

Biophysical Journal, Volume 121

Supplemental information

**Slow oscillations persist in pancreatic beta cells lacking phosphofru-
ctokinase M**

Isabella Marinelli, Vishal Parekh, Patrick Fletcher, Benjamin Thompson, Jinhua Ren, Xiaoqing Tang, Thomas L. Saunders, Joon Ha, Arthur Sherman, Richard Bertram, and Leslie S. Satin

1 **Slow oscillations persist in pancreatic beta cells lacking**
2 **phosphofructokinase M**

3 I. Marinelli**, V. S. Parekh**, P. A. Fletcher, B. Thompson, J. Ren, X. Tang, T. L. Saunders,
4 J. Ha, A. Sherman, R. Bertram, L. S. Satin

5 **Co-first authors

6

7 **Supporting Material**

8 **1. List of TaqMan assay probes**

Gene	TaqMan Probe ID	
	Mouse	Human
PFKM	Mm01309576_m1	Hs01075411_m1
PFKP	Mm00444792_m1	Hs00737347_m1
PFKL	Mm00435605_mH	Hs01036347_m1
TBP	Mm01277042_m1	Hs00427620_m1

Table S1. List of TaqMan assay probes for gene expression analysis by RT-qPCR.

9 **2. Model equations and parameters**

10 The Integrated Oscillator Model (IOM) used in this paper is built upon previously developed
 11 mathematical models [1, 2] and consists of modules. The first module describes the cellular
 12 electrical activity and intracellular Ca^{2+} dynamics. The second module describes the
 13 components of the metabolic pathway included in our model: glycolysis and mitochondrial
 14 metabolism.

15 *The electrical and calcium module*

16 The rate of change of the cellular membrane potential, V_M , is expressed by

$$\frac{dV_M}{dt} = \frac{1}{C} [I_{\text{Ca}} + I_{\text{K(Ca)}} + I_{\text{K(ATP)}} + I_{\text{K}}], \quad (\text{S1})$$

17 where C is the membrane capacitance, I_{Ca} is the V_M -dependent Ca^{2+} current, $I_{\text{K(Ca)}}$ is the Ca^{2+} -
 18 activated K^+ current, $I_{\text{K(ATP)}}$ is the ATP-dependent K^+ current, and I_{K} is the delayed-rectifying
 19 K^+ current:

$$I_{\text{Ca}} = g_{\text{Ca}} m_{\infty}(V_M)(V_M - V_{\text{Ca}}) , \quad (\text{S2})$$

$$I_{\text{K(Ca)}} = g_{\text{K(Ca)}} q_{\infty}(c)(V_M - V_{\text{K}}) , \quad (\text{S3})$$

$$I_{\text{K(ATP)}} = g_{\text{K(ATP)}} o_{\infty}(\text{ADP}, \text{ATP})(V_M - V_{\text{K}}) , \quad (\text{S4})$$

$$I_{\text{K}} = g_{\text{K}} n(V_M - V_{\text{K}}) . \quad (\text{S5})$$

20 The upstroke and downstroke of action potentials are mediated by I_{Ca} and I_{K} , respectively. The
 21 K(Ca) and K(ATP) currents are involved in clustering action potentials into bursts.

22 The activation functions for I_{Ca} , $I_{\text{K(Ca)}}$, and $I_{\text{K(ATP)}}$ are given by

$$m_{\infty}(V_M) = \frac{1}{1 + \exp[(v_m - V_M)/s_m]} , \quad (\text{S6})$$

$$q_{\infty}(Ca) = \frac{Ca^2}{k_d^2 + Ca^2} , \quad (\text{S7})$$

$$o_{\infty}(\text{ADP}, \text{ATP}) = \frac{0.08 + 0.89 \left(\frac{\text{MgADP}}{k_{dd}} \right)^2 + 0.16 \left(\frac{\text{MgADP}}{k_{dd}} \right)}{\left(1 + \frac{\text{MgADP}}{k_{dd}} \right)^2 \left(1 + \frac{\text{ATP}^{4-}}{k_{tt}} + \frac{\text{ADP}^{3-}}{k_{td}} \right)} , \quad (\text{S8})$$

23 with $\text{MgADP} = 0.165 \text{ ADP}$, $\text{ATP}^{4-} = 0.05 \text{ ATP}$, and $\text{ADP}^{3-} = 0.135 \text{ ADP}$. The parameters of
 24 this module are given in Table S2.

25 The activation variable for the delayed-rectifying K^+ current, n , is given by

$$\frac{dn}{dt} = \frac{n_{\infty}(V_M) - n}{\tau_n} , \quad (\text{S9})$$

where

$$n_{\infty}(V_M) = \frac{1}{1 + \exp[(v_n - V_M)/s_n]} . \quad (\text{S10})$$

26 The dynamics of the free Ca^{2+} concentration in the cytosol, Ca , in the mitochondria, Ca_m , and
 27 in endoplasmic reticulum (ER), Ca_{er} , are given by

$$\begin{aligned} \frac{dCa}{dt} &= f_{Ca}(J_{\text{mem}} - J_{\text{er}} - J_m) , \\ \frac{dCa_m}{dt} &= f_{Ca}\sigma_m J_m , \\ \frac{dCa_{er}}{dt} &= f_{Ca}\sigma_{er} J_{er} , \end{aligned} \quad (\text{S11})$$

28 Here, f_{Ca} is the fraction of Ca^{2+} ions not bound to buffers, and J_{mem} , J_m , and J_{er} represent the
 29 Ca^{2+} flux densities across the plasma membrane, into the mitochondria, and into the ER,
 30 respectively:

$$J_{\text{mem}} = - \left[\frac{\alpha}{V_{\text{cyt}}} I_{Ca} + k_{\text{PMCA}} Ca \right] , \quad (\text{S12})$$

$$J_{er} = k_{\text{SERCA}} Ca - k_{\text{NaCa}} (Ca_m - Ca) , \quad (\text{S13})$$

$$J_m = J_{\text{uni}} - J_{\text{NaCa}} . \quad (\text{S14})$$

31 The terms J_{uni} and J_{NaCa} represent the flux through the Ca^{2+} pumps and through the $\text{Na}^+/\text{Ca}^{2+}$
 32 exchanger, respectively:

$$J_{\text{uni}} = (p_{21}\psi_m - p_{22})Ca^2 , \quad (\text{S15})$$

$$J_{\text{NaCa}} = p_{21}(Ca_m - Ca)\exp(p_{24}\psi_m) . \quad (\text{S16})$$

33

Parameter	Value	Parameter	Value	Parameter	Value
C	5300 fF	k_d	0.5 μM	σ_{er}	31
g_{Ca}	1000 pS	k_{dd}	17 μM	α	5.18 $\times 10^{-18} \mu\text{mol} \cdot \text{A}^{-1} \cdot \text{ms}^{-1}$
$g_{\text{K}(\text{Ca})}$	150 pS	k_{tt}	1 μM	V_{cyt}	$1.15 \times 10^{-12} \text{l}$
$g_{\text{K}(\text{ATP})}$	19700 pS	k_{td}	26 μM	k_{PMCA}	0.2 ms^{-1}
g_{K}	2700 pS	τ_n	20 ms	k_{SERCA}	0.4 ms^{-1}
V_{Ca}	25 mV	v_n	-16 mV	p_{21}	$0.013 \mu\text{M}^{-1} \cdot \text{ms}^{-1} \cdot \text{mV}^{-1}$
V_{K}	-75 mV	s_n	5 mV	p_{22}	$1.6 \mu\text{M}^{-1} \cdot \text{ms}^{-1}$
v_m	-20 mV	f_{Ca}	0.01	p_{23}	$0.0015 \mu\text{M} \cdot \text{ms}^{-1}$
s_m	12 mV	σ_m	290	p_{24}	0.016mV^{-1}

Table S1. Parameter values for the electrical and calcium module.

35

36 ***The metabolic module***

37 The cytosolic concentrations of F6P and FBP are described by

$$\frac{d\text{F6P}}{dt} = 0.3(J_{\text{GK}} - J_{\text{PFK}}), \quad (\text{S17})$$

$$\frac{d\text{FBP}}{dt} = J_{\text{PFK}} - \frac{1}{2} \frac{J_{\text{PDH}}}{\sigma_m},$$

38 where J_{GK} is the glucose-dependent glucokinase (GK) reaction rate, J_{PFK} is the
39 phosphofructokinase (PFK) reaction rate defined in (1), and J_{PDH} is the pyruvate
40 dehydrogenase (PDH) reaction rate. Since the glucose level is the same in all simulations, J_{GK}
41 does not vary. Flux through PDH is described by

$$J_{\text{PDH}} = v_{\text{PDH}} \frac{1}{K_{\text{NADH}_m, \text{PDH}} + \frac{\text{NADH}_m}{\text{NAD}_m}} J_{\text{GPDH}}, \quad (\text{S18})$$

42 where v_{PDH} is the maximum PDH reaction rate. The glycerol-3-phosphate dehydrogenase
 43 (GPDH) reaction rate, J_{GPDH} , is

$$J_{GPDH} = \frac{Ca_m}{K_{GPDH} + Ca_m} \sqrt{FBP} . \quad (S19)$$

44 The adenosine diphosphate (ADP) dynamics are given by

$$\frac{dADP}{dt} = J_{hyd} - \frac{J_{ANT}}{\sigma_m} , \quad (S20)$$

45 where J_{hyd} reflects ATP hydrolysis and J_{ANT} is the flux of ATP produced in the mitochondria
 46 and transported to the cytosol through the adenine nucleotide translocator (ANT),

$$J_{hyd} = (k_{hyd}Ca + k_{hyd,bas})ATP , \quad (S21)$$

$$J_{ANT} = p_{19} \frac{\frac{ATP_m}{ADP_m}}{\frac{ATP_m}{ADP_m} + p_{20}} \exp\left(\frac{F}{2RT} \psi_m\right) . \quad (S22)$$

47 The hydrolysis term has a Ca^{2+} -independent term that represents ATP hydrolysis for cell
 48 homeostasis, and a Ca^{2+} -dependent term that represents hydrolysis by Ca^{2+} pumps present on
 49 the plasma and ER membranes.

50 The model assumes that the total nucleotide concentrations in the cytosol and in the
 51 mitochondria (A_{tot} and $A_{tot,m}$, respectively) is constant, and that the sum of both cytosolic and
 52 mitochondrial nucleotides are conserved:

$$ATP = \frac{1}{2} \left[A_{tot} + \sqrt{-4ADP^2 + (A_{tot} - ADP)^2} - ADP \right] , \quad (S23)$$

$$ATP_m = A_{tot,m} - ADP_m . \quad (S24)$$

53 There are two terms for NADH production: production due to pyruvate dehydrogenase (J_{PDH}),
 54 and production due to the combined action of dehydrogenases in the citric acid cycle (J_{DH}).
 55 The mitochondrial concentration of NADH is then

$$\frac{dNADH_m}{dt} = J_{PDH} + J_{DH} - J_O , \quad (S25)$$

56 where J_{PDH} is given by (S18) and J_{DH} and the oxygen consumption rate (J_O) are:

$$J_{DH} = v_{DH} \frac{Ca_m}{K_{DH} + Ca_m} \frac{1}{K_{NADH_m, DH} + \frac{NADH_m}{NAD_m}} , \quad (S26)$$

$$J_O = p_4 \frac{NADH_m}{p_5 + NADH_m} \frac{1}{1 + \exp\left(\frac{\psi_m - p_6}{p_7}\right)} . \quad (S27)$$

57 The model assumes nucleotide conservation:

$$NAD_m = N_{tot,m} - NADH_m , \quad (S28)$$

58 where $N_{tot,m}$ is the total concentration in the mitochondria.

59 The changes in the dynamics of the mitochondrial membrane potential, ψ_m , are described by

$$\frac{d\psi_m}{dt} = \frac{1}{C_m} [J_{Hres} - J_{Hatp} - J_{Hleak} - J_{ANT} - J_{NaCa} - 2J_{uni}] . \quad (S29)$$

60 Here, C_m is the mitochondrial inner membrane capacitance, J_{Hres} is the flux through respiration-
 61 driven proton pumps, J_{Hatp} is the proton flux entering the mitochondria through the ATPase,
 62 while J_{Hleak} is the proton flux entering the mitochondria through leakage down the proton
 63 gradient:

$$J_{Hres} = p_8 \frac{NADH_m}{p_9 + NADH_m} \frac{1}{1 + \exp\left(\frac{\psi_m - p_{10}}{p_{11}}\right)} , \quad (S30)$$

$$J_{Hatp} = 3J_{F1F0} , \quad (S31)$$

$$J_{Hleak} = p_{17}\psi_m - p_{18} . \quad (S32)$$

64 The term J_{F1F0} in (S31) is the rate at which the F1F0 ATP synthase phosphorylates ADP to
 65 form ATP:

$$J_{F1F0} = p_{16} \frac{p_{13}}{p_{13} + ATP_m} \frac{1}{1 + \exp\left(\frac{p_{14} - \psi_m}{p_{15}}\right)} . \quad (S33)$$

66 Since mitochondrial ATP production comes at the expense of ADP, the mitochondrial ADP
 67 level (ADP_m) is given by

$$\frac{d\text{ADP}_m}{dt} = J_{\text{ANT}} - J_{\text{FIF0}} \quad , \quad (\text{S34})$$

68 with J_{ANT} and J_{FIF0} given in (S22) and (S33), respectively.

69 Parameter values for the metabolic module are given in Table S3.

Parameter	Value	Parameter	Value	Parameter	Value
J_{GK}	$0.001 \mu\text{M ms}^{-1}$	p_4	$0.55 \mu\text{M ms}^{-1}$	p_{15}	8.5 mV
v_{PDH}	$0.4 \mu\text{M ms}^{-1}$	p_5	250 μM	p_{16}	$4 \mu\text{M ms}^{-1}$
$K_{\text{NADH}_m, \text{PDH}}$	1.3	p_6	165 mV	p_{17}	$0.0014 \mu\text{M ms}^{-1} \text{mV}^{-1}$
K_{GPDH}	$1.5 \mu\text{M}$	p_7	5mV	p_{18}	$0.02 \mu\text{M ms}^{-1}$
k_{hyd}	$1.864 \times 10^{-6} \mu\text{M ms}^{-1}$	p_8	$7.4 \mu\text{M ms}^{-1}$	p_{19}	$0.6 \mu\text{M ms}^{-1}$
$k_{\text{hyd, bas}}$	$6.48 \times 10^{-7} \mu\text{M ms}^{-1}$	p_9	100 μM	p_{20}	2
v_{DH}	$1.1 \mu\text{M ms}^{-1}$	p_{10}	165 mV	A_{tot}	3000 μM
$K_{\text{NADH}_m, \text{DH}}$	1.3	p_{11}	5 mV	$A_{\text{tot}, m}$	15000 μM
K_{DH}	$0.8 \mu\text{M}$	p_{13}	10000 μM	$N_{\text{tot}, m}$	10000 μM
$\frac{F}{2RT}$	0.037	p_{14}	190 mV	C_m	180 mV

Table S3. Parameter for the metabolic module.

71 3. Linear mixed effects modelling

72 To compare the oscillation properties of islets between different groups of animals, care must
73 be taken to account for the fact that measurements from islets have an inherent non-
74 independence: islets from a given mouse are not independent samples when multiple animals
75 are used in a study. In the case of Ca^{2+} imaging, a batch of islets from an individual animal are
76 assayed in one recording, such that inter-animal variability is not present within recordings
77 from a given animal, but only between recordings from different animals. Similarly, variability
78 due to recording conditions occurs when comparing islets from different recordings, but not
79 within a single recording. Finally, within a single recording we recorded islet responses to
80 multiple glucose levels. Linear mixed effects modelling is a technique designed to explicitly
81 handle precisely this type of hierarchical structure in the data. The response variable of interest
82 is modelled as a function of predictor variables (so-called fixed effects) while accounting for
83 the fact that variance is shared among hierarchical groupings in the data (random effects).

84 To test whether oscillation properties were different between islets from male and female
85 PFKM-KO and wild-type animals, we fit linear models using the R function `lm`, or mixed
86 models using the R function `lmer` from the `lme4` package. For each of voltage, Ca^{2+} , and
87 PKAR data, we fit models for oscillation period and plateau fraction. We included PFKM-KO
88 status, sex, and glucose as fixed effects, except in PKAR models where glucose was always
89 11.1 mM. Mouse, recording, and islet were specified as random effects for the analysis of Ca^{2+}
90 data. For voltage recordings, in which only one islet is measured per recording, recording was
91 omitted as a random effect. For PKAR, islets were only exposed to a single glucose level, so
92 islet was omitted as a random effect. The model specification and fitting summaries are shown
93 below; all models were fit using `REML=TRUE`. Summary tables were generated using the
94 “`tab_model`” function from the R package `sjPlot`, with `p.val="Satterthwaite"` .

<i>Predictors</i>	Period (min)			Plateau Fraction		
	<i>Estimates</i>	<i>CI</i>	<i>p</i>	<i>Estimates</i>	<i>CI</i>	<i>p</i>
(Intercept)	2.05	0.24 – 3.85	0.028	0.28	0.17 – 0.38	0.001
Condition [KO]	-1.12	-2.28 – 0.05	0.067	-0.02	-0.11 – 0.06	0.582
Sex [male]	0.71	-0.80 – 2.21	0.361	0.13	0.03 – 0.23	0.046
Glucose [11.1]	2.52	1.26 – 3.79	<0.001	0.29	0.25 – 0.34	<0.001
Random Effects						
σ^2	3.0313			0.0041		
τ_{00}	0.0867 _{Mouse}			0.0035 _{Islet}		
				0.0020 _{Mouse}		
ICC	0.0278			0.5730		
N	14 _{Mouse}			14 _{Mouse}		
				21 _{Islet}		
Observations	38			38		
Marginal R^2 / Conditional R^2	0.338 / 0.357			0.638 / 0.846		

96 Table S4. Summary of linear mixed modelling of period and plateau fraction in voltage
97 recordings. Model formulas were: Period ~ Condition + Sex + Glucose + (1|Mouse); Plateau
98 Fraction ~ Condition + Sex + Glucose + (1|Mouse) + (1|Islet). The reference group (intercept)
99 was Female Control at 8mM glucose. Estimates, 95% confidence intervals, and p-value (bold,
100 $p < 0.05$) for each predictor of Period (left) and Plateau Fraction (right) are shown. A summary
101 of the random effects are also shown: σ^2 , mean variance of random effects; τ_{00} , random
102 intercept variance (between subject variance) for each random effect; ICC, intraclass
103 correlation coefficient (proportion of variance explained by the grouping structure); N, number
104 of groups per random effect; Observations, total number of recordings of islets in any
105 combination of fixed effects; Marginal R^2 , R^2 value considering only fixed effects; Conditional
106 R^2 , R^2 considering both fixed and random effects.

107

108

<i>Predictors</i>	Period (min)			Plateau Fraction		
	<i>Estimates</i>	<i>CI</i>	<i>p</i>	<i>Estimates</i>	<i>CI</i>	<i>p</i>
(Intercept)	5.28	4.66 – 5.90	<0.001	0.32	0.25 – 0.40	0.005
Condition [KO]	-0.71	-1.60 – 0.17	0.151	0.00	-0.10 – 0.11	0.984
Sex [male]	0.72	-0.20 – 1.63	0.154	0.13	0.02 – 0.24	0.088
Glucose [11.1]	-2.22	-2.60 – -1.84	<0.001	0.21	0.20 – 0.23	<0.001
Random Effects						
σ^2	0.9826			0.0021		
τ_{00}	0.1487 _{Recording}			0.0020 _{Islet}		
	0.1152 _{Mouse}			0.0023 _{Recording}		
				0.0021 _{Mouse}		
ICC	0.2117			0.7548		
N	6 _{Mouse}			6 _{Mouse}		
	10 _{Recording}			10 _{Recording}		
				111 _{Islet}		
Observations	156			156		
Marginal R ² / Conditional R ²	0.491 / 0.599			0.653 / 0.915		

110 Table S5. Summary of linear mixed modelling of period and plateau fraction in calcium
111 recordings. Model formulas were: Period ~ Condition + Sex + Glucose + (1|Mouse) +
112 (1|Recording); Plateau Fraction ~ Condition + Sex + Glucose + (1|Mouse) + (1|Recording).
113 The reference group was Female Control at 8mM glucose. The meaning of table entries is as
114 in Table S4.

<i>Predictors</i>	Period (min)			Plateau Fraction		
	<i>Estimates</i>	<i>CI</i>	<i>p</i>	<i>Estimates</i>	<i>CI</i>	<i>p</i>
(Intercept)	7.90	6.48 – 9.32	<0.001	0.59	0.53 – 0.64	<0.001
Condition [KO]	-1.44	-2.90 – 0.02	0.053	-0.02	-0.07 – 0.03	0.397
Sex [male]	0.63	-0.84 – 2.09	0.403	-0.06	-0.11 – -0.01	0.029
Random Effects						
σ^2	0.59					
τ_{00}	0.34 _{Recording}					
	1.11 _{Mouse}					
ICC	0.71					
N	23 _{Recording}					
	14 _{Mouse}					
Observations	51			51		
Marginal R ² / Conditional R ²	0.289 / 0.794			0.096 / 0.058		

117 Table S6. Summary of linear mixed modelling of period and plateau fraction in PKAR
118 recordings. Model formulas were: Period ~ Condition + Sex + (1|Mouse) + (1|Recording);
119 Plateau Fraction ~ Condition + Sex. The reference group was Female Control at 11mM
120 glucose. The meaning of table entries is as in Table S4.

4. Number of mice, islets, and recordings

Modality	Sex	Condition	Mice	Islets	Recordings
V _M	female	ctrl	2	3	3
		KO	1	3	3
	male	ctrl	5	7	7
		KO	6	8	8
Ca ²⁺	female	ctrl	2	55	4
		KO	1	25	2
	male	ctrl	1	10	1
		KO	2	22	3
PKAR	female	ctrl	2	5	3
		KO	5	15	8
	male	ctrl	5	22	8
		KO	2	10	4

Table S7: Number of mice, islets, and recordings per sex and PFKM-KO condition included in quantitative analysis of period and plateau fraction.

5. Summary of islet-level data (sex)

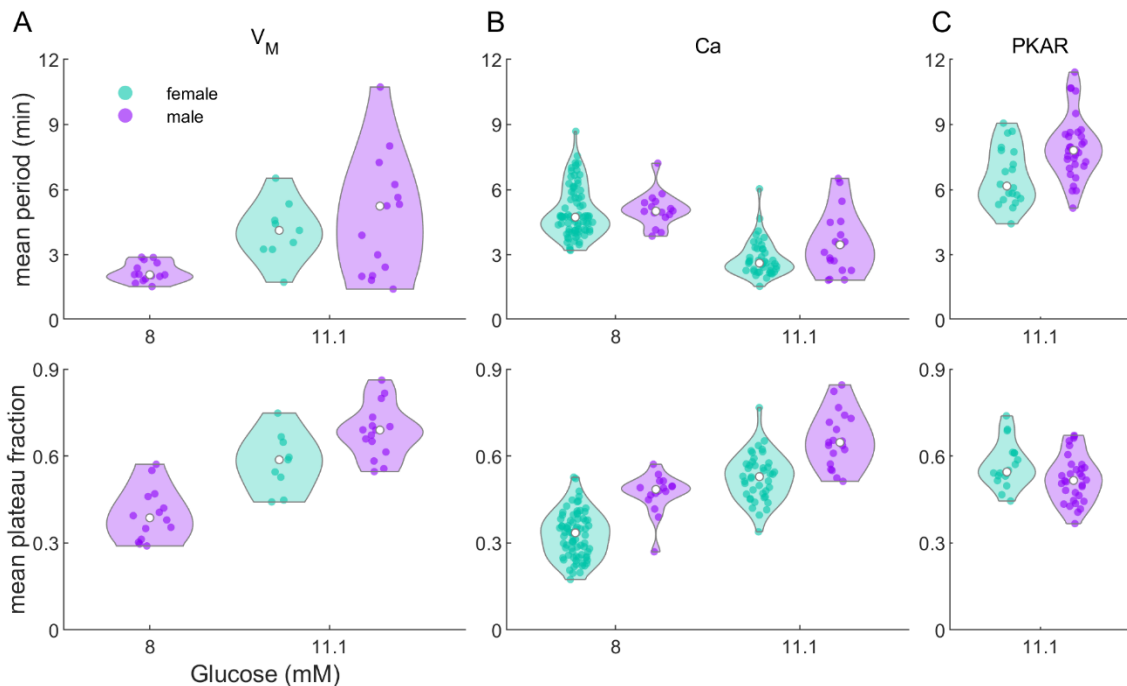


Fig. S1. Comparison of oscillation period and plateau fraction between female and male mice. Violin plots showing mean oscillation period (top panels) and plateau fraction (bottom panels) for islets exposed to specific glucose levels: 8 mM and 11.1mM glucose for membrane potential (panel A) and Ca^{2+} concentration (panel B), or at 11.1 mM glucose for PKAR (panel C). White dots indicate the median across all islets.

124

125

126 References Cited

127

- 128 1. Bertram, R., et al., *Interaction of glycolysis and mitochondrial respiration in metabolic*
 129 *oscillations of pancreatic islets*. *Biophys. J.*, 2007. **92**(5): p. 1544-55.
- 130 2. Marinelli, I., et al., *Transitions between bursting modes in the integrated oscillator*
 131 *model for pancreatic beta-cells*. *J. Theor. Biol.*, 2018. **454**: p. 310-319.

132