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Appendix S1: Detailed description of model equations, its parameters, and rate formulas.

Table S1. Full set of equations for community models I, II and III. For values, definitions, units and references of the variables, rates and parameters, see Table S2 below.

Community I	Community II	Community III
Two unstructured species	One stage-structured species	Two stage-structured species
$\frac{dR_{S}}{dt} = \delta_{R_{S}} (R_{S \max} - R_{S}) - I_{C_{S}}(R_{S}) C_{S} - I_{C_{L}}(R_{S}) C_{L}$ $\frac{dR_{L}}{dt} = \delta_{R_{L}} (R_{L \max} - R_{L}) - I_{C_{S}}(R_{L}) C_{S} - I_{C_{L}}(R_{L}) C_{L}$ $\frac{dC_{S}}{dt} = \beta_{C_{S}} I_{C_{S}} C_{S} - m_{C_{S}} C_{S} - \mu_{C_{S}} C_{S}$ $\frac{dC_{L}}{dt} = \beta_{C_{L}} I_{C_{L}} C_{L} - m_{C_{L}} C_{L} - \mu_{C_{L}} C_{L}$ $I_{C_{S}} = \frac{p \frac{I_{C_{S}R_{S}} \max}{H_{C_{S}R_{S}}} R_{S} + (1 - p) \frac{I_{C_{S}R_{L}} \max}{H_{C_{S}R_{L}}} R_{L}}$ $I_{C_{L}} = \frac{(1 - p) \frac{I_{C_{L}R_{S}} \max}{H_{C_{L}R_{S}}} R_{S} + p \frac{I_{C_{L}R_{L}} \max}{H_{C_{L}R_{L}}} R_{L}}$	$\frac{dR_S}{dt} = \delta_{R_S} (R_{S \max} - R_S) - I_J(R_S) J - I_A(R_S) A$ $\frac{dR_L}{dt} = \delta_{R_L} (R_{L \max} - R_L) - I_J(R_L) J - I_A(R_L) A$ $\frac{dJ}{dt} = \max(v_A, 0) A + v_J J - \max(v_J, 0) J - \mu_J J$ $\frac{dA}{dt} = \max(\gamma_J, 0) J + \min(v_A, 0) A - \mu_A A$ $I_J = \frac{p \frac{I_{JR_S} \max}{H_{JR_S}} R_S + (1 - p) \frac{I_{JR_L} \max}{H_{JR_L}} R_L}{1 + \frac{p}{H_{JR_S}} R_S + \frac{(1 - p)}{H_{JR_L}} R_L}$ $I_A = \frac{(1 - p) \frac{I_{AR_S} \max}{H_{AR_S}} R_S + p \frac{I_{AR_L} \max}{H_{AR_L}} R_L}{1 + \frac{(1 - p)}{H_{AR_S}} R_S + \frac{p}{H_{AR_L}} R_L}$ $v_J = \beta_J I_J - m_J$ $v_J = \beta_A I_A - m_A$	$\frac{dR_{S}}{dt} = \delta_{R_{S}} (R_{S\max} - R_{S}) - I_{J_{S}}(R_{S}) J_{S} - I_{A_{S}}(R_{S}) A_{S} - I_{J_{L}}(R_{S}) J_{L}$ $\frac{dR_{L}}{dt} = \delta_{R_{L}} (R_{L\max} - R_{L}) - I_{A_{S}}(R_{L}) A_{S} - I_{J_{L}}(R_{L}) J_{L} - I_{A_{L}}(R_{L}) A_{L}$ $\frac{dJ_{S}}{dt} = \max(v_{A_{S}}, 0) A_{S} + v_{J_{S}} J_{S} - \max(\gamma_{J_{S}}, 0) J_{S} - \mu_{J_{S}} J_{S}$ $\frac{dA_{S}}{dt} = \max(\gamma_{J_{S}}, 0) J_{S} + \min(v_{A_{S}}, 0) A_{S} - \mu_{A_{S}} A_{S}$ $\frac{dJ_{L}}{dt} = \max(v_{A_{L}}, 0) A_{L} + v_{J_{L}} J_{L} - \max(\gamma_{J_{L}}, 0) J_{L} - \mu_{J_{L}} J_{L}$ $\frac{dA_{L}}{dt} = \max(\gamma_{J_{L}}, 0) J_{L} + \min(v_{A_{L}}, 0) A_{L} - \mu_{A_{L}} A_{L}$ $v_{J_{S}} = \beta_{J_{S}} I_{J_{S}} - m_{J_{S}}$ $\gamma_{J_{S}} = \frac{v_{J_{S}} - \mu_{J_{S}}}{1 - z_{J_{S}A_{S}}} \sum_{1 - z_{J_{L}A_{L}}} \sum_{1 - v_{J_{L}}} \sum_{$
		$1 - z_{J_L A_L} \qquad \forall J_L$
		$\nu_{A_L} = \beta_{A_L} I_{A_L} - m_{A_L}$

Variable or rate	Formula	Definition and unit	References
R_j	-	Resource biomass density (mg dry mass/L)	-
C_i	-	Consumer biomass density (mg dry mass/L)	-
<i>J</i> , <i>J</i> _{<i>i</i>}	-	Juvenile consumer biomass density (mg dry mass/L)	-
A, A_i	-	Adult consumer biomass density (mg dry mass/L)	
R _{S max}	$4.2 \cdot 10^{-3} \cdot \exp(0.15/(k \cdot T))$	Supply (maximum) R_S biomass density (mg dry mass/L)	1, 8, 12, 16
R_{Lmax}	$5.9 \cdot 10^{-7} \cdot \exp(0.38/(k \cdot T))$, or = $R_{S max}$	Supply (maximum) R_L biomass density (mg dry mass /L)	1, 12, 16
I _{i max}	$\frac{1}{M_j} \cdot 19 \cdot M_j^{0.7} \cdot \exp\left(\frac{-\left(T - T_{opti}\right)^2}{2 \cdot s^2}\right)$	Mass-specific maximum ingestion rate of C_i (mg/[mg·day]) [†]	15, 16
m _i	$\frac{1}{M_i} \cdot 8.5 \cdot 10^8 \cdot M_i^{0.7} \cdot \exp\left(-0.56/(k \cdot T)\right)$	Mass-specific metabolic rate of C_i (1/day)	3, 8, 16
Parameter	Value	Definition and unit	
M _i	$C_S, J, J_S = 0.1; C_L, A, A_S, J_2 = 1; A_L = 10$	Body mass of C_i (ng dry mass in the model, here given in μg) [‡]	2, 6, 9, 10, 11, 19
Т	Control parameter; 273.15–313.15	Ambient temperature (K; 0–40 °C)	-
T _{opti}	C_S , J , J_S =24; C_L , A , A_S , J_L =20; A_L =16, or =20 for all	Temperature optimum of $I_{i max}$ of C_i (K in the model, here given in °C)	13, 16, 17
S	8	Curve breadth of the temperature dependence of $I_{i max}$ (K)	16
k	$8.6 \cdot 10^{-5}$	Boltzmann constant (eV/K)	-

Table S2. The list of values, definitions, units and references of the variables, rates and parameters used in models I, II and III. The reference list is found below.

δ_{R_j}	0.1	R_j supply (inflow) rate (1/day)	4, 5, 7
β_i	0.6	C_i conversion efficiency (unitless)	14, 15
p	Control parameter; 0–1	Diet preference (unitless)	-
H_{iR_j}	0.2	Half-saturation constant of C_i on R_j (mg dry mass/L) [†]	15, 16
Z _{kl}	0.1	Juvenile k to adult l body mass ratio (unitless)	2, 6, 9, 10, 11, 19
μ_i	0.01	Background mortality of C_i (1/day) [•]	5, 18

Footnotes

[†] We used the Monod instead of the Holling function, as the former allows to assume temperature dependence of only a single parameter – in our case the maximum ingestion rate I_{max} – while keeping the half-saturation constant *H* body size- and temperature-independent (Fussmann et al. 2014, Mulder and Hendriks 2014). As the half-saturation constant is strongly correlated with the maximum ingestion rate, changing either of these two parameters affects the consumer functional response in a similar way (Kiørboe and Andersen 2019, Barraquand and Gimenez 2021).

[‡] The lowest size category $M = 0.1 \,\mu\text{g}$ was assumed for consumer species C_S , and consumer juveniles J and J_S in models I, II and III, respectively. This size corresponds to small planktonic grazers such as rotifers, juveniles of small crustacean species such as *Bosmina*, or naupliar stages of copepods. The medium size category $M = 1 \,\mu\text{g}$ was assumed for consumer species C_L , consumer adults A, and adults A_S and juveniles J_L in models I, II and III, respectively. This corresponds to planktonic grazers such as adult *Bosmina* and juvenile (copepodite) copepod stages. The largest size category $M = 10 \,\mu\text{g}$ was assumed for consumer adults for consumer adults A_L in model III, and corresponds to adult stages of copepods and larger crustaceans.

* Our formulation of the stage-structured model requires the background mortality $\mu > 0$ (see the formula for the maturation rate γ). The background mortality can represent additional sources of consumer biomass loss (apart from metabolic rate) such as predation by higher trophic levels or anthropogenic exploitation.

Here, we assume a low background mortality rate identical for all species and stages, and explore model sensitivity to changes in this parameter in Appendix S2: Fig. S1.

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Figure S1. Temperature-dependent and body mass M-dependent rate parameters across the temperature gradient T. For parameter definitions and references, see Appendix S1: Table S2.

A: Supply (maximum) resource density (mg dry mass/L) with a size-temperature interaction present. In absence of a size-temperature interaction, for both resources their supply densities are equal to $R_{s max}$ (dashed line).

B1: Mass-specific maximum ingestion rate of consumers (mg resource dry mass per day per mg consumer dry mass) with a size-temperature interaction present. B2: Mass-specific maximum ingestion rate of consumers (mg resource dry mass per day per mg consumer dry mass) with a size-temperature interaction absent, i.e. the temperature optimum of I_{max} occurs at 20 °C for all consumers.

C1: Mass-specific metabolic rate of consumers (per day per mg dry mass) with a size-temperature interaction absent. C2: Mass-specific metabolic rate of consumers (per day per mg dry mass) with a size-temperature interaction present in the allometric exponent of the metabolic rate $m = \frac{1}{M} \cdot 8.5 \cdot 10^8 \cdot M^{(0.7+0.0005 \cdot T)} \cdot \exp(-0.56/(k \cdot T))$, where *M* is the consumer dry body mass (ng), and *k* is the Boltzmann constant.

Curves from C1 (without a size-temperature interaction) are shown as thinner dashed lines. Note that each consumer suffers from higher metabolic rate in the presence of a size-temperature interaction proportionally to its size, with the largest consumer having the highest relative increase in *m*. For further information and results including this assumption, see Appendix S2, and Figure S4 therein.



