1	Supplementary Materials for
2	Intralayer phonons in multilayer graphene moiré superlattices
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Abstract

The contents of the Supplementary Materials are summarized as follows: (1) optical images of multilayer graphene moiré superlattice (MLG-MS) and the lattice structures; (2) comparison of frequency difference of Davydov components between vdW model and experimental results; (3) Davydov splitting of nonfolded ZO modes in t(1+2)LG and t(2+2)LG; (4) the vibration patterns for each Davydov component of mZO modes in t(m + n)LGs.

²³ 1 Optical images of MLG-MS and the lattice structures

Here we show the typical optical images and the schematic lattice structures of MLG-MS. The layer
 number of MLG flakes is identified by optical contrast and Raman spectra.



Figure 1: Optical images of t(m+n)LGs. Optical images of (a) t(2+2)LG with twist angle $\theta_t=16.8^{\circ}$ (b) t(1+2)LG and t(1+3)LG twist angle $\theta_t=7.9^{\circ}$. (a) is prepared by self-folding during the exfoliation while (b) is produced by transferring. The scale bars are shown.



Figure 2: Optical contrast and Raman spectra of t(1+3)LG. (a) Optical contrast of t(1+3)LG and 4LG. (b) Raman spectra of t(1+3)LG, 1LG and 3LG in the G and 2D spectral range.



Figure 3: Moiré pattern in t(m + n)LG. Schematic structure of t(1+3)LG with the 1LG (green) sitting on the top of the 3LG (red). The 1LG and 3LG constituents are twisted by an angle (θ_t) of 11.3°, which shows evident moiré pattern. Vectors L_1 and L_2 define the supercell.

²⁶ 2 Comparison of frequency difference of Davydov compo ²⁷ nents between vdW model and experimental results

The Davydov splitting in multilayer and twisted transition metal dichalcogenides (TMDs) are well represented by the vdW model by considering the interlayer coupling as the first approximation,



Figure 4: Frequency differences between Davydov components of nonfolded ZO modes based on vdW model. The experimental (black crosses) and calculated (open circles) frequency differences $(\Delta \omega)$ between each Davydov components and the lowest-frequency one in t(m+n)LGs without (a) and with (b) interfacial coupling considered.

where the frequency differences between each Davydov component and the lowest-frequency one 30 can be estimated by the frequency of the corresponding layer-breathing phonon with the same 31 number of in-phase/out-of-phase interlayer vibrations between the nearest adjacent atomic planes 32 [1–3]. Here we tried to apply the vdW model to understand the observed Davydov components in 33 MLG-MS. Firstly, we neglect interfacial coupling and apply the vdW model to the calculate the 34 frequency difference between the Davydov components and the uncoupled (lowest-frequency) one 35 in mLG and nLG constituents. We predict the Davydov components in t(1+2)LG and t(1+3)LG36 are respectively the same as those in 2LG and 3LG. Indeed, the number of the observed Davydov 37 components is in line with the prediction. However, clear deviations of frequency differences are 38 present in Figure 4(a). Considering the interfacial coupling is close to the interlayer coupling in 39 AB-stacked MLG, the corresponding Davydov components can be also calculated. In this case, both 40 the number of Davydov components and frequency differences between each Davydov component 41 and the lowest-frequency one are inconsistent with the experimental results, as elucidated in Figure 42 4(b). This suggests that the vdW model commonly used to reproduce the Davydov splitting in 43 TMDs consisting of three-atomic layers is not applicable for MLG-MS. 44

45 3 Davydov splitting of nonfolded ZO modes in t(1+2)LG and 46 t(2+2)LG

⁴⁷ According to the PM, the Davydov splitting of nonfolded ZO phonon in t(2+2)LG is localized within ⁴⁸ the 2LG constituents, as shown in Figure 5(a). This is the same as in t(1+2)LG (Figure 5(b)) and ⁴⁹ consistent with the observation in experiment, further confirms the validity of PM to understand the ⁵⁰ localized Davydov components of nonfolded ZO phonons within the constituents of t(m + n)LGs, ⁵¹ including the assumption of negligible perturbation from patterned interfacial coupling (i.e., $\epsilon_t=0$).

(a) t(1+2)LG			
ZO _{2,1} : 868.2	ZO _{1,1} : 870.9	ZO _{2,2} : 871.3	
0 -0 0 00 0- 0	ő-<u>9</u> 0 000 0 0	0 -0-0000-0	
ê ,	-00-00-00-	60-00-00-	
ę ės es a	••••• ••	÷	
(b) t(2+2)LG			
ZO _{2,1} : 868.2	ZO _{2,1} : 868.2	ZO _{2.2} : 871.3	ZO _{2,2} : 871.3
0-0-0-00000 G	• •••••••• •	0-0-0-00000 G	0−0−0 0000 0
0-0-0-0-0	6- <u>90000</u> a	200000	0 -0-0000-0
			- 00-00-
			

Figure 5: Davydov splitting of nonfolded ZO modes in t(1+2)LG and t(2+2)LG. Atomic displacements and mode frequencies of Davydov components for nonfolded ZO phonons in (a) t(1+2)LG and (b) t(2+2)LG by the SPM, the arrow lengths represent the amplitudes of atomic displacements.

⁵² 4 The vibration patterns for each Davydov component of ⁵³ mZO modes in t(m+n)LGs



Figure 6: Atomic displacements of Davydov components of mZO modes in t(1+2)LG. Atomic displacements of three Davydov components of mZO in a 3×3 supercell of t(1+2)LG with $\theta_t=21.8^\circ$: (a) mZO₁ (b) mZO₂ and (c) mZO₃.

The modulations from moiré superlattices can be directly reflected by the corresponding atomic displacements of each Davydov component of mZO modes. In contrast to nonfolded ZO phonon where the interfacial coupling is really weak to couple three layers, the patterned interfacial coupling introduces a perturbation to the mZO phonons and leads to three Davydov components, as shown in Figure 6. Furthermore, the vibrations for mZO phonons in t(1+2)LG are modulated by the moiré superlattices and the vibrations at each layer show high symmetry. However, the atomic



Figure 7: Atomic displacements of Davydov components of the corresponding unfolded ZO modes in 2LG. Atomic displacements of three Davydov components of the corresponding unfolded ZO(q)in AB-stacked 3LG: (a) $ZO_1(q)$ (b) $ZO_2(q)$ and (c) $ZO_3(q)$, where q is the wave vector same as the moiré reciprocal basic vector.

- displacements of the corresponding unfolded $ZO_i(q)$ (i = 1, 2, 3) phonon in 3LG exhibit distinctly
- $_{61}$ different vibration patterns (Figure 7), without any signature of C_3 symmetry.

62 References

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