

Supplementary Materials for  
**Protein diffusion in *Escherichia coli* cytoplasm scales with the mass of the complexes and is location dependent**

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Supplementary Text  
Figs. S1 to S6  
Table S1  
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**Other Supplementary Materials for this manuscript includes the following:**

Tables S2 and S3

**Other Supplementary Materials for this manuscript includes:**

- Table S2: Lengths and widths of analyzed cells.

This table reports information on the length and the width of all the analyzed cells. Cells' lengths and widths are separated in columns according to the protein they were expressing.

- Table S3: Diffusion coefficients and displacements of analyzed cells.

This table reports information on the number of displacements measured in each region (cell center, right pole, left pole) of each cell and the related diffusion coefficient. Diffusion values and number of displacements are separated in different columns, representing the different regions of the cell. Data are then further separated in clusters representing the expressed protein.

## Supplementary Text

### On cytoplasmic viscosity

We observe that the diffusion coefficient scales with the complex molecular mass in the following manner:

$$D_{\text{observed}} \approx \alpha M_{\text{complex}}^{-0.54}$$

Where  $M_{\text{complex}}$  represents the complex molecular mass, which was calculated as sum of the mass of the monomeric protein plus the fluorescent probe (mEos3.2) and multiplied by the oligomeric state number.

The Einstein-Stokes equation states that for non-interacting spherical particles moving of Brownian motion:

$$D = \frac{k_B T}{6\pi\eta r} \quad (1)$$

where  $k_B$  is the Boltzmann constant,  $T$  is the absolute temperature,  $\eta$  is the viscosity of the solvent and  $r$  is the radius of the diffusing particle. We can rewrite this equation as:

$$D = \frac{k_B T}{6\pi\eta R} = \frac{k_B T}{6\pi\eta \sqrt[3]{\frac{3}{4\pi} V_{\text{sphere}}}} \quad (2)$$

We know that:

$$V = \frac{m}{\rho} \quad (3)$$

$$m = \text{moles} * M_{\text{complex}} \quad (4)$$

$$1 \text{ mole} \equiv 1 N_A \text{ of particles} \quad (5)$$

Hence, we obtain:

$$V = \frac{M_{\text{complex}}}{\rho N_A} \quad (6)$$

So, we can rewrite the Einstein-Stokes equation as:

$$D \sim \frac{k_B T}{6\pi\eta \sqrt[3]{\frac{3}{4\pi} \frac{M_{\text{complex}}}{\rho N_A}}} \quad (7)$$

which means that:

$$D \propto M_{\text{complex}}^{-0.33} \quad (8)$$

Our experimental relationship differs substantially from the Einstein-Stokes equation. What is the basis for this difference? Clearly, the proteins are not perfect spheres, but if this parameter is important we would not have found the relationship with complex molecular mass. A similar argument could be made for surface charge. If deviations from the Einstein-Stokes equation are due to differences in protein charge, we would have lost the observed relationship. Another possibility would be that random walk is not an appropriate model for describing the diffusion of

proteins inside the bacterial cell. However we do not see any clear dependence of diffusion on any of the analyzed parameters (abundance, loneliness or oligomeric state) except for the complex mass. If random walk was not an appropriate model for diffusing particles in the bacterial cytoplasm, then we should have seen some relationship with one of the other analyzed parameters.

To ensure that our results were not biased by a systematic error, we compared a regression model with unconstrained fitting parameters and with an exponent power constrained to -0.33, which is the value given by the Einstein-Stokes equation. According to the extra sum-of-squares F test, which compares the goodness-of-fit of two alternative nested models (unconstrained and constrained), the unconstrained model with an exponent value of -0.54 was significantly better (p-value  $\ll 0.01$ ) than the constrained model for describing the relationship between apparent diffusion and complex molecular weight for the set of native proteins. As a quantitative measure of fitting error for unconstrained and constrained regression models, the absolute sum of squares was selected. The absolute sum of squares for the unconstrained and constrained models are 741.4 and 1059.1, respectively, which indicates a 43% decrease in the deviation for the unconstrained fitting model. Hence, we conclude that the power-law model with an exponent of -0.54 is a better fit for correlating experimental diffusion data with the molecular weight of the protein complexes. We also notice that the protein density is more or less constant for proteins bigger than 30 kDa, with a fixed value of  $\sim 1.41 \text{ g/cm}^3$  as reported by Fischer et al. (71). Hence, this parameter is not a factor in the scaling of the diffusion coefficients of proteins. We hypothesize that the cell cytoplasm is a dilatant, non-Newtonian fluid, in which the viscosity increases as a function of the stress applied to the environment. Bigger particles diffusing in the solution will impose a higher stress compared to the smaller particles, which in turn will make the environment more viscous. By rearranging the Einstein-Stokes equation, we compare the perceived viscosity with the macromolecular size of the particles as a function of the observed diffusion coefficients:

$$\eta \sim \frac{k_B T}{6\pi D_{observed} \sqrt[3]{\frac{3}{4\pi} \frac{M_{complex}}{\rho N_A}}} \quad (9)$$

Hence, the perceived viscosity in the cytoplasm of *E. coli* can be written as a function of the mass of the macromolecules:

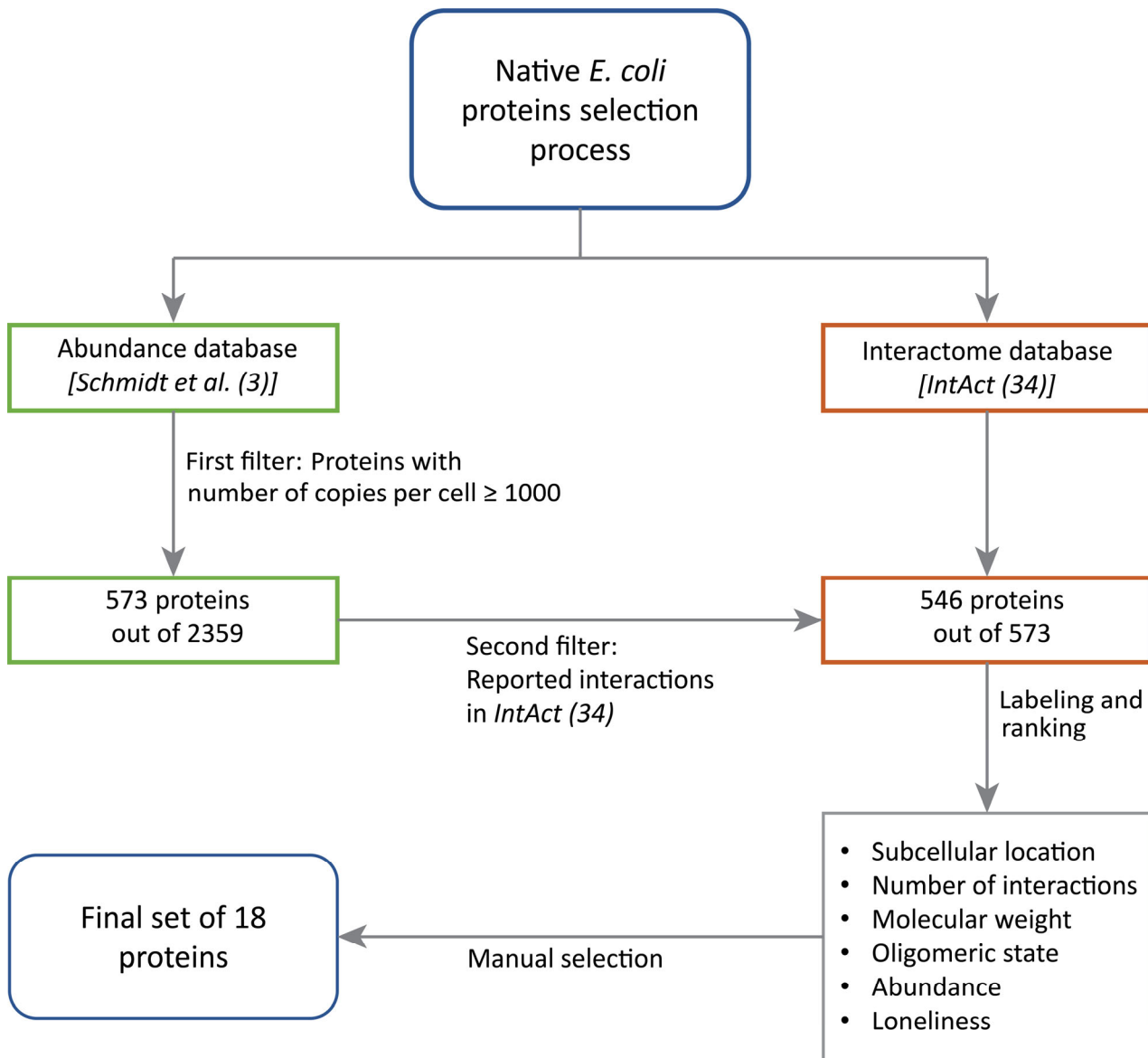
$$\eta_{perceived} \sim \alpha M_{complex}^{\beta} \quad (10)$$

If we want to obtain the relation of Equation 8, given the formula reported in equation 7, we will have that

$$\beta = -0.333 - (-0.535) = 0.202 \quad (11)$$

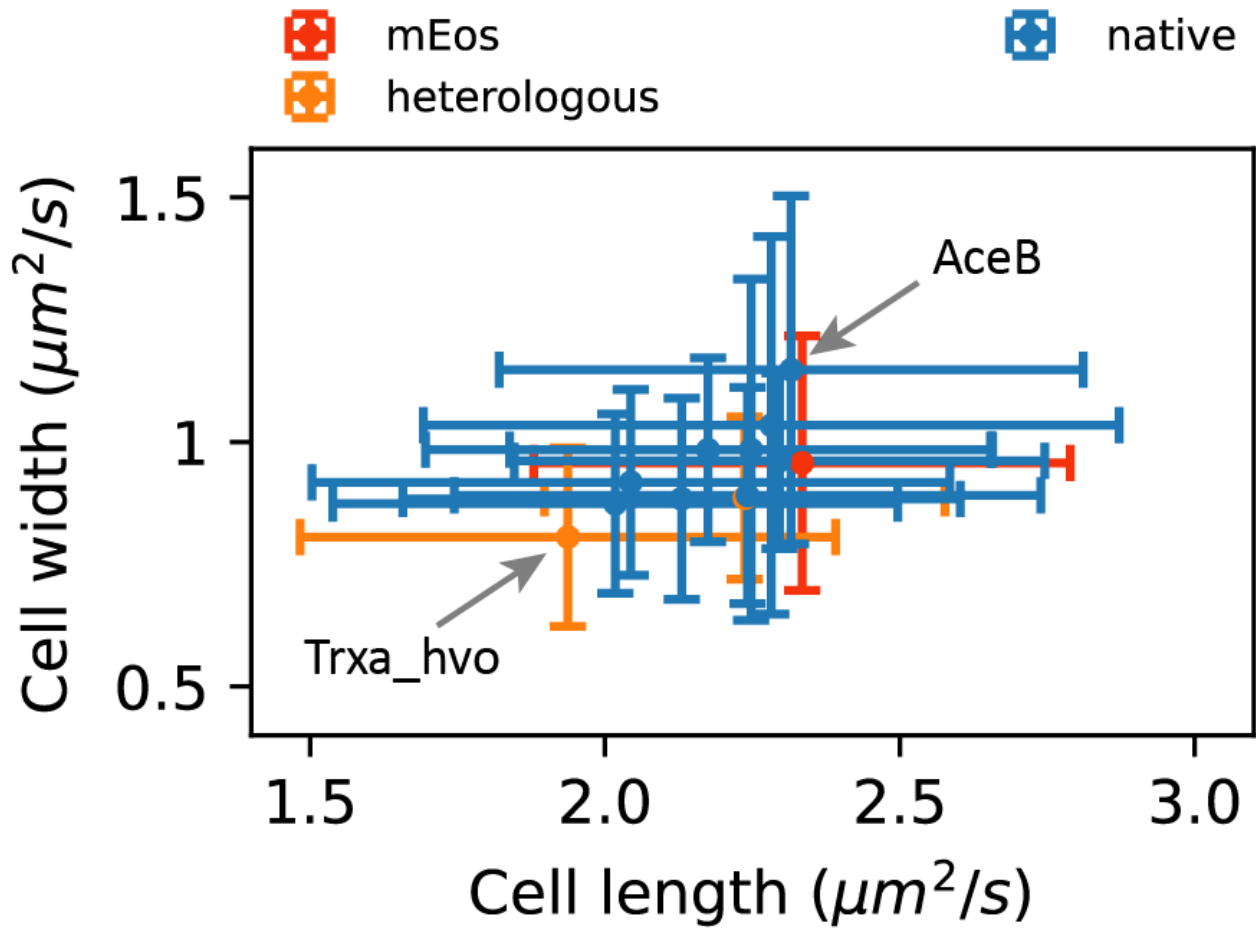
Hence:

$$\eta_{perceived} \sim \alpha M_{complex}^{0.20} \quad (12)$$



**Fig. S1.**

Schematic of the target selection process. The native *E. coli* proteins selected for SMdM analysis are specified in Supplementary Table S1.



**Fig. S2.**

Comparison of cell width and cell length for each expression construct. The mean values are represented by dots; the error bars represent the standard deviation.

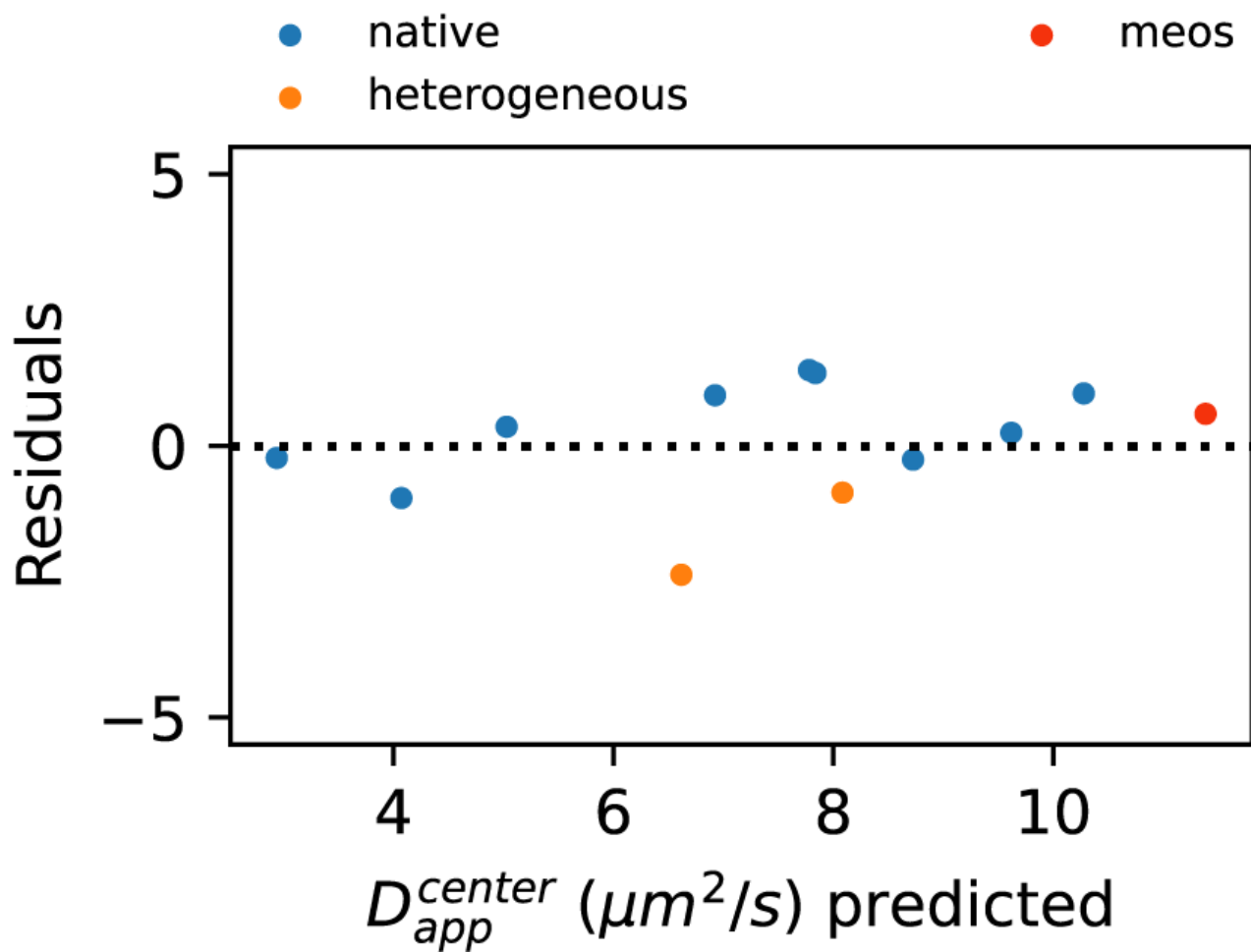
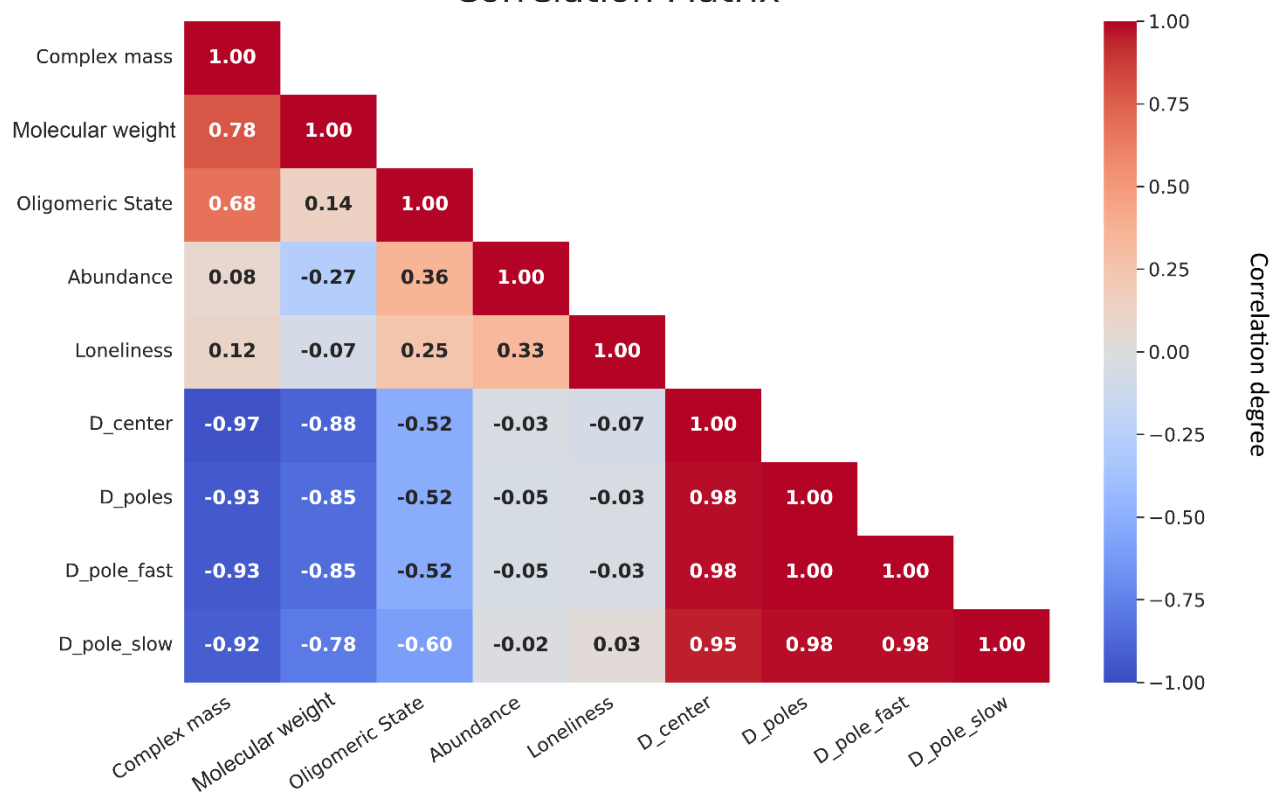


Fig. S3.

Analysis of the residuals from the plots in Figure 6D. The analysis shows no signs of correlation for the residuals. The diffusion coefficients of the heterologous proteins appear to be outliers when compared to the dataset obtained from only native proteins.

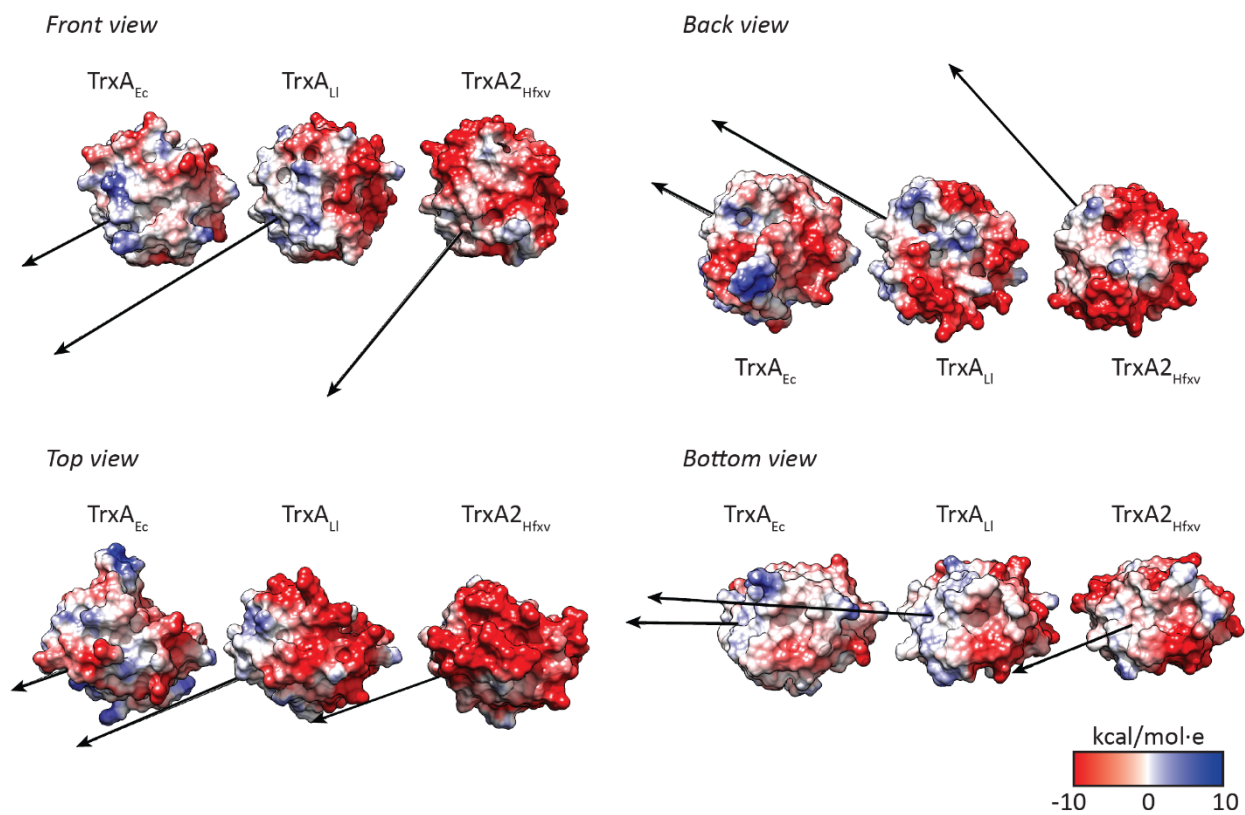
## Correlation Matrix



**Fig. S4.**

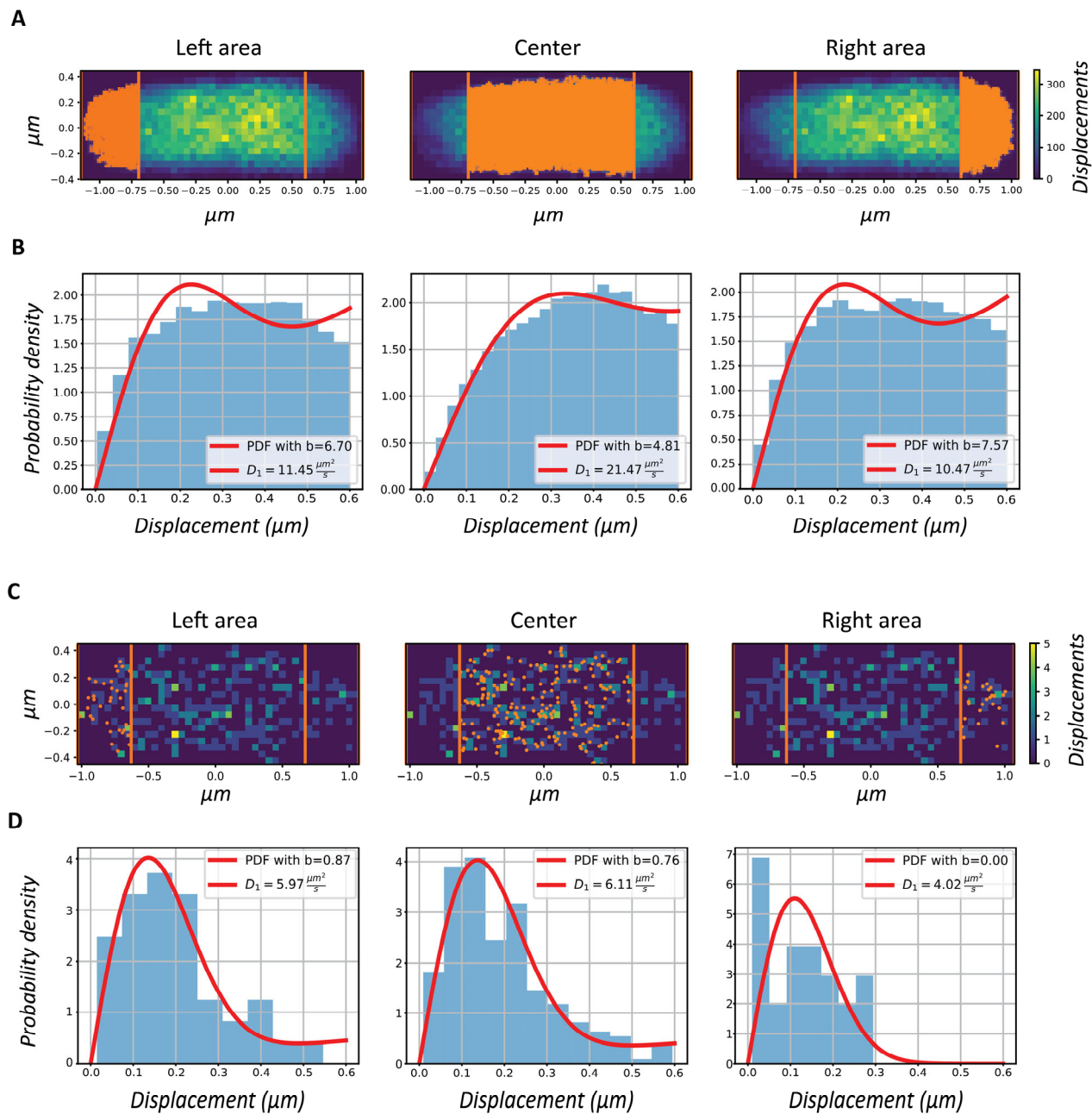
Multi-parameter analysis. Each variable has been tested for correlation with every other variable using the Spearman's rank correlation test. No correlation was found between loneliness and molecular weight, loneliness and abundance, and abundance and molecular weight. A moderate correlation between molecular weight and complex mass and between oligomeric and complex mass is observed, which is expected as the complex mass is calculated as the sum of the molecular weight of the monomeric protein plus fluorescence reporter and multiplied by the oligomeric state number. No correlation is observed between molecular weight and oligomeric state.





**Fig. S5.**

Different views of the surface charge distribution of the three homologous TrxA proteins. Top view corresponds to Fig. 5A.



**Fig. S6.**

Examples of cells discarded from the analysis. A) Cell having too many displacements for being analyzed. B) Fitting of the cell in panel B. Too many displacements result in a poor fitting due to the high amount of background fluorescence. C) Cell not having enough displacements for being analyzed. D) Fitting of the cell in panel D. Too little displacements result in a poor fitting, which is especially evident for the fit of the right area.

| Construct ID | UNIPROT ID | Protein name | MW (kDa) | Oligomeric state | Abundance (copies/cell) | Loneliness | comment             |
|--------------|------------|--------------|----------|------------------|-------------------------|------------|---------------------|
| 2            | P0A9G6     | AceA*        | 47.5     | 4                | 74908                   | 47.2       | aggregation         |
| 3            | P00934     | ThrC         | 47.1     | 1                | 11109                   | 0.35       | --                  |
| 4            | P18843     | NadE*        | 30.6     | 2                | 3084                    | 0.0037     | aggregation         |
| 5            | P0A836     | SucC*        | 41.3     | 2/4              | 11673                   | 0.037      | heterotetramer      |
| 6            | P0A9K9     | SlyD*        | 20.8     | 1                | 15259                   | 0.032      | partial aggregation |
| 7            | P0C0L2     | OsmC*        | 15.1     | 2                | 8157                    | 0.78       | aggregation         |
| 8            | P0AC62     | GrxC         | 9.1      | 1                | 6170                    | 89.4       | --                  |
| 9            | P05793     | IlvC         | 54.0     | 4                | 29065                   | 36.2       | --                  |
| 10           | P00864     | Ppc*         | 99.0     | 4                | 2185                    | 10.02      | failed to clone     |
| 11           | P08997     | AceB         | 60.2     | 1                | 8308                    | 10.4       | --                  |
| 12           | P0A6A8     | AcpP         | 8.6      | 1                | 28863                   | 0.12       | --                  |
| 13           | P0ACC3     | ErpA         | 12.1     | 2                | 3460                    | 0.1        | --                  |
| 14           | P0A763     | Ndk*         | 15.4     | 4                | 17326                   | 0.42       | aggregation         |
| 15           | P0AA25     | TrxA         | 11.8     | 1                | 18242                   | 0.025      | --                  |
| 16           | P07813     | LeuS         | 97.2     | 1                | 1505                    | 0.005      | --                  |
| 17           | P30125     | LeuB*        | 39.5     | 2                | 5032                    | 9.5        | partial aggregation |
| 18           | P0A817     | MetK*        | 41.9     | 4                | 6822                    | 0.022      | aggregation         |
| 19           | P08200     | Icd          | 45.7     | 2                | 24591                   | 1.02       | --                  |

**Table S1.**

Final set of proteins chosen for SMdM analysis. Most of the proteins were successfully expressed as C-terminal fusions with mEos3.2. We noted the following exceptions: SlyD and LeuB expression yielded a mix of aggregating and non-aggregating cells; OsmC, Ndk, NadE, AceA, MetK displayed polar aggregation after overexpression in the majority of their cells; SucC forms an obligatory heterotetrameric complex with SucD; and Ppc failed to produce an expressing clone. Proteins marked with an asterisk were excluded from diffusion mapping. MW is the molecular weight ( $M_w$ ) of a single chain; oligomeric state is according to the UNIPROT entry; abundance in copies per cell was taken from Schmidt et al. (3) for cells grown in M9-glycerol.

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