Supplementary Information

2 A Ziegler-type Spherical Cap Model Reveals

3 Early Stage Ethylene Polymerization Growth

4 Versus Catalyst Fragmentation Relationships

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1. X-ray Photo-electron Spectroscopy

30 The La 3d_{5/2}, La 4p and Cl 2p X-ray photo-electron spectroscopy (XPS) data of the three reference 31 materials, namely La₂O₃, LaOCI and LaCI₃, are given in Figure S1. Li et al., have shown in an in-situ 32 study on the energy calibration of Lanthanum compounds with XPS that the component splitting (ΔE) 33 of the La $3d_{5/2}$ signal, which in principle can be used for chemical diagnostics, is highly prone to the 34 measurement conditions and surface chemistry [1]. They found, for instance, that the ΔE value of an 35 as-prepared La₂O₃ material changed from 3.6 eV to 4.3 eV after vacuum treatment at 800 °C, which 36 basically removes carbon and oxygen adsorbates. Furthermore, they provide a literature summary of 37 reported ΔE values for La₂O₃, La(OH)₃ and La₂O₂(CO)₃ where differences up to 0.7 eV are reported 38 within the same materials. Therefore, although the ΔE values of the three reference materials are 39 provided in Figure S1 and a trend is observed showing a decrease in the splitting value with increasing 40 degree of surface chlorination from 4.05 eV for La₂O₃ to 3.99 eV for LaOCI and finally 3.72 eV for 41 LaCl₃ the absolute values should be taken with caution. Additionally, the use of the La 4p and Cl 2p 42 XPS signals to follow the surface chemistry of the LaOCI spherical caps before and after reaction with 43 TiCl₄ is highly challenging due to massive signal interference (strong overlap) of the La 4p and the Cl 44 2p XP signals. This prevents the determination of an accurate fitting model for the LaOCI spherical cap 45 samples, since the individual signal features of the La 4p signal (e.g., the position of the high binding 46 energy shoulder), which depend on the exact chemical environment (e.g., the degree of surface 47 chlorination), cannot be properly determined. However, to provide rough trends on the degree of 48 surface chlorination, Table S1 summarizes the results of a simplified fitting approach, neglecting the 49 La 4p signal shoulder at high binding energies. Assuming that this leads to a systematic error (a 50 systematic underestimation of the La 4p signal contribution), it should still be possible to derive trends 51 related to the CI fraction. Again, it should be noted here that the absolute values should be considered 52 with caution due to the aforementioned fitting issues.

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Figure S1. X-ray photo-electron spectroscopy (XPS) results of three Lanthanum reference materials. (a) The multiplet split of the La $3d_{5/2}$ signals are shown for the anhydrous reference materials (La₂O₃, LaOCI and LaCl₃) together with the split energy, ΔE , in electron volts. (b) The La 4p and Cl 2p signals of the three reference materials. The blue arrow indicates the La 4p signal shoulder at high binding energies for La₂O₃ that overlaps with the Cl 2psignals for the chlorinated samples.

71 The La 3d_{5/2}, La 4p and Cl 2p XPS results on the LaOCI spherical caps before (SC-P) and after (SC-72 Ti) treatment with TiCl₄ at 95 °C are given in Figure S2. As discussed earlier, the ΔE splitting value is 73 highly sensitive to the local chemical environment and the sample preparation steps. Since ΔE is 74 approximately the same before and after the reaction of the LaOCI spherical cap with TiCl₄ (4.32 eV 75 vs. 4.30 eV respectively) and significantly lower than the multiplet split difference between the LaOCI 76 and the LaCl₃ reference powders ($\Delta(\Delta E) = 0.27 \text{ eV}$) and therefore the LaOCl surface of the spherical 77 cap doesn't seem to be chlorinated further towards LaCl₃ upon treatment with TiCl₄ at 95 °C. 78 The areas of the XPS signal contributions assigned to CI, La and Ti of the spherical cap samples are

summarized in Table S1. As expected, the Ti 2p XP signal is only observed after the reaction of the LaOCI spherical caps with TiCl₄. The broadening of the Ti $2p_{3/2}$ signal towards lower binding energies (~456-457 eV) hints clearly towards the presence of reduced Ti³⁺ species [2]. This could be due to a similar mechanism reported for the dissociative chemisorption of CCl₄ on the LaOCI surface, which 83 gives rise to a CCI⁵⁺-CI⁵⁻ pair coordinated to respectively the Lewis acid La³⁺ and Lewis basic O²⁻ 84 surface groups [3,4]. However, it should be mentioned here that the majority of the Ti species remains 85 in the +4 oxidation state in the absence of the co-catalyst, triethylaluminium. To exclude a dominating 86 detrimental influence by the uncovered silicon areas on the LaOCI spherical cap sample in this 87 context, a Si(100) substrate reference was treated with both TiCl4 and the reducing triethylaluminium 88 co-catalyst and subsequently analyzed with XPS. The corresponding Ti 2p signal is shown in blue in 89 Figure S2c (denoted as Si-Ti/Al). For the Si-Ti/Al reference, the presence of reduced Ti species can 90 also be observed, which can be attributed to the interaction with the reducing co-catalyst. However, 91 the fraction of the reduced signal contributions is 3.4 times for the LaOCI SC-Ti sample than for the Si-92 Ti/AI reference. Therefore, the reduced Ti species can be mainly attributed to interactions with the 93 LaOCI spherical caps.



Figure S2. X-ray photo-electron spectroscopy (XPS) results of the LaOCI spherical cap model system before and after reaction with TiCl₄. (a) The multiplet split of the La *3d*_{5/2} spectrum is given for the LaOCI spherical cap model system before (SC-P, red) and after (SC-Ti, green) reaction with TiCl₄. (b) The La 4*p* and Cl 2*p* spectra of SC-P and SC-Ti. (c) The Ti 2*p* spectrum of SC-P, SC-Ti and Si-Ti/AI (blue). The blue arrows show the presence of reduced Ti^{x+} species.

107 The ratios of CI:La-related signals (CI 2*p*:La 3*d*_{5/2} and CI 2*p*:La 4*p*) of the pristine SC-P sample are

108 slightly higher than those of the LaOCI reference, but considerably lower than those of the pure LaCI₃

109 reference. The slight deviation from the LaOCI reference might be caused by topography-related

- 110 effects and the different sample geometry (spherical caps versus powder references). However, after
- 111 reaction with TiCl₄ the Cl:La ratios increase significantly. Here, due to massive signal interference, it is
- 112 not entirely clear, whether this is due to a further chlorination of LaOCI towards LaCl₃ with TiCl₄ acting
- 113 as the chlorination reagent or simply due to the chemisorption of $TiCl_x$ species on the external surface
- 114 of LaOCI. Since the La $3d_{5/2}$ splitting value is not affected by the reaction with TiCl₄ as mentioned
- 115 earlier, it seems more likely that the increased ratio of the CI:La peaks is due to the chemisorption of
- 116 TiCl_x species.

117 Table S1. The area under the selected La, CI and Ti XP signals and the respective signal ratios. Values are

- 118 given for the three reference materials La₂O₃, LaOCI and LaCl₃ as well as the pristine and TiCl₄ treated LaOCI
- 119 spherical cap systems called SC-P and SC-Ti, respectively.

Sample	Area La 3 <i>d</i> 5/2	Area La 4 <i>p</i> *	Area Cl 2 <i>p</i>	Area Ti 2 <i>p</i>	Ratio Cl 2p : La 3d _{5/2}	Ratio Cl 2 <i>p</i> : La 4 <i>p</i>	Ratio Cl 2p : Ti 2p
La ₂ O ₃	232.3	364.2	-	-	-	-	-
LaOCI	269.2	406.1	337.5	-	1.3	0.8	-
LaCl₃	168.3	185.0	525.1	-	3.1	2.8	-
SC-P	65.7	103.6	104.4	0.0	1.6	1.0	-
SC-Ti	38.2	61.2	79.9	81.8	2.1	1.3	1.0

The area under the La 4p is obtained using a single signal (GL(30) line shape) and doesn't take the
 high binding energy shoulder observed around 200 eV into account.

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2. Raman Micro-Spectroscopy

126 In Figure S3, the Raman spectra are given for the pristine LaOCI spherical cap, the Si (100) wafer

- 127 background and the LaOCI powder reference material also used as the XPS reference. For the
- 128 spherical cap model system, only the LaOCI chemical phase is detected. Conventional Raman micro-
- 129 spectroscopy (e.g., in the absence of surface-enhancement techniques) is a bulk-probing technique
- 130 that nicely complements the surface-sensitivity of XPS analysis in this scenario to study the spherical
- 131 cap model system.
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Figure S3. Raman micro-spectroscopy to determine the bulk chemical phase of the LaOCI spherical cap model system. In blue and black, the Raman spectra are given for respectively the LaOCI powder reference that was also used for XPS studies and a clean Si(100) wafer substrate. In red, the Raman spectrum is given for the LaOCI spherical cap model system, where the stars denote peaks belonging to the LaOCI chemical phase based on the blue spectrum and the octothorp denotes peaks belonging to the Si(100) wafer substrate.

155 In Figure S4, the Raman spectra are given for the LaOCI spherical caps after specified (0,1,2,5,10,20 156 and 60) min of ethylene polymerization, as well as the Si (100) wafer background on the 20 min 157 ethylene polymerized sample, a pristine LaOCI spherical cap (without TiCl₄) but with TEAL after 60 158 min of ethylene polymerization and a HDPE reference film. All Raman spectra are normalized to the 159 521 cm⁻¹ peak of the Si (100) substrate, which can be regarded as an internal standard. For all 160 samples, the measured spot was optimized based on that part of the spherical cap that gave the most 161 intense polyethylene signal. For all LaOCI/TiCl4/TEAL ethylene polymerized samples, Raman micro-162 spectroscopy confirms that polyethylene is formed mainly on the LaOCI spherical caps, with no 163 observable amount detected on the background substrate and no polyethylene or other carbon 164 phases are found on the pristine sample (0 min PE). The LaOCI/TEAL sample without TiCl4 treatment 165 and after 60 min of ethylene polymerization showed no formation of polyethylene.



Figure S4. Raman spectra taken after different ethylene polymerization times on the LaOCI spherical caps as well as a HDPE reference film. Raman spectra are given from the pristine up to 60 min of ethylene polymerization on the LaOCI spherical cap model system (labelled as *x min PE*) as well as the Si (100) background of the 20 min ethylene polymerized sample (background 20 min PE), a pristine LaOCI spherical cap (without TiCl₄) but with TEAL after 60 min of ethylene polymerization and a HDPE reference film. In all cases, normalization was performed using the Si (100) background 521 cm⁻¹ peak as an internal standard.

186 The strength of Raman micro-spectroscopy is the ability to differentiate and map chemical phases 187 over the region of interest. In this case, it allows us to visualize the distribution of polyethylene on the 188 LaOCI spherical caps at different polymerization times. In Figure S5, the Raman micro-spectroscopy 189 maps of the 2700-3100 cm⁻¹ are given, which visualize the asymmetric and symmetric -CH₂- stretching 190 modes of polyethylene. Unlike the normalized spectra in Figure S4, using the Si(100) 512 cm⁻¹ 191 substrate peak, these maps aren't normalized since this internal standard vibration fell outside of the 192 imaged region. The inset in each Raman micro-spectroscopy map is the correlated optical microscopy 193 image that shows the contours of the LaOCI spherical caps imaged. As shown in Figure S5, the 194 pristine sample shows no detectable formation of polyethylene or other carbon phase with -CH₂-

195 groups that would fall in the same imaged region. Starting at the 1 min ethylene polymerized sample, 196 we mainly observe polyethylene fibres distributed on the centre of the spherical cap with a few 197 hotspots at the edge. The next samples, going from 2 min to 20 min ethylene polymerization, continue 198 the trend with the formation of a polyethylene fibre network in the centre of the spherical caps and the 199 formation of dense polyethylene regions around the edges. For both the 10 and 20 min ethylene 200 polymerization samples, dense regions also start to appear in the centre of the spherical caps. Finally, 201 the 60 min ethylene polymerization sample still shows some polyethylene fibres on top of the spherical 202 cap but the dense regions have grown significantly enough in size to almost fully cover the spherical 203 cap. For the 5, 20 and 60 min ethylene polymerized imaged spherical caps long polyethylene fibres 204 spanning over 10 microns in length can be observed to grow away from the spherical cap and lay on 205 the Si (100) substrate background.



Figure S5. Raman micro-spectroscopy maps of the 2700-3100 cm⁻¹ region on different ethylene polymerization times. The 2700-3100 cm⁻¹ region imaged for each ethylene polymerization time shows the distribution of the asymmetric and symmetric -CH₂- stretching modes of polyethylene on a LaOCI spherical cap. The inset images show the correlated optical microscopy overview of the pristine and ethylene polymerized LaOCI spherical caps. The scale bars depict the size in microns.

In Figure S6 the Raman spectra are given for the pristine and ethylene polymerized reference MgO/MgCl₂ caps. Starting with the 2 min ethylene polymerized sample, the polyethylene characteristic peaks, especially around 2700-2900 cm⁻¹ are clearly visible.



Figure S6. Raman spectra taken after different ethylene polymerization times on the reference MgO/MgCl₂ caps as well as a HDPE reference film. Raman spectra are given from the pristine up to 60 min of ethylene polymerization on the reference MgO/MgCl₂ cap samples (labelled as *MgO/MgCl₂ X min*) and a HDPE reference film. In all cases, normalization was performed using the Si (100) background 521 cm⁻¹ peak as an internal standard.

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In Figure S7 the Raman maps are given of the 2, 10 and 60 min ethylene polymerized reference MgO/MgCl₂ caps. The 2700-3100 cm⁻¹ region is portrayed that visualizes the asymmetric and symmetric -CH₂- stretching modes of polyethylene. Whereas only a weak signal for polyethylene is observed for the 2 min polymerized sample, which is in agreement with the spectrum given in Figure S6, strong signals are observed for both the 10 and 60 min polymerized samples. Furthermore, whereas for LaOCI spherical caps both small yet intense spheroidal regions are observed and a fibre-like weaker intensity region, for the MgO/MgCl₂ samples a more homogeneous polyethylene phase is observed of strong intensity.



Figure S7. Raman micro-spectroscopy maps of the 2700-3100 cm⁻¹ region on different ethylene polymerization times of the reference MgO/MgCl₂ caps. The 2700-3100 cm⁻¹ region imaged for each ethylene polymerization time shows the distribution of the asymmetric and symmetric -CH₂- stretching modes of polyethylene on a LaOCI spherical cap. The inset images show the correlated optical microscopy overview of the 2, 10 and 60 min ethylene polymerized MgO/MgCl₂ caps. The scale bars depict the size in microns.

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3. Time-of-Flight Secondary Ion Mass Spectrometry

267 The mass spectra obtained from the imaged region are the convolution of the spherical caps and the 268 Si(100) substrate. Therefore, to study if the charged mass fragments (called secondary ions) 269 originating from the spherical caps, a region of interest (ROI) was drawn inside the analysis software 270 on top of the spherical caps. The resulting mass spectra of both this spherical cap ROI and the inverse 271 ROI that represents the Si(100) substrate, are given in Figure S8a as well as the insets that show the 272 drawn ROIs. Additionally, the first few sputter seconds were typically disregarded from the analysis, as 273 shown in Figure S8b, due to the presence of adsorbed carbon species from the air that are removed in 274 these first few sputter cycles. The cut-off was based on reaching a stable intensity profile for the m/z275 species.



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Figure S8. Time-of-Flight Secondary Ion Mass Spectrometry (ToF-SIMS) data and sputter profile explaining the chosen ROIs. (a) Mass spectra of the spherical cap model catalyst after 20 min polymerization time (inset map) recorded with ToF-SIMS. A ROI was picked selecting only the spherical caps, removing non-relevant mass fragments from the analysis. The ROI (top spectrum, all unmarked area in the inset map) contains the majority of the catalyst (LaOCl₂- indicated) and PE (repeating unit) compared to the substrate (bottom spectrum). (b) To avoid the interference of surface adsorbed species from the analysis, a z-ROI was chosen after the initial exponential increase/decrease of the organic fragments passed.

284 A selection of mass fragments is shown in Figure S9. Based on the ion generated SE images, the 285 polyethylene phase can be clearly distinguished from the LaOCI spherical caps. It should be 286 mentioned here that the ion counts for the LaOCI⁻ fragment is typically orders of magnitude higher than 287 for polyethylene fragments such as C₉H₁₃. This may be related to charging effects and the low 288 ionisation probability of polyolefins, making them particularly challenging to be measured with ToF-289 SIMS. Additionally, the sample geometry (spherical caps with rough surfaces after polymerization 290 instead of planar systems) could also cause adverse effects here. The C₉H₁₃ mass fragment was 291 chosen here to represent the polyethylene phase as based on the work by Kern et al. [5]. This 292 polyethylene mass fragment is also found for the pristine sample, but with considerably lower ion 293 counts or intensity and is thus more likely to be from adventitious carbon due to air exposure of the 294 samples. Nevertheless, as is mostly visible for the 2 and 10 min maps, the C₉H₁₃ mass charge 295 fragment shows strong correlation with the polyethylene phase visible in the SE images.

296	The integrated intensity for this fragment, found in the different mass spectra, is plotted in Figure S10.
297	As the polymerization time increases, more of this fragment is found (note that all measurement points
298	have the same sputter time) until after 10 min a saturation effect starts to appear. This is in line with
299	the AFM analysis performed in Figures S11-13, where the polyethylene volume on the external
300	surface of the LaOCI spherical caps was estimated for different ethylene polymerization times and
301	showed a saturation of the estimated polyethylene volume at intermediate polymerization times. This
302	could be explained by a mass transfer limitation effect occurring at such intermediate polymerization
303	times, where the fragmentation rate is not sufficiently high yet to facilitate high enough diffusion of
304	ethylene monomers to the active sites within the spherical cap composite phase and hence a decline
305	in the polymerization rate is observed.
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Figure S9. Time-of-flight secondary ion mass spectrometry (ToF-SIMS) secondary electron (SE) images, complemented by a selection of mass fragments, for different times of ethylene polymerization. The LaOCIfragment is chosen to represent the polymerization catalyst, while the C_9H_{13} - fragment is representing the polyethylene. The Si⁻ fragment is shown to highlight the substrate on which the spherical caps were synthesized, and emphasizes that the LaOCI is only present in the patterned area as intended during the synthesis.



Figure S10. Integrated area of the C_9H_{13} mass fragment. Representing polyethylene, the integrated area of the C₉H₁₃ mass fragment (m/z = 121 u), also shown in the mass images in Figure S9, is shown after increasing times of ethylene polymerization. Whereas first a linear increase is found, the integrated intensity starts to flatten out after roughly 20 min of ethylene polymerization. This indicates that the surface coverage of each island increases until a nearly full surface coverage is obtained.

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4. Scanning Probe Microscopy

364 Atomic Force Microscopy (AFM) was used to investigate the topological and morphological evolution 365 of the LaOCI spherical caps as a function of ethylene polymerization time. Figure S11 shows the 366 topological images of 6 LaOCI spherical caps per ethylene polymerization time. The height contrast is 367 set to be identical for the 0 to 20 min of polymerization time at a 0-1µm range. However, the ethylene 368 polymerized LaOCI spherical caps of the 60 min sample were considerably thicker on average and 369 therefore required a different height contrast as shown ranging from 0-4 µm. Purely based on the 370 topological information provided by AFM it becomes clear that these LaOCI spherical caps become 371 covered with polyethylene fibers of varying lengths already at ethylene polymerization times as early 372 as 1 min. With an increase of polymerization times, thicker blobs of polyethylene start to appear (dark 373 purple in color). It should be noted here that due to the different height scale bar in the 60 min sample, 374 large features may appear to have a lighter (green-blue) color, which would have appeared dark 375 purple with the height contrast used for the 0-20 min samples.

376 However, using purely the height of the polymer features itself isn't accurate enough to describe the 377 polymer yield per polymerization time, as the patterns can vary in shape (diameter or height) even 378 within the same wafer substrate. Instead, our approach to attempt to track the polymerization yield as 379 a function of time is shown in Figure S12. The individual micrographs were first flattened on the 380 background (substrate) and then x and y cross-sectional profiles were taken from the background 381 through the center of the spherical caps. From the resulting line profiles, the height (h) and cap base 382 radius (a) were measured by fitting the visible parts of uncovered catalyst with a power function. From 383 these values the catalyst caps volumes were approximated with the following equation 3:

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$$V = \pi . h \left(a^{\frac{1}{4}} + h^{\frac{1}{3}} \right)$$
(3)

385 where V is the cap volume in μm^3 , h is the height of the cap in μm and a is the cap base radius, or 386 chord length, in µm [6]. It should be said here that this approach does not allow us the quantify the 387 amount of polyethylene present within the spherical cap. For such an approach, X-ray 388 nanotomography techniques, such as ptychography X-ray computed tomography as done in our 389 previous works could offer a solution [7,8]. 390



391 392 393 Figure S11. Atomic Force Microscopy (AFM) on individual catalyst caps after different ethylene 394 polymerization times. Six LaOCI spherical caps were scanned per ethylene polymerization time, all shown using 395 a z contrast of 1 µm, with the exception of 60 min, where only 3 viable micrographs could be obtained shown with 396 a z contrast of 4 µm due to the excessive thickness of the polymer features which were too challenging for our 397 scanning probe microscopy system. A general trend shows that the coverage and thickness of the formed polymer 398 increase with increasing ethylene polymerization time. Furthermore, with the exception of 60 min, the edges of the 399 patterned catalyst caps remain fairly visible whereas the centre part of the cap gets covered by PE strings and 400 larger features. Notes: i) At 2 min, top-right; the catalyst consisted of a non-spherical shape. ii) 5 min, bottom-left; 401 the catalyst was measured before by SEM analysis (explaining the grid-like background) iii) 10 min, top-left and 402 bottom-right; some noise was found only on the background, not on the formed PE. White scale bars are 5 µm.





405 Figure S12. Estimation of the LaOCI spherical cap volume after ethylene polymerization and for the pristine 406 hemispherical caps. A) The individual micrographs shown in Figure S11 were each flattened on their background 407 (substrate) around the LaOCI spherical cap and polyethylene, shown here as example after 10 min polymerization 408 (Figure S11, 10 min, center-top spot). B) Then, a x and y cross-section was taken and the resulting height profiles 409 were fitted with a power function over the exposed polymer-free catalyst surface. Using the software measurement 410 tools, the cap base radius or chord length and catalyst height were measured. These were then used to estimate 411 the volume of the catalyst, which could subsequently be subtracted from the total volume obtained in the micrograph 412 (above the background height) to result in a net volume of polyethylene. C) To show that the patterned catalyst 413 indeed consist of hemispherical caps, not i.e. pancake- or disc shapes, and thus can be fitted with a power function, 414 the cross section of all the measured pristine caps (for both Figure S11 and S13) are shown together with a box 415 chart showing their maximum height.

The total volume of all features measured, which represents the LaOCI spherical cap and polyethylene phases, minus the estimated volume of the sole LaOCI spherical cap as described above, results in the estimated volume of polyethylene (per micrograph). This volume was plotted in Figure S13 for all micrographs recorded as shown in Figure S11, and for all full micrographs recorded with PiFM as shown in Figure S15 (*vide infra*), to visualize the increase of polyethylene over time ignoring the initial pore volume of the catalyst which might be filled up at the early stages.



Figure S13. Mean volume of the polyethylene phase (PE) measured on the external LaOCI spherical caps as a function of ethylene polymerization time. The mean volume of the polyethylene phase growing on the external LaOCI spherical cap surface was calculated using the micrographs of Figure S11 and correction for the estimated volume of the LaOCI catalyst framework as discussed in Figure S12.

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438 In Figure S14 the extreme sensitivity of the MgO/MgCl₂ caps to moisture is visualized with a time-laps 439 series of AFM measurements. It is due to the typically rough shapes observed for these MgO/MgCl₂ 440 samples that we have decided to refer to them simply as caps as they don't resemble spherical caps as 441 is the case for LaOCI. This seems to be caused by both the transformation step of $Mg(NO_3)_2 \times H_2O$ to 442 MgO and the subsequent partial chlorination with TiCl₄ to MgO/MgCl₂. The first AFM measurement on 443 the left was obtained with the use of an AFM operating inside a glovebox at <1 ppm O_2 and H_2O values 444 whereas the subsequent two measurements were obtained with an AFM operating under ambient 445 conditions after exposure times of respectively 15 and 35 min to moisture. All images were collected

446 with the same type of AFM apparatus and cantilevers as described in the methodology section. The line 447 profile of each image obtained at the same X,Y positions shows a dramatic change in the morphology 448 of the cap over time. Not only does the overall height of the cap collapse from almost 1.2 microns at the 449 peak towards 0.8 microns, the minimum observed at a line profile position of 0 µm (X-axis of the plot) 450 also changes. Interestingly, this value changes from almost 0 µm in height under controlled atmosphere 451 to 0.4 µm in height after 15 min exposure and back to 0.2 µm in height after 35 min. This shows that the 452 hydration and subsequent morphological changes induced on the MgO/MgCl₂ framework can be a 453 rather slow process. Additionally, due to the severe morphological changes, care has to be taken 454 especially when analyzing the pristine MgO/MgCl₂ caps or at low polymerization times when there is still 455 a large exposed surface of MgO/MgCl₂.



Figure S14. Time-laps AFM results on a single pristine MgO/MgCl₂ cap before (AFM positioned inside a glovebox operating at <1 ppm O₂ and H₂O) and after (AFM operating under ambient conditions) exposure to moisture. Additionally, on the bottom row the line profiles are provided going on the same position of each cap as shown via the dashed white line.

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Going from 0-20 min ethylene polymerization a saturation effect of the polyethylene volume growing on the external surface of the LaOCI spherical cap is observed. This could be explained by first the formation of many extruded polyethylene fibres at early polymerization times as well as the filling of the internal pore network of the LaOCI spherical cap. As the internal pore network becomes filled with 473 a polyethylene phase that can't be assessed with this approach (since AFM only measured topological 474 information and not internal), these extruded polyethylene fibres will show a non-linear decaying 475 growth rate due to mass transfer limitations. This is because new ethylene monomers will now have to 476 diffuse through a dense polyethylene phase within the internal pore network to reach the active sites. 477 However, at 60 min of ethylene polymerization a drastic change is observed with a considerably higher 478 average external polyethylene volume when compared to the 5-20 min samples. This sudden large 479 increase of the 60 min sample corresponds well to the FIB-SEM observations that the internal LaOCI 480 spherical cap has been completely disintegrated into small fragments dispersed well within the 481 polyethylene phase, whereas for the 5-20 min samples most of the internal LaOCI framework was still 482 intact, albeit with many crack lines and increasing amount of fragments observed. Therefore, the 60 483 min sample is expected to experience less mass transfer limitations due to the fragmentation of the 484 framework, which is a necessary phenomenon to ensure polymerization activity [9,10].

485 In Figure S15 the micrographs recorded with PiFM are shown per PE time; 0 min shows a full 486 spherical cap and the corresponding 1600 cm⁻¹ signal, which most likely belongs to the C=O stretching 487 vibration of surface absorbed carbonate species [11,12]. Interestingly, the 1600 cm⁻¹ signal is 488 enhanced at the surface cracks, most likely due to the presence of exposed unsaturated lattices or 489 lattice defects that can chemisorb CO₂ and therefore also TiCl₄. It should be emphasized here that 490 exposure to CO₂ only happens for the LaOCI spherical caps after either ethylene polymerization or in 491 the case of this pristine sample when performing ex-situ surface analysis. Therefore, the presence of 492 these carbonate absorbed species isn't expected to be present during the grafting of TiCl₄ in an inert 493 atmosphere. The subsequent times show a full spherical cap (top left), zoom-in micrograph (top right) 494 and the corresponding intensity maps for the 1461 + 1471 cm⁻¹ vibration (magenta) and the 1600 cm⁻¹ 495 vibration (cyan), respectively.



Figure S15. Individual Photo-induced Force micrographs of a full spherical cap, a zoom-in and the corresponding intensity maps for the 1461 + 1471 cm⁻¹ and 1600 cm⁻¹ vibrations on different ethylene polymerization times. Per polymerization time, the height micrographs are shown for a full spherical cap (top left) and a zoom-in (top right). The corresponding PiFM intensity maps are shown for the 1461 + 1471 cm⁻¹ vibrations (magenta), and the 1600 cm⁻¹ vibration (cyan) representing the PE and catalyst support, respectively. Note that the z-scale for all height micrographs is 1 μ m, except for 60 min polymerization time, which has a z-scale of 5 μ m. The pink inset scale bars represent 5 μ m while the white scale bars represent 1 μ m.

505 The extracted point spectra from the three markers, shown in the 1461+1471 cm⁻¹ PiFM map in Figure 506 S15 for the 5 min ethylene polymerized sample, are given in Figure S16. The markers show that on 507 top of a polyethylene fibre that only the doublet peaks of the 1461+1471 cm⁻¹ are present, which 508 belong to a crystalline polyethylene phase. The other two markers on low intensity regions (of the 509 1461+1471 cm⁻¹ signal) that are closer to respectively the centre and edge of the spherical cap show a 510 broad band around 1600 cm⁻¹, which is attributed to adsorbed CO₂ surface species on the LaOCI 511 framework after exposure of the sample to air and therefore allows us to also localize LaOCI with 512 PiFM. On these positions, especially for the green marker one can still distinguish the doublet peak of 513 polyethylene from the background, albeit with a poor signal to noise ratio.





516 **Figure S16.** Point spectra recorded using Photo-induced Force Microscopy (PiFM) on the markers indicated 517 in Figure S15 for the 5 min sample. Especially for the green and blue point spectra, a significant interference of 518 water vapour can be observed for the LaOCI catalyst framework. The yellow spectrum is recorded on a polyethylene 519 fibre and shows the characteristic polyethylene -CH₂- bending vibrations at 1461 and 1471 cm⁻¹.

521 The spectra shown in Figure 3c were obtained after averaging all spectra obtained on 9 different 522 patterns per polymerization time. The spectra were pre-processed by applying a Whittaker baseline 523 correction and normalization using the PLS Toolbox of Eigenvector. All individual spectra were then 524 subjected to a multivariate curve resolution (MCR) analysis with non-negativity constraints, in which 4 525 spectral components were generated, as shown in Figure S17.



Figure S17. Point spectra recorded on 9 different LaOCI spherical caps after 1 min ethylene polymerization and the 4 different spectral components used in a multivariate curve resolution (MCR) analysis. The different spectral components represent the crystalline polyethylene phases (spectral components 1 and 4) as they consist purely of the -CH₂- bending vibrations of crystalline polyethylene in the orthorhombic phase, whereas spectral component 3 consists of a broad amorphous polyethylene -CH₂- bending vibration. Spectral component 2 represents interference caused by moisture present in the system and hence on the LaOCI surface and the PiFM scanning tip.

535 The recorded spectra were then fitted by summing the components multiplied by a certain score. 536 Hence, this score represents the contribution of a certain component to this spectrum. Spectral 537 components 1 and 4 represent the crystalline polyethylene -CH₂- bending vibrations, B_{1u} and B_{2u} , at 538 respectively 1461 and 1471 cm⁻¹, whereas component 3 is comprised of a broad band centred around 539 1464 cm⁻¹ and is attributed to an amorphous polyethylene phase [13]. It should be noted here that a 540 100% crystalline polyethylene phase isn't feasible as the degree of crystalline is limited by the high 541 viscosity of the polyethylene chains and thus this amorphous polyethylene contribution should always 542 be present [14]. Spectral component 2 represents the water vapour interference, and hence we can 543 compare the crystallinity within our own dataset by taking the percentage of the crystalline 544 components (1 + 4) over all PE components (1 + 3 + 4), plotted in the main manuscript Figure 3c. 545 Note that these percentages are an outcome of our MCR scores and hence don't represent the mass 546 or molar percentage of crystalline PE, but still can be used to study the evolution of crystallinity over 547 time within this dataset.

Figure S18 shows the average PiF spectra recorded on multiple MgO/MgCl₂ caps after increasing polymerization times (topology micrographs of representative patterns are shown at the bottom). An identical MCR analysis with the same components was performed as done on the LaOCl system, and the resulting percentage of crystalline components over polymerization time is shown in Table S2 for both the MgO/MgCl₂ and LaOCl system (also shown in the main manuscript Figure 3c).

553 Noteworthy, we see a similar saturation of the fraction of crystalline components for both systems. 554 However, the saturation for the Mg system seems to happen at lower ratios. This might be related to the 555 difficulty experienced while measuring the MgO/MgCl₂ system: the caps were very irregular due to 556 hydration under ambient conditions leading to frequent presence of PiFM tip artefacts that can influence 557 the quality of the spectra obtained. This becomes clear in Table S2 with the larger error for the 558 MgO/MgCl₂ system, especially at earlier polymerization times where less polyethylene is formed and 559 more MgO/MgCl₂ is exposed. It should be noted that these percentages represent a ratio of MCR 560 components and not an absolute degree of polyethylene crystallinity. Nonetheless, we can conclude 561 that the saturation of the fraction of crystalline components takes place for both systems already after 562 roughly 10 minutes of ethylene polymerization under mild slurry-phase conditions.



MgO/MgCl₂ caps after a) 0, b) 2, c) 10 and d) 60 min polymerization time. Atomic force microscopy images recorded using PiFM of representative patterns are shown at the bottom. The red spectrum represents the average of all recorded spectra (grey) for that specific polymerization time as also performed in Figure S17 for the LaOCI spherical cap samples. The scale bars represent 2 µm.

Table S2. Overview of the fraction of crystalline components (1461 cm⁻¹ and 1471 cm⁻¹ bands) versus the

amorphous single amorphous component (broad band at 1463 cm⁻¹). The fractions were assessed with MCR

analysis on the PiF spectra (as explained in Figure S17) obtained at respectively, 2, 10 and 60 min of ethylene

polymerization on both MgO/MgCl₂ caps and LaOCI spherical caps after functionalization with TiCl₄.

Sample	Polymerization time (min)			
	2	10	60	
MgO/MgCl ₂	39,17 ± 10,4	64,4 ± 5,8	62,5 ± 6,0	
Mean of crystalline MCR components (%)				
LaOCI	$49,4 \pm 4,8$	88,6 ± 4,5	80,2 ± 4,4	
Mean of crystalline MCR components (%)				

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5. Scanning Electron Microscopy

587 In Figure S19, an overview is given of the SEM results of all ethylene polymerization times, starting at 588 the top with a pristine LaOCI spherical cap sample up to 60 min of ethylene polymerization at the 589 bottom. From left to right first, an overview of multiple LaOCI spherical caps at a specific ethylene 590 polymerization is provided, followed by a single spherical cap and finally a zoom-in on this spherical 591 cap. Starting at the 1 min ethylene polymerized sample, it becomes clear that the polyethylene fibres 592 that are extruded out of the spherical caps contain large amounts of small LaOCI fragments. The 593 extrusion of the polyolefin fibres has been reported for immobilized single-site catalysts in well-defined 594 microporous and mesoporous support matrixes for polyolefin catalysts, such as the silica-based MCM-595 41 and SBA-15 with pore diameters in the range of 2-25 nm [15-20]. The small LaOCI fragments must 596 have been peeled off the internal and possibly external surface of the catalyst. This indicates the 597 presence of the shrinking core or also called layer-by-layer fragmentation model, as illustrated in 598 Figure S21. After ten min of ethylene polymerization, the external surface of the centre of the spherical 599 caps are observed to be fully covered in a polyethylene fibre network. Additionally, starting at this 600 polymerization time, large LaOCI fragments are observed to lay intertwined with and on top of this 601 polyethylene fibre network. The zoom-in on the 10 min ethylene polymerized sample shows one such 602 large LaOCI fragment laying on top of the centre of the spherical cap and is actually observed to 603 already have been cleaved into several smaller fragments that are being pushed away from each 604 other by the growing polyethylene fibres. This internal cleavage shows the presence of the continuous 605 bisection fragmentation model, as illustrated in Figure S21, occurring even at the external surface of 606 the spherical cap.



Ethylene Polymerization Time

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Figure S19. Secondary Electron Microscopy (SEM) results on the LaOCI spherical caps after different ethylene polymerization times. From left to right first, an overview consisting of multiple LaOCI spherical caps at a certain polymerization time are given followed by a single spherical cap and finally a zoom-in on that specific spherical cap. From top to bottom, an increase of ethylene polymerization time is given, starting at a pristine nonpolymerized sample and going up to 60 min of ethylene polymerization. The yellow, orange and red scalebars represent a width of respectively 20, 5 and 2 microns. 614 In Figure S20 an overview is given of the SEM results on the reference MgO/MgCl₂ caps for a pristine, 615 2, 10 and 60 min ethylene polymerized samples. From left to right, full single caps are first shown in a 616 top-down fashion followed by a zoom-in and then repeated as cross-sectional images on the exact 617 same caps with again a full size image and a zoom-in. The pristine MgO/MgCl₂ caps, which have been 618 exposed to moisture due to the absence of a transfer chamber for the SEM, shows a rough appearing 619 surface with some large exposed cracks and seems to bleed onto the Si(100) substrate. This bleeding 620 effect could be due to the rapid vacuum treatment used to evacuate the SEM chamber upon sample 621 transfer of the hydrated MgCl₂ layer. This high moisture sensitivity of the MgO/MgCl₂ caps was also 622 observed earlier in supplementary information section 4 with AFM time-lapse measurements before 623 and after exposure of the MgO/MgCl₂ pristine caps to moisture. Upon 2 min of ethylene polymerization 624 the first polyethylene fibers and globules can be observed on the caps, albeit that the weak Z-contrast 625 between MgO/MgCl₂ and polyethylene as compared to LaOCI make it more difficult to observe at this 626 stage. It is only upon increased polymerization times, ergo 10 and 60 min, that the imaging contrast 627 between the MgO/MgCl₂ support matrix and the formed polyethylene becomes clear enough due to 628 the strong fragmentation of the original support matrix to spatially resolve the different chemical phase. 629 Here it becomes clear that the MgO/MgCl₂ support matrix is mainly fragmenting internally into 630 successively smaller units according to the continuous bisection. Especially for the 60 min polymerized 631 sample, a complete disintegration of the framework is observed where small MgO/MgCl₂ fragments 632 only a few tens of nm in size are homogeneously distributed within the formed polyethylene phase. At 633 the highest point in this specific cross-section, a thickness of 7.2 µm is obtained, compared to the 5.7 634 µm thickness for the 60 min LaOCI spherical cap. It should be mentioned here that more 635 representative values would be obtained with quantitative 3-D or topological measurements such as 636 AFM (albeit that this sample is too thick for the height limits of the AFM piezo stage) or X-ray nano-637 tomography.

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Figure S20. Secondary Electron Microscopy (SEM) results on the reference MgO/MgCl₂ caps after different ethylene polymerization times. From left to right first a top-down view of a single cap is shown at a certain polymerization time followed by a zoom-in on that specific cap. This is followed by cross-sectional images of the same caps and the respective zoom-ins based on the red box. From top to bottom, an increase of ethylene polymerization time is given, starting at a pristine non-polymerized sample and going up to 60 min of ethylene polymerization. The orange and red scalebars represent a width of respectively 5 and 2 microns. The cyan dashed line in the cross-sectional SEM image of the 60 min ethylene polymerized MgO/MgCl₂ cap depicts a length of 7.2 microns.



678 catalyst framework fragmentation. The shrinking core fragmentation mode starts at the surface of the catalyst679 particle whereas the continuous bisection fragmentation mode starts at the core outwards.



Figure S22. A schematic representation of the fragmentation behaviour of the LaOCI spherical cap model system during ethylene polymerization. Three different polymerization stages are drawn, starting from the pristine spherical cap. In the first stage (i) the internal macroporous cavities and externally accessible cracks of the LaOCI spherical cap starts to be filled with polyethylene and leads to both the extrusion of polyethylene fibres from these cracks, as well as a locally heavy degree of framework fragmentation at the outer rim of the spherical caps, indicating the occurrence of both the shrinking 693 core and continuous bisection fragmentation models in Figure S21. In the second stage (ii) both polymer phases, that is the 694 extruded polyethylene fibres and the thick internal polyethylene regions at the outer rims of the spherical caps, keep growing 695 steadily and cause the formation of additional cracking lines on the framework. Finally, in the third stage (iii) the original morphology 696 of the spherical caps has disintegrated into both large and small LaOCI fragments that are dispersed uniformly throughout the 697 polymer phase, showing that the continuous bisection fragmentation model has become dominant.

The SEM images and EDX maps, shown in Figure S23 of the pristine and 20 min ethylene

699 polymerized sample, are of the same spherical caps, as shown in Figures 2 and 4. EDX shows the

700 presence of La, O and Cl, the constituents of LaOCI both before and after ethylene polymerization.

701 The high photon energies of especially La at 4651 eV for the L α_1 emission line means that the formed

polyethylene phase (carbon binding energy is ~284 eV) will barely lead to attenuation of these photons

and therefore cause the La phase to be easily observable through the polymer phase. For the pristine

LaOCI spherical cap, only a small contribution of carbon is found, most likely due to the adsorption of
 carbonate species due to exposure to air during sample transfer. However, after 20 min of ethylene

polymerization, the carbon signal of the formed polyethylene phase becomes clear.



Figure S23. Top-view Secondary Electron Microscopy Energy Dispersive X-ray spectroscopy (SEM-EDX) results on the LaOCI spherical caps before and after ethylene polymerization. On the left and right side, the top-view back-scattered electron images of respectively the pristine and 20 min ethylene polymerized spherical caps are given alongside the EDX maps of La, Cl, O, C, Ti and Si. The scalebars depict a width of 10 microns.

726 The SEM and EDX images, shown in Figure S24, belong to the cross-sectional regions of the pristine, 727 2 min and 60 min of ethylene polymerization, as shown in Figure 4. The cross-sections are taken 728 around the centre of each spherical cap. For the pristine LaOCI spherical cap, no carbon phase is 729 observed within the cross-section, as expected, whereas for the 2 min ethylene polymerized sample a 730 faint carbon signal can be seen, albeit difficult due to the deposition of carbon on the platinum coating 731 above the spherical cap during the sputtering process. For the 60 min ethylene polymerization, a clear 732 carbon phase can be observed now, as well as the LaOCI fragments dispersed within the carbon 733 phase.



60 min of ethylene polymerization. The red boxes in the SEM images portray the area of the EDX maps in case it

is smaller than the SEM image shown. The scalebars depict a width of 2 microns. A yellow, transparent overlay is provided that indicates the coated Pt layer, all though in some cases it is observed to penetrate into the porous polyethylene layer.

754 In Figure S25, the SEM-EDX images are shown of the pristine and 60 min ethylene polymerized 755 reference MgO/MgCl₂ caps from a top-down perspective. The SEM-EDX of the pristine sample shows 756 the presence of the Mg, O and Cl signals, which is expected from the MgO/MgCl₂ core-shell structure 757 as reported by Chammingkwan et al. [21]. Despite the use of TiCl4 as the chlorinating agent to convert 758 MgO partially into MgO/MgCl₂ as well as that TiCl₄ is the pre-active site, EDX shows no clear signal for 759 Ti on the pristine sample. This might indicate a lower weight loading of Ti on the MgO/MgCl₂ caps with 760 respect to the LaOCI spherical caps where the Ti signal was noticeable in Figure S23. The odd shape 761 of the pristine MgO/MgCl₂ cap could be due to the hydration of the framework upon transfer through 762 ambient conditions towards the SEM apparatus, who's severe effect was shown before by the AFM 763 time-laps in Figure S14. The SEM-EDX images of the 60 min sample clearly show the presence of a 764 highly intense carbon signal, which is attributed to the polyethylene phase when taking the Raman and 765 PiFM results into account. Here the carbon signal is so intense that no clear presence of the Mg, O or 766 CI peaks from the catalyst framework can be observed.



Figure S25. Top-view Secondary Electron Microscopy Energy Dispersive X-ray spectroscopy (SEM-EDX)
results on the reference MgO/MgCl₂ caps before and after ethylene polymerization. On the left and right side,
the top-view back-scattered electron images of respectively the pristine and 60 min ethylene polymerized caps are
given alongside the EDX maps of Mg, Cl, O, C, Ti and Si. The scalebars depict a width of 10 microns.

781 In Figure S26, the cross-sectional SEM-EDX images are shown for the pristine, 2 and 60 min ethylene 782 polymerized reference MgO/MgCl₂ caps. The pristine sample shows that the extent of MgO chlorination 783 seems to be uniform from the external surface towards the interface with the Si(100) substrate and 784 therefore TiCl₄ pre-active sites could potentially speaking be chemisorbed also uniformly throughout the 785 MgO/MgCl₂ volume (on exposed, unsaturated lattices that is) all though again the Ti weight loading 786 seems to be below the detection limit of these EDX experiments. For the 2 min ethylene polymerized 787 sample, the Mg, Cl, O and C signals are all visible whereas for the 60 min ethylene polymerized sample, 788 Mg is barely visible with CI and O signals being too diluted within the highly intense C signal from the 789 formed polyethylene. The zoom-in cross-sectional image of this same 60 min ethylene polymerized cap 790 in Figure S20 also showed how finely the original MgO/MgCl₂ has fragmented as compared to the 60 791 min ethylene polymerized LaOCI spherical cap where larger support fragments were still clearly visible 792 with EDX.



- 804 Figure S26. Cross-sectional Secondary Electron Microscopy Energy Dispersive X-ray spectroscopy (SEM-
- 805 EDX) results on the refence MgO/MgCl₂ caps before and after ethylene polymerization. The cross-sectional
- 806 back-scattered electron images alongside the EDX maps of Mg, Cl, O, C, Ti and Si are given for the pristine, 2 min
- 807 and 60 min of ethylene polymerization. The red boxes in the SEM images portray the area of the EDX maps in case
- 808 it is smaller than the SEM image shown. The scalebars depict a width of 5 microns. A yellow, transparent overlay
- 809 is provided that indicates the coated Pt layer, all though in some cases it is observed to penetrate into the porous
- 810 polyethylene layer.

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811 Supplementary References

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