## SUPPLEMENTARY FIGURES



**Supplementary Figure 1**. Smoothed spindle power links distinct spindle events over time. (A) mPFC LFP filtered in the spindle frequency band (red) and its power (black) during a representative SWS-to-REM transition. The thicker black curve is the smoothed spindle power (right y axis) while the dashed green line depicts the SWS detection threshold. Blue and yellow bands above mark the periods identified as SWS and REM, respectively. Vertical dashed lines: the boundaries of the example intervals in B and C. (B) Representative examples of raw PFC LFP during SWS (left) and REM (right) during the intervals marked in A. The two representative spindles are marked by the red rectangles. (C) Representative examples of the PFC LFP filtered in the spindle frequency band (red) and its power (black).



Supplementary Figure 2. Separation of periods with high vs. low spindle power. (A) Effectiveness of separation of high vs. low spindle power periods as a function of smoothing window width. The curve peaks at 14 seconds (red dashed line). (B) Bimodality of smoothed (window of 14s) spindle power distributions in all subjects. Red dashed vertical lines indicate individual spindle power thresholds obtained with k-means.



**Supplementary Figure 3**. Detection of REM sleep with theta/delta ratio signal from the PFC. (**A**) Overlap between REM periods detected using HPC LFP and REM periods detected using PFC LFP of the same cortical channel used for SWS detection as a function of smoothing of the PFC theta/delta ratio. Solid line: average across 57 recording sessions. Shaded area: SEM. Note that the optimal overlap was obtained using a Gaussian window of 8 s (vertical yellow line). (**B**) Overlap between HPC and PFC-obtained REM periods as in (A) across all recorded sessions, with the PFC theta/delta ratio smoothed with Gaussian window at 8 s. Circles: individual sessions; box and whisker plots: median and 25th and 75th percentiles. (**C,D**) Example of REM detection with PFC smoothed theta/delta. Same example as in Fig. 2.



**Supplementary Figure 4**. Sleeping during training is an indicator of calmness. Correlation between the time spent freezing during the first two CS+ presentations and time spent sleeping in cued extinction sessions. Sleep time and freezing time are significantly anti-correlated (Spearman rank test, p < 0.001).



Supplementary Figure 5. Representative recording positions in the mPFC (left) and dorsal HPC (right).