

Paleoceanography and Paleoclimatology

Supporting Information for

Earth System Model Analysis of how Astronomical Forcing is Imprinted onto the Marine Geological Record: The role of the Inorganic (Carbonate) Carbon Cycle and Feedbacks

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Table S1. Input parameters for carbonate (Ca) weathering, silicate (Si) weathering, volcanic outgassing, and the reference temperature for weathering for the initial spin-up state of SYMM and ASYM simulations. Below, the steady state model output values for atmospheric carbon dioxide ($_{p}CO_{2}$) concentrations, global annual mean atmospheric temperature, surface and deep ocean temperature, total amount of ocean alkalinity (ALK) and dissolved inorganic carbon (DIC), and global mean calcium carbonate (CaCO₃) in marine sediment.

Parameters	SYMM	ASYM			
Ca weathering flux	7.00 Tmol C yr ⁻¹	7.00 Tmol C yr ⁻¹			
Si weathering flux	6.93 Tmol C yr ⁻¹	5.60 Tmol C yr ⁻¹			
Volcanic outgassing	7.00 Tmol C yr ⁻¹	7.00 Tmol C yr ⁻¹			
Reference temperature	23.79°C	19.45°C			
Results	SYMM	ASYM			
Atmospheric <i>p</i> CO ₂	834 ppm	828 ppm			
Atmospheric temperature	22.6°C	23.1°C			
Surface/deep ocean temperature	24.5°C / 6.6°C	27.2°C / 7.8°C			
Ocean ALK	1629 μmol kg ⁻¹	1517 μmol kg ⁻¹			
Ocean DIC	1661 μmol kg ⁻¹	1557 μmol kg ⁻¹			
Sedimentary CaCO ₃	51 wt%	47 wt%			

Table S2. The average ranges of individual astronomical cycles in the global annual mean benthic temperature (ben T), atmospheric CO₂, benthic DIC δ^{13} C, and wt% CaCO₃ across the modeled four million years. Average ranges are calculated from the FFT amplitude spectrum. Below, the relative phasing (in degrees) between the imposed short and long eccentricity forcing and the proxies. Positive values indicate that eccentricity forcing is leading. Negative values indicate that the proxy leads eccentricity. Green shows relatively in-phase relationships. Red colors suggest a relatively anti-phased relationship.

	ASYM							SYMM	SYMM	
	Exp.0	Exp.1	Exp.2	Exp.3	Exp.4	Exp.0	E	kp.1	kp.1 Exp.2	kp.1 Exp.2 Exp.3
Average range (=amplitude*2)										
ben T, precession	0.07°C	0.05°C	0.06°C	0.06°C	0.11°C		-	-		
ben T, obliquity		0.08°			0.08°C	0.06°C	C).06°	0.06° 0.05°C	0.06° 0.05°C 0.06°C
ben T, short ecc	0.25°C	0.28°C	0.26°C	0.30°C	0.25°	0.22°C	0	.24°C	.24°C 0.23°C	.24°C 0.23°C 0.27°C
ben T, long ecc	0.30°C	0.33°C	0.31°C	0.39°C	0.25°C	0.26°C	0.2	8°C	8°C 0.28°C	8°C 0.28°C 0.34°C
CO ₂ , precession	2.2 ppm	2.4 ppm	5.5 ppm	3.9 ppm	17 ppm	2.6 ppm	2.8 p	pm	pm 1.4 ppm	pm 1.4 ppm 2.7 ppm
CO ₂ , obliquity	4.8 ppm	5.2 ppm	1.9 ppm		11 ppm				2.4 ppm	2.4 ppm 2.4 ppm
CO ₂ , short ecc	4.8 ppm	5.2 ppm	2.9 ppm	12 ppm	9 ppm	3.6 ppm	3.8 ppn	n	n 3.4 ppm	n 3.4 ppm 12 ppm
CO ₂ , long ecc	5.6 ppm	6.2 ppm	3.5 ppm	19 ppm	26 ppm	4.2 ppm	4.5 ppm	1	4.0 ppm	4.0 ppm 17 ppm
d ¹³ C, precession	0.016 ‰	0.016 ‰	0.021 ‰	0.021 ‰	0.028 ‰	0.012 ‰	0.012 ‰		0.013 ‰	0.013 ‰ 0.013 ‰
d ¹³ C, obliquity	0.024 ‰	0.024 ‰	0.025 ‰	0.022 ‰	0.028 ‰	0.003 ‰			0.005 ‰	0.005 ‰ 0.005 ‰
d ¹³ C, short ecc	0.005 ‰	0.005 ‰	0.005 ‰	0.009 ‰	0.009 ‰	0.003 ‰	0.003 ‰		0.003 ‰	0.003 ‰ 0.003 ‰
d ¹³ C, long ecc	0.005 ‰	0.006 ‰	0.006 ‰	0.011 ‰	0.036 ‰	0.002 ‰	0.002 ‰		0.002 ‰	0.002 ‰ 0.003 ‰
CaCO ₃ , precession	0.3 wt%	0.3 wt%	0.1 wt%	0.1 wt%	0.4 wt%				0.2 wt%	0.2 wt% 0.2 wt%
CaCO ₃ , obliquity	0.4 wt%	0.4 wt%	0.1 wt%	0.1 wt%	0.3 wt%	0.1 wt%	0.1 wt%			0.1 wt%
CaCO ₃ , short ecc	0.3 wt%	0.3 w%	0.5 wt%	0.4 wt%	0.7 wt%	0.2 wt%	0.6 wt%		0.6 wt%	0.6 wt% 0.4 wt%
CaCO ₃ , long ecc	0.4 wt%	0.5 wt%	0.7 wt%	0.2 wt%	1.1 wt%	0.3 wt%	0.8 wt%	0	.9 wt%	.9 wt% 0.2 wt%
Relative phasing (multi-taper o	oherence) [va	lues in degr	ees]							
short ecc - ben T		l 5	4	11	-9	4	4		4	4 10
short ecc - CO ₂	e	5 7	6	36	-112	 10) 11		9	9 29
short ecc - d ¹³ C	29) 29	29	33	-82	132	. 132		136	136 108
short ecc - CaCO ₃	29	9 29	31	-18	37	25	26	•	26	26 -17
long ecc - ben T	1	L 1	1	4	-30	1	. 1		. 1	. 1 3
long ecc - CO ₂	2	2 2	1	10	-125	 2	2	2	2 2	2 2 8
long ecc - d ¹³ C	7	7 8	7	-22	-117	164	163		166	166 -110
long ecc - CaCO ₃	e	5 7	8	-50	-9	6	6		7	7 -40



Figure S1. Ocean depth of SYMM and ASYM. A latitude-longitude ocean sediment depth grid for (a) SYMM and (b) ASYM. Bright yellow colors indicate land masses. The hypsometric curve for (c) SYMM and (d) ASYM ocean sediments showing the cumulative distribution of ocean sediment depth generated with 'muffingen' v0.9.25 (DOI: 10.5281/zenodo.5130677).







Figure S3. Exp.1, ocean circulation and CO₂ solubility feedbacks in SYMM. (a) Astronomical forcing parameters (eccentricity, obliquity (in degrees), and precession index (e sin ϖ)) and their Fast Fourier Transform (FFT) normalized to the highest individual power. (b) Change in benthic ocean temperature. (c) Change in the maximum Southern Hemisphere ocean overturning strength, defined by the maximum overturning strength reached in the SH across all ocean depth levels. (d) Change in atmospheric CO₂. (e) Change in benthic DIC δ^{13} C. (f) Change in wt% CaCO₃. All variables are annual global mean values and are accompanied by their respective FFTs, normalized to the peak with maximum power.



Figure S4. Exp.2, marine surface productivity feedback in SYMM. (a) Astronomical forcing parameters (as per Figure 3a). (b) Change in the export of particulate organic carbon (POC). (c) Change in the export of CaCO₃. (d) Change in atmospheric CO₂. (e) Change in benthic DIC δ^{13} C. (f) Change in wt% CaCO₃. All variables are annual global mean values and are accompanied by their respective FFTs, normalized to the peak with maximum power. In blue, the values are plotted as anomalies with the previous experiment and depict the change driven by the marine productivity feedback only. Likewise, the FFTs are plotted as anomalies. A positive (green) value on the y-axis indicates an increase in relative power and a negative (red) value indicates a decrease in relative power compared to the previous experiment.



Figure S5. Exp.3, deep marine CaCO₃ feedback in SYMM. (a) Astronomical forcing parameters (as per Figure 3a). (b) Change in benthic ocean temperature. (c) Change in the export of CaCO₃. (d) Change in atmospheric CO₂. (e) Change in benthic DIC δ^{13} C. (f) Change in wt% CaCO₃. All variables are annual global mean values and are accompanied by their respective FFTs, normalized to the peak with maximum power. In blue, the values are plotted as anomalies with the previous experiment and depict the change driven by the marine CaCO₃ feedback only. Likewise, the FFTs are plotted as anomalies. A positive (green) value on the y-axis indicates an increase in relative power and a negative (red) value indicates a decrease in relative power compared to the previous experiment.



Figure S6. Exp.4, terrestrial rock weathering feedback in SYMM. (a) Astronomical forcing parameters (as per Figure 3a). (b) Change in surface land temperature. (c) Change in the rate of terrestrial weathering. (d) Change in atmospheric CO₂. (e) Change in benthic DIC δ^{13} C. (f) Change in wt% CaCO₃. All variables are annual global mean values and are accompanied by their respective FFTs, normalized to the peak with maximum power. In blue, the values are plotted as anomalies with the previous experiment and depict the change driven by the terrestrial weathering feedback only. Likewise, the FFTs are plotted as anomalies. A positive (green) value on the y-axis indicates an increase in relative power and a negative (red) value indicates a decrease in relative power compared to the previous experiment.



Figure S7. Cumulative astronomical impact of SYMM simulations. (a) Astronomical forcing parameters (as per Figure 3a). (b) Annual global mean temperature change in the benthic (black) and surface (blue) ocean. (c) Annual global mean pCO₂ change. (d) Annual global mean DIC δ^{13} C change in the benthic (black) and surface (blue) ocean. (e) Global mean sedimentary CaCO₃ change. All variables are accompanied by their respective FFTs, normalized to the peak with maximum power. The combined impact of all four climate-carbon feedbacks on atmospheric, ocean, and sedimentary reservoirs.



Figure S8. Relative spectral power of astronomical elements. The relative spectral power of the long (267-500 kyr) and short (78-154 kyr) eccentricity, obliquity (36-41 kyr), and precession (18-24 kyr) cycles in the simulated (a) pCO_2 , (b) marine CaCO₃, and (c) DIC δ^{13} C in the four experimental designs of Exp.1, Exp.2, Exp.3, and Exp.4. Left bars are results from the SYMM simulations and right bars are ASYM results.



Figure S9. Benthic carbonate ion concentrations. The change in carbonate ion concentration ($[CO_3^{2-}]$) as a result of astronomically induced changes in ocean temperature, circulation, and ocean solubility (Exp.1) for (a) ASYM and (b) SYMM with their respective FFT power spectra normalized to the peak with maximum power.