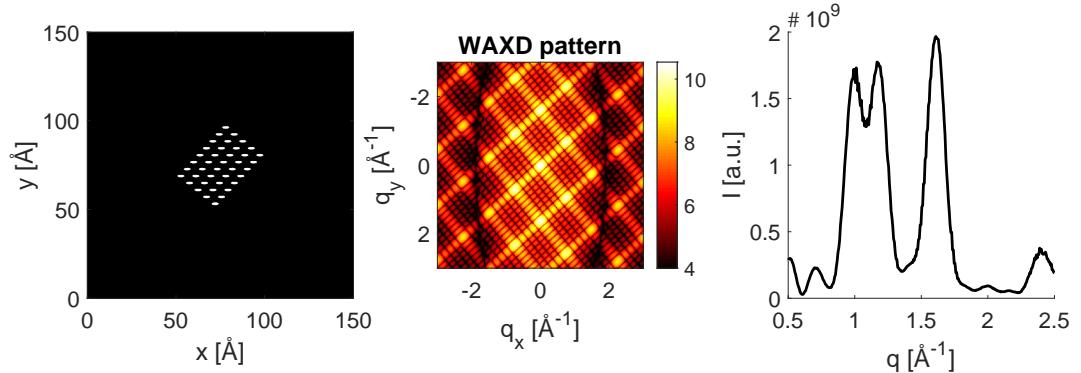
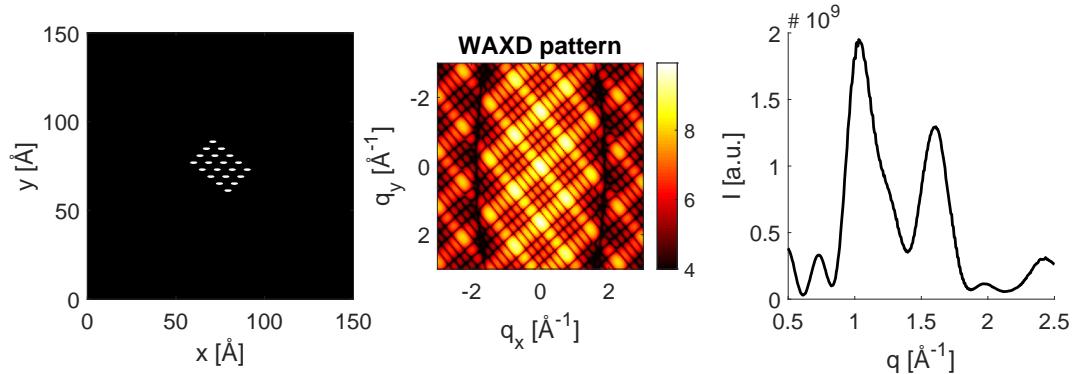
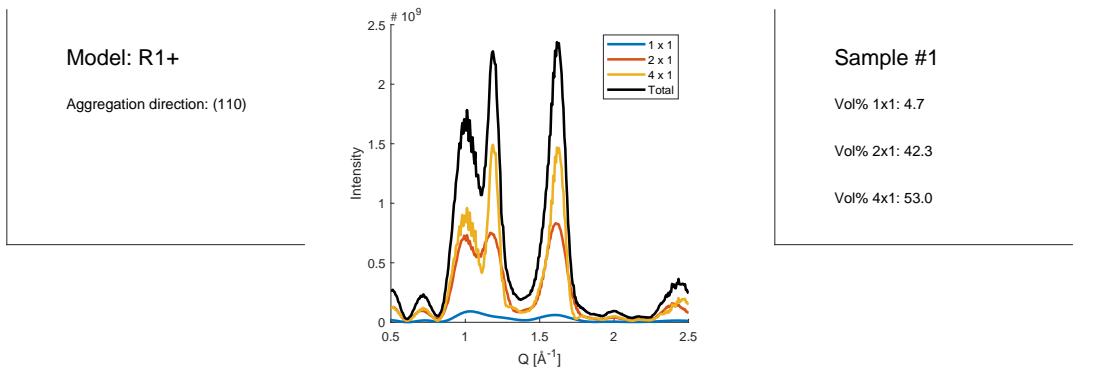
**Sample #1**

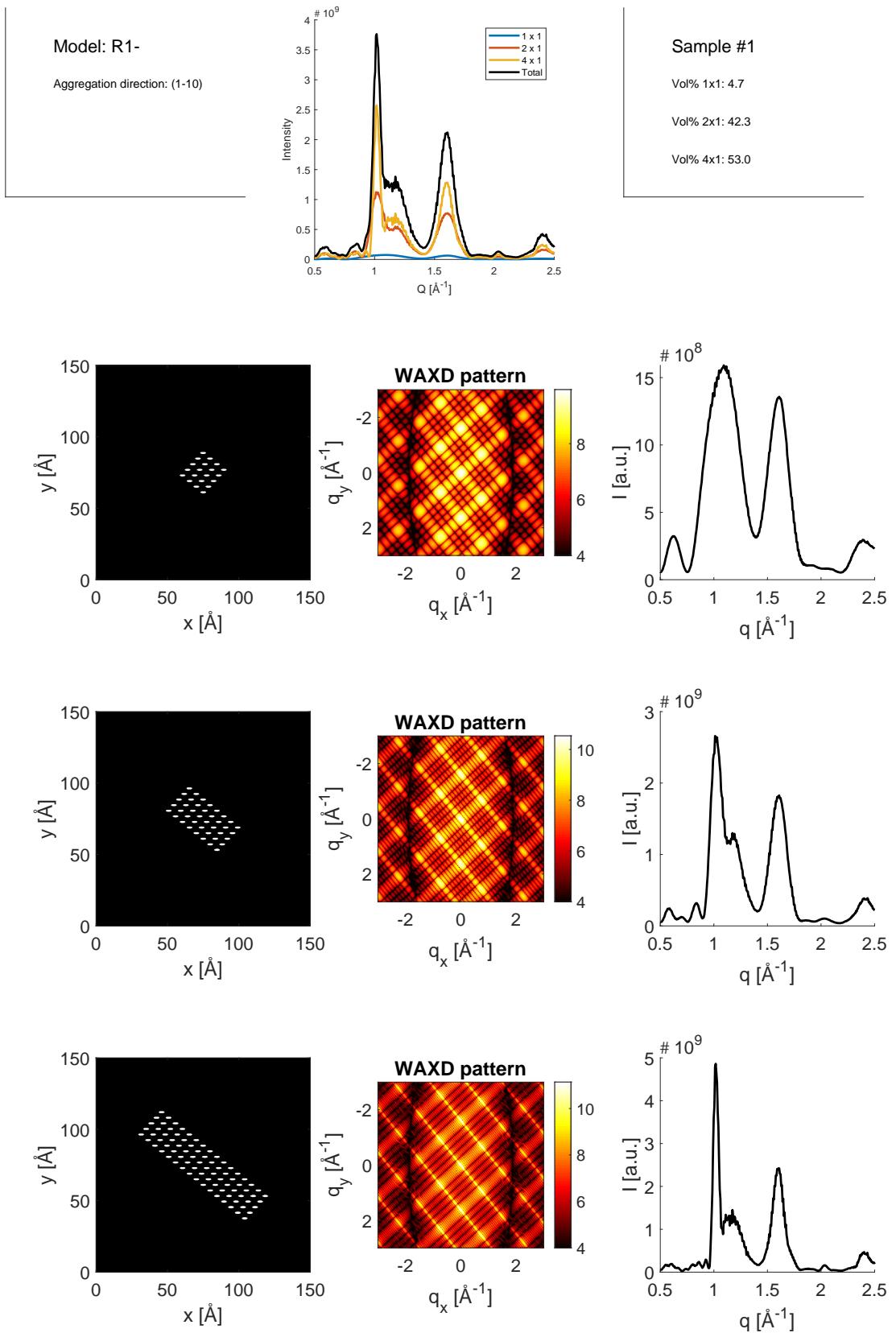
Vol% 1x1: 4.7

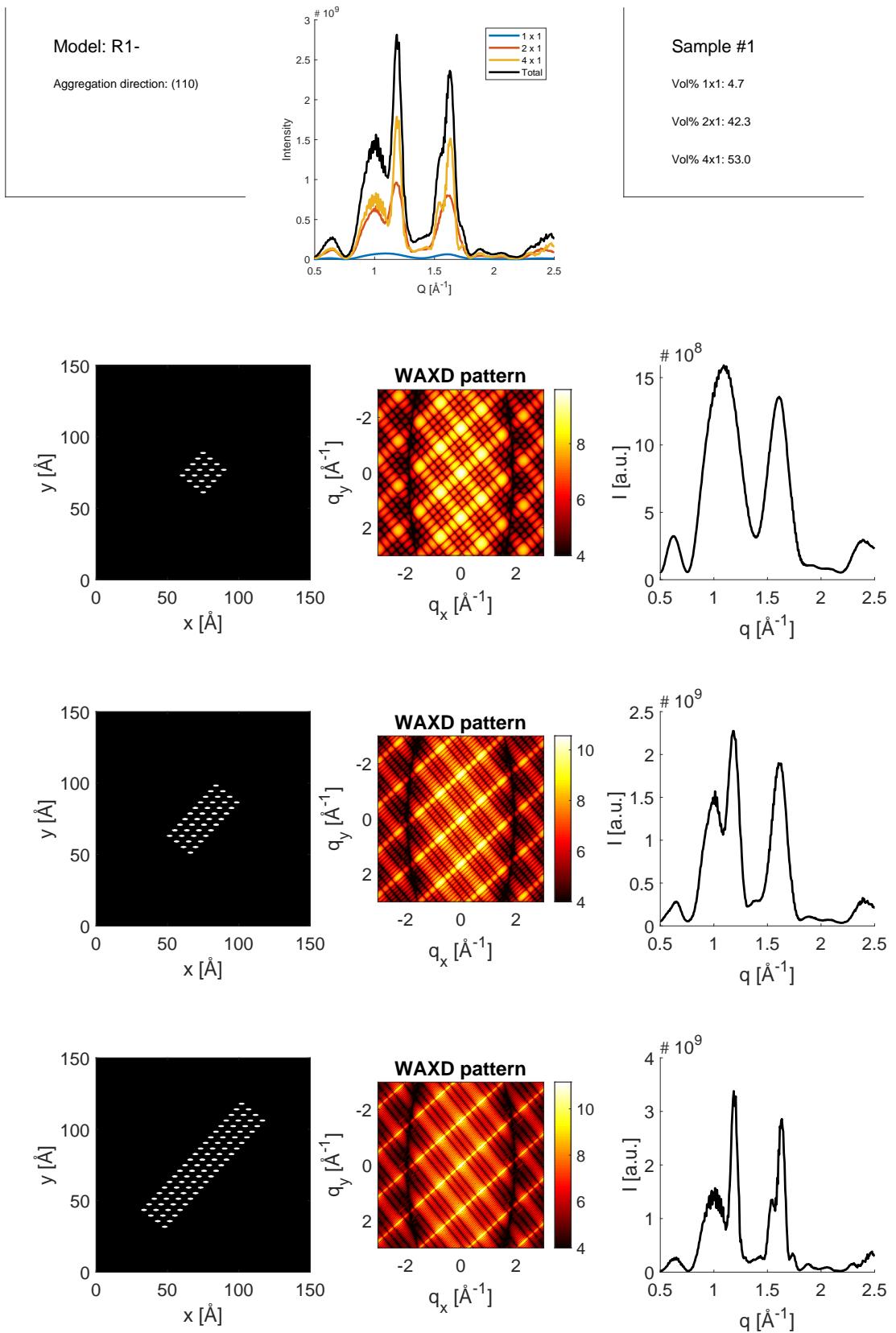
Vol% 2x1: 42.3

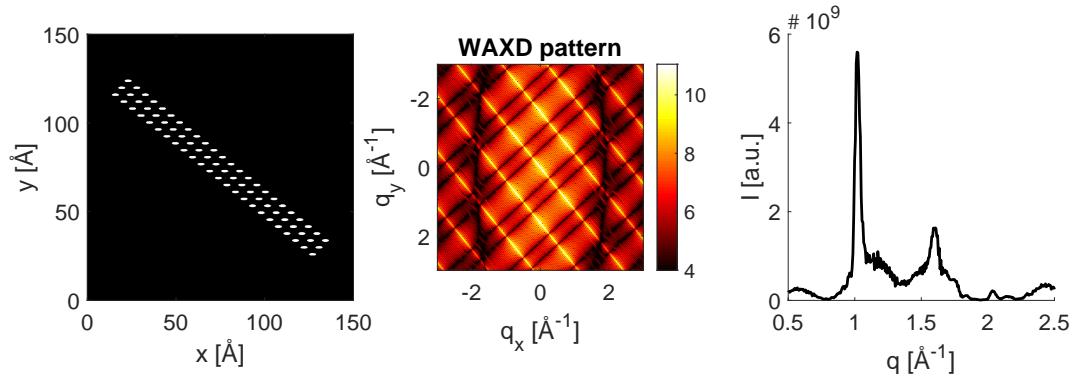
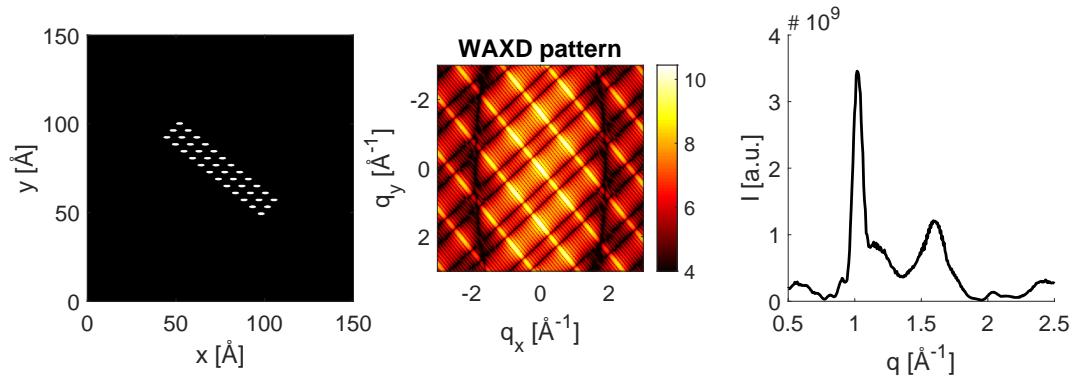
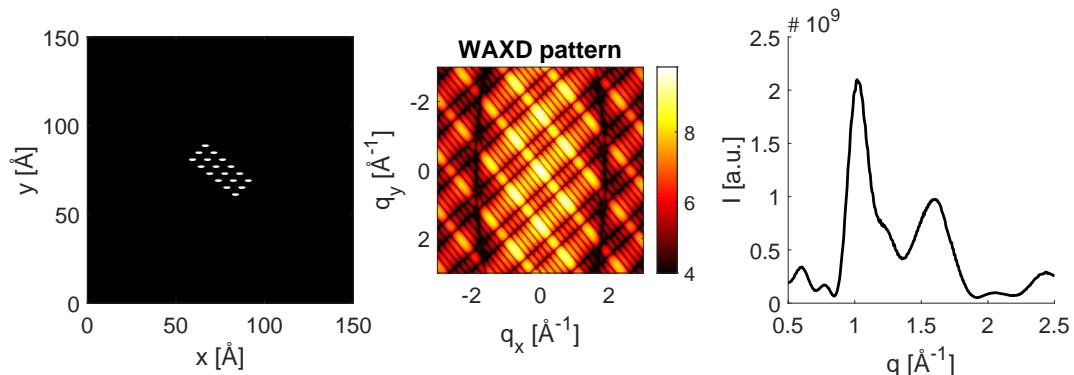
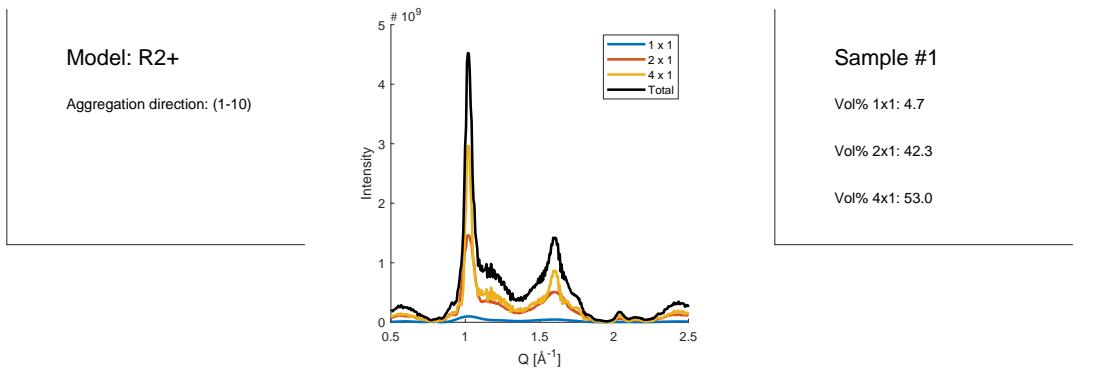
Vol% 4x1: 53.0

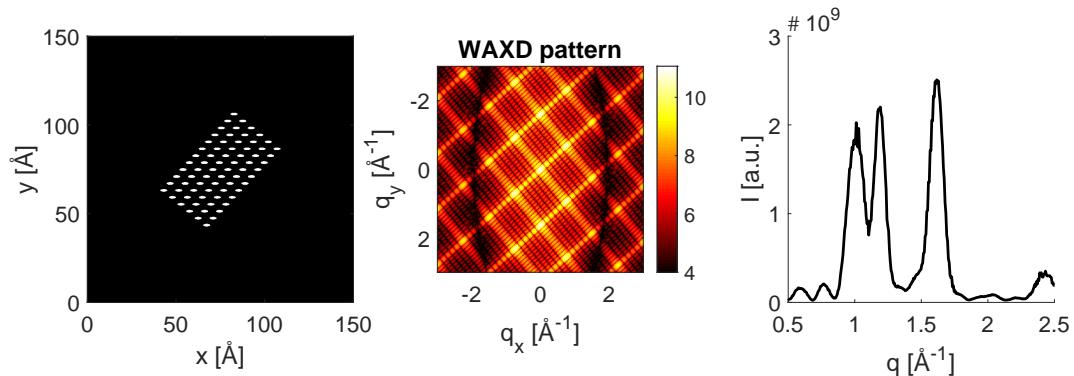
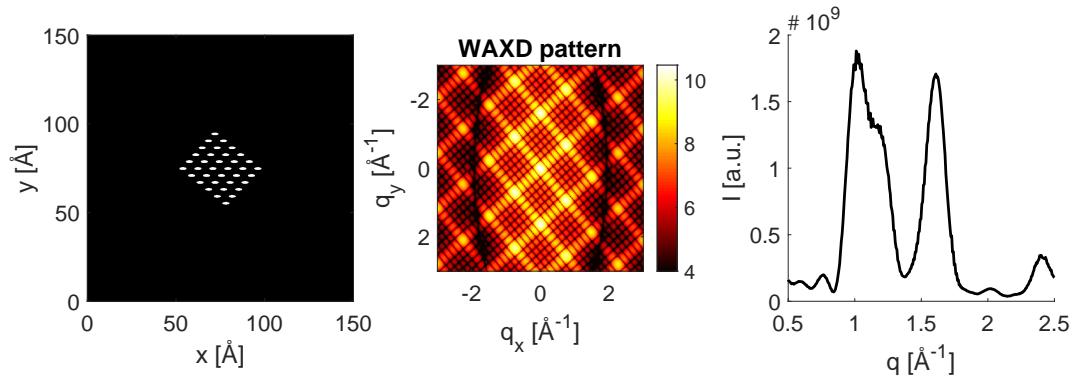
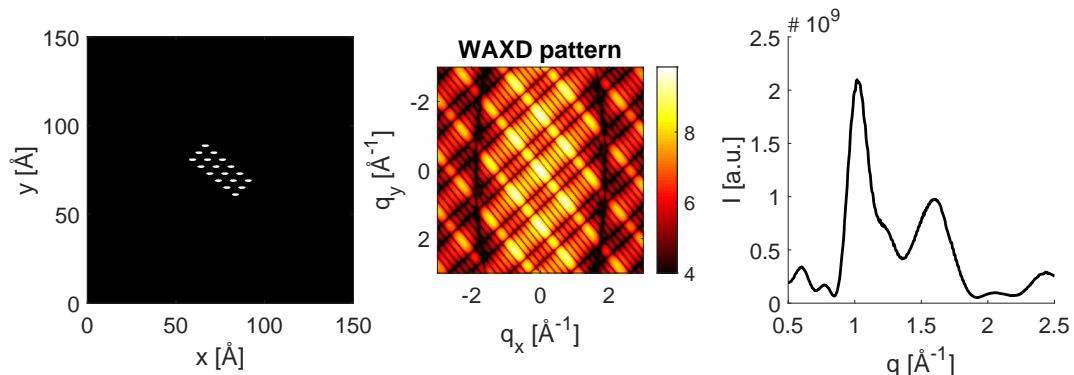
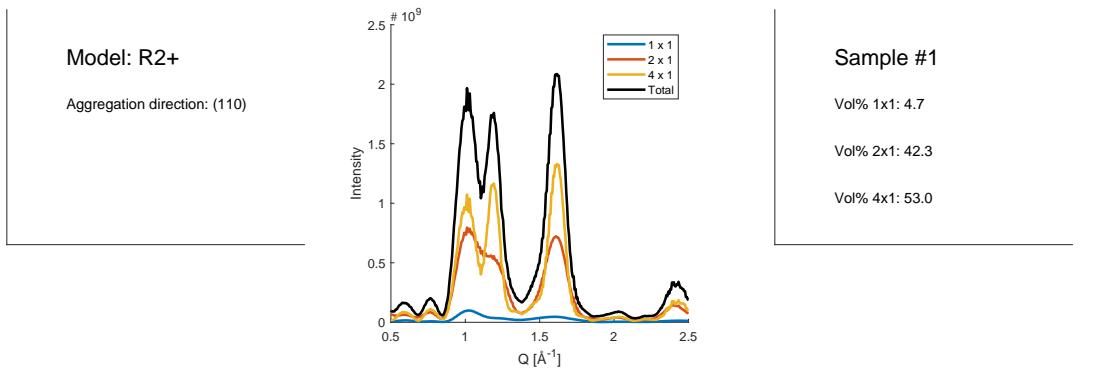


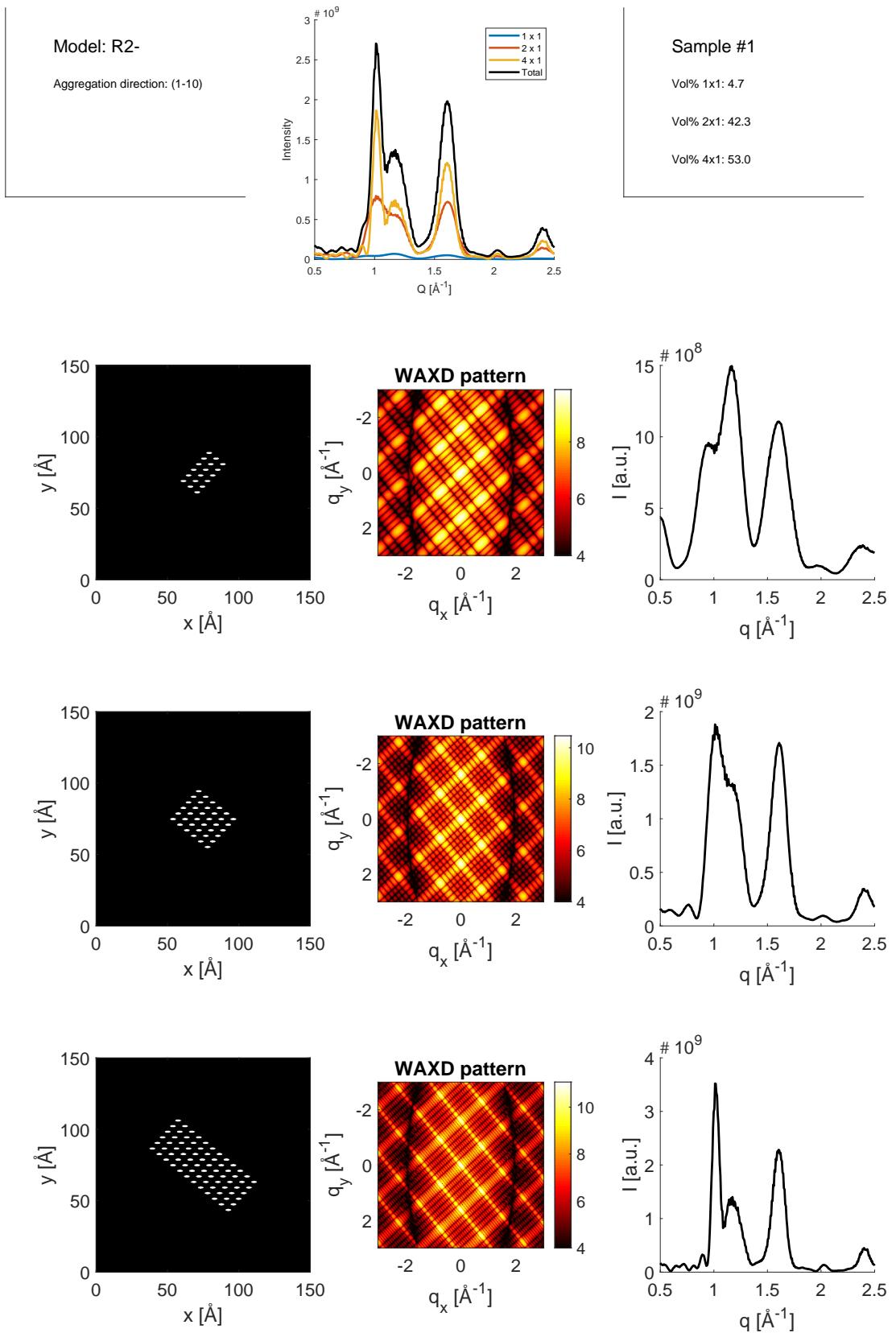


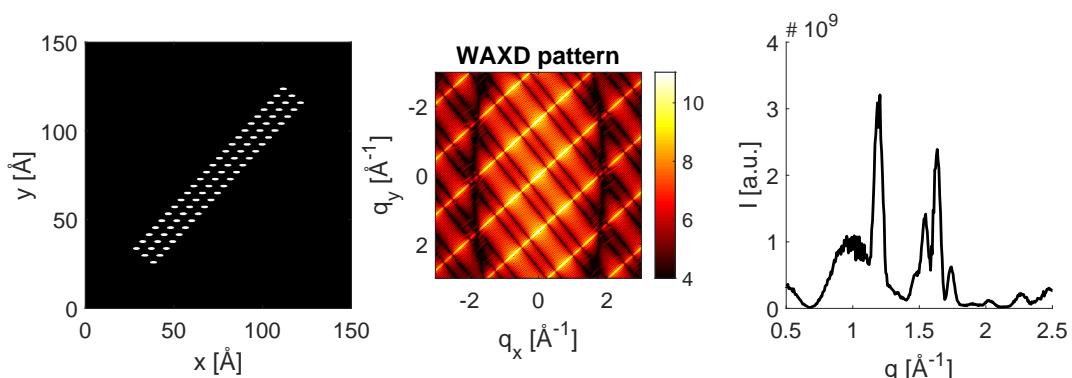
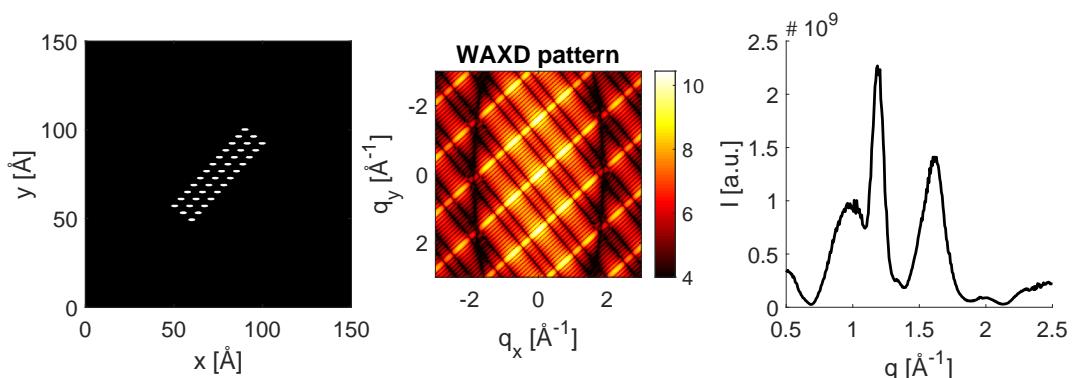
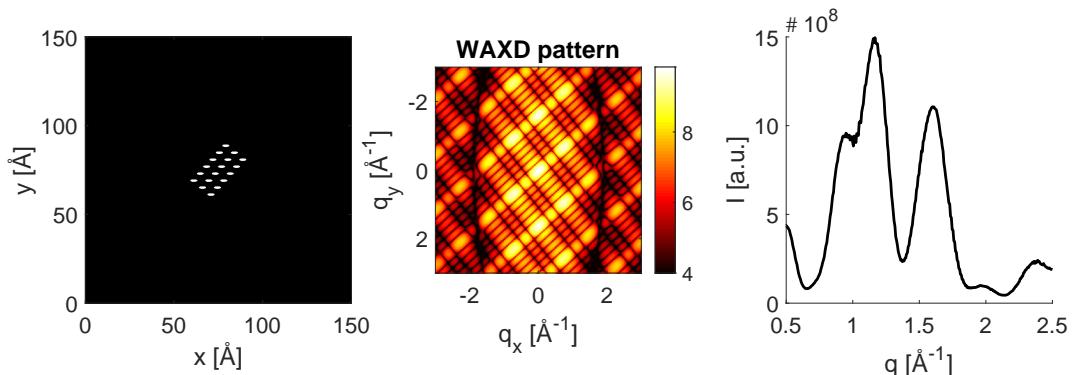
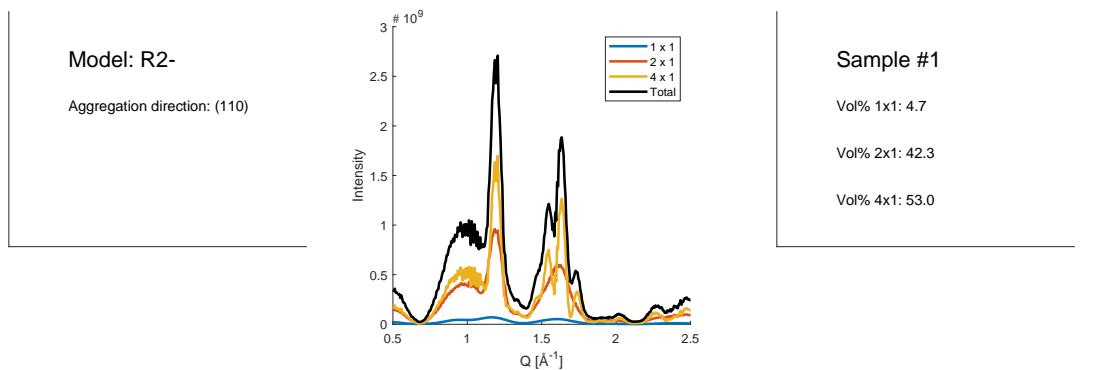


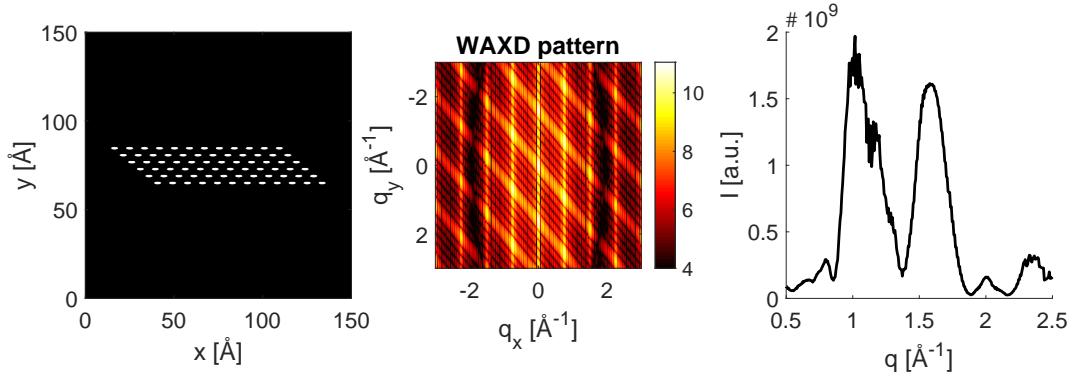
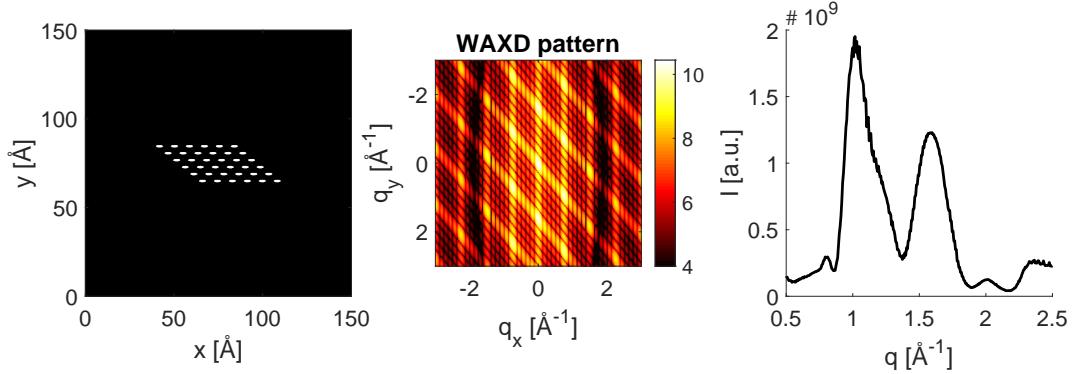
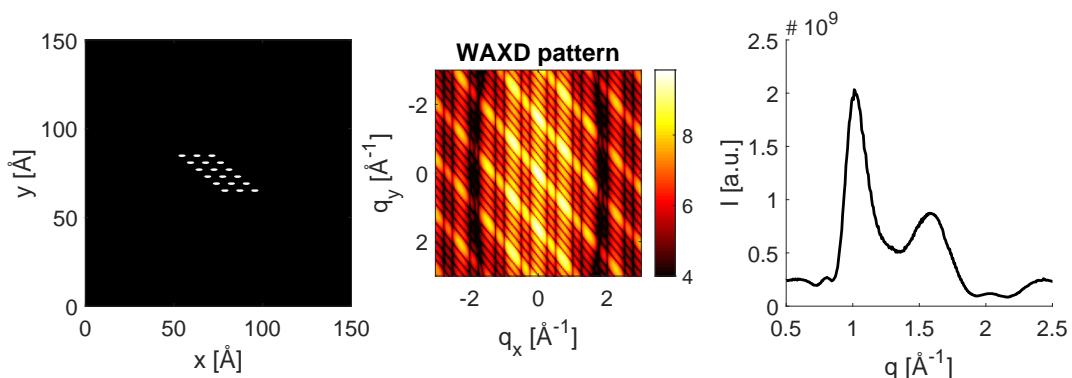
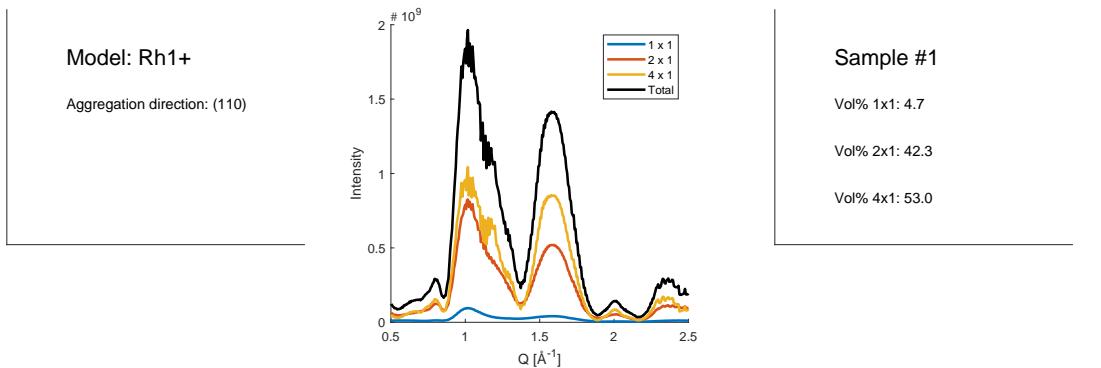


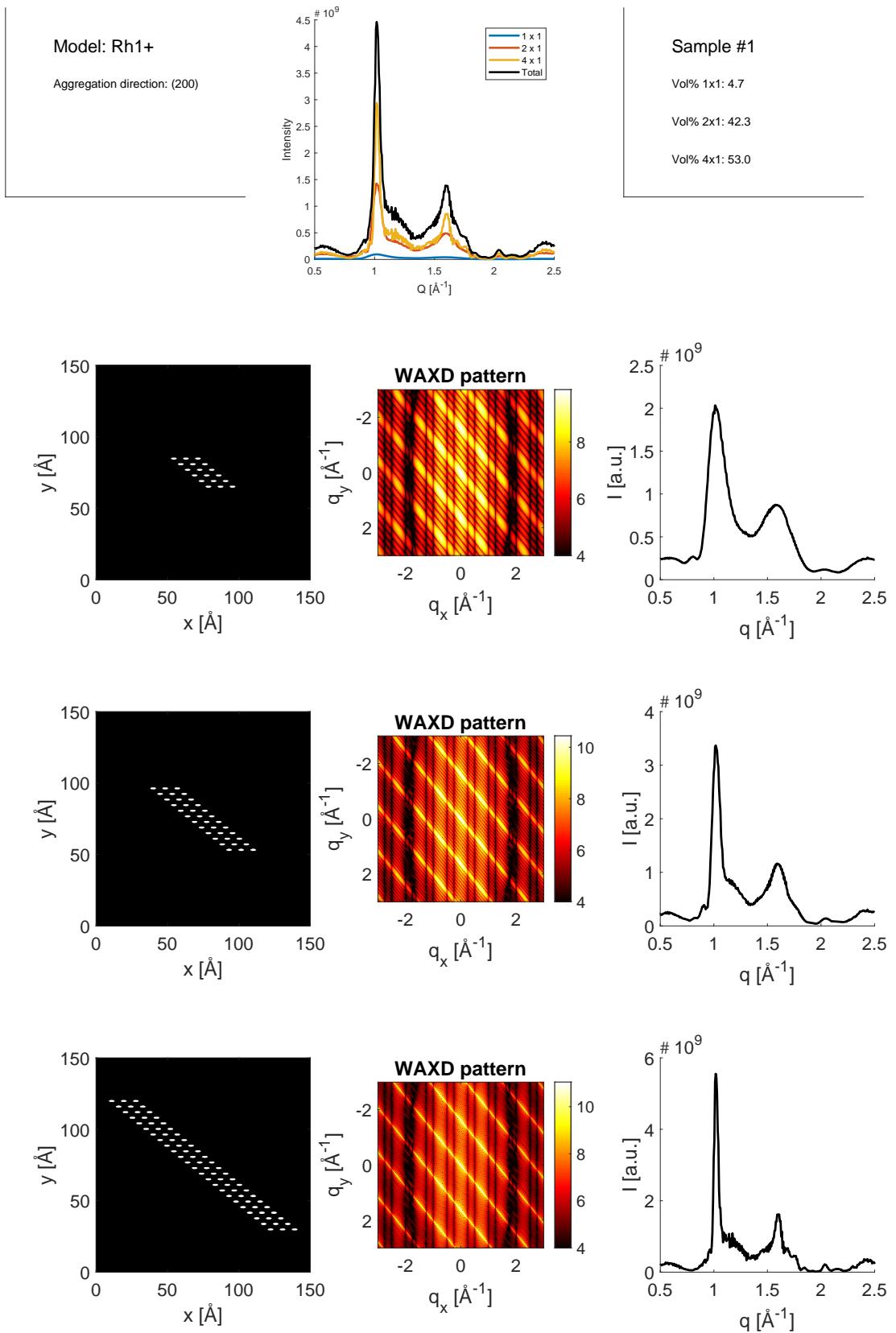


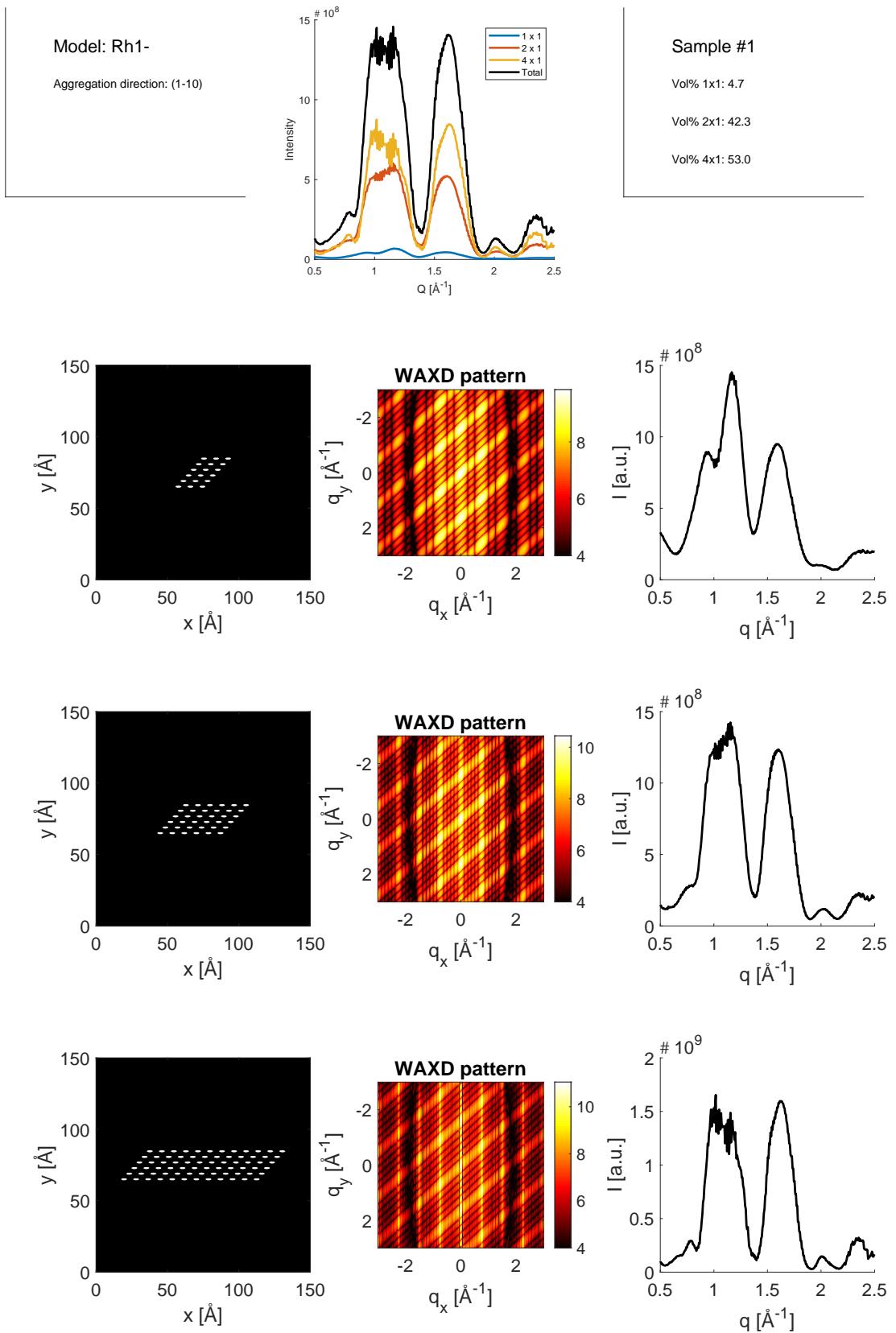


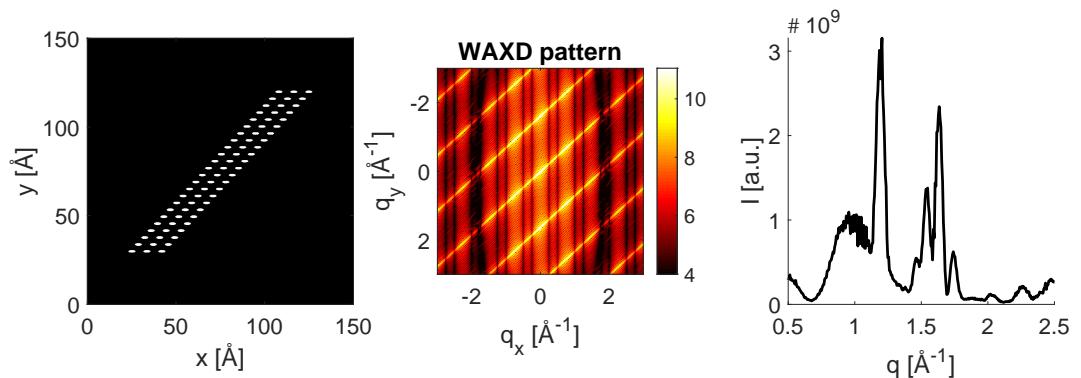
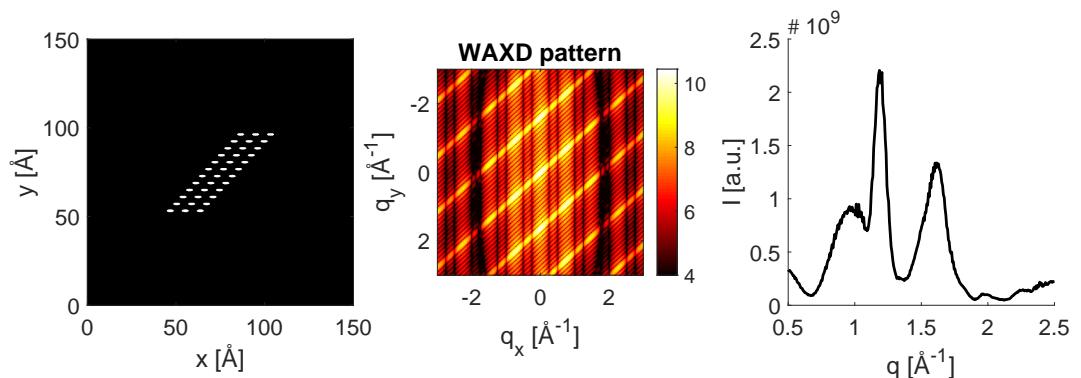
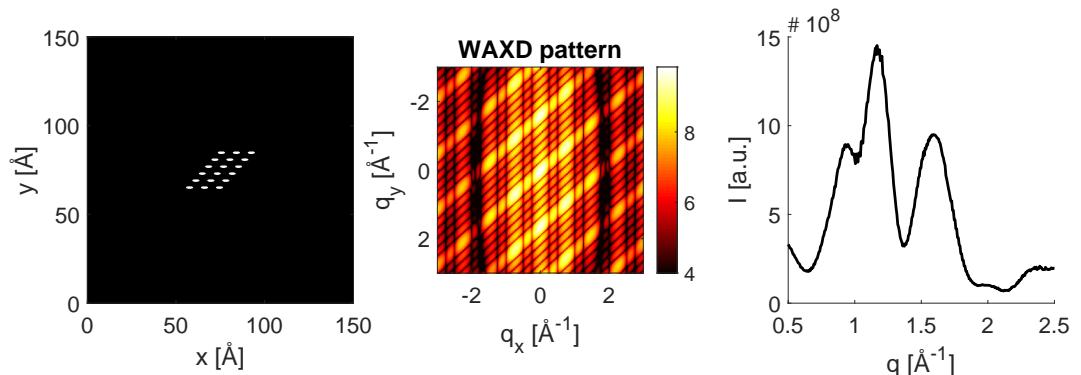
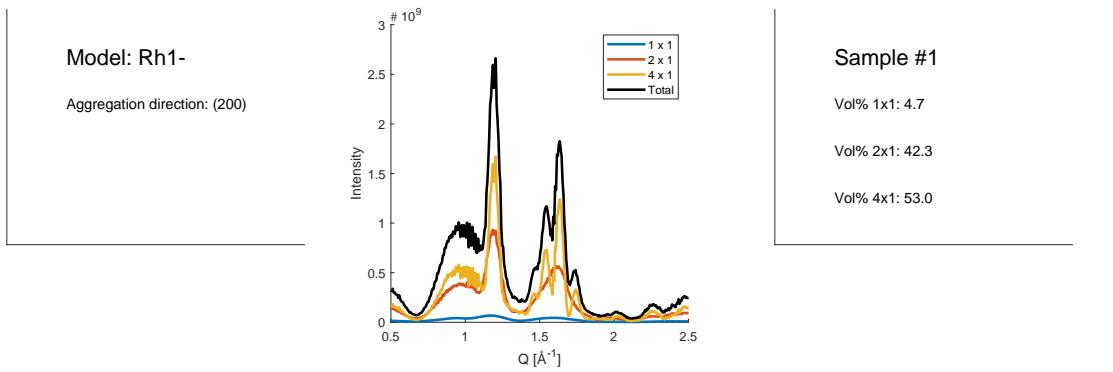


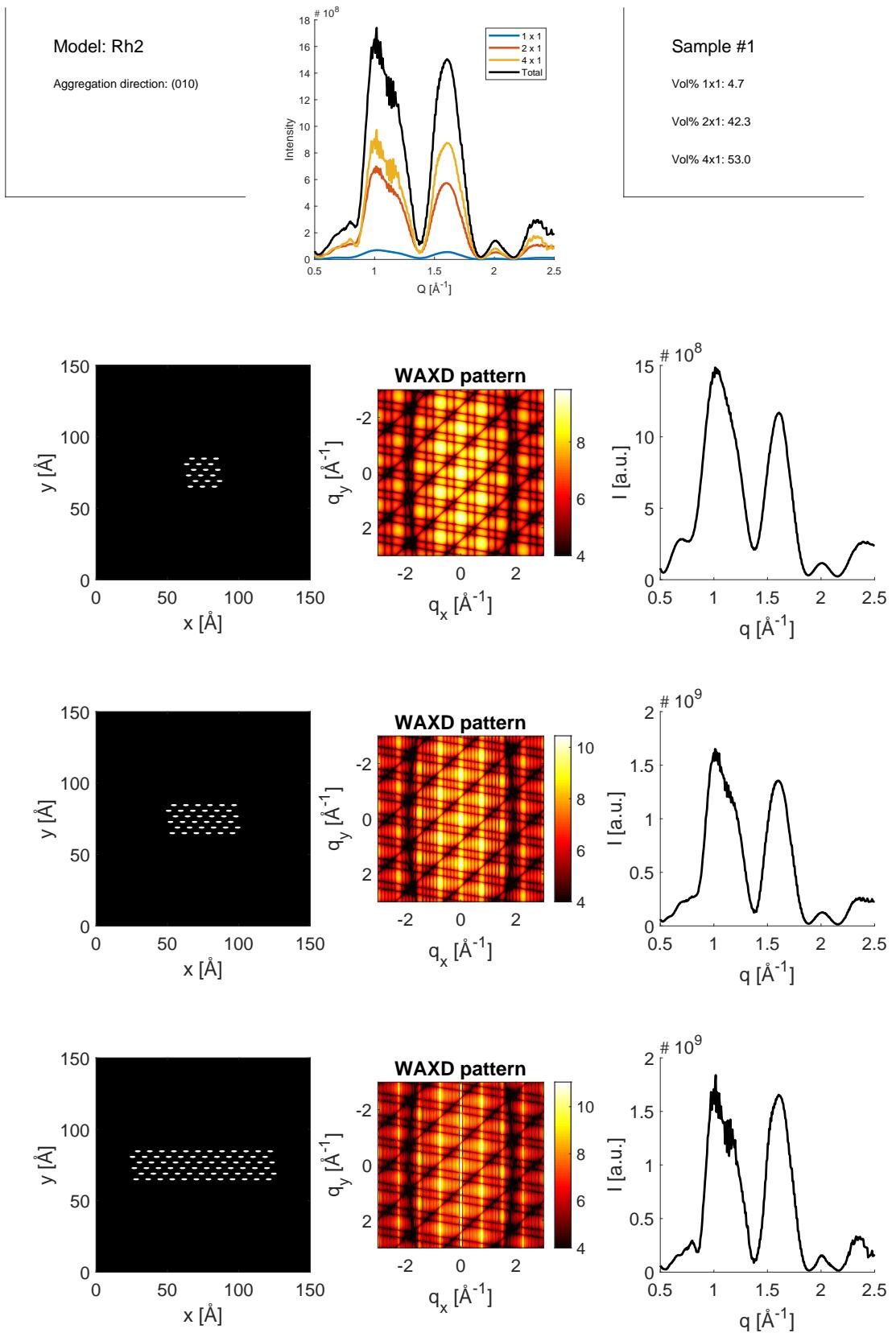


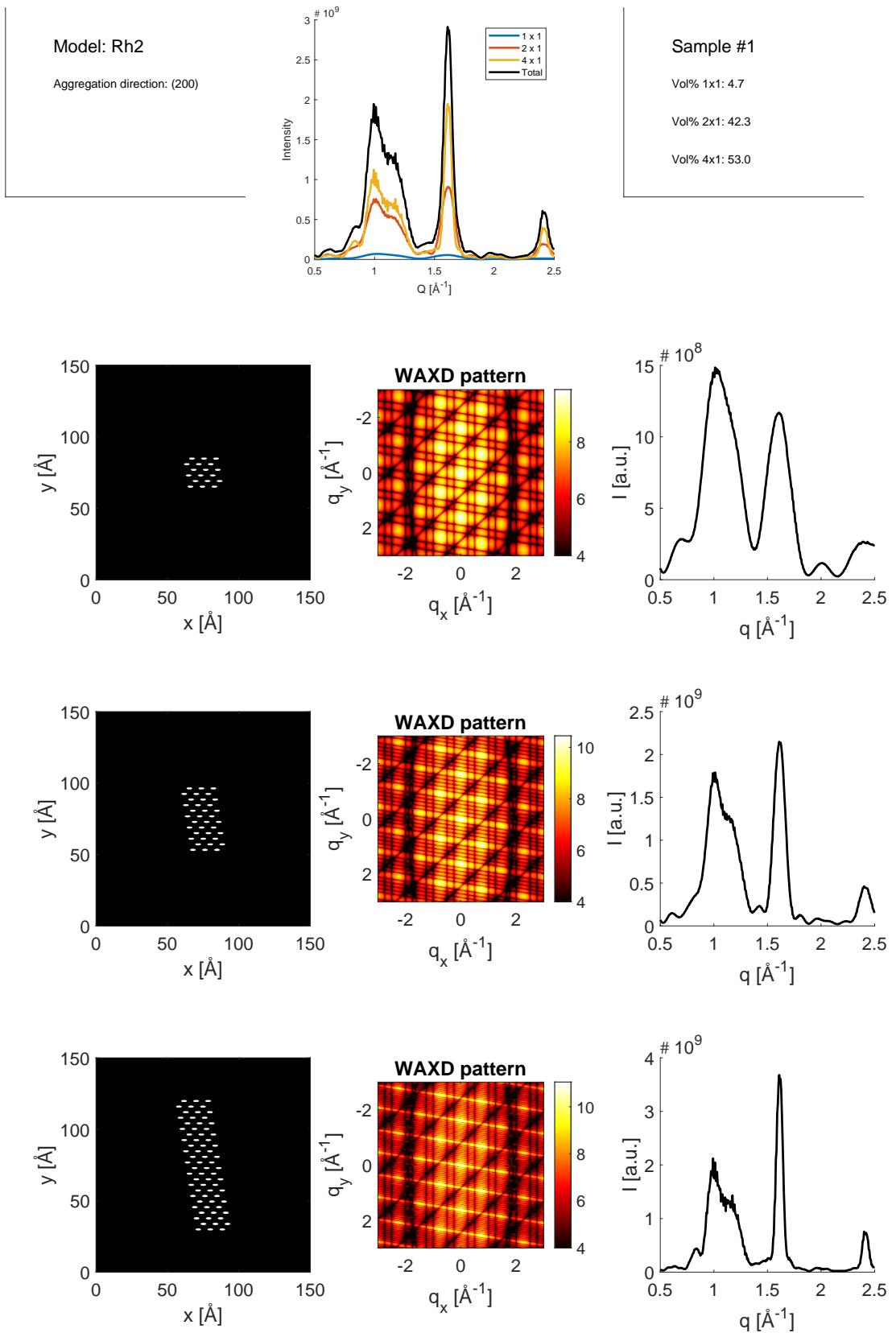


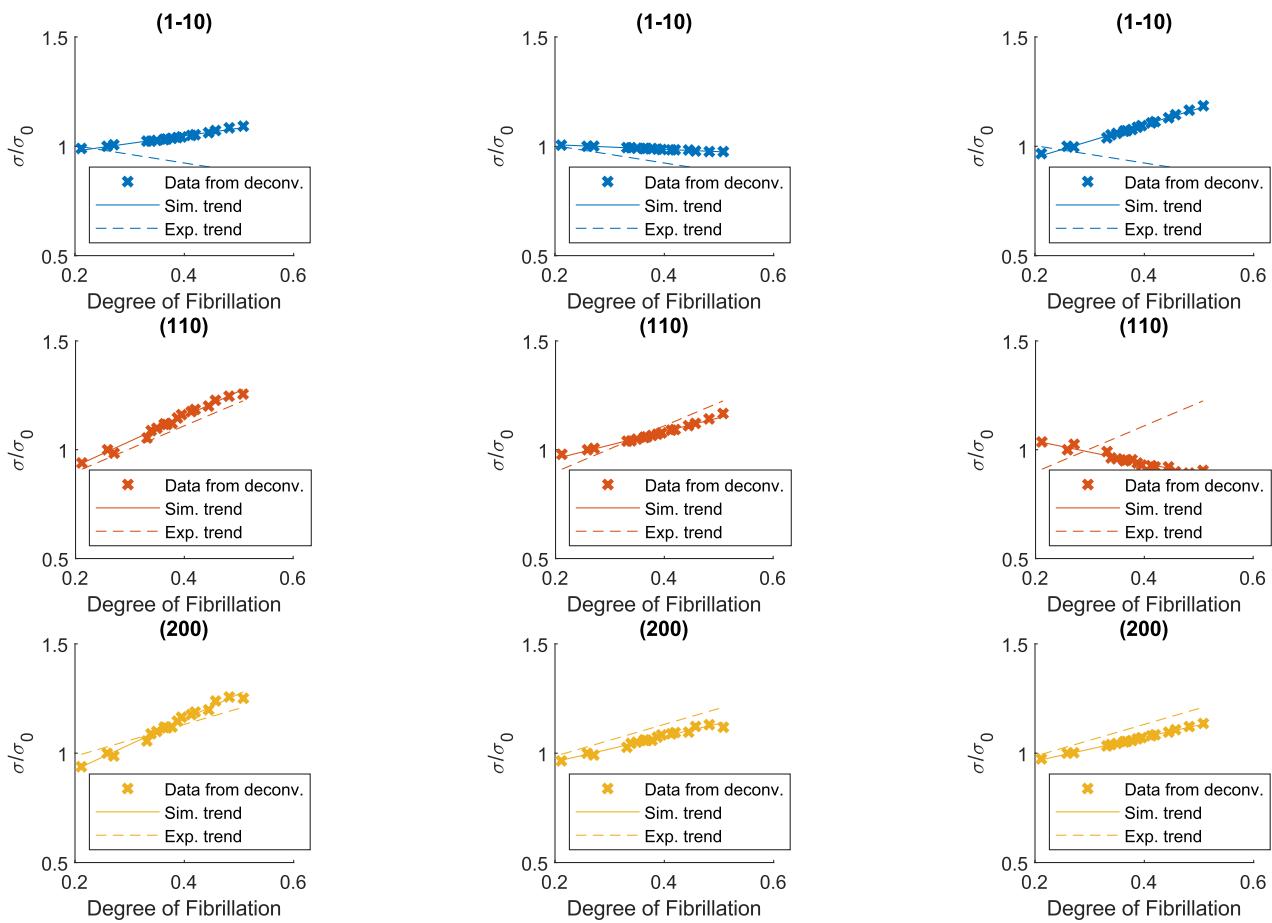
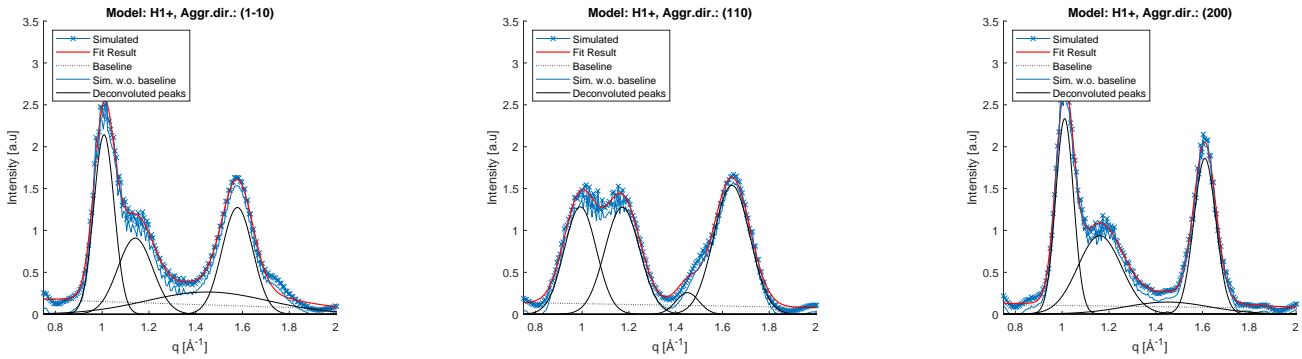


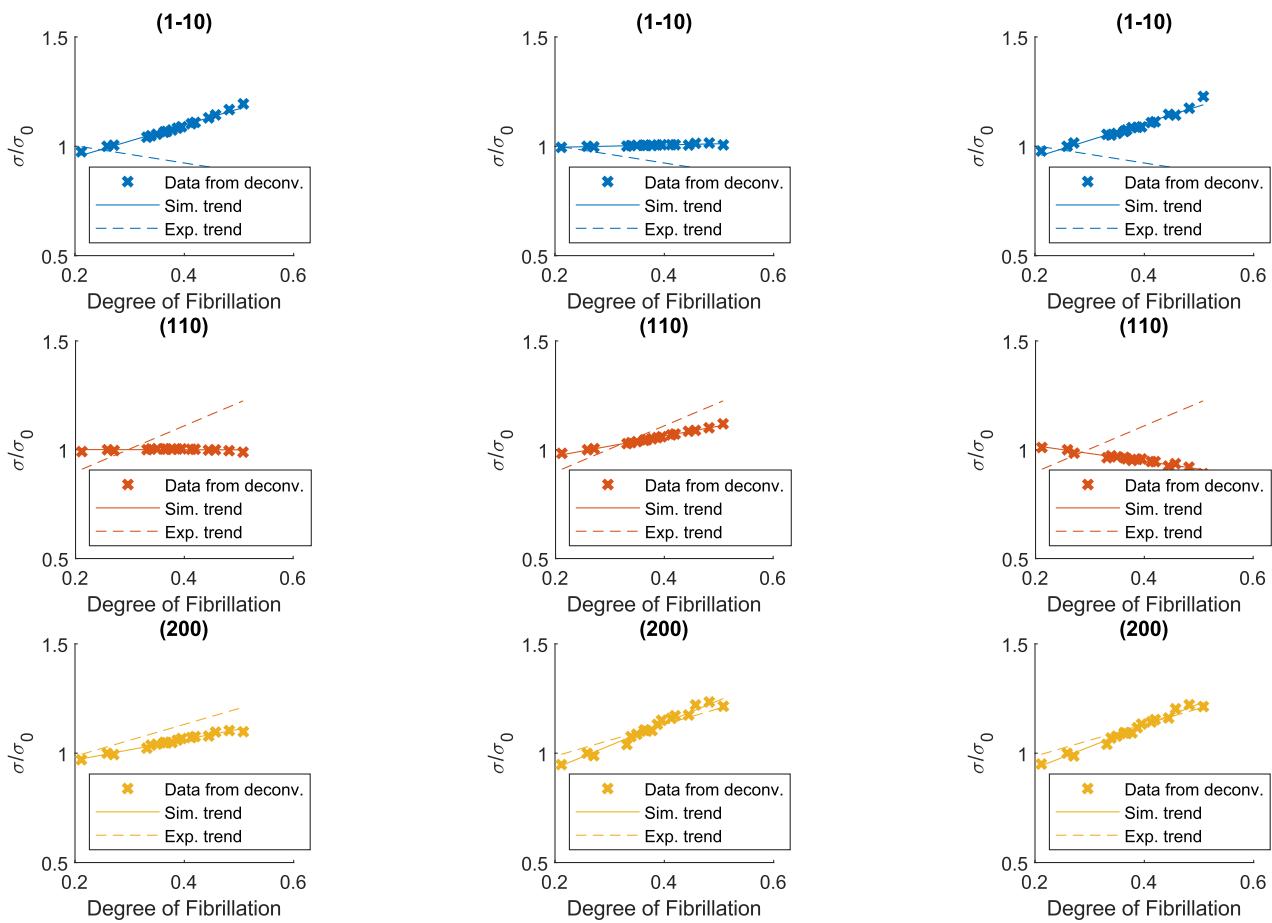
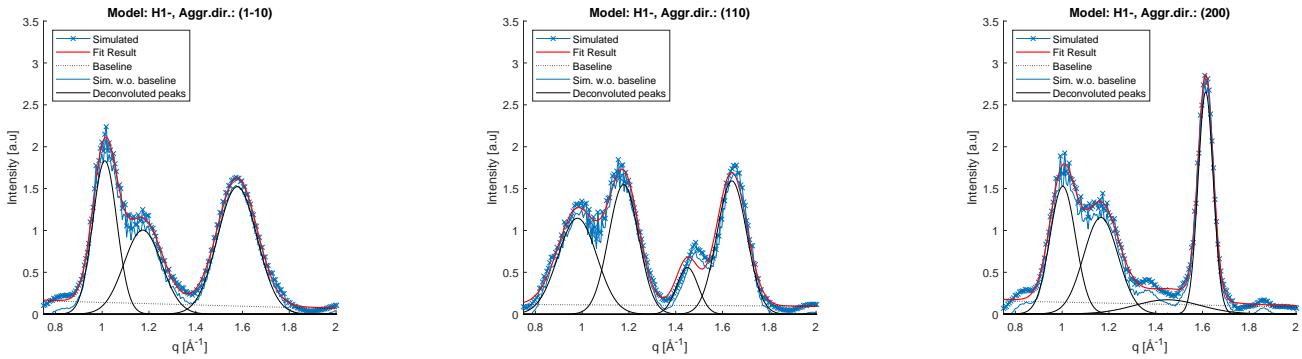


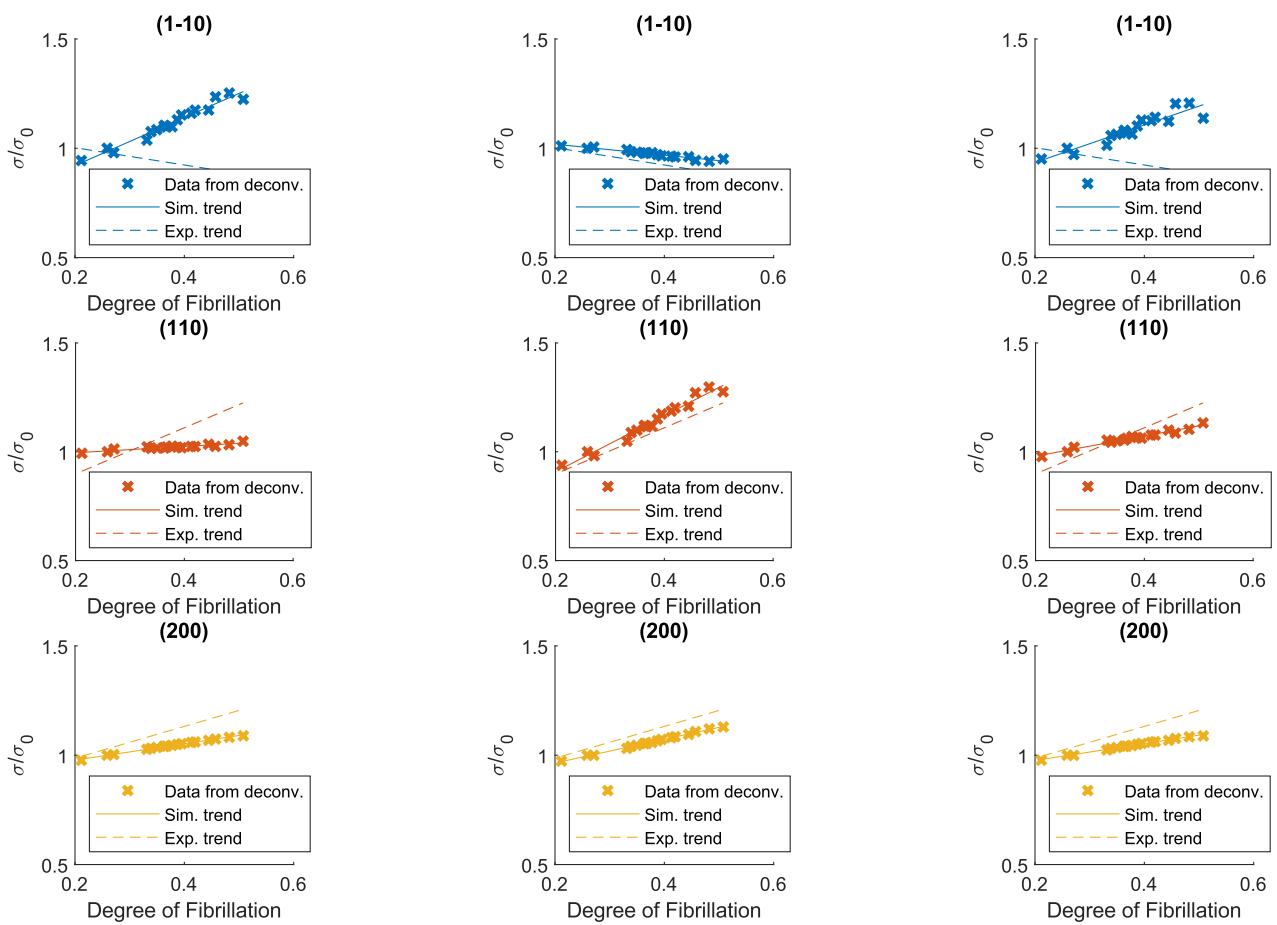
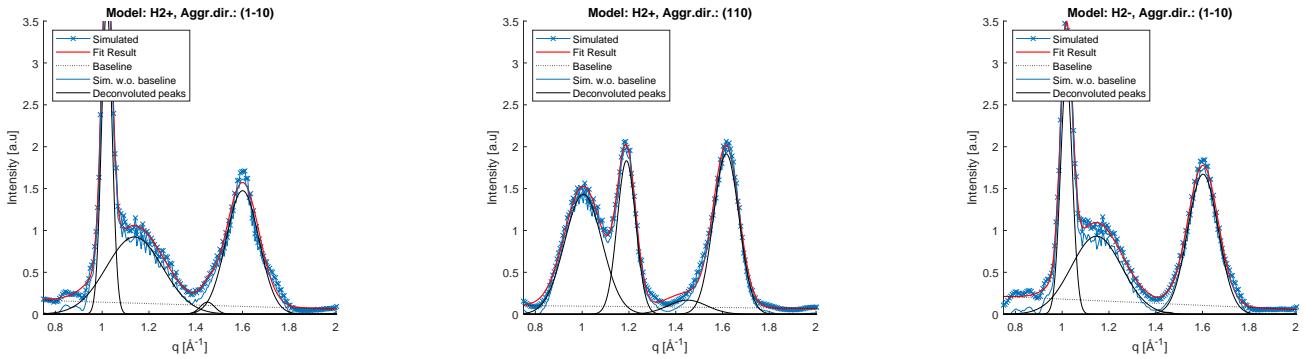


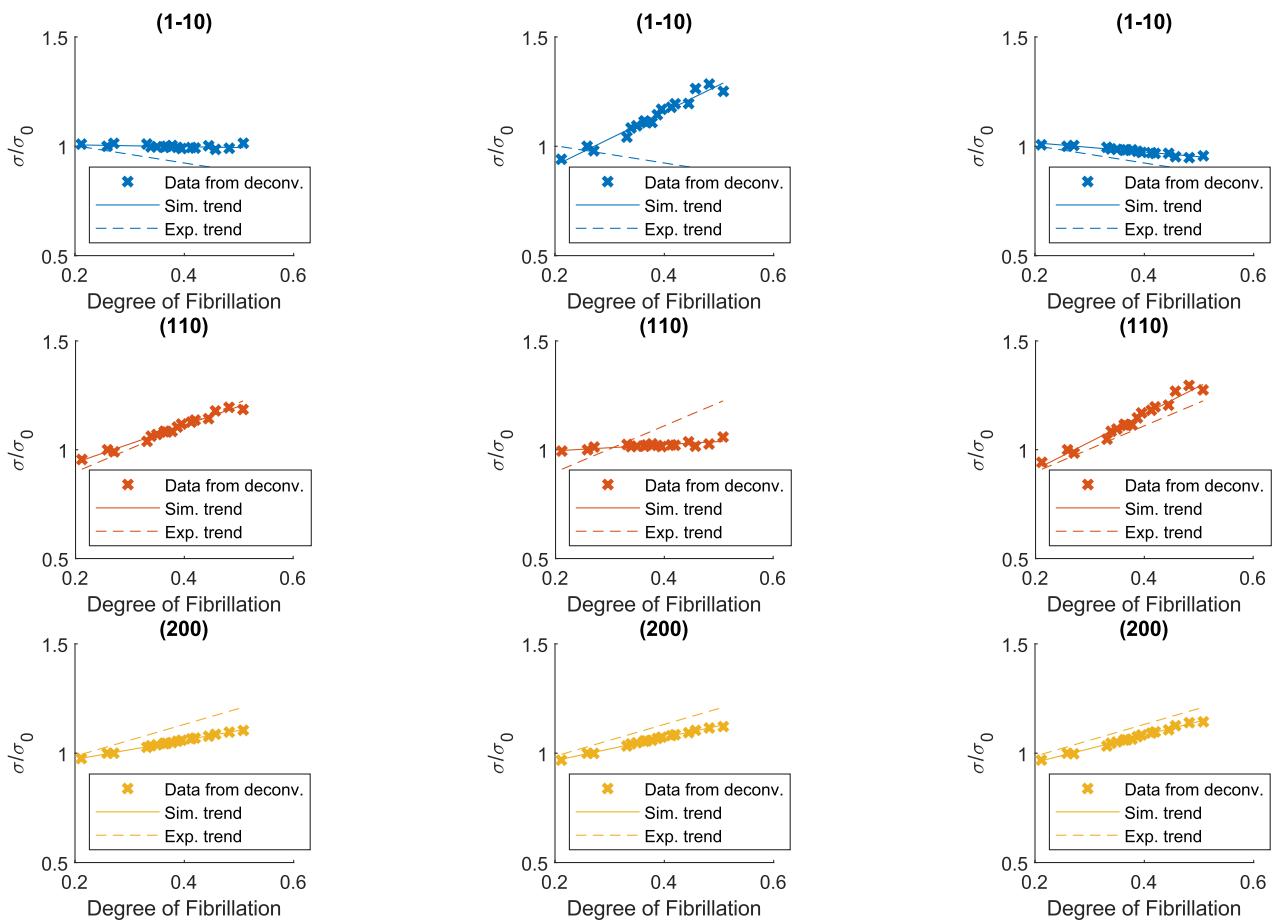
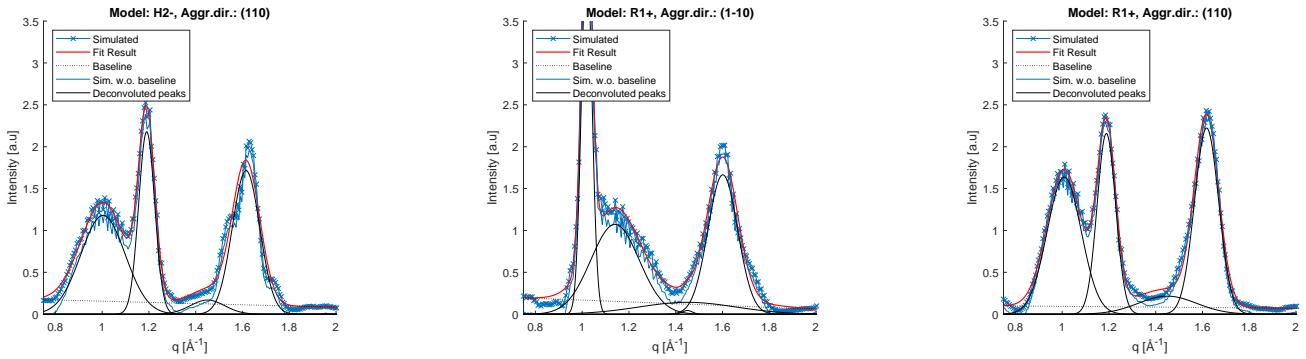


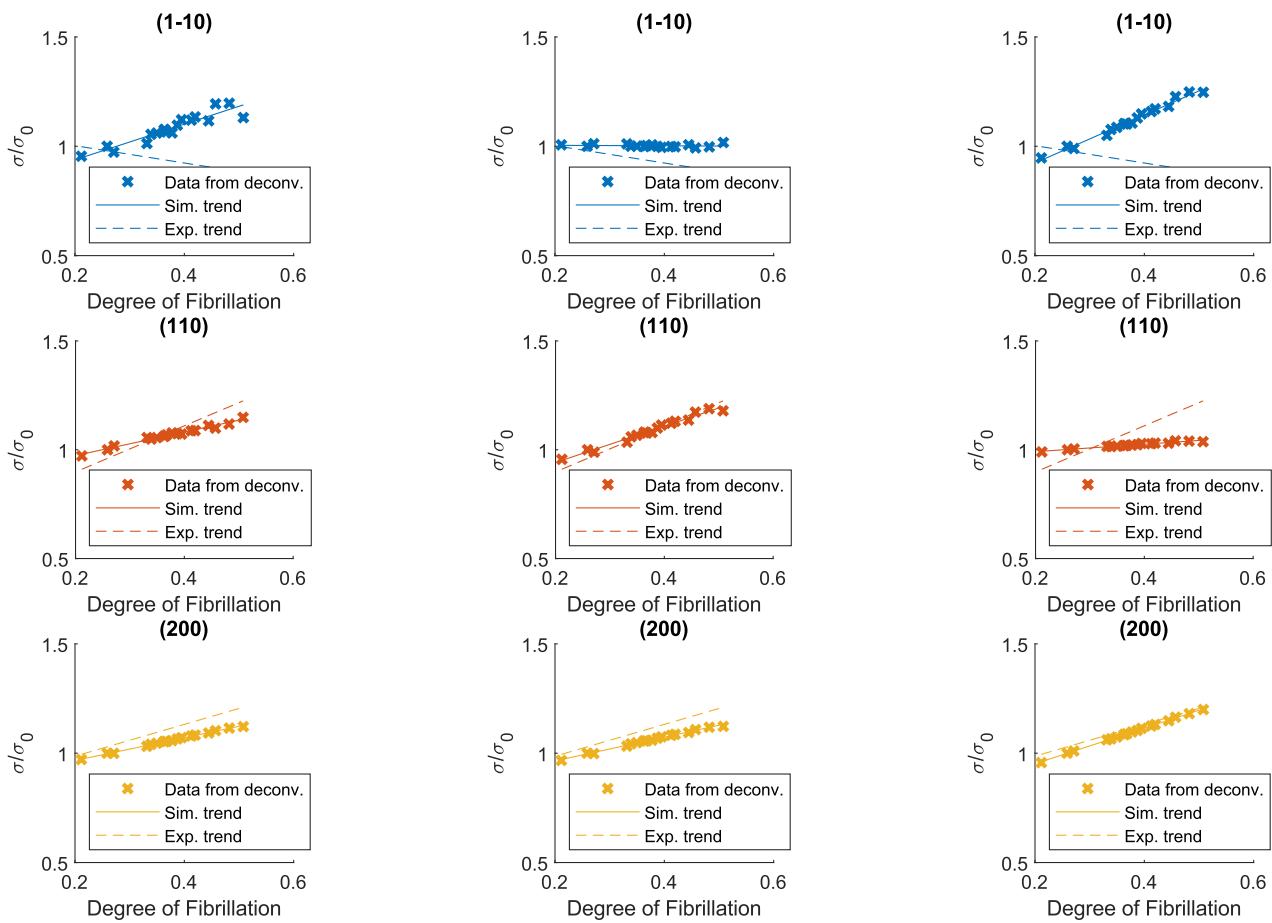
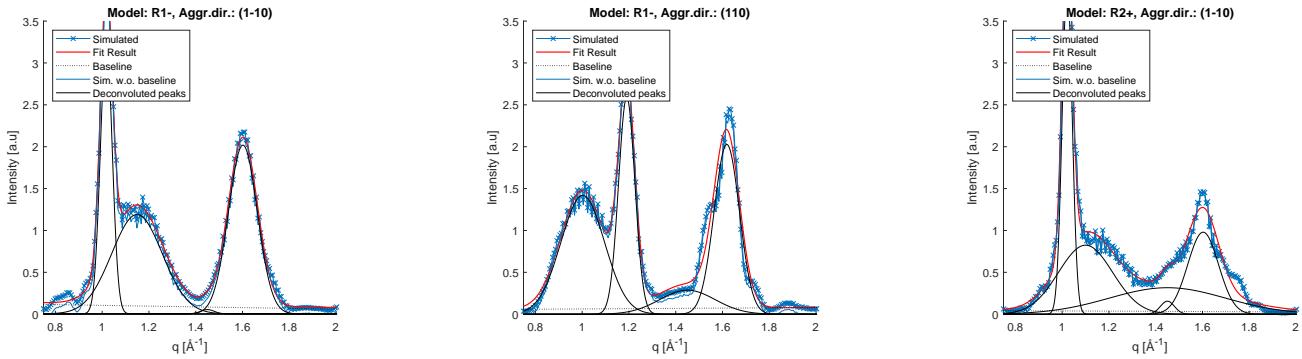


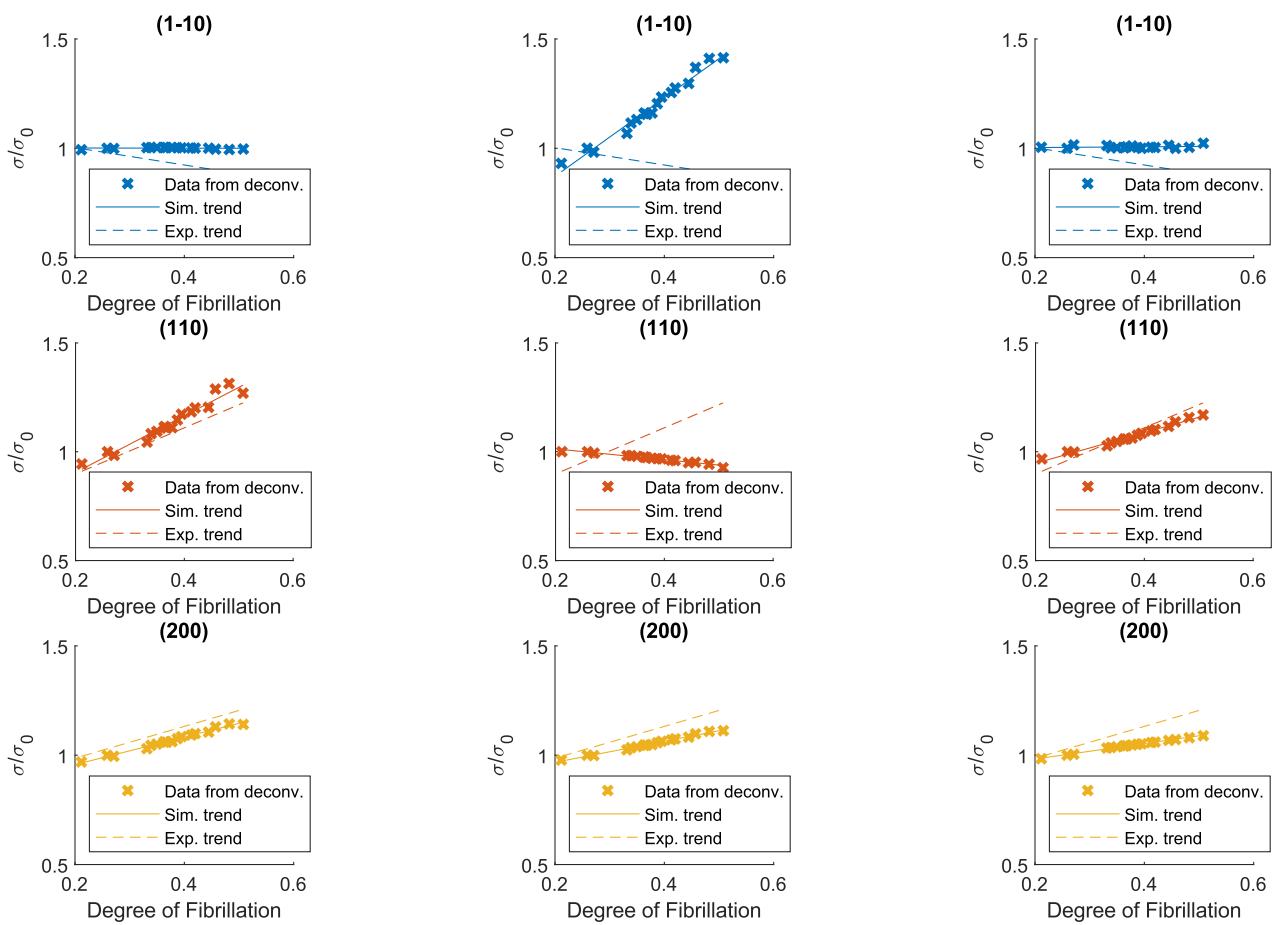
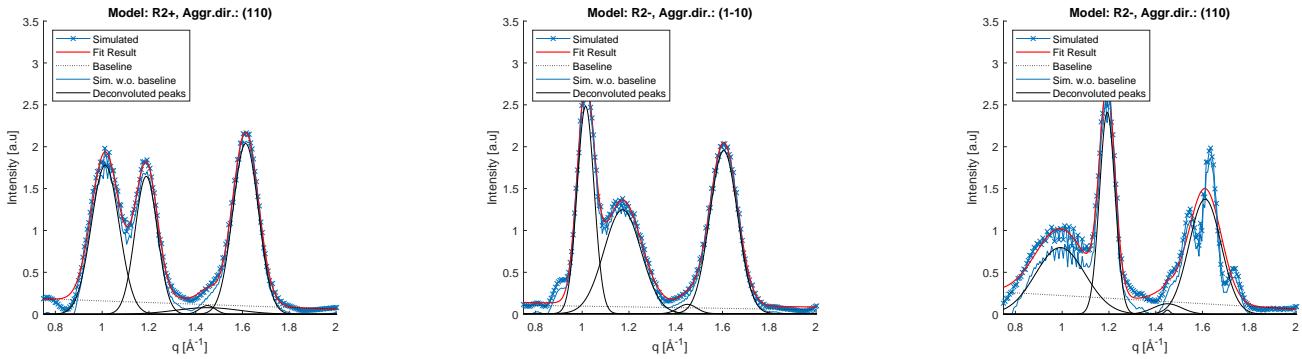


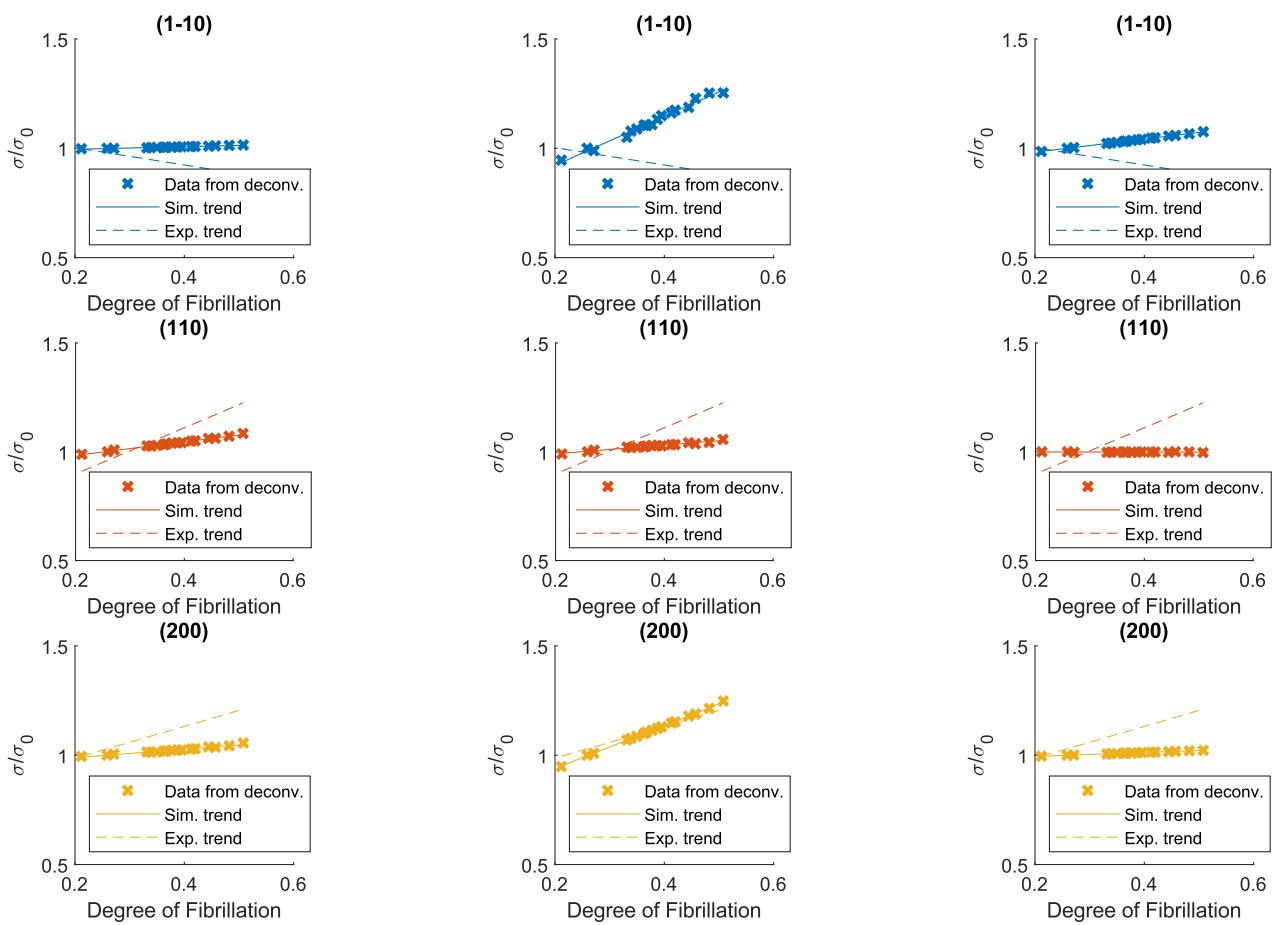
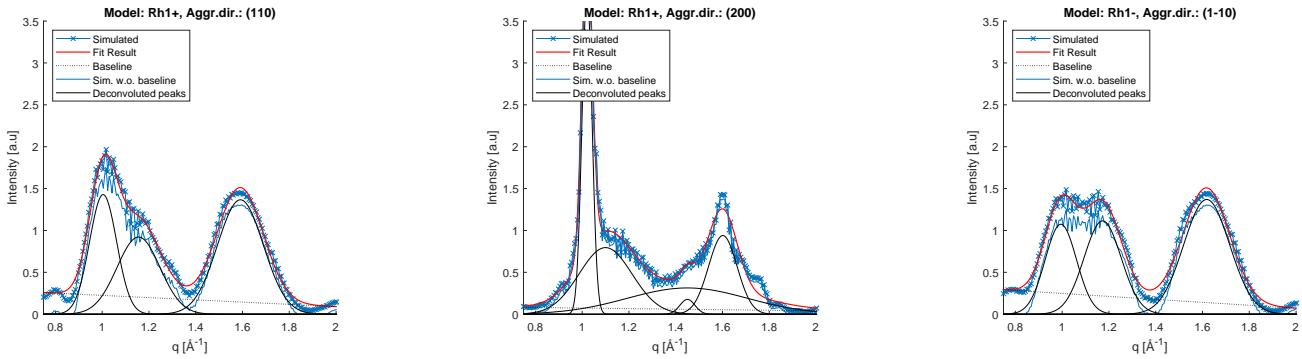


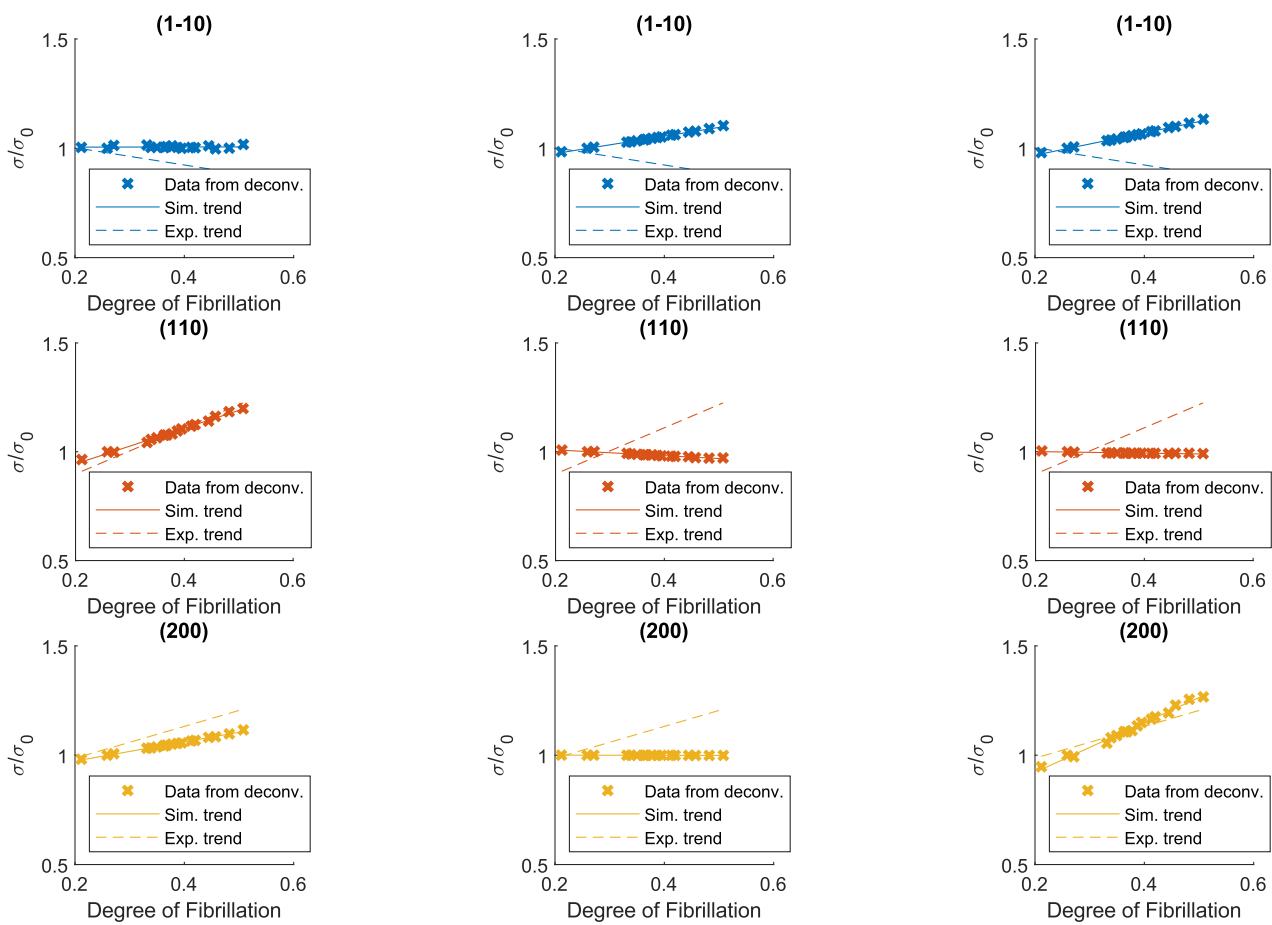
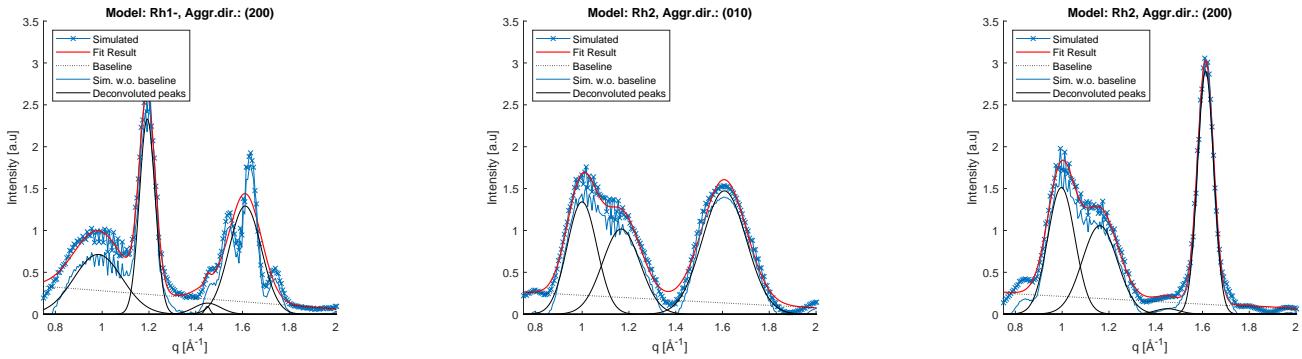




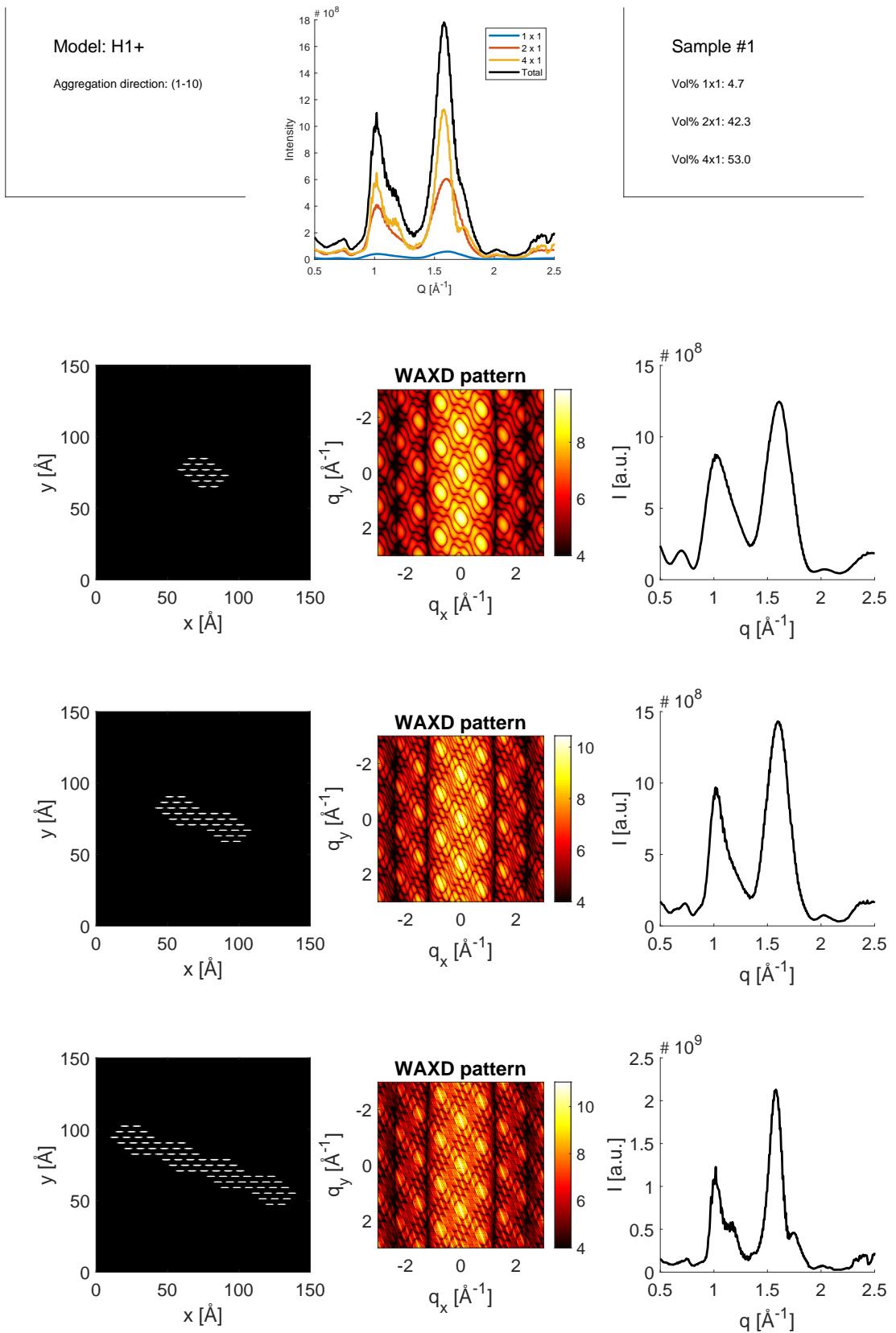


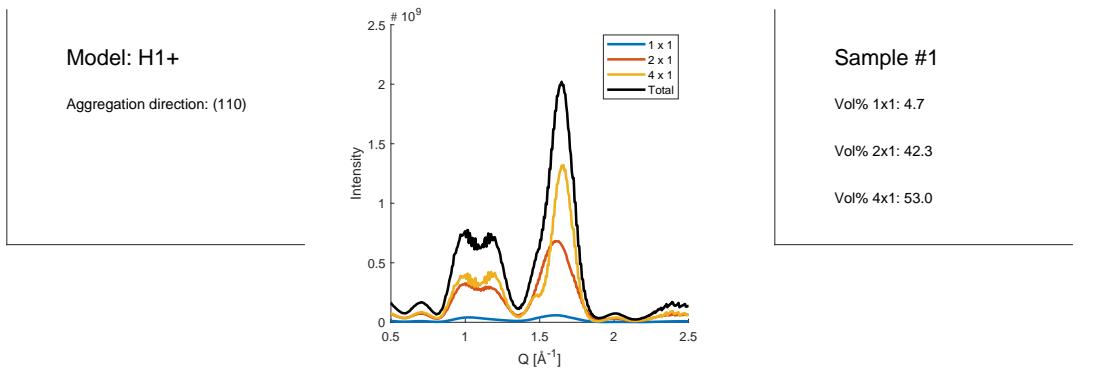






**WAXD simulations: Results**  
**Form factor of a CNF chain with semi-axes**  
**3 Å x 0.5 Å**



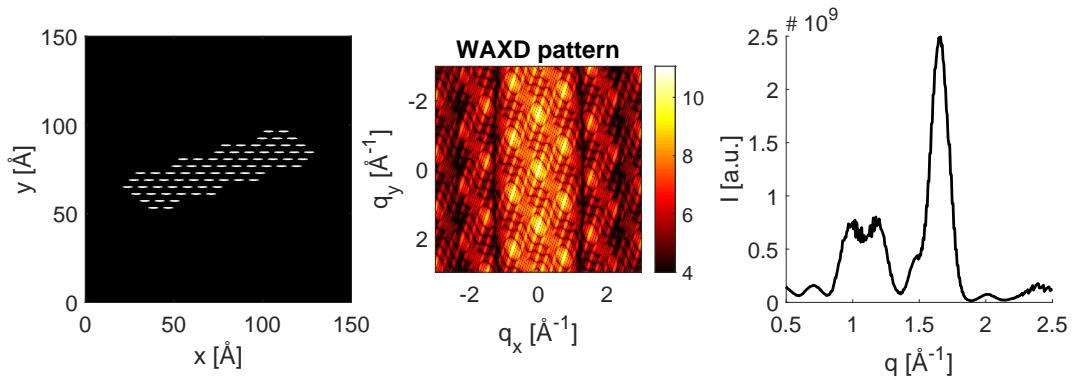
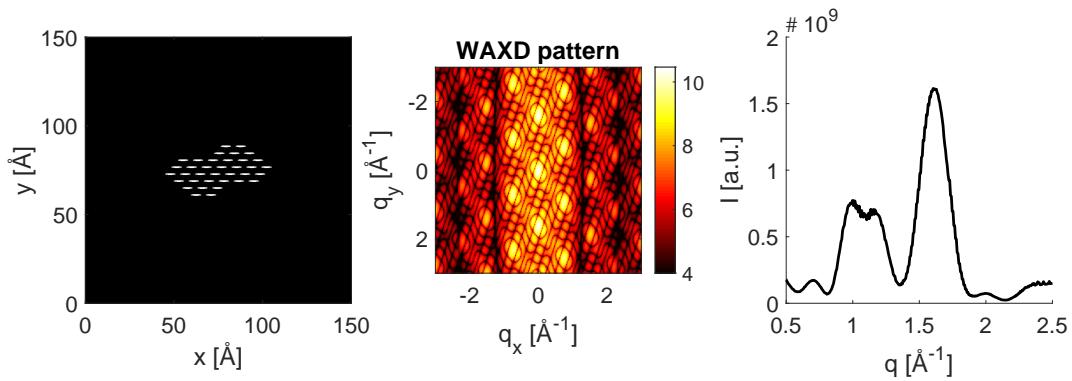
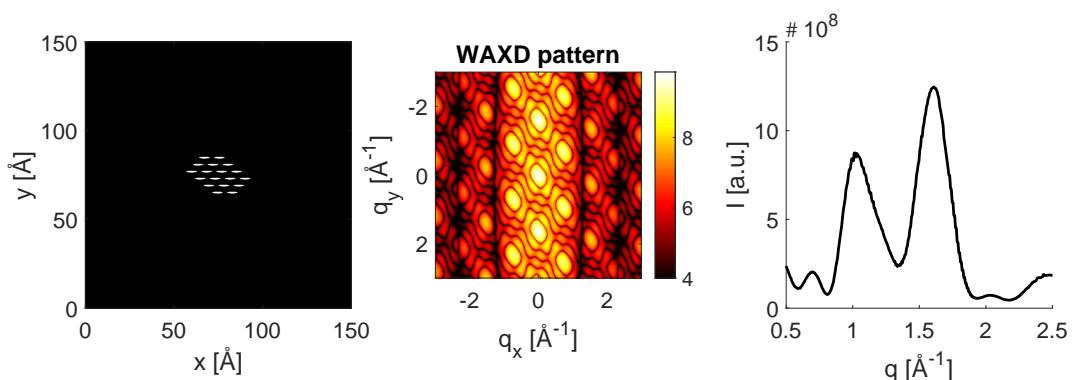


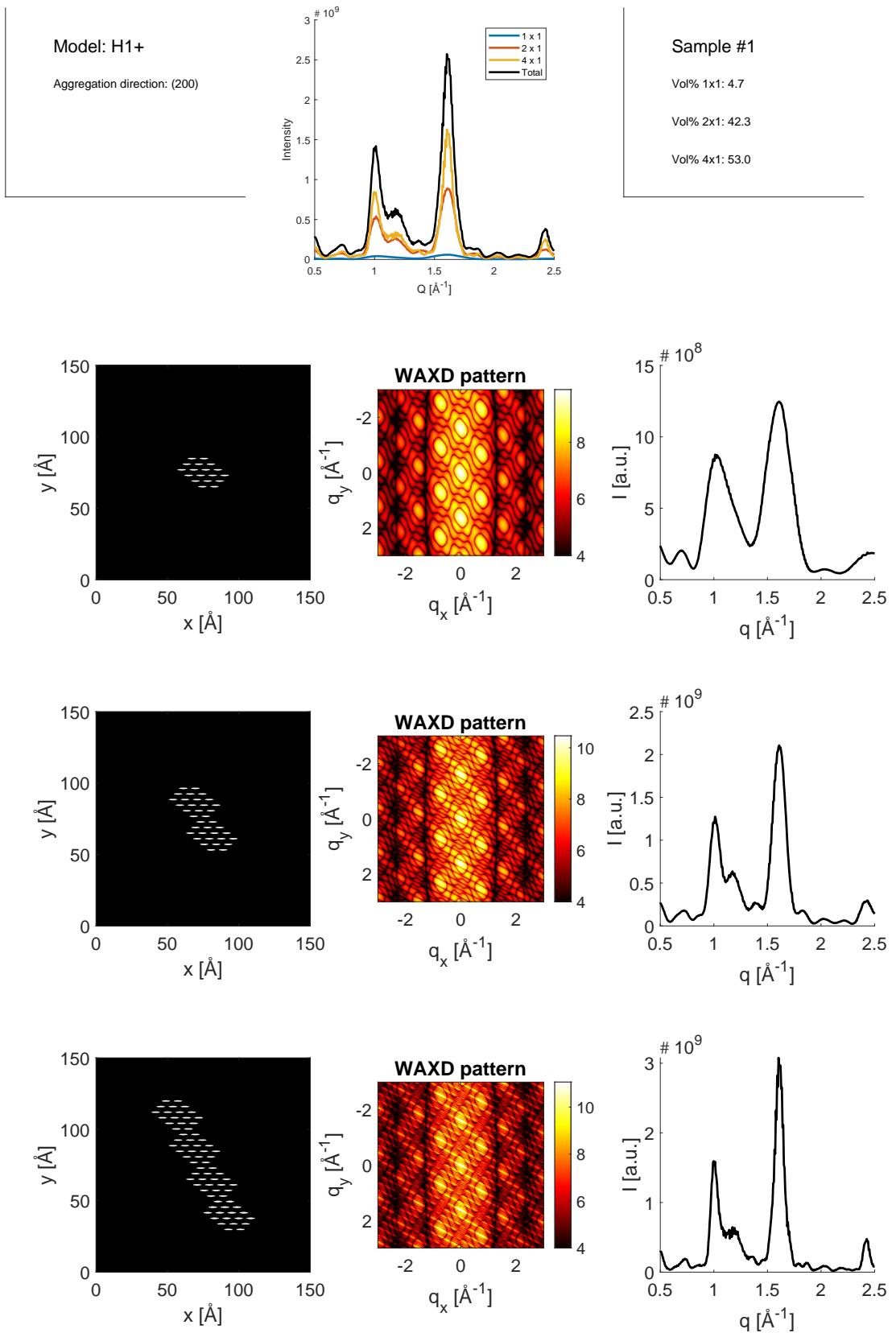
**Sample #1**

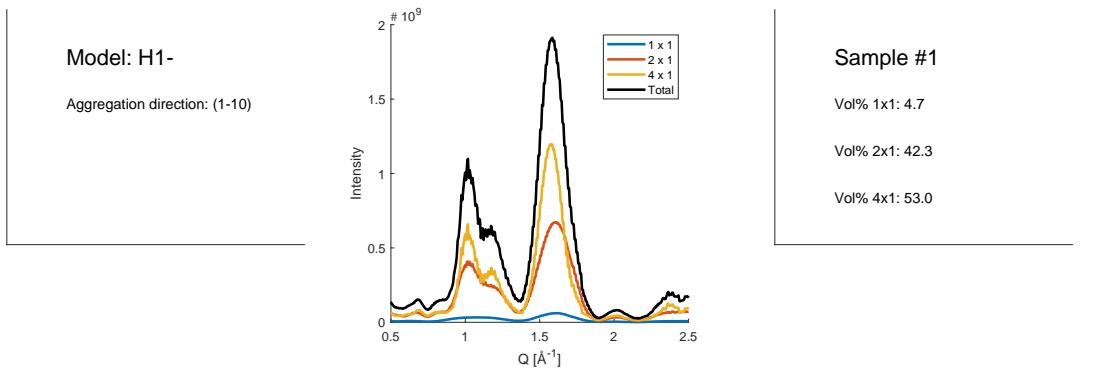
Vol% 1x1: 4.7

Vol% 2x1: 42.3

Vol% 4x1: 53.0





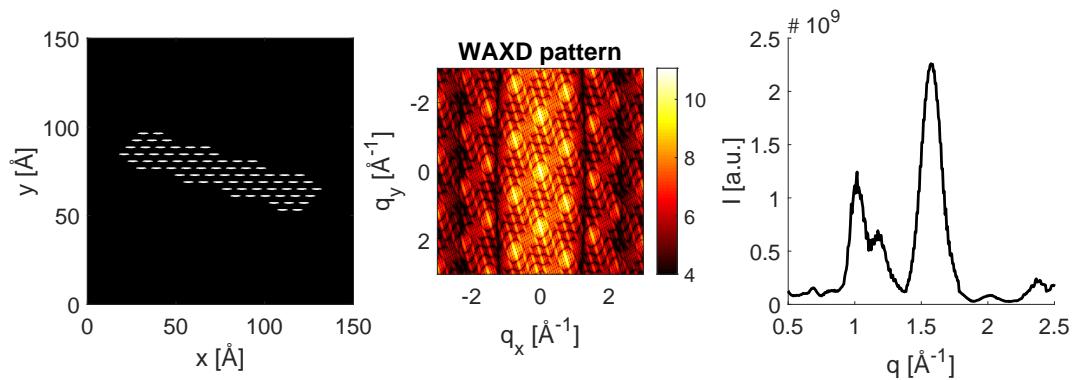
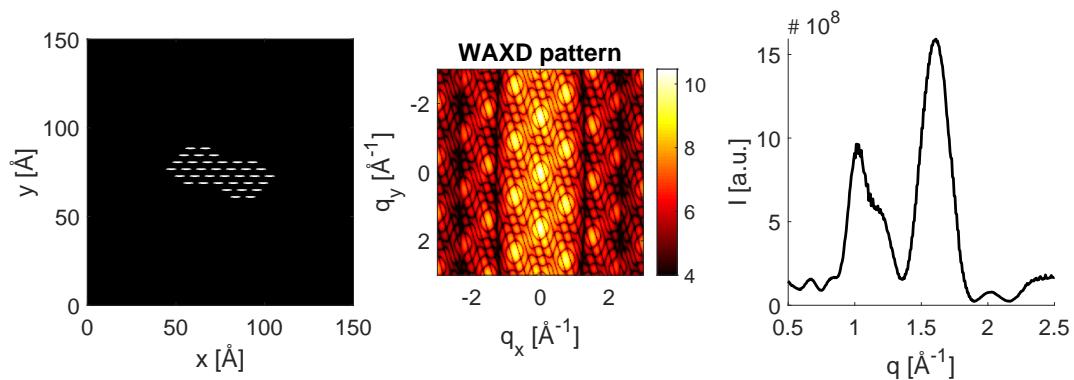
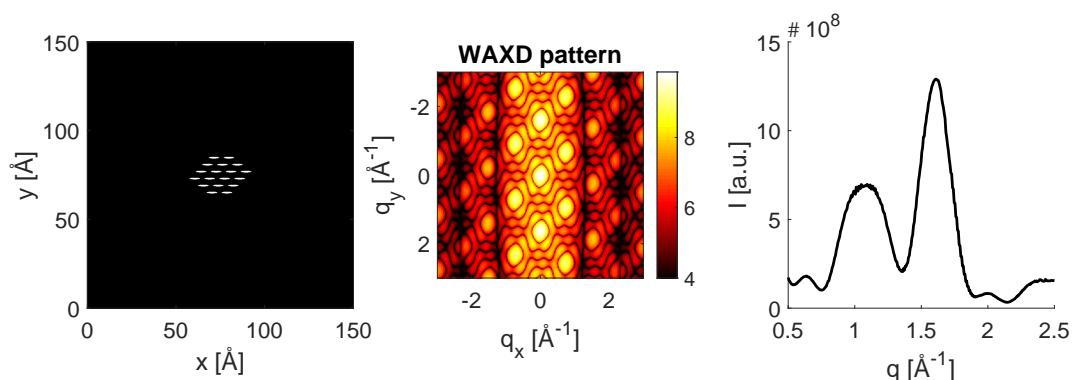


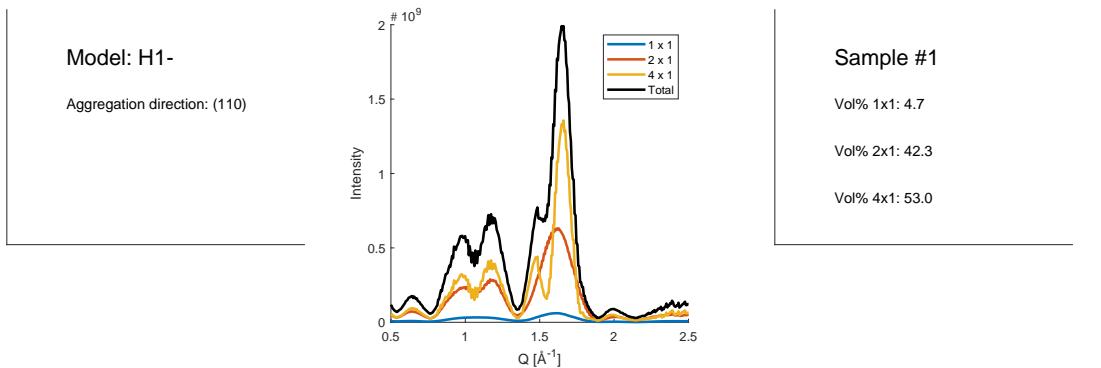
**Sample #1**

Vol% 1x1: 4.7

Vol% 2x1: 42.3

Vol% 4x1: 53.0



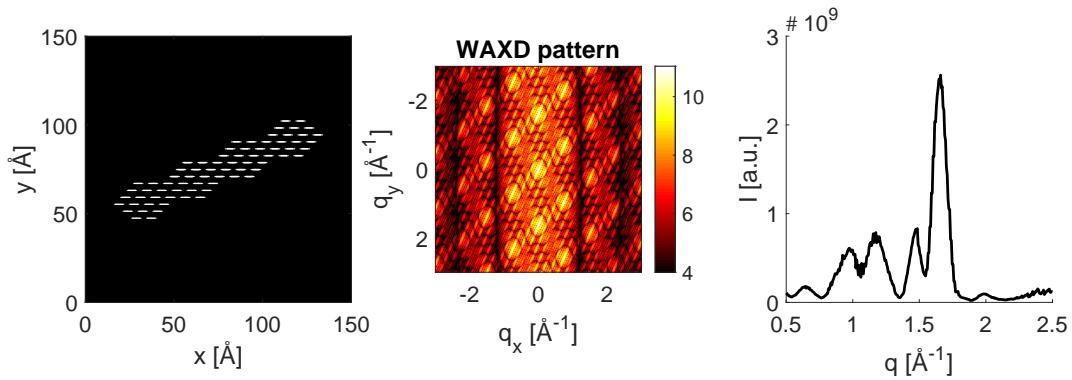
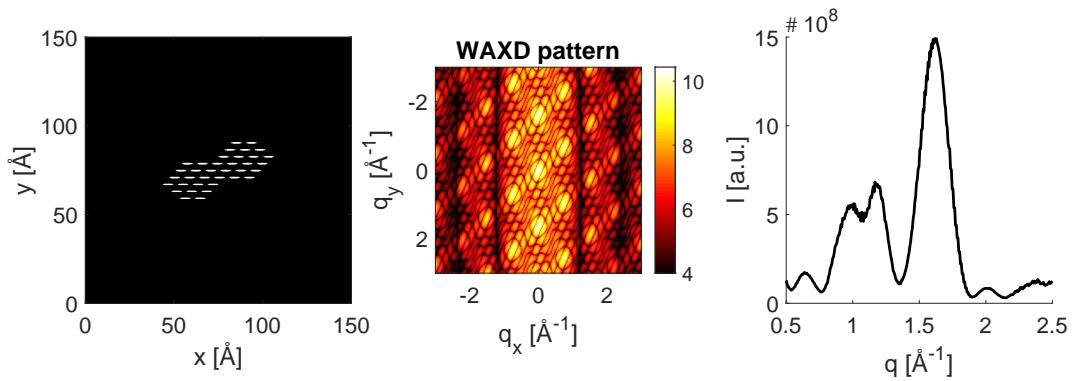
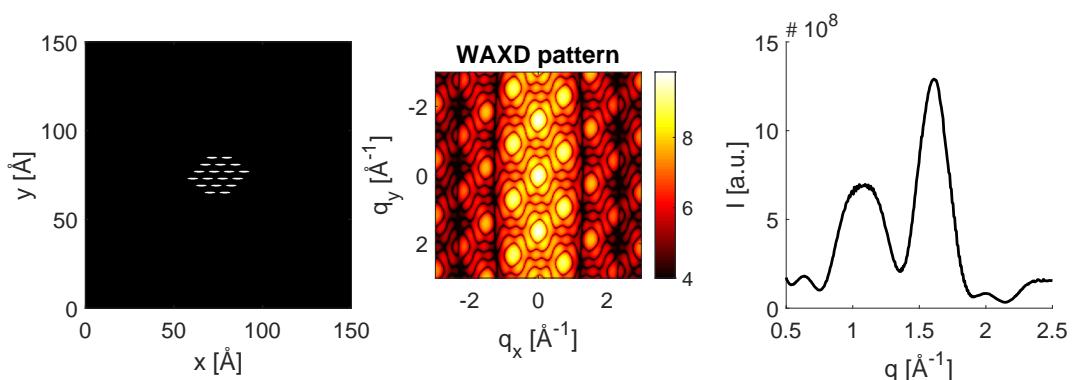


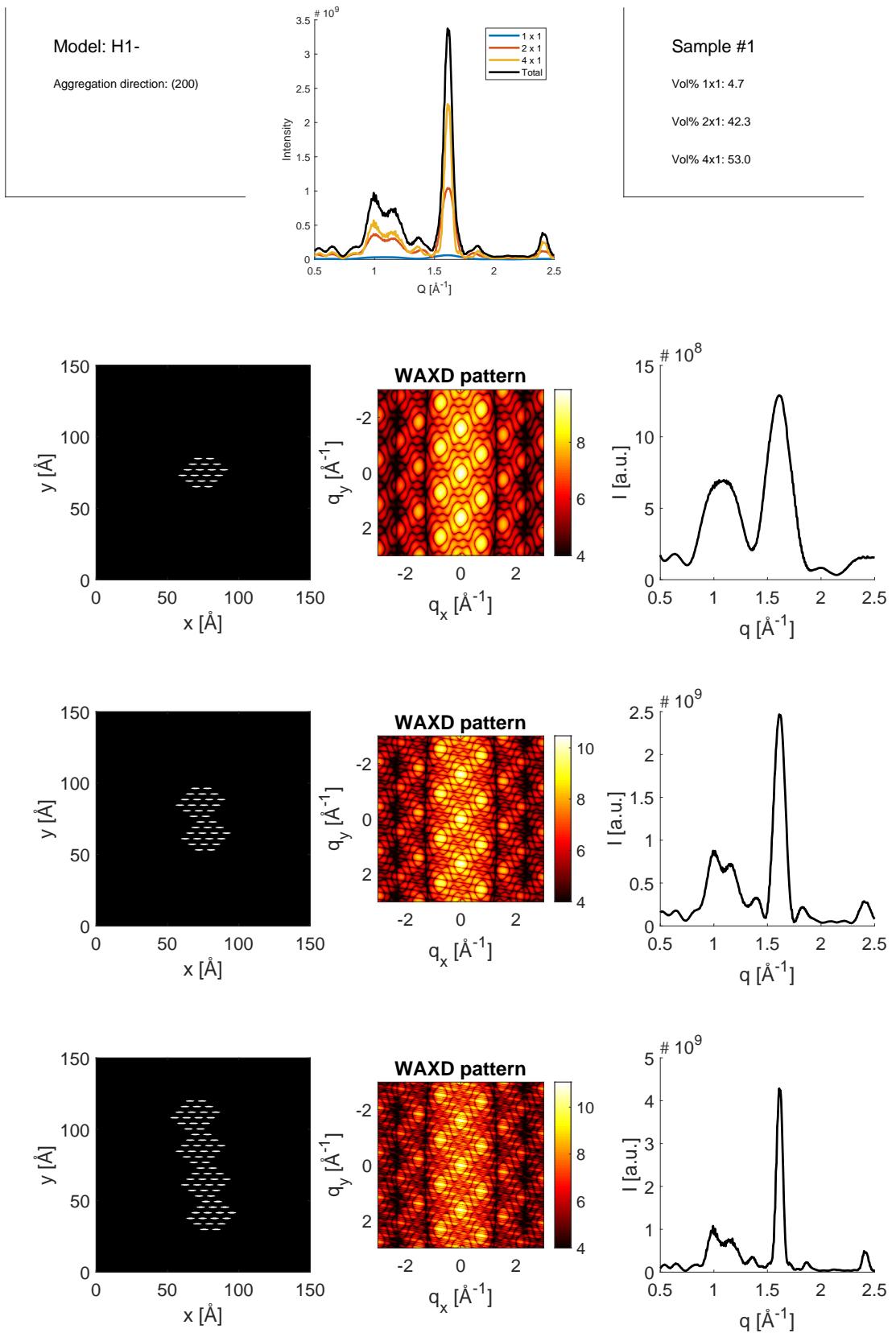
**Sample #1**

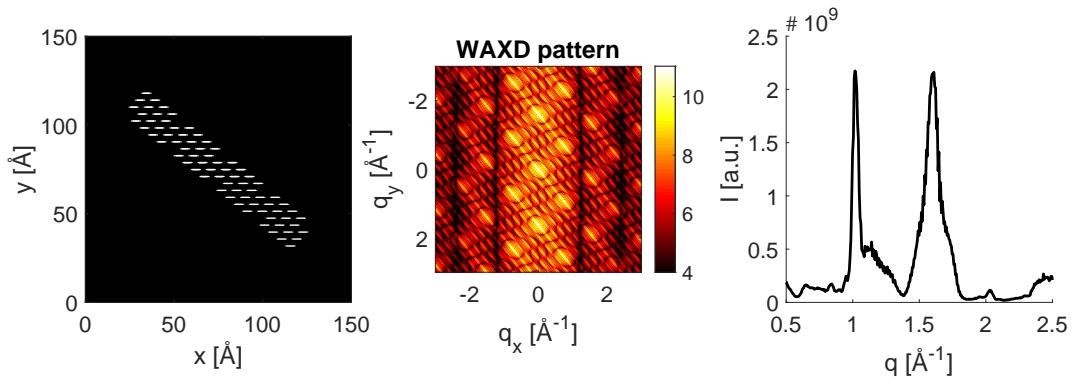
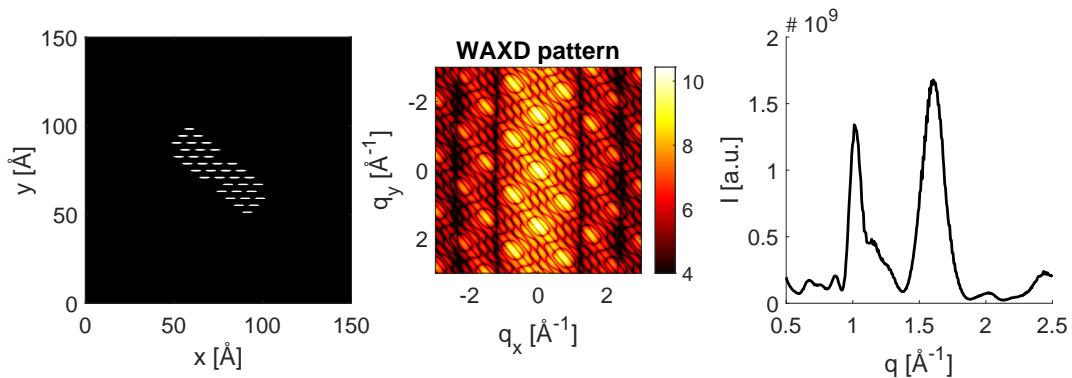
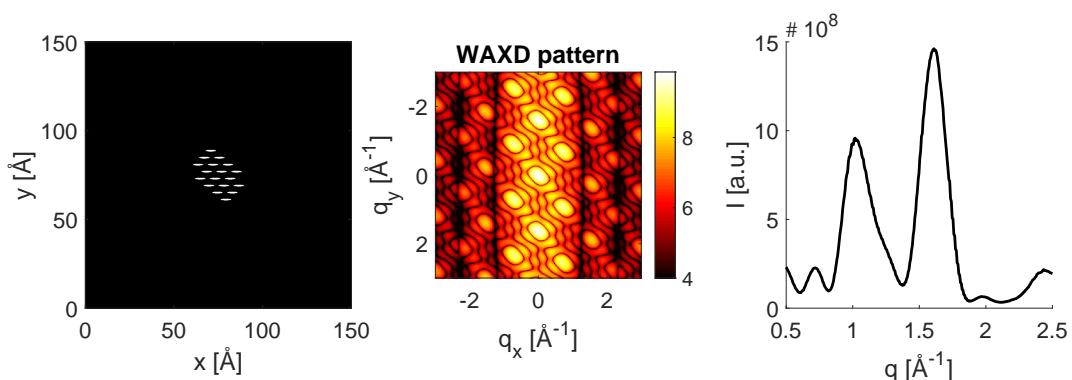
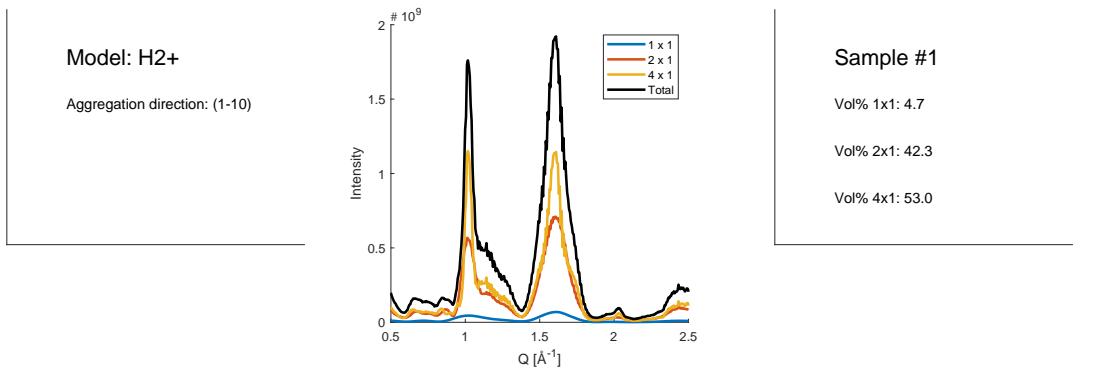
Vol% 1x1: 4.7

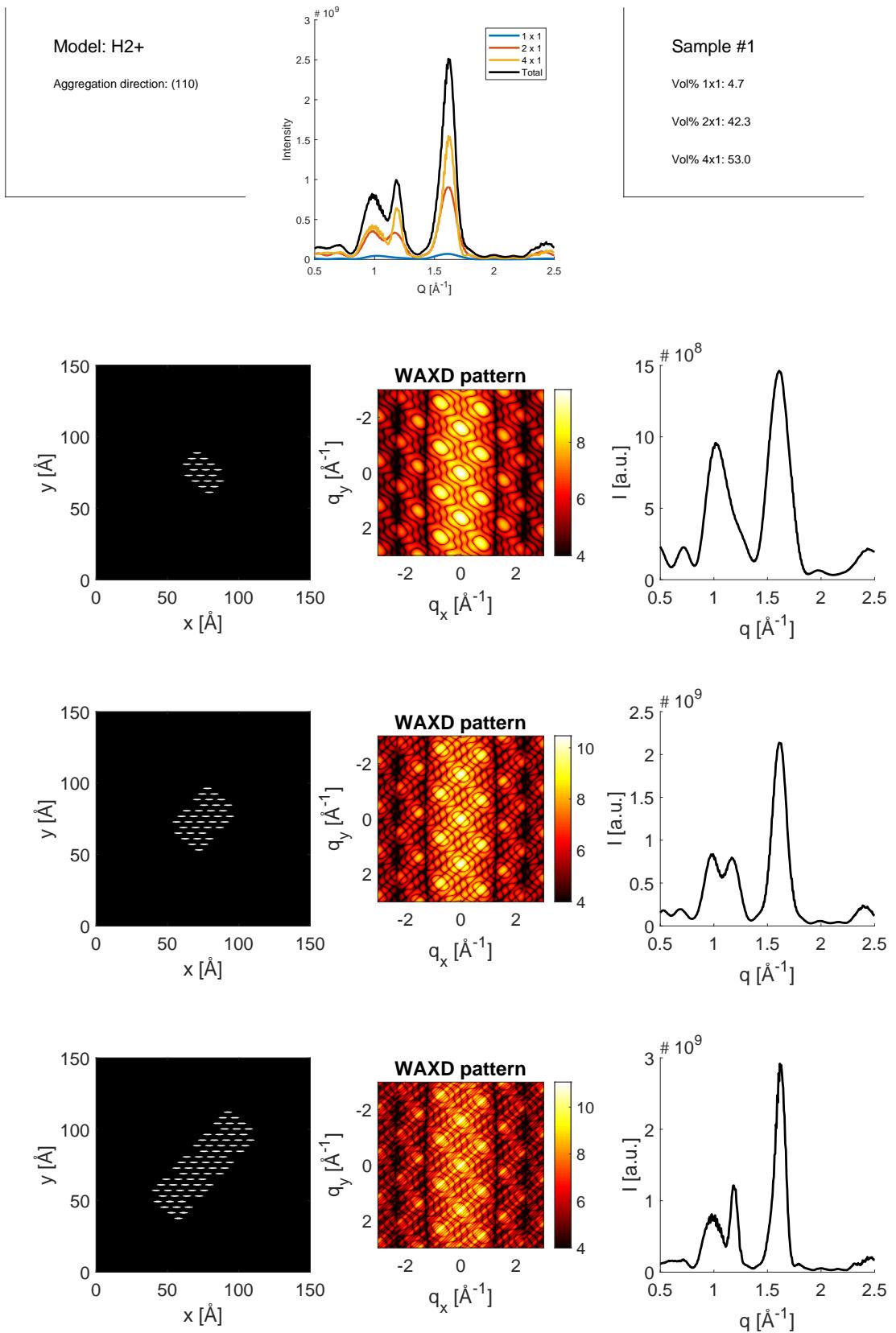
Vol% 2x1: 42.3

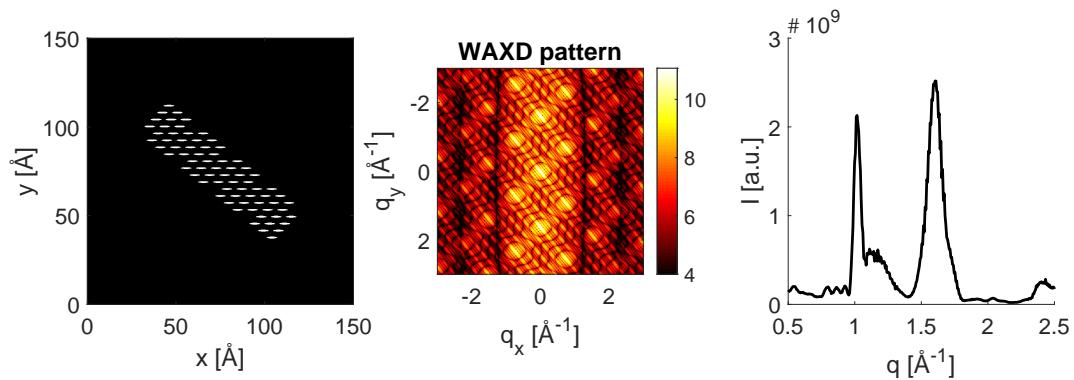
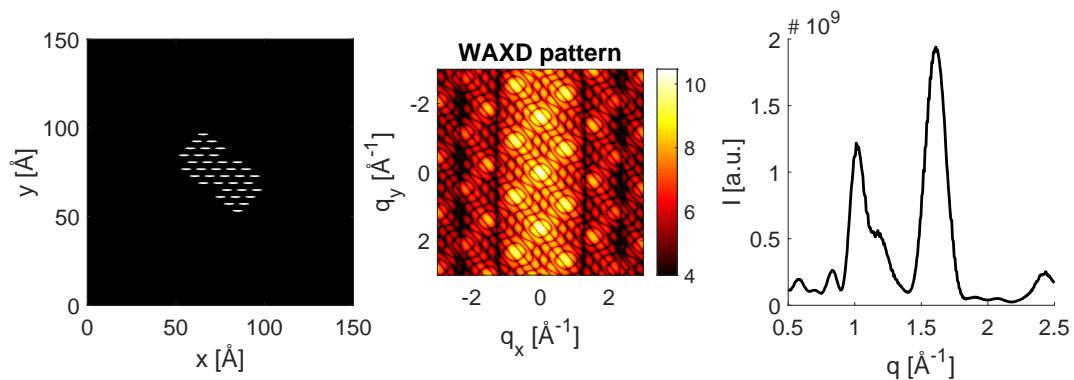
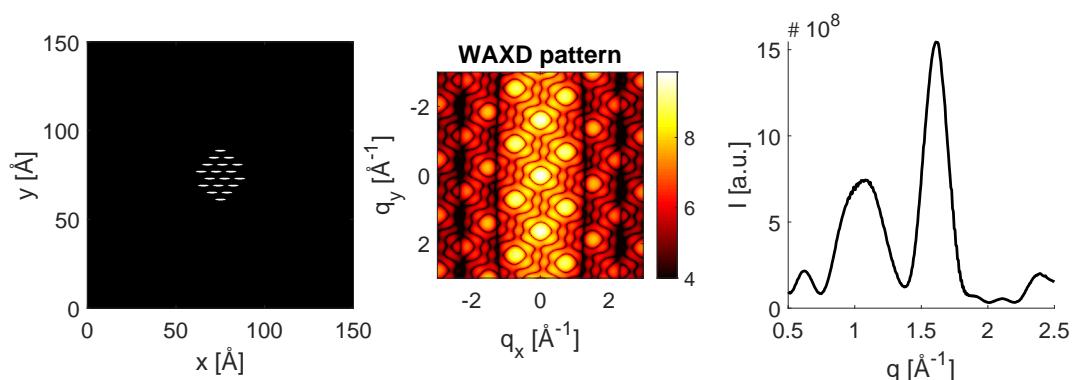
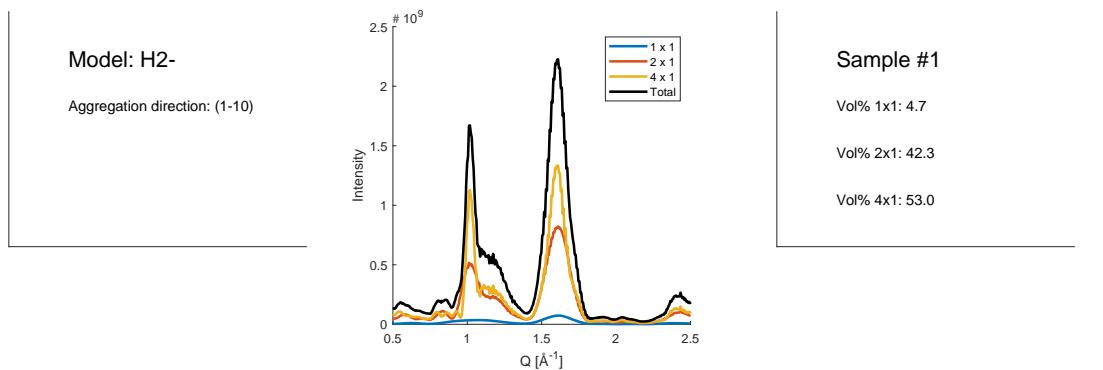
Vol% 4x1: 53.0

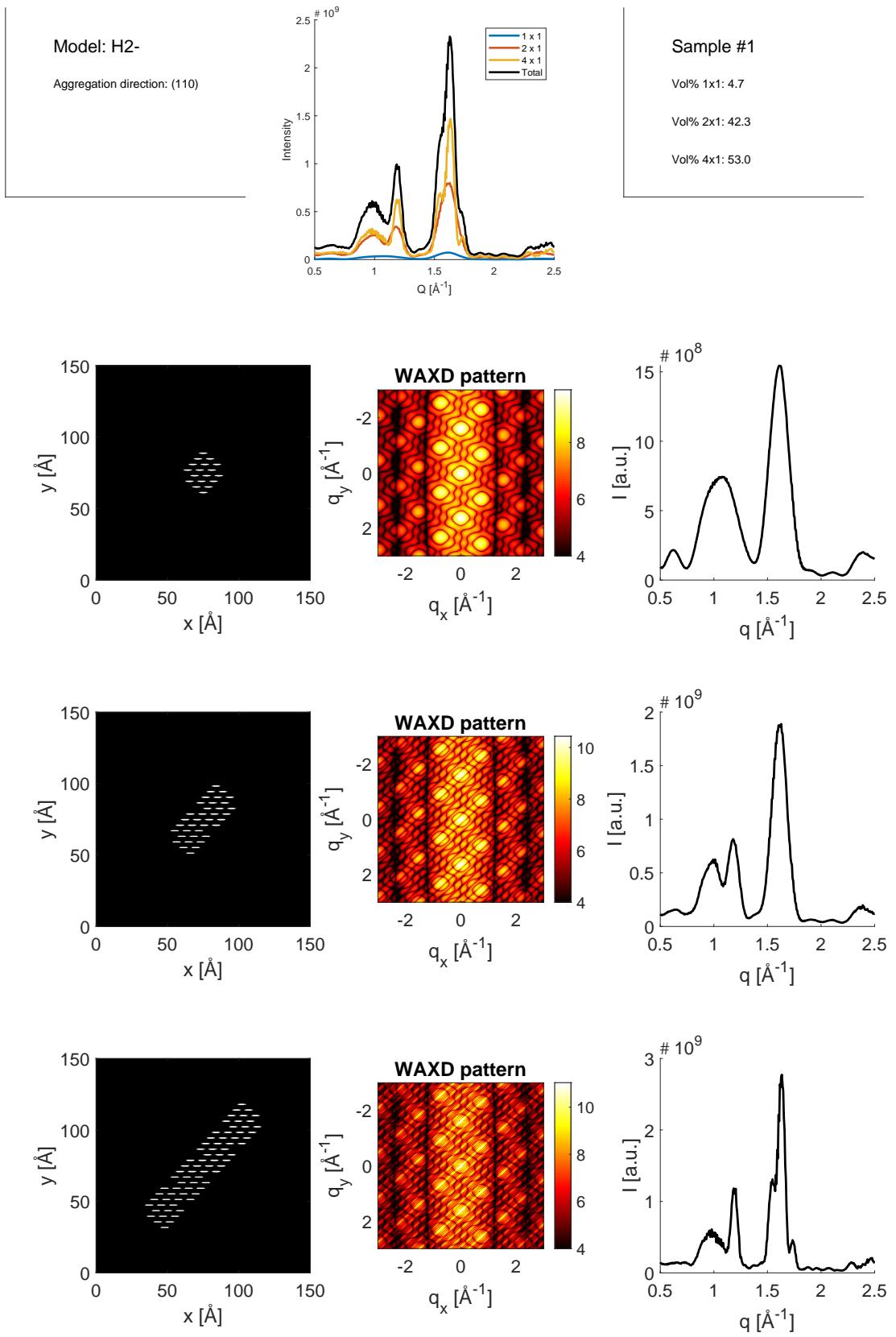


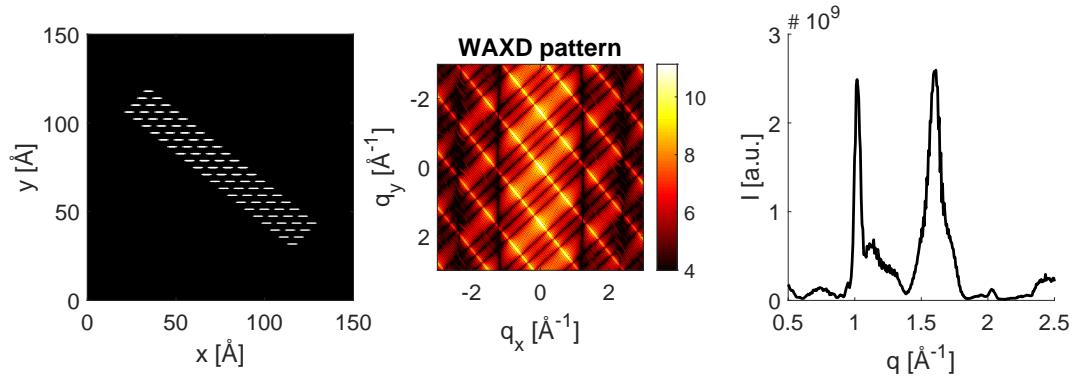
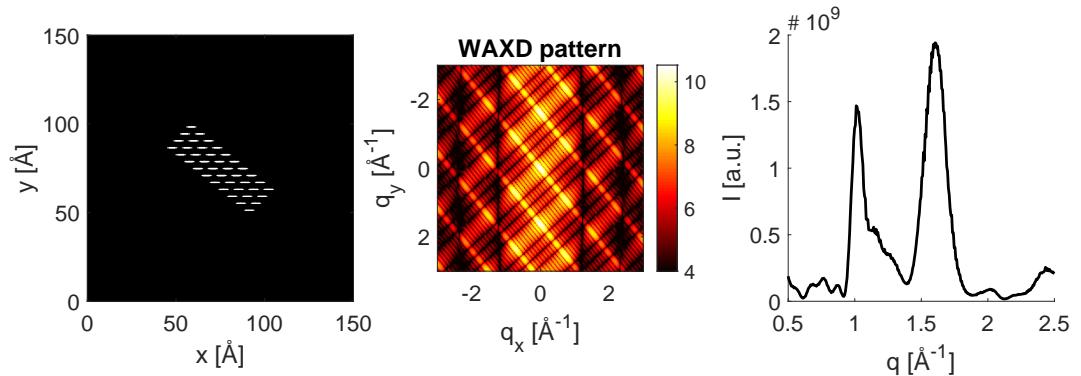
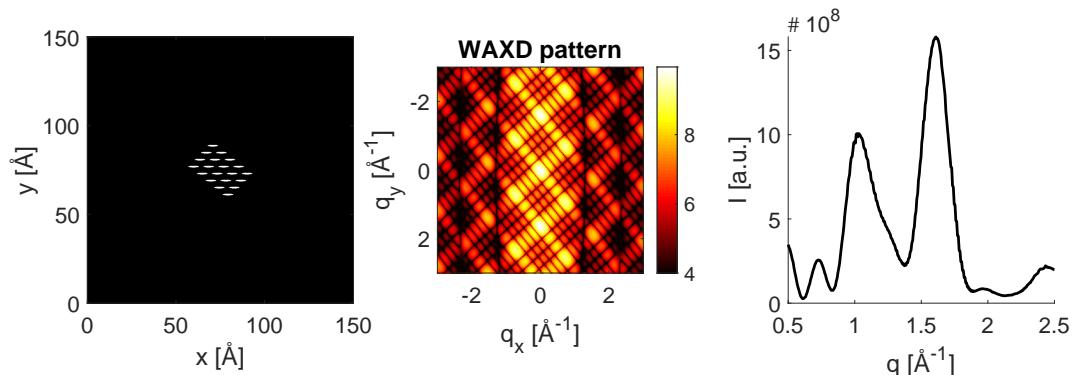
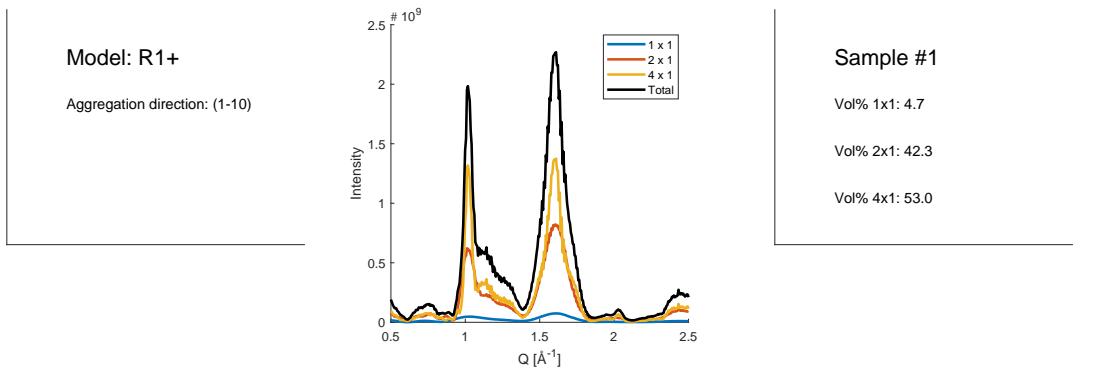


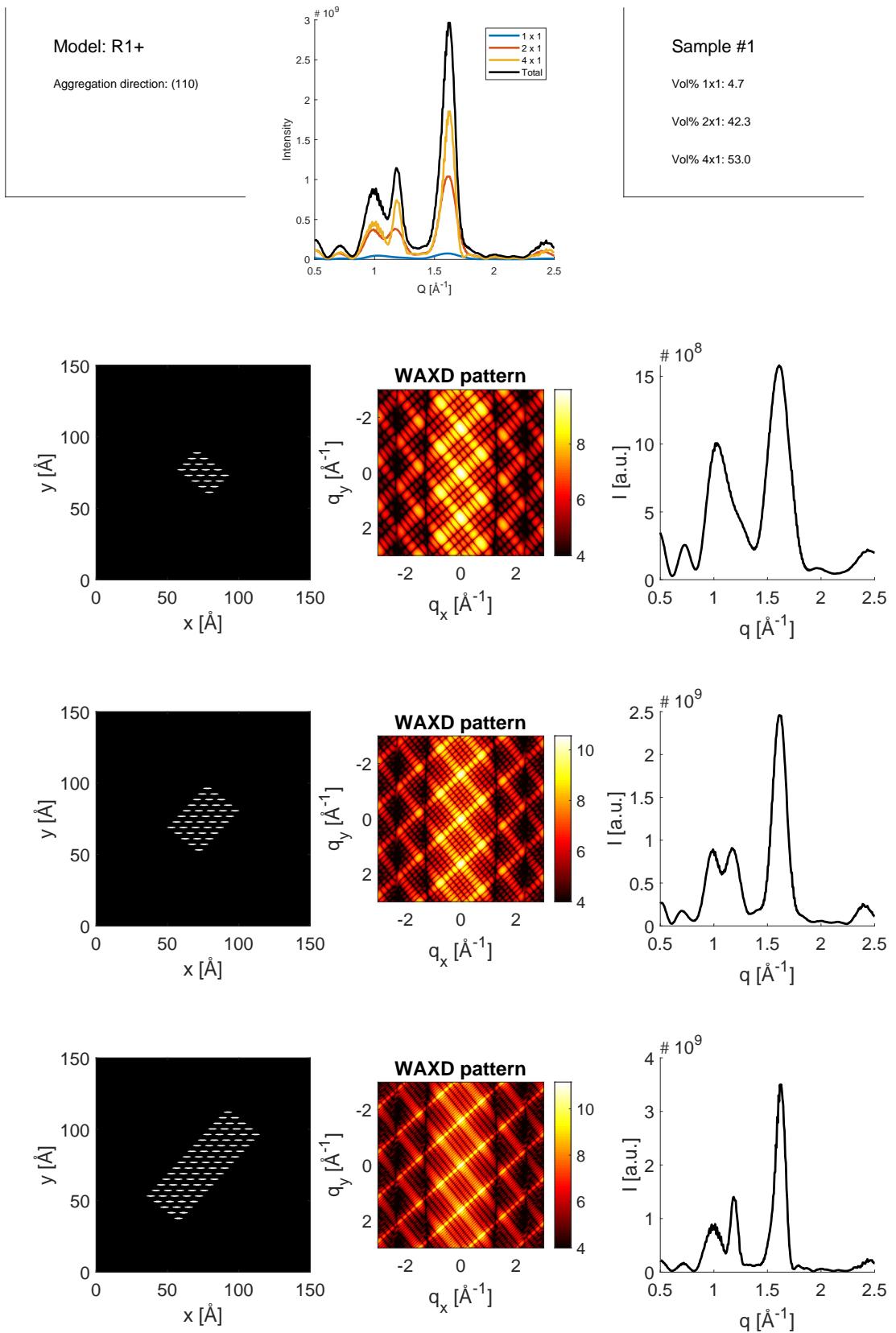


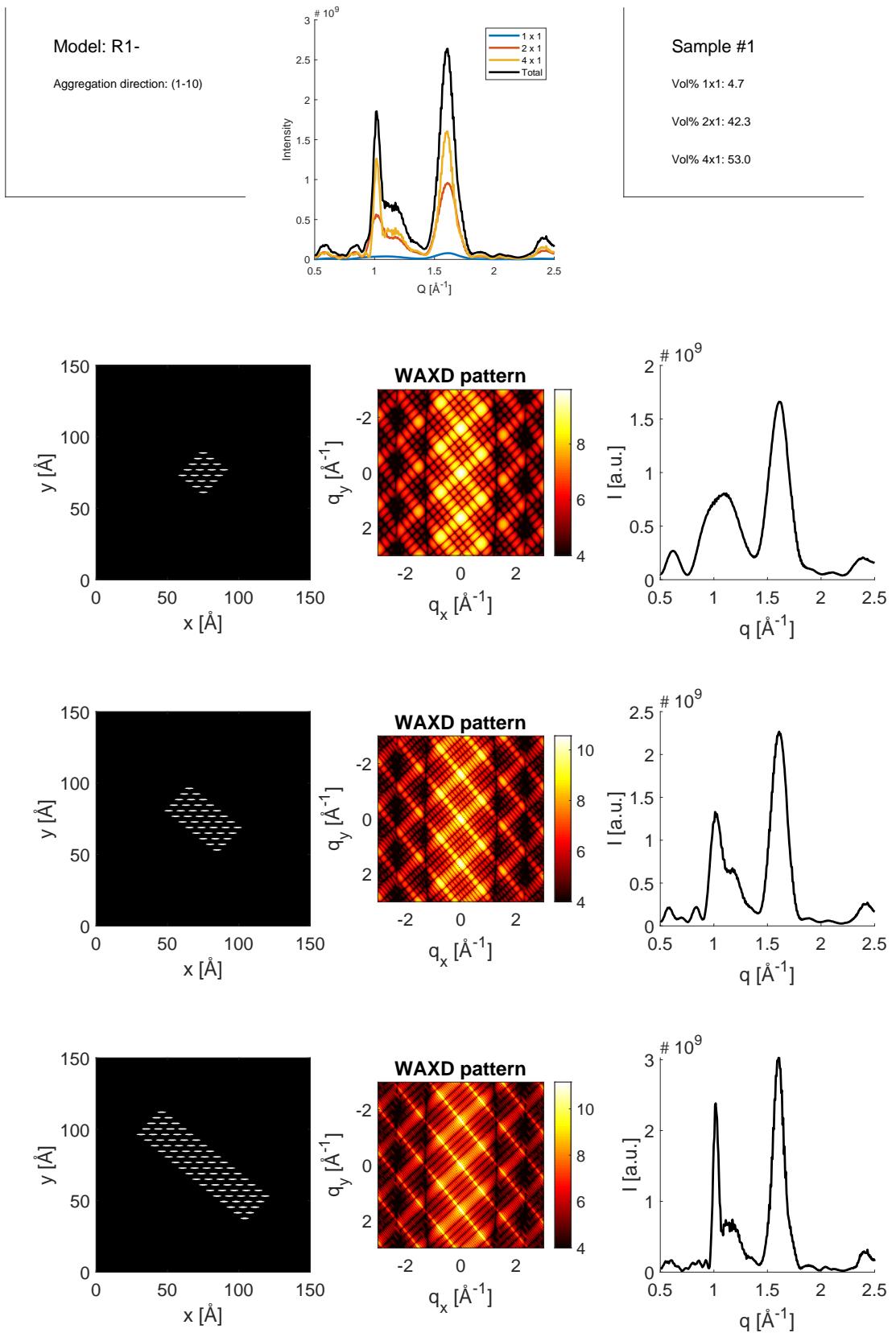


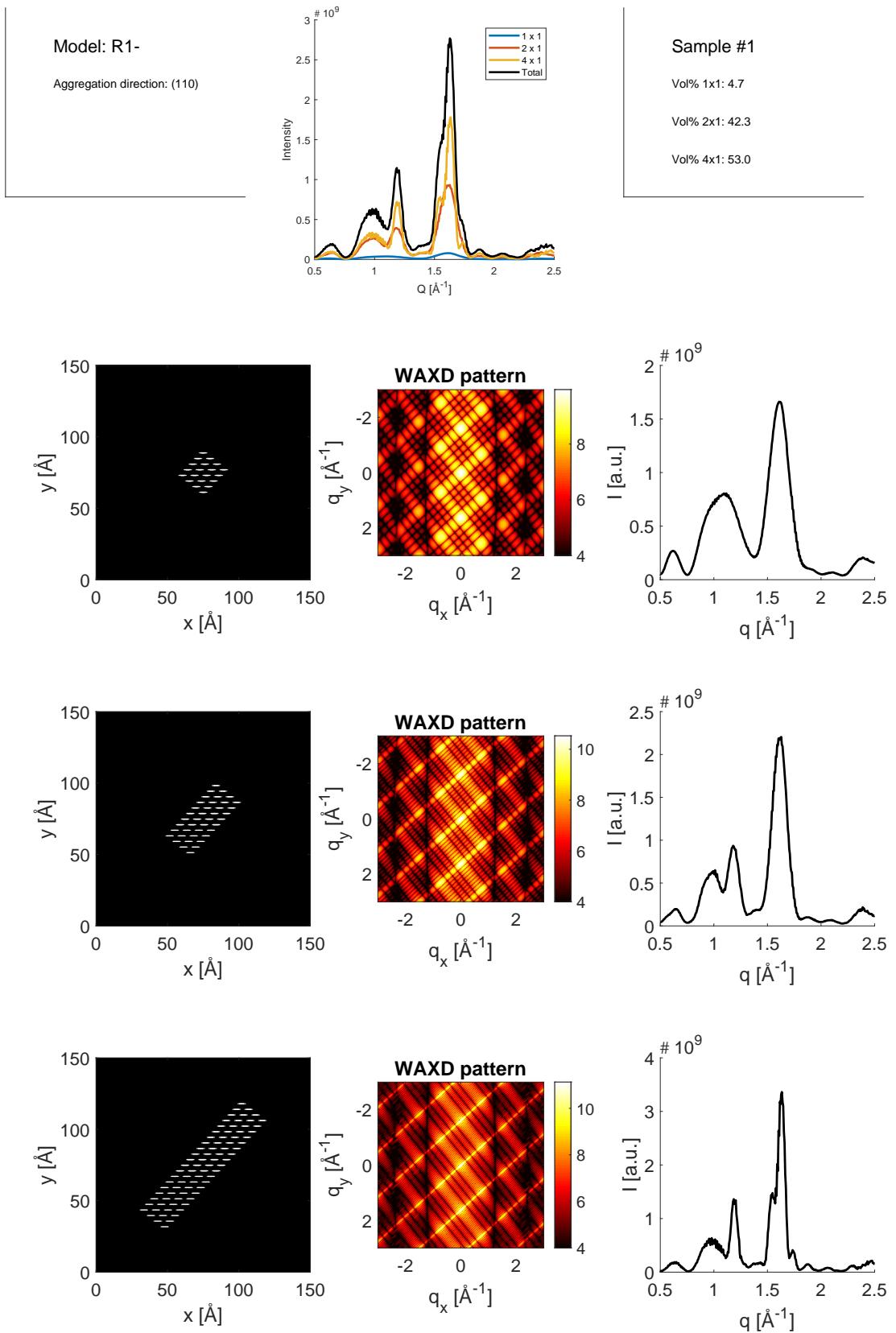


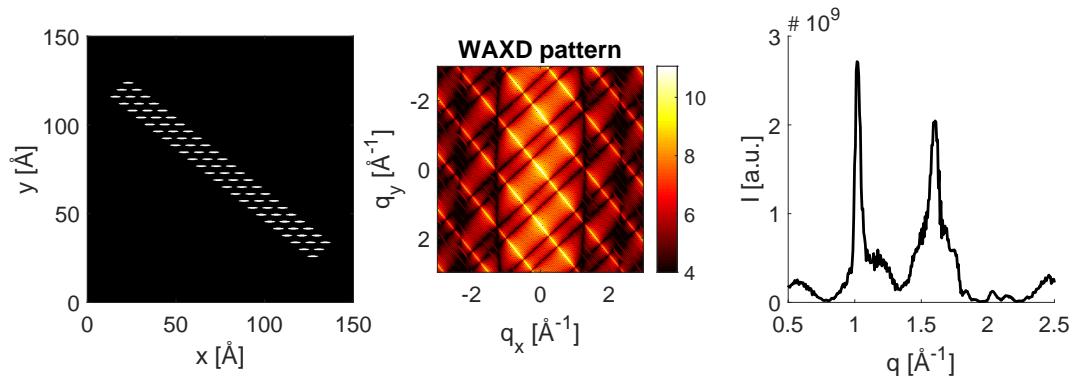
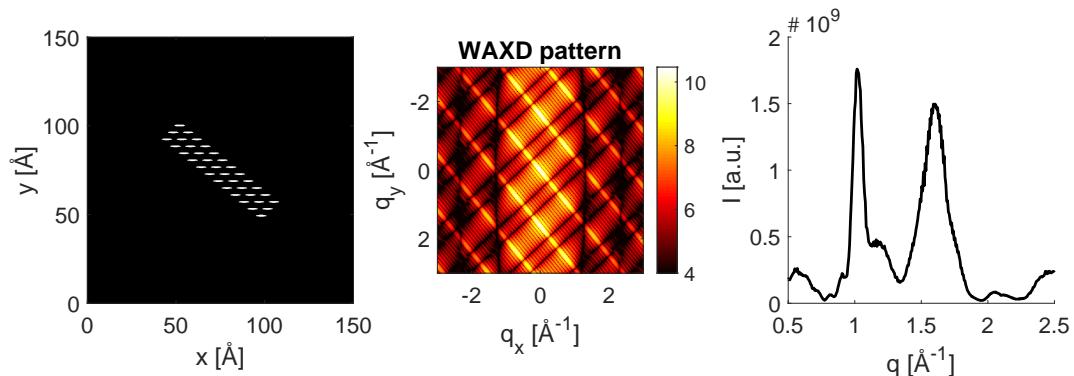
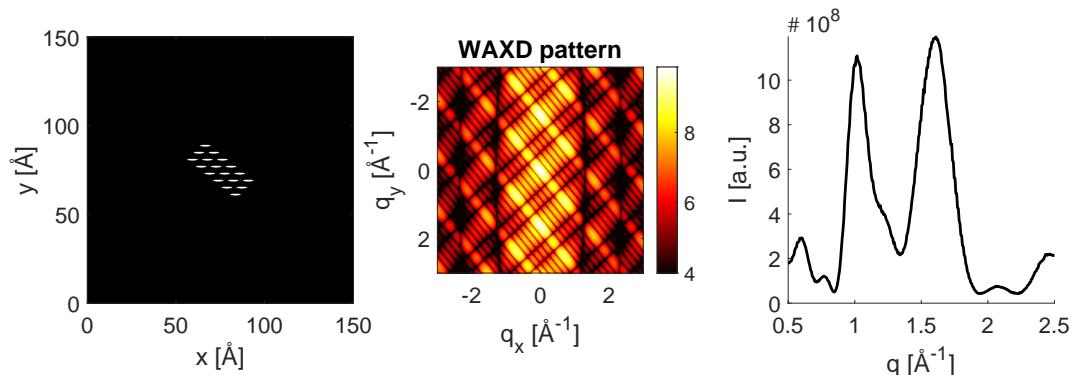
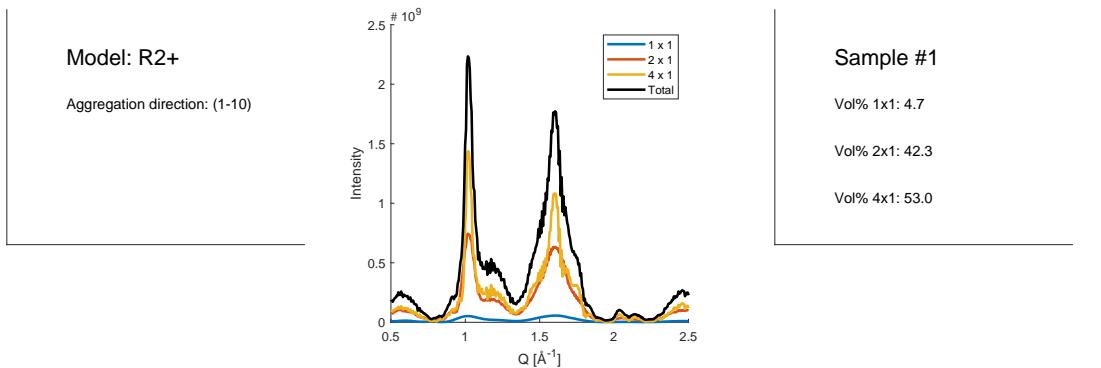


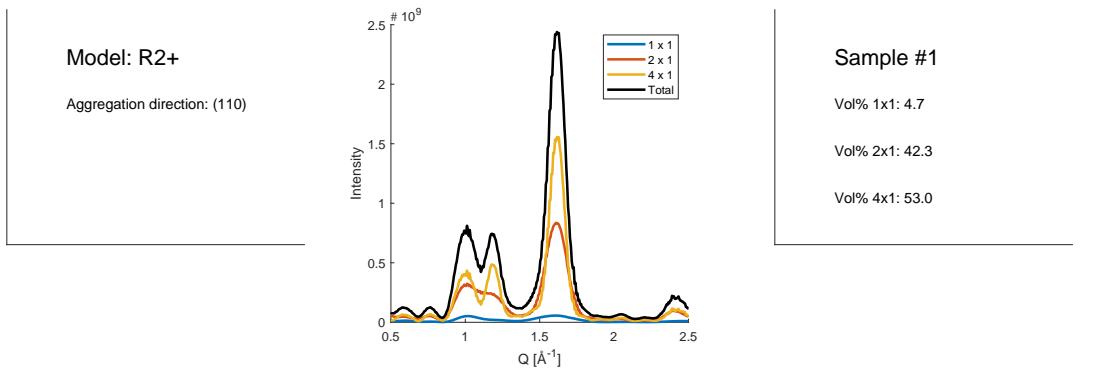










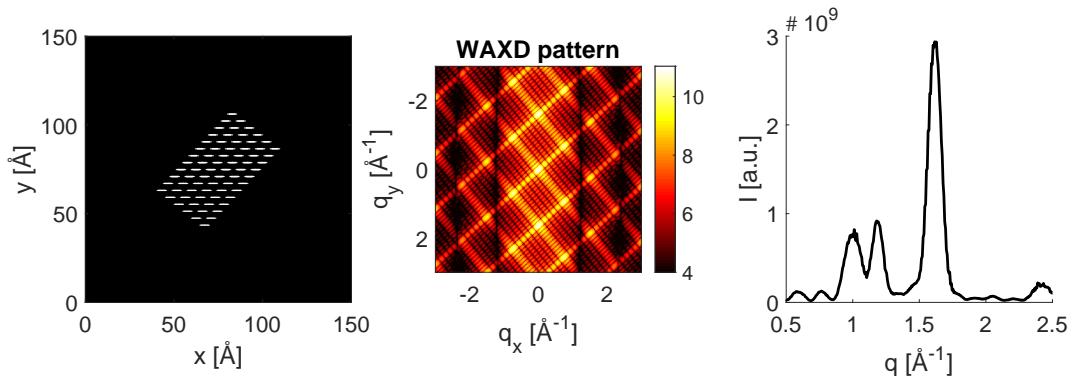
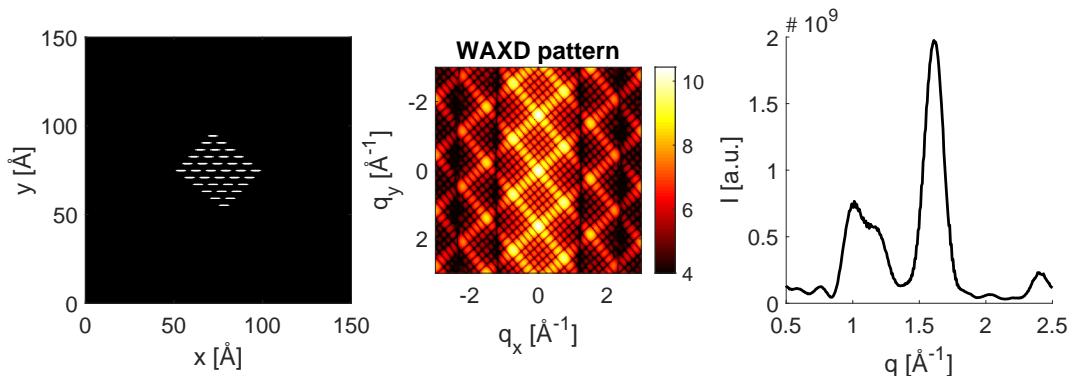
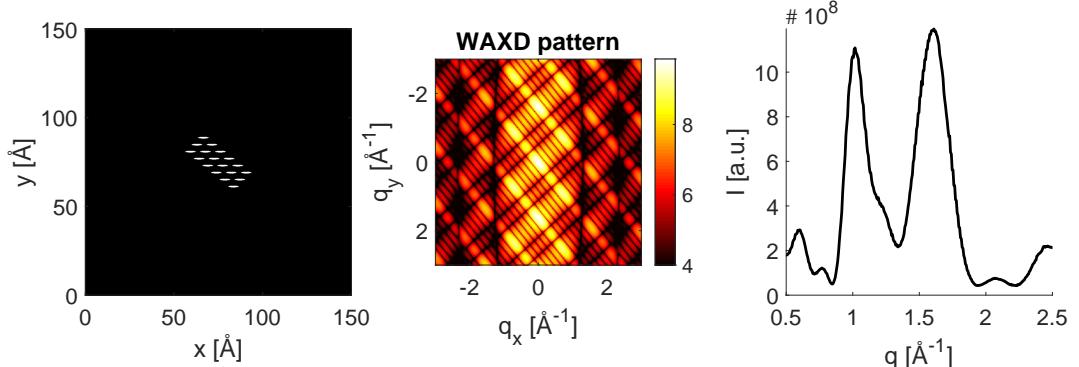


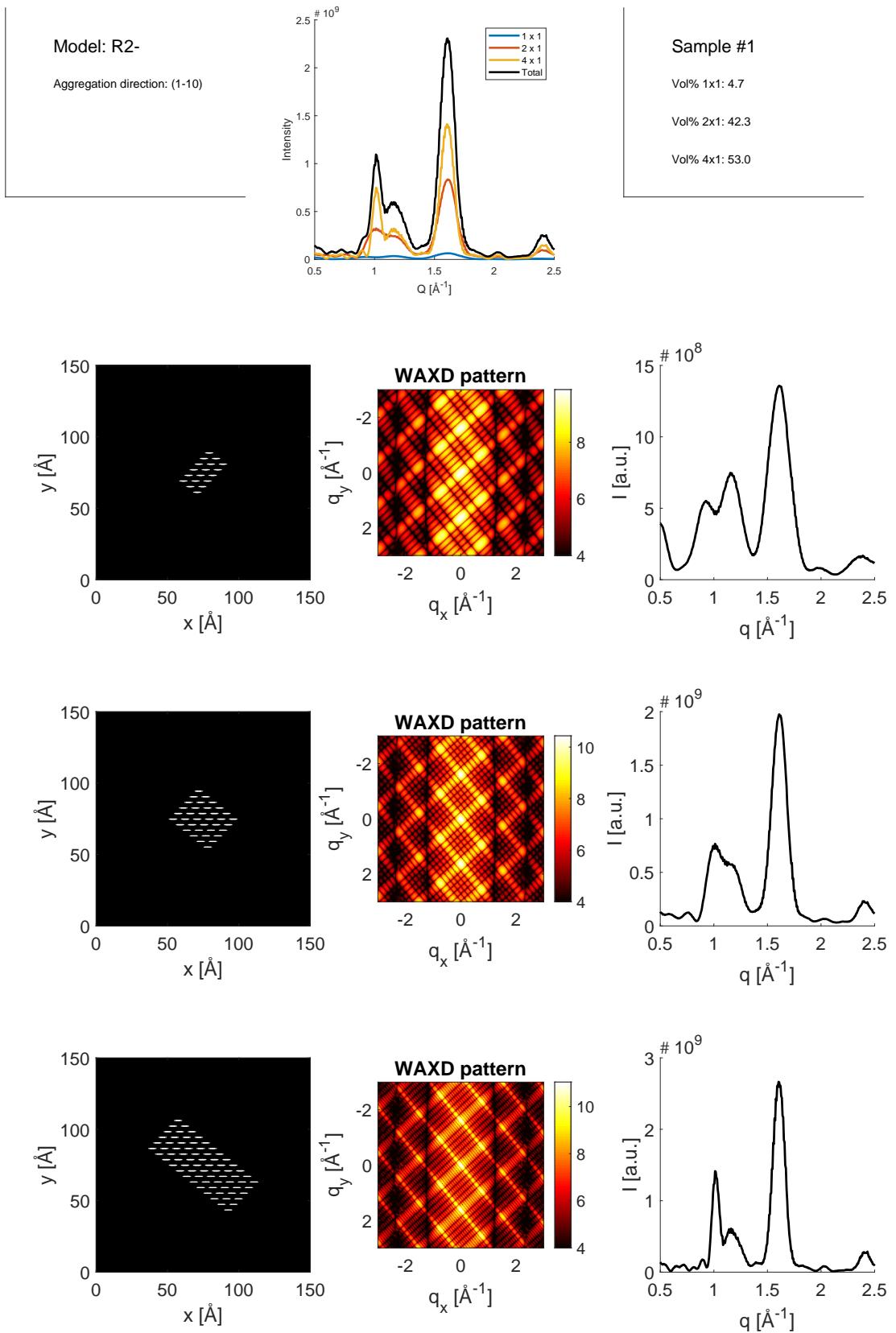
Sample #1

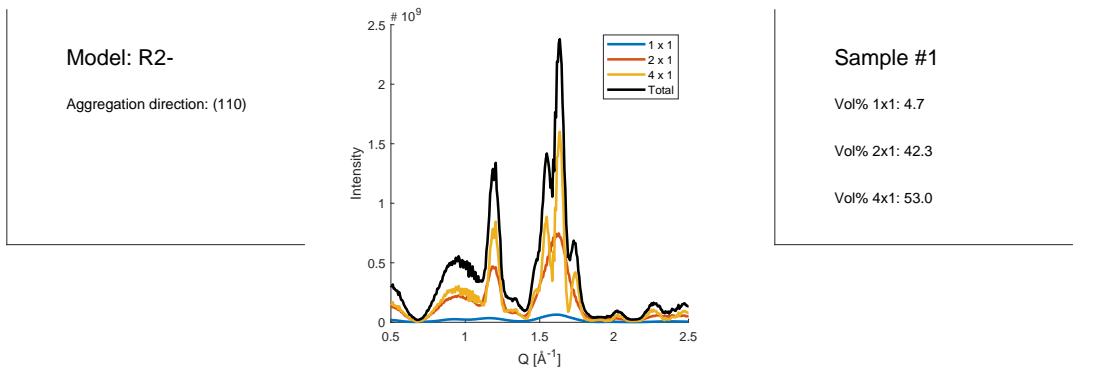
Vol% 1x1: 4.7

Vol% 2x1: 42.3

Vol% 4x1: 53.0





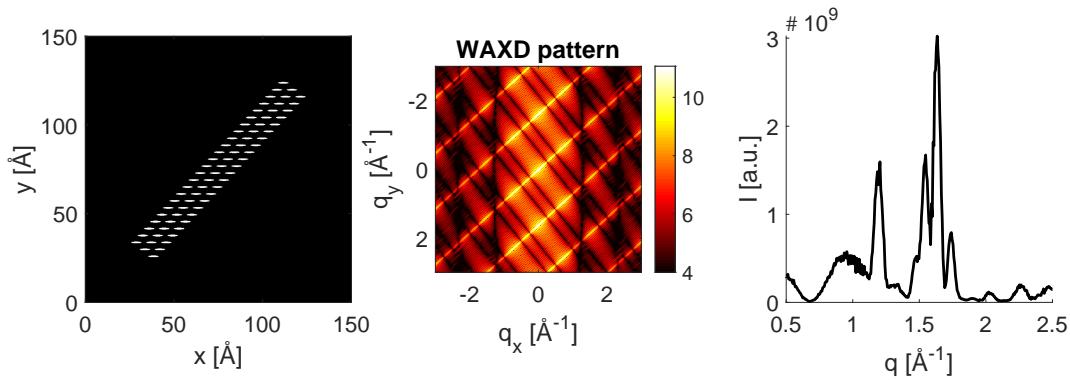
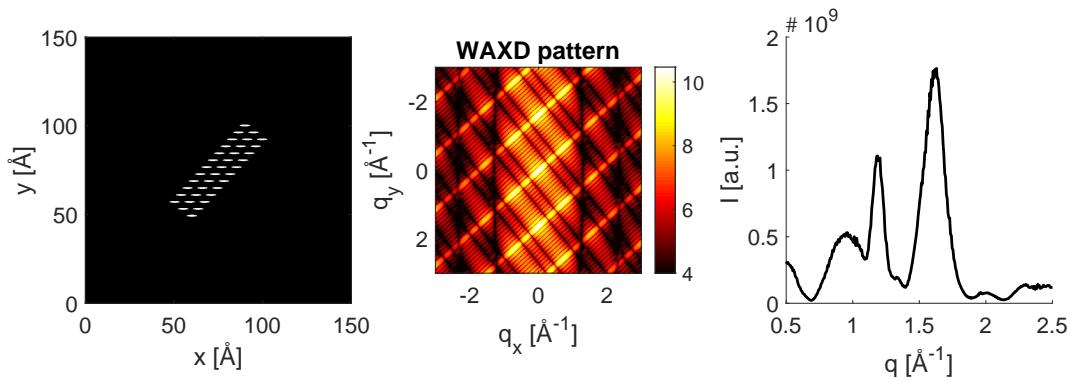
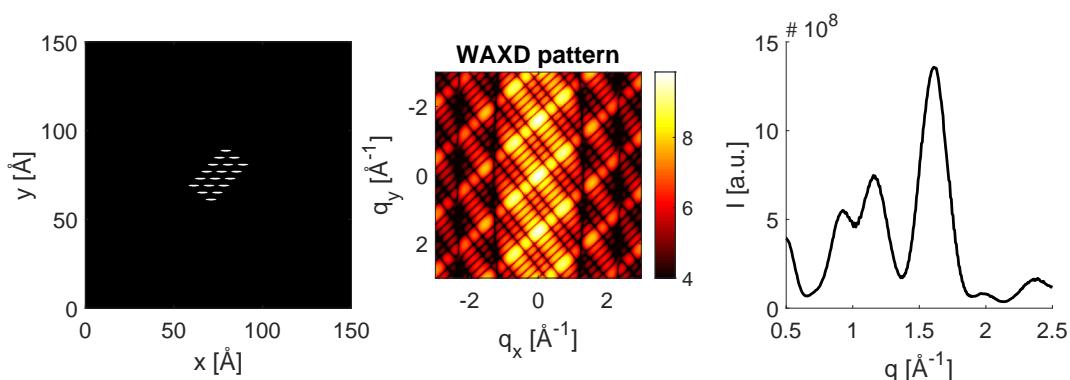


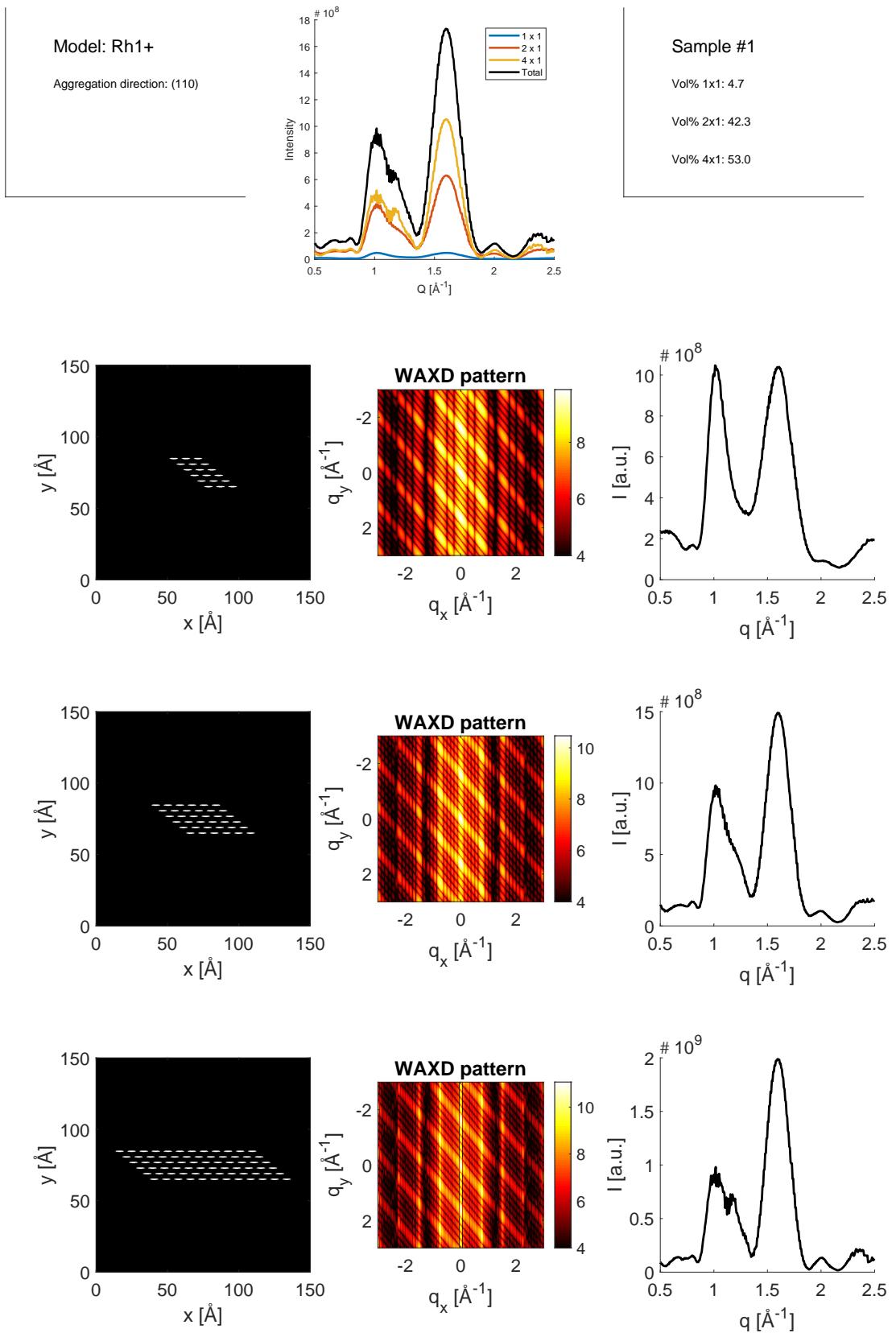
**Sample #1**

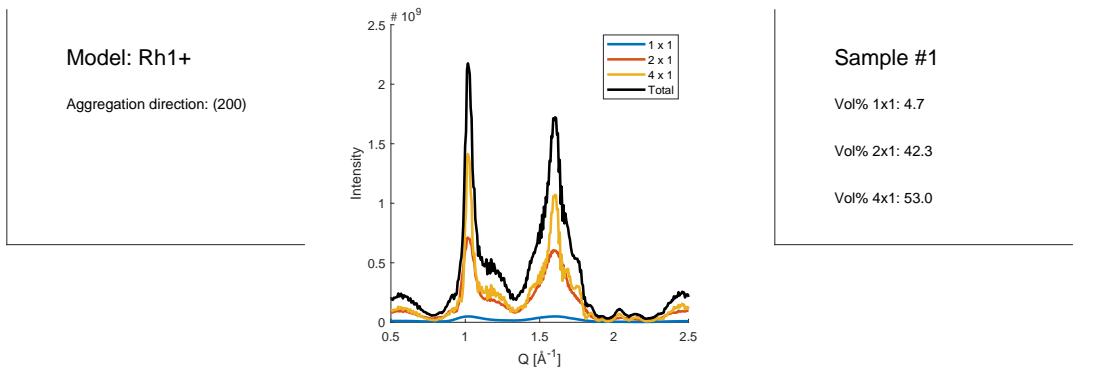
Vol% 1x1: 4.7

Vol% 2x1: 42.3

Vol% 4x1: 53.0





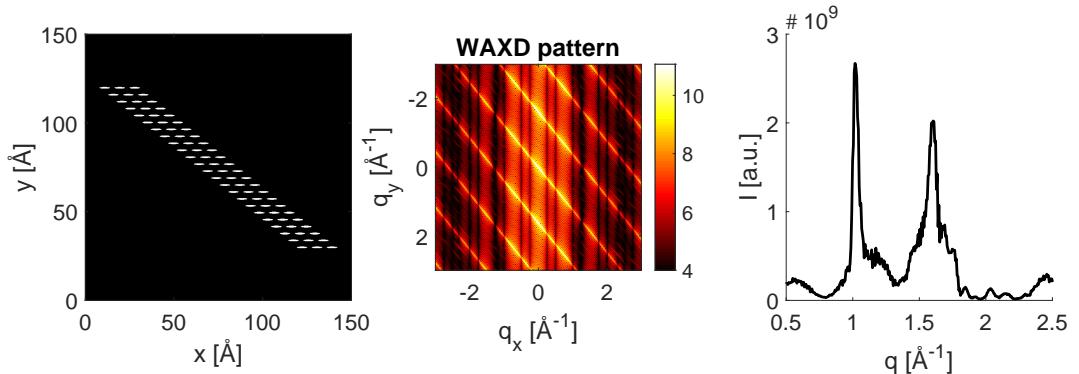
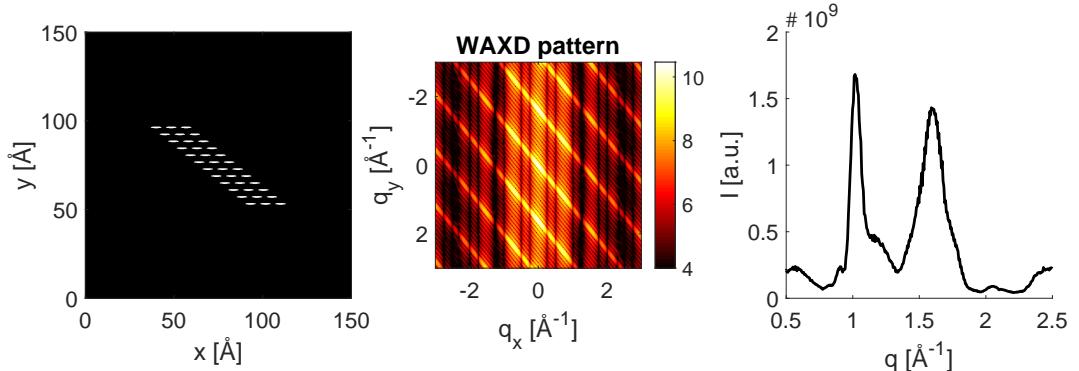
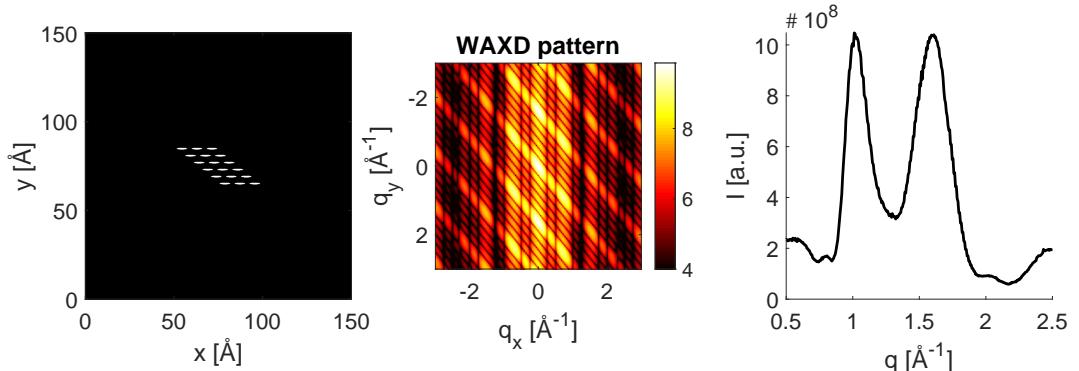


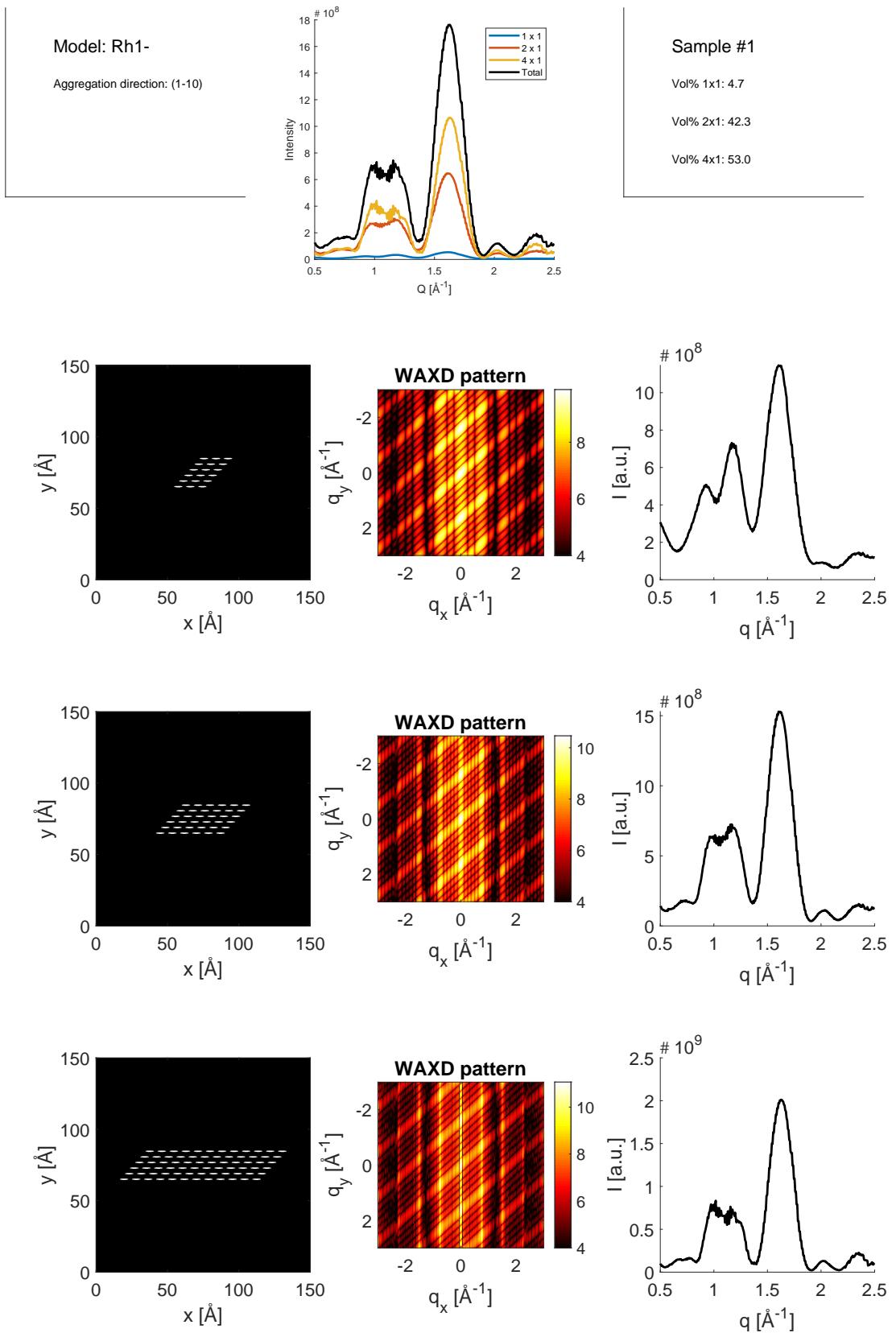
**Sample #1**

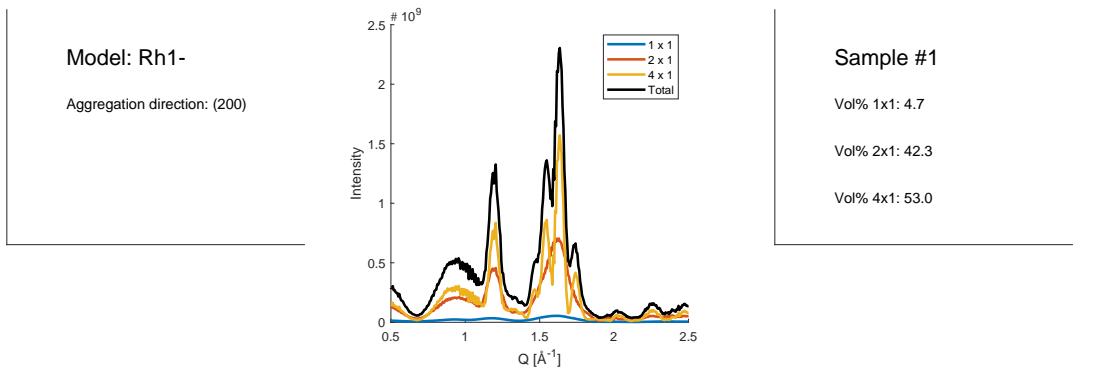
Vol% 1x1: 4.7

Vol% 2x1: 42.3

Vol% 4x1: 53.0







Sample #1

Vol% 1x1: 4.7

Vol% 2x1: 42.3

Vol% 4x1: 53.0

