### Supplemental Material

# Mechanistic Modeling of a Human IgG4 Monoclonal Antibody (Tralokinumab) Fab Arm Exchange with Endogenous IgG4 in Healthy Volunteers

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#### DIFFFERENTIAL EQUATION SYSTEMS AND INITIAL CONDITIONS

Endogenous IgG4 and half molecules

$$\frac{dXX}{dt} = K_{syn} - \frac{CL}{V_c} \cdot XX + \frac{k_{on}}{V_c} \cdot X \cdot X - k_{off} \cdot XX - \frac{Q}{V_c} \cdot XX + \frac{Q}{V_n} \cdot XX_p \tag{1}$$

$$\frac{dXX_p}{dt} = \frac{Q}{V_C} \cdot XX - \frac{Q}{V_p} \cdot XX_p \tag{2}$$

$$\frac{dX}{dt} = -\frac{cL_{hf}}{V_c} \cdot X - 2 \cdot \frac{k_{on}}{V_c} \cdot X \cdot X + 2 \cdot k_{off} \cdot XX - 2 \cdot \frac{k_{on}}{V_c} \cdot A \cdot X + k_{off} \cdot AX - \frac{Q}{V_c} \cdot X + \frac{Q}{V_p} \cdot X_p$$
(3)

$$\frac{dX_p}{dt} = \frac{Q}{V_c} \cdot X - \frac{Q}{V_p} \cdot X_p \tag{4}$$

Tralokinumab and half maolecules

$$\frac{dAA}{dt} = -\frac{CL}{V_c} \cdot AA + \frac{k_{on}}{V_c} \cdot A \cdot A - k_{off} \cdot AA - \frac{Q}{V_c} \cdot AA + \frac{Q}{V_p} \cdot AA_p$$
 (5)

$$\frac{dAA_p}{dt} = \frac{Q}{V_C} \cdot AA - \frac{Q}{V_D} \cdot AA_p \tag{6}$$

$$\frac{dA}{dt} = -\frac{cL_{hf}}{V_c} \cdot A - 2 \cdot \frac{k_{on}}{V_c} \cdot A \cdot A + 2 \cdot k_{off} \cdot AA - 2 \cdot \frac{k_{on}}{V_c} \cdot A \cdot X + k_{off} \cdot AX - \frac{Q}{V_c} \cdot A + \frac{Q}{V_p} \cdot A_p$$

$$(7)$$

$$\frac{dA_p}{dt} = \frac{Q}{V_c} \cdot A - \frac{Q}{V_p} \cdot A_p \tag{8}$$

Hybrid IgG<sub>4</sub>

$$\frac{dAX}{dt} = -\frac{CL}{V_c} \cdot AX + 2 \cdot \frac{k_{on}}{V_c} \cdot A \cdot X - k_{off} \cdot AX - \frac{Q}{V_c} \cdot AX + \frac{Q}{V_p} \cdot AX_p \tag{9}$$

$$\frac{dAX_p}{dt} = \frac{Q}{V_c} \cdot AX - \frac{Q}{V_p} \cdot AX_p \tag{10}$$

Total IgG<sub>4</sub>

$$DV = AA + XX + AX + \frac{1}{2}A + \frac{1}{2}X \tag{11}$$

Total tralokinumab

$$DV = AA + \frac{1}{2}A + \theta \cdot AX \tag{12}$$

Initial condition from total IgG4 assay,

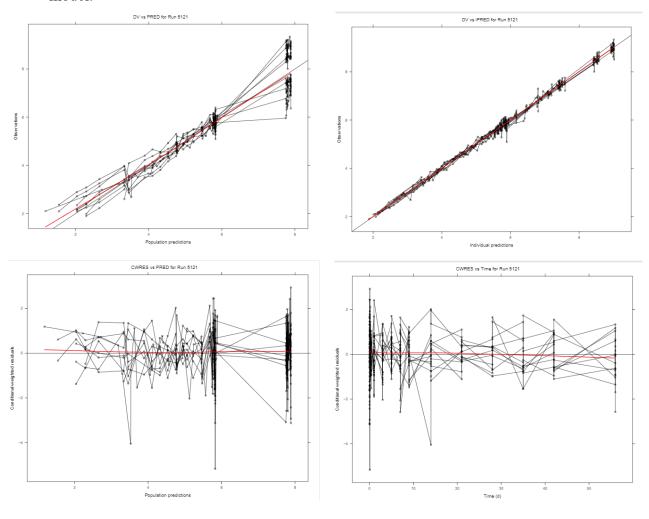
$$G_0 = IgG4_{baseline} \cdot V_c = XX_0 + \frac{1}{2}X_0 \tag{13}$$

$$X_0 = \frac{-(k_{hf} + k_{off}) + \sqrt{(k_{hf} + k_{off})^2 + 16 \cdot k_{on} \cdot k_{off} \cdot G_0}}{4 \cdot k_{on}}$$
(14)

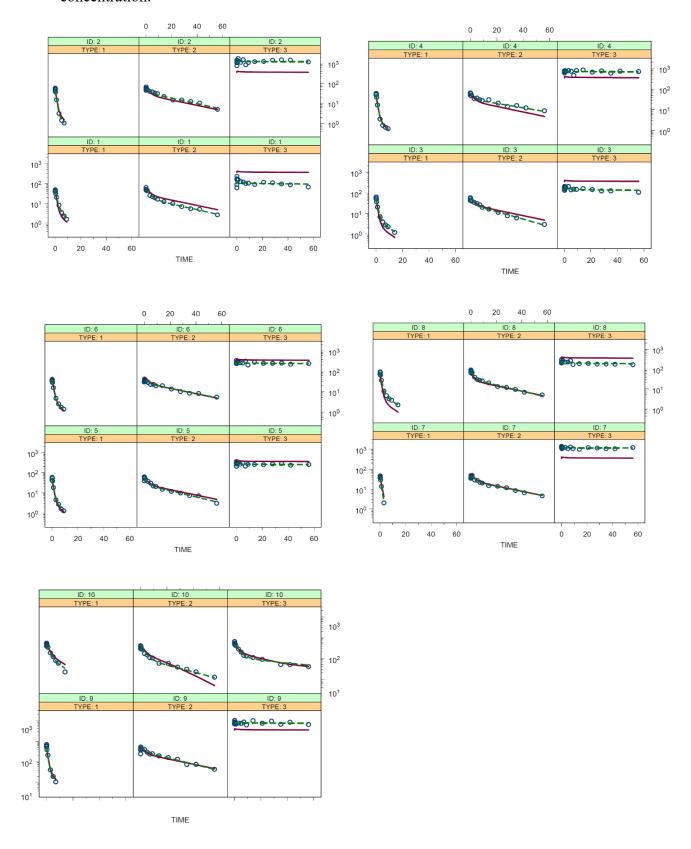
$$K_{syn} = k_{ab} \cdot XX_0 + \frac{1}{2}k_{hf} \cdot X_0 \tag{15}$$

$$XX_{0,p} = \frac{v_p}{v_c} \cdot XX_0 \tag{16}$$

**Supplemental Figure \$1** Basic goodness-of-fit plots for mechanistic IgG<sub>4</sub> Fab-arm exchange model.



## **Supplemental Figure S2** Observed and model-predicted tralokinumab and IgG<sub>4</sub> serum concentration.



#### Supplemental Figure S3 Model-predicted typical half- and hybrid IgG<sub>4</sub> profiles.

