

1 Supplementary Materials for

2

3 Spatiotemporal dynamics of self-organized branching in pancreas-derived

4 organoids

5

6 S. Randriamanantsoa, A. Papargyriou, H. C. Maurer, K. Peschke, M. Schuster, G. Zecchin, K. Steiger, R.

7 Öllinger, D. Saur,

8 C. Scheel, R. Rad, E. Hannezo, M. Reichert*, A.R. Bausch*

9 These authors contributed equally: S. Randriamanantsoa, A. Papargyriou

10 *Correspondence to: abausch@mytum.de, maximilian.reichert@tum.de

11

12 **This PDF file includes:**

13

14 Supplementary Note

15 Figs. S1 to S7

16 Tables S1 to S3

17 References

18

19 **Other Supplementary Materials for this manuscript include the following:**

20

21 Movies S1 to S15

23 **Supplementary Note**

24 **I. MINIMAL ANALYTICAL MODEL OF BRANCHING ORGANOID GROWTH**

25 We first provide detail for the minimal theoretical model used to understand the branching
26 structure of pancreatic organoids. We start with the case of a single branch, before moving to
27 the description, backed by numerical simulations, of entire branched trees.

28

29 **A. *Single branch elongating without branching, nor proliferative feedback***

30 We consider a cylindrical branch with width w (or radius $r = w/2$) and length L , made up of N
31 cells with volume V_c , so that by volume conservation, branch width and length must be related
32 by $\pi L w^2/4 = N V_c$. We consider that cells divide at a constant rate k_d , and that the cell at the very
33 tip exerts a pulling force f_0 on the tube, which tends to elongate it. We denote as ζ the friction
34 coefficient of cells migrating through the matrix.

35 Force balance on the tip cell then reads:

$$36 \quad \zeta L'(t) = f_0 + \sigma_{branch} \quad (S1)$$

37 i.e. the tube can elongate at speed $v = L'(t)$ either due to active migration at the tip (which
38 predicts a linear increase at speed f_0/ζ), or due to compressive forces σ_{branch} from the bulk of
39 the follower cells in the branch which can be dividing. A simple assumption is that those
40 compressive forces are dependent on the 1D cell density $\rho(t) = N(t)/L(t)$, so that $\sigma_{branch} = \chi\rho(t)$
41 where χ is a compressibility¹. We now write the evolution of cell numbers in the branch, which
42 can increase due to proliferation, or decrease due to elongation:

$$N'(t) = L'(t)\rho(t) + L(t)\rho'(t) = k_d N(t) \quad (S2)$$

so that force balance can be re-wrote as

$$\zeta L'(t) = f_0 + \chi e^{kat}/L(t) \quad (\text{S3})$$

43 In this simplified model, there is no feedback on cellular proliferation, so that the cell number
 44 increases exponentially, as does length $L(t) \propto e^{kat/2}$ at long time scales ($L \rightarrow \infty$). On the other
 45 hand, migration force f_0 causes a linear increase, which is thus always negligible compared to
 46 proliferation at long enough time scales. Moreover, in the early time points, one expects the
 47 branch to be under tension (because $f_0 \gg \sigma_{branch}$, i.e. tips pull more than they are pushed) -
 48 which is the time at which there could be breakage as observed in the data (see for instance the
 49 “high branch count” real organoid in Fig. 4h, where some of the cells at the tips occasionally
 50 transiently detach). In the late time points, proliferation always wins and catches up, so that the
 51 length increases exponentially, pushed by the back. Note however that even in this simple
 52 scenario, the cell density also exponentially increases (because $N(t) \propto e^{kat}$, so much faster
 53 than length), which is due to frictional slowing down.

54

55 ***B. Single branch elongating without branching, but with proliferative feedback***

56 This is clearly unphysical, and feedback mechanisms on proliferation must be included in the
 57 theory. Indeed, there is extensive evidence for stress/density feedbacks on proliferation²⁻⁵,
 58 which has been proposed as a source of stabilization of tissue growth^{6,7}. At linear order, the
 59 conservation equation for cell numbers with feedback reads:

$$60 \quad N'(t) = L'(t)\rho(t) + L(t)\rho'(t) = k_d N(t)(1 - \alpha\rho(t)) \quad (\text{S4})$$

61 Note that because we have assumed a simple linear relationship between stress and density,
 62 both enter the feedback in the same way, making this equation quite general^{6,7}. This regulates
 63 density to a well-defined maximal value of $\rho_0 = 1/\alpha$. Under this assumption, density will always
 64 saturate to ρ_0 , while length grows linearly with slope $L'(t) = (f_0 + \chi\rho_0)/\zeta$. This means that a
 65 phase of exponential growth (proliferation-limited) will be succeeded by a phase of linear

66 growth (migration-limited), due to the frictional forces penalizing growth-driven motion (note
67 that for the limit $\zeta \rightarrow 0$, we get back to the results of the first section as expected).

68 Importantly, as long as the maximal proliferative stress $\chi\rho_0$ is larger than migration forces f_0 ,
69 the branch will always transition from early tension/low density (where migration forces thin
70 the branch more than it can be replenished by proliferation), to a state of late compression/high
71 density (where proliferation catches up).

72 **C. *Branching tree growth with constant tip speed and no proliferative feedback***

73 This analysis suggests that growth of a single branch will always converge to a linear regime in
74 the presence of proliferative feedbacks. However, we haven't considered so far the branching
75 of one tip into two (rate k_b), which drives branching morphogenesis. For tip branching, the total
76 number of tips grows in time as $T(t) \propto e^{k_b t}$, with the total number of branches scaling as $2T(t)$
77 (for a symmetrically branching tree). If all tips grow with speed v_0 , this means that the total
78 length of the tree (equal to the sum of all branches) will scale as

$$79 \quad L(t) = \frac{v_0}{k_b} e^{k_b t} \quad (\text{S5})$$

80 and if cellular proliferation occurs at a constant rate k_d , the 1D cellular density (or branch radius)
81 will scale as

$$82 \quad \rho(t) = \frac{k_b}{v_0} e^{(k_d - k_b)t} \quad (\text{S6})$$

83 which now compares two exponential processes, instead of a linear edge growth vs. an
84 exponential bulk growth. In particular, if $k_b > k_d$, branching is too fast relative to cell division,
85 and cellular density/branch thickness is expected to decrease. On the other hand, even if
86 branching is slower than cell division, the transition towards significant branch thickening is
87 expected to be strongly delayed compared to the previous section.

89 **D. Branching tree growth with constant tip speed and feedbacks**

90 Finally, combining the results from the previous sections, we can investigate the case of
 91 branching trees together with feedback on proliferation from branch thickness/density. Again,
 92 we make the simplifying assumption that all branches have equal thickness, something we will
 93 relax in numerical simulations in the next sections. The equations for total cell number $N(t)$,
 94 total tree length $L(t)$ and branch radius/width $r(t) \propto \sqrt{N(t)/L(t)}$ read:

$$95 \quad \begin{cases} N'(t) = L'(t)r^2(t) + 2r(t)L(t)r'(t) = k_d N(t) \left(1 - \frac{w(t)}{w_0}\right) \\ L'(t) = \frac{v_0}{k_b} e^{k_b t} \end{cases} \quad (S7)$$

96 Interestingly, this again revealed two regimes of growth. At early stages of small cell numbers,
 97 migration dominates over proliferation, and branches are expected to be thin ($r \ll w_0$) allowing
 98 for fast growth at rates close to k_d . Thus, the total number of cells in a branched organoid is
 99 expected to grow exponentially as $e^{k_d t}$ at early time points. At later times however, the width
 100 converges towards a steady state, and we find that this growth phase is limited by the branching
 101 rate, with cell numbers growing as $e^{k_b t}$, so that

$$102 \quad w(\infty) = w_0(1 - k_b/k_d) \quad (S8)$$

103 which corresponds to a width smaller than the maximal one w_0 at which proliferation stops, and
 104 at which the proliferation is slowed down enough to allow a steady-state, corresponding to a
 105 match between the branching rate k_b and the division rate $k_d(1 - w/w_0)$. It should be noted that
 106 this can only occur for $k_b < k_d$, which is similar to the criterion to the section above: if branching
 107 is faster than divisions, then branches would thin to zero-radius because branch proliferation
 108 could not keep up with the generation of moving tips.

109

110 **II. PARAMETER ESTIMATION AND MODEL PREDICTIONS**

111 We now seek to estimate each of the model parameter from the data, as well as experimentally
112 verify some of our key assumptions.

113 We note that we intentionally restrict our model to the modelling of the branching and early
114 thickening dynamics, occurring in general between day 1 and 9, and excluding the Lumen
115 Formation phase of the organoids. Indeed, we experimentally find that, while the Onset,
116 Extension, and early Thickening phases rely on similar processes of extension, branching, and
117 proliferation, the late Thickening phase involves strong contraction, and the Lumen Formation
118 phase appears to involve different processes, such as fluid intake, fluid pressure, or cell shape
119 changes.

120 The formation of a lumen inside the branches also complicates the extension of the present
121 model to the Lumen Formation phase: indeed, it would imply redefining the way some
122 parameters are defined between phases, ultimately leading to a different model, with different
123 validating experiments. For instance, the present manuscript uses the width of the branches as
124 a proxy to estimate the maximal division rate k_d : this approximation is valid when the branches
125 are not hollow; it however loses its validity when the lumen start swelling, and when fluid
126 intake starts contributing to the thickness of the branch, independently of whether proliferation
127 is actually taking place.

128 *A. Assumptions of migratory and proliferation feedback*

129 A key assumption that we have made is to i) assume a feedback from branch thickness on
130 proliferation and ii) to take it as a linear dependency for simplicity (although the analysis would
131 be largely similar in the presence of more complex functional forms). To check this in the data,
132 we made use of a live-imaging dataset for organoid morphogenesis between day 7 to day 10,
133 where we tracked the morphometrics of single branches in real-time for a few hours. This
134 included a systematic quantification of tip speed, branch length and branch width for a number
135 of randomly selected terminal branches in the organoid.

136 As a proxy for proliferation, we calculated at each time point the volume of a branch $V(t) =$
137 $\pi w^2(t)L(t)/4$, and estimated the rate of volumetric growth $K(t)$ (which is a proxy for division
138 rate k_d , although in principle a death rate of cells would negatively impact volume, so that the
139 rate k_d could be seen as a balance between growth and loss) by comparing consecutive time
140 points (separated by Δt) as $K(t) = \frac{V(t+\Delta t)-V(t)}{V(t)\Delta t}$. We checked that the average $\langle K(t) \rangle$ over all
141 branches was approximately constant in time, as expected when considering time scales of a
142 few hours, which served as a control that the system is not slowing down due to photo-toxicity
143 while imaging for instance.

144 Importantly, although $K(t)$ was very broadly distributed, plotting its value for each branch at
145 each time point against the corresponding branch width $w(t)$ revealed a clear trend, where
146 growth was markedly slowed down for larger branch radius, in a roughly linear manner. This
147 verifies one of our key assumptions and allows us, from comparing data with the model of $K =$
148 $k_d(1 - w/w_0)$, to fit both the maximal division rate k_d and the maximal width w_0 (at which
149 proliferation is fully abrogated). Quantitatively, from a linear fit (Fig. 4b), we find $k_d = 3.9 \pm 1.2$
150 d^{-1} and $w_0 = 25 \pm 6 \mu\text{m}$ (best fit parameter \pm standard error of the fit).

151 A second important assumption from the section above is that we considered tip speed v_0 to be
152 constant. Given the dependency of volumetric branch growth on branch width, we reasoned
153 that it was an important control to see whether or not the speed of a given tip was correlated to
154 the morphometric of its branch (width or length). However, we found no such correlation, and
155 a constant value of $v_0 = 80 \mu\text{m/day}$ was extracted from this dataset (Fig. 5h). We also found that
156 detached cells migrated through the matrix at a similar velocity, arguing that tip
157 movement/matrix degradation is the dominant phenomena setting tip growth (as opposed to
158 stresses from the bulk/leader cells, which could explain why tip speed is not dependent on
159 branch morphometrics).

160

161 **B. *Estimation of other parameters***

162 Although measuring the branching rate from live-imaging is technically difficult, it can be
163 estimated by comparing the tip elongation rate v_0 to the average length of a branch l_0 , which we
164 found to be $l_0 \approx 150 \mu\text{m}$. From this, we could estimate that a constant branching rate of around
165 once every 2 days $k_b \approx 0.55 \text{ d}^{-1}$, further corroborated by measuring the average number of
166 branches of organoids from day 1 to day 9 (Fig. 4f, and see A. Summary of parameter
167 estimation and simulation inputs in the Supplementary Note).

168

169 **C. *Predictions from the model on unperturbed and perturbed organoid growth***

170 With these orders of magnitude, one can estimate that the transition from 1D cell density/branch
171 thickness decrease (due to linear growth of the tip) to density/thickness increase where contact
172 inhibition (due to proliferation) should occur on very rapid time scales of less than a day. This
173 means that organoid growth should largely be over during these timescale (i.e. if there weren't
174 branching events). However, as mentioned above, tip branching at rate k_b causes an exponential
175 increase of the number of tips at rate $e^{k_b t}$, and if each of these tips elongate at a speed v_0 , this
176 means that the "edge" of the pancreas grows exponentially - rather than linearly in the case of
177 a single branch (or classical 1D/2D/3D cohesive cellular colonies). We predict that such an
178 exponential branching allows pancreatic organoids at their "full" exponential capability k_d to
179 grow for longer (3-4 days), with contact inhibition occurring only after, and branching allowing
180 continued exponential growth (albeit at a slow rate k_b), which matches well the experimental
181 observations.

182 More quantitatively, turning to the prediction for the average number of cells in time in an
183 organoid, we found that the model predicted very well the data across all time points (see Fig.

184 4d, even though the width to proliferation feedback was fitting only from short-term tracking
185 around day 7). In particular, the model reproduces well the inflexion of growth shown in the
186 data (Fig. 2d, Fig. 4d), which is predicted to arise due to the increase of average branch thickness
187 in time (which feedbacks negatively on proliferation). Again, both of these predicted features
188 agreed well with the data showing i) a steady decrease in the number of proliferative cells (as
189 assessed by the Ki67 to DAPI ratio, Fig. 2c-e), and ii) a steady increase in branch thickness
190 within the first days, then a more gradual plateau until day 10 (Fig. 4d).

191 We note that the apparent deviation of the “experimental” terminal branch average thickness
192 from the “theoretical” value at day 8 and 9 (Fig. 4e), can be explained by the fact that, due to
193 heterogeneity, some organoids phenotypes can display budding and occasionally start lumen
194 expansion earlier than others, thereby driving the increase in apparent average thickness. As the
195 current model does not take into account the lumen formation phase, for aforementioned
196 reasons, such discrepancies might emerge. While, for comparison purposes with the model, we
197 have taken care to exclude branches that displayed obvious, large and optically resolvable
198 lumens, early fluid intake in branch tips (which can still lead to a noticeable increase in
199 thickness), can be difficult to detect using the method described in the Methods section “Branch
200 thickness measurement (static)”.

201 We then proceeded to test some of the model predictions upon pharmacological perturbation.
202 We first performed a batimastat treatment, which is expected to decrease the ability of tip cells
203 to migrate through the ECM. Indeed, we found that upon addition of batimastat at day 7, average
204 tip speed was reduced to zero. We input this in the model (together with a reduction of branch
205 growth of 80% which we found experimentally, and could be due to secondary effects of the
206 drug). We found that whereas WT organoids grew little in width between day 7 and day 9 (as
207 expected in the second phase of growth predicted by the model), batimastat-treated organoids

208 were predicted to show larger branch thickness growth (proliferation without concomitant
209 elongation), something we observed experimentally (Fig. 5c and Fig. S6f).

210 Turning to aphidicolin treatments, we found that it displayed an inhibition of tip volumetric
211 growth (k_d reduced by 56%), as expected from this drug, while having a more moderate effect
212 on tip elongation speed (v_0 reduced by 42%). Modelling these changes in the model from day
213 7 predicted a decrease in branch thickness (due to continued elongation with less proliferation),
214 a feature that mirrored the data of branch thinning upon aphidicolin treatment (Fig. S6d, S6h).

215

216 III. NUMERICAL SIMULATIONS OF SPATIAL BRANCHED ORGANOID 217 GROWTH

218 So far, we have used a mean-field model to fit the data, where we have averaged morphological
219 parameters over an entire organoid, and predicted the temporal variations of these averages.
220 However, the model described above can easily be simulated spatially.

221 To do this, we took the framework of branching random walks in space⁸, where an organoid is
222 represented by elongating and branching tips (resp. at constant deterministic speed v_0 and
223 stochastic rate k_b , i.e. branching as a Poisson process), as well as the ducts they leave behind.
224 Each tip i is represented by its coordinates (x_i, y_i) in a 2D plane and each branch j has a given
225 width w_j and length l_j (which elongates at rate v_0 if connected to an active, unbranched tip).
226 Branch width w_j can change either due to tip elongation (if the branch is terminal, i.e. connected
227 to an active tip, which reduces width w_j to maintain constant branch volume upon elongation -
228 no elongation occurs if the branch is not terminal), or due to growth (which increases width at
229 rate $K = k_d(w_0 - w_j)$ without changing length l_j).

230 More specifically, given that the volume of a branch j is given by $V_j = \pi l_j (w_j/2)^2$, a tip
231 elongation from a length $l_j(t)$ at time t to a length $l_j(t + \delta t) = l_j(t) + v_0 \delta t$ at time $t + \delta t$

232 obeys the conservation law $V_j(t) = V_j(t + \delta t)$, meaning that it rescales width as $w_j(t + \delta t) =$
 233 $\frac{w_j(t)}{\sqrt{1+v_0\delta t/l_j(t)}}$. Similarly, growth at rate K from time t to $t + \delta t$ increases branch volume by a
 234 quantity $KV_j(t)\delta t$, so that the width is rescaled as $w_j(t + \delta t) = w_j(t)\sqrt{1 + K\delta t}$.

235 **A. Summary of parameter estimation and simulation inputs**

236 Overall, the parameters that we use for the spatial simulations are the same as for the continuum
 237 model (with a few additional variables that have little to no impact on the resulting dynamics),
 238 which we summary here, both showing the values that we use for these parameters in Fig. 4,
 239 but also the origin of their estimation:

- 240 • Growth parameters k_d and w_0 . These have been fitted from the short-term imaging of
 241 tip elongation and growth between day 7 and 10 – from a linear fit of the data shown in
 242 Fig. 4b. Best-fit values used in the simulations: $k_d = 3.9 d^{-1}$ and $w_0 = 25 \mu\text{m}$.
- 243 • Tip elongation velocity v_0 . These have been estimated as the average of tip elongation
 244 speed from the short-term imaging between day 7 and day 9, which show no significant
 245 correlation with other variables such as tip width w (Fig. 5h, Fig. S5g). Values used in
 246 simulation $v_0 = 80 \mu\text{m/day}$.
- 247 • Branching rate k_b . Estimated from the average branch length measured between day 7
 248 and day 9 ($l_0 \approx 150\mu\text{m}$), which together with an estimated elongation speed of v_0 ,
 249 would result in a typical branching rate of $k_b = \frac{v_0}{l_0} \approx 0.55/\text{day}$. Alternatively, we can
 250 also fit it from the increase in branch number, which leads to a best fit value of $k_b =$
 251 $0.75/\text{day}$, consistent with the alternative estimation. We note that the overall
 252 quantitative dynamics of organoids is only weakly affected by this range of parameters
 253 (which controls the second phase of slower exponential growth). Value used in
 254 simulations $k_b = 0.75/\text{day}$.

- 255 • Initial conditions. At the beginning of the simulations (day 1), we considered that there
256 is a single cell, consisting of a single branch. We initialize the simulations with a width
257 of $w = 5 \mu m$ and length of $l = 20 \mu m$. At each branching event, we apply the same
258 initial condition, considering that the nascent branch has a width of $w = 5 \mu m$.
- 259 • Branching angle. This parameter does not impact any of the results, as tips do not
260 interact spatially, and is thus only relevant for the visualization of the trees (Fig. 4c, 4h).
261 We take angles of branching between mother and daughter branches of $\pi/3$.

262

263 ***B. Simulation output: variability in organoid branching***

264 A typical outcome of these simulations is shown in Fig. 4c, 4h - although we show in Fig. 4h
265 that because of the stochasticity of the branching process different runs with the exact same
266 parameters can have very different morphometrics (which could explain the variability we find
267 in the data in a minimal way). Note that we neglected tip termination – as we model the first
268 phase of growth where tips elongate at a near constant velocity (see above), so that the
269 stochasticity comes purely from the timing of stochastic branching, rather than from spatial
270 interactions between tips as in branching and terminating random walks ⁸.

271 Importantly, when averaging over many simulations ($n = 100$, as shown in Fig. 4), we find that
272 these recapitulate not only the temporal dynamics of branching (near-constant exponential
273 growth in the number of branches per organoid, as predicted by a constant branching rate k_b),
274 but also the organoid to organoid variability (assessed by standard deviation in number of
275 branches per organoids). Indeed, this standard deviation also grew exponentially with similar
276 values as the average, providing a non-trivial prediction of our model of stochastic branching
277 (Fig. 4f-g). Note that this model of stochastic branching also makes the prediction, at smaller
278 scales, that branching can happen at any time with equal probabilities, so that we expect also a
279 broad (exponential) distribution in branch length. We tested this by measuring non-terminal

280 branch length across organoids at day 7 to 10 during the extension phase. Keeping in mind that
281 branches cannot have very small lengths (<15 microns, i.e. comparable to cell size), we indeed
282 found that branch length was very broadly distributed and consistent with an exponential
283 distribution (Fig. S5e). This is in contrast to what would happen with a Turing instability on a
284 simple domain ⁹, which would lead to periodic branching and thus highly peaked distribution –
285 although continuous ductal growth can also cause more complex dependencies. This could be
286 addressed in the future by measuring in further detail the relationship between branch age and
287 length ¹⁰, although the strong non-stereotypicity that we observe both between organoids and
288 in different regions of a given organoid suggest that intrinsic branching stochasticity is a simple
289 explanation for the broadness of the length distribution.

290

291 **C. *Simulation output: temporal dynamics in branch thickening and cell number***

292 When comparing the average predictions of the simulations with the analytical model, we found
293 that both agreed well with each other. In particular, when examining the total cell number per
294 organoid, the simulations confirm the predicted cross-over between exponential growth at rate
295 k_d initially (Fig. S6a-d, left column) when branch thickness is small (Fig. S6a-d, right column),
296 before a second phase where thickness plateaus and growth of cell numbers (Fig. S6a-d) still
297 follow an exponential trend but at rate k_b . Manipulating the branching rate k_b , elongation speed
298 v_0 and division rate k_d in the computational model by halving or multiplying by two their value
299 compared to the measured parameters confirmed these insights (see Fig. S6a-d for such a
300 sensitivity analysis).

301 In particular, the simulations agreed well with the analytical prediction that branch width should
302 plateau to a value of $w = w_0(1 - k_b/k_d)$ (which represents a compromise between thickening
303 via growth and thinning via branching/elongation). Using the parameters inferred above, this
304 plateau width is predicted to be approximately 20 μm , which fits well with the data after a first

305 phase of gradual thickening during the first days (Fig. 4e). Conversely, when examining the
306 average number of cells per organoid, we found similar dynamics as predicted, with a first phase
307 of very fast growth well-fitted by the model (close to k_d) before a second phase of slower
308 growth (dictated by k_b) – see Fig. 4d.

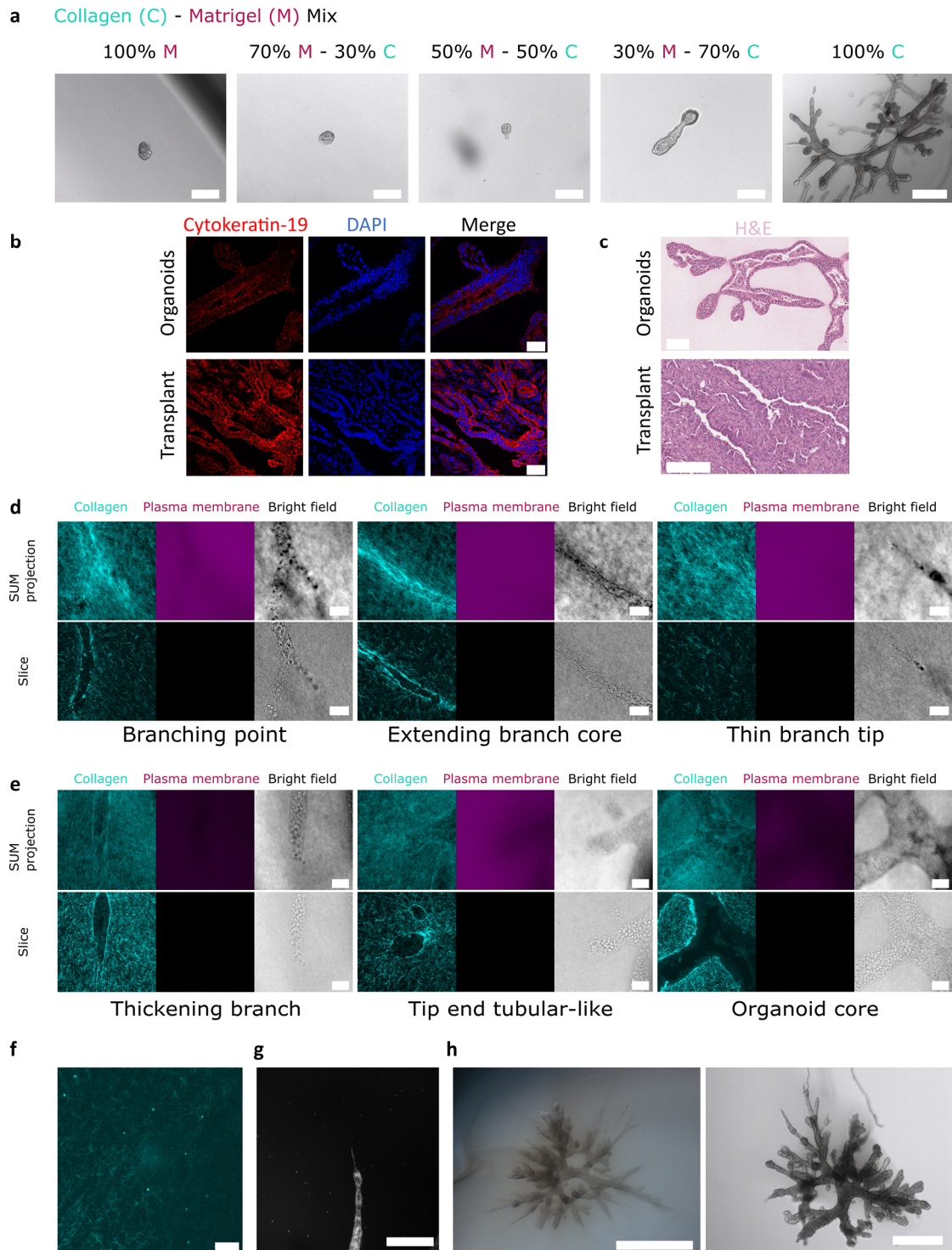
309 ***D. Simulation output: spatial dynamics of tip and branch morphometrics***

310 Finally, we also predict in the simulations some spatial features (which are by definition beyond
311 the scope of the analytical, non-spatial model). For instance, newly formed branches first
312 undergo a phase of branch thinning due to tip elongation before containing enough cells so that
313 proliferation dominates (and width increases) - and so that branch width plateaus to its maximal
314 value at which proliferation is arrested. Thus, the simulation predicts a dependency of width on
315 branch "age": branches close to the origin of the organoid are the widest and less proliferative
316 while more recently formed branches at the periphery are thinner and more proliferative. This
317 fits qualitatively with our observations of branching morphologies (Fig. 2c-e), and to back this
318 up more quantitatively, we separately outputted in the simulations the width of terminal
319 branches (which are elongating) and non-terminal branches (generation of more than one since
320 the origin). This was binned in such two categories to be able to straightforwardly compare to
321 data, where we separately measured at all time points the width of tip branches and the width
322 of branches past a branch point. Interestingly, we found good agreement between data and
323 simulations, with both quantities showing a plateau in time (as does the average width across
324 all branches), but at very different width (Fig. 4e).

325 In the computational model, it was also possible to explore the effect of additional potential
326 mechanisms. Indeed, so far we have treated each branch as separate, non-communicating
327 entities (so that volumetric growth of a branch was only due to its proliferation). However, in
328 particular at the initial stage where a new top just branched, and volume of a new branch is
329 very small, it could be that fluxes occur between branch and are significant for volumetric

330 growth. To model this in a simple way, we performed the simulations again, but allowing for
331 pressure driven fluxes q_{ij} to occur between two branches in contact i and j (from i to j). For
332 simplicity, we took the simplest linear constitutive equation $q_{ij} = -\alpha(w_i - w_j)$ (i.e. $\alpha > 0$
333 necessary for stability, meaning that wide branches flow into thin ones, a simple assumption
334 based on the fact that width w_i is proportional to the pressure exerted on surrounding matrix).
335 Importantly however, when exploring different values of α , we found that these did not
336 markedly change the dynamics, when plotting the total cell number (Fig. S6a, left) or branch
337 thickness (Fig. S6a, right). The main change was that α "smoothed" the spatial variations with
338 branch age (for $\alpha \rightarrow \infty$, all branches have the same thickness and the mean-field model is
339 recovered exactly).

340



341

342 **Fig. S1. Influence of the matrix composition, and remodeling of the collagen**
 343 **environment.**

344 **(a)** Bright field pictures of organoids at day 13 (D13), cultured in mixtures of collagen I and
 345 Matrigel in various proportions (n = 3 individual experiments).

346 **(b)** Immunostaining of Cytokeratin-19 (red) and DAPI staining (blue) in D13 collagen-grown
347 PDAC organoids and *in vivo* transplants of PDAC cells (n = 3 technical replicates).

348 **(c)** Haematoxylin and eosin (H&E) staining of D13 collagen-grown organoid and orthotopic
349 transplant sections (n = 3 technical replicates).

350 **(d), (e)** Organoids were treated at D8 (d, n = 3 organoids) or D11 (e, n = 3 organoids) with
351 Triton-X 100 and fixed. Triton-X 100 degrades the cell membrane and provoke the
352 dissociation of organoids. Organoids are stained with CellMask, a plasma membrane marker
353 (magenta), to ensure that the membrane has been properly washed away after the Triton-X
354 treatment. Collagen fibers are visualized with reflection microscopy (cyan). The architecture
355 of the collagen surrounding the organoids is preserved, indicating a plastic deformation of the
356 ECM. Summed slices projections and single confocal slices are shown.

357 **(f)** Collagen fibres far away from organoids, visualized with reflection microscopy (n = 3
358 organoids). The fibres display no particular alignment far away from organoids. Confocal
359 slice.

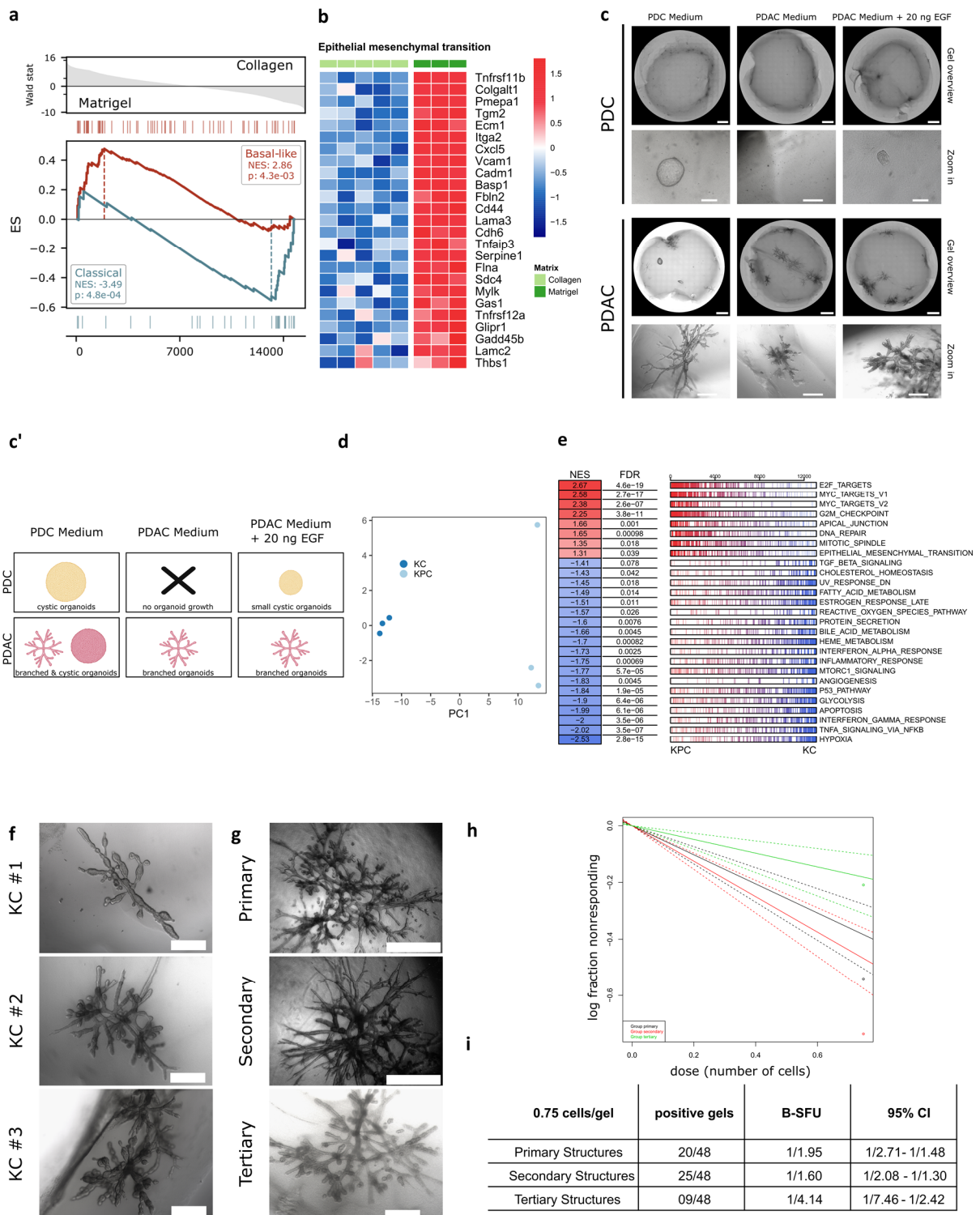
360 **(g)** Plasma membrane staining of an invasive protrusion at D7 (n = 13 organoids). Summed
361 slices projection.

362 **(h)** Bright field pictures of a D13 organoid in collagen (left) and after collagen digestion
363 (right) (n = 3 individual experiments).

364

365 Scale bars in (a), from left to right: 200 μm for the first four pictures, 500 μm for the fifth; in
366 (b): 50 μm ; in (c), 100 μm (top), 200 μm (bottom); (d), (e), (f): 50 μm ; in (g): 100 μm ; in (h)
367 from left to right: 1000 μm , 500 μm .

368



369

370 **Fig. S2. PDAC organoids epithelial plasticity drives branching morphogenesis with**
 371 **distinct structure forming capabilities.**

372 **(a)** Expression scores for the “Classical” and “Basal-like” signatures displayed by Matrigel-
 373 and collagen-grown organoids at Day 13.

374 **(b)** Expression patterns for epithelial to mesenchymal transition (EMT) related markers,
375 differentially expressed between Matrigel- and collagen-grown organoids at Day 13.

376 **(c)** Representative collagen gels containing PDC or PDAC cells, cultured in PDC medium
377 (see Methods for the full composition)¹¹, DMEM + 10 % FBS (PDAC medium), and PDAC
378 medium + 20 ng EGF. Results are summarized graphically in **(c')**: PDC form cystic
379 organoids in PDC medium, and small cystic organoids in PDAC medium + 20 ng EGF.
380 PDAC cells can form both branched or cystic organoids in PDC medium, and form branched
381 organoids in PDAC medium and PDAC medium + 20 ng EGF. Created with BioRender.com
382 “Gel overview” pictures scale bars: 2000 μm . “Zoom-in” PDC pictures scale bars, from left to
383 right: 200 μm , 500 μm , 100 μm . “Zoom-in” PDAC pictures scale bars: 500 μm . “Gel
384 overview” pictures were stitched from a tile scan of a culture well and cropped to display the
385 collagen gel.

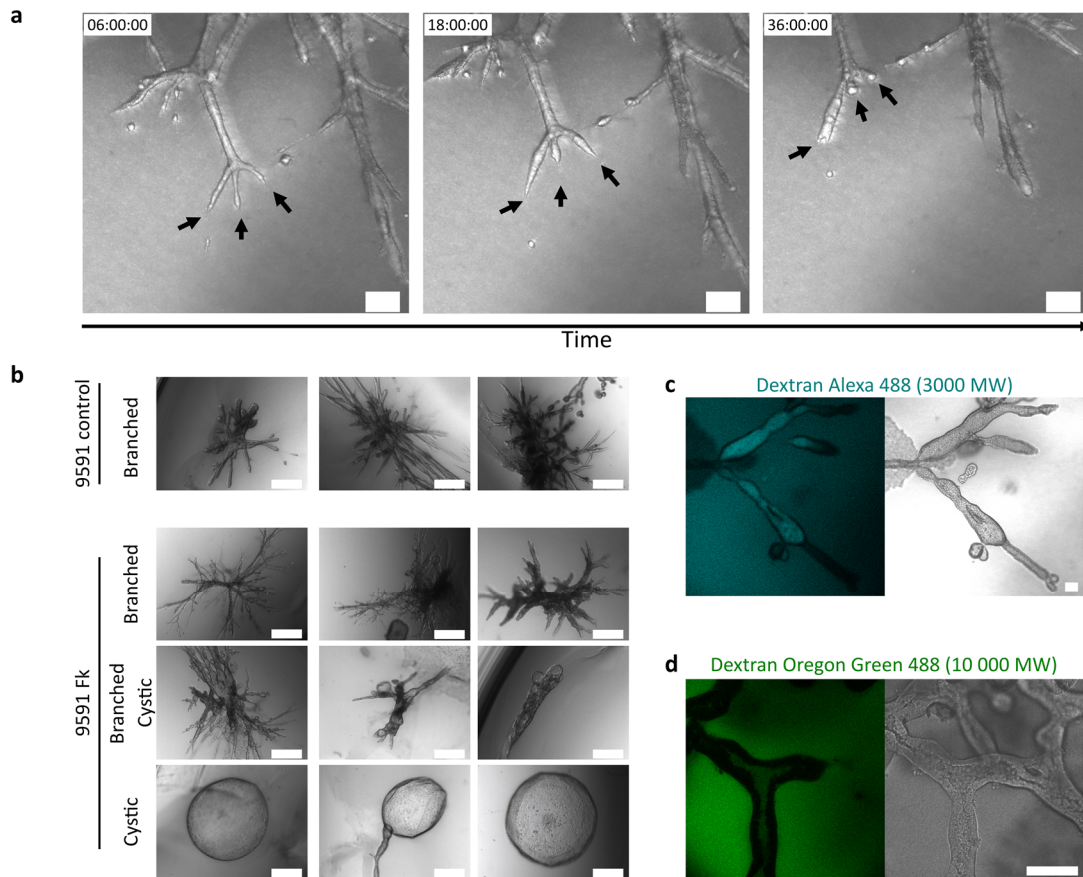
386 Principal component analysis of bulk RNA sequencing of Day 13 collagen-grown organoids
387 originating from cells derived from KC or KPC mice **(d)**, and corresponding summary of gene
388 set enrichment analysis **(e)**. NES, FDR bars represent each individual gene for a given gene
389 set.

390 **(f)** Representative Day 13 collagen-grown organoids originating from PDAC cells derived
391 from three distinct KC mice ($n = 3$ individual experiments). Scale bars: 500 μm .

392 **(g)** Organoids were grown until Day 13 in collagen (“Primary” structures), dissociated at the
393 single cell level and then seeded again in collagen, giving rise to “Secondary” structures.
394 Repeating this process on “Secondary” structures at Day 13 in turn yielded “Tertiary”
395 structures. Scale bars, from top to bottom: 1000 μm , 1000 μm , 500 μm .

396 **(h)** Log plot of non-responding well against cell dose.

397 **(i)** Extreme Limiting Dilution Analysis summary table.



399

400 **Fig. S3. Chemical perturbations via aphidicolin and forskolin.**

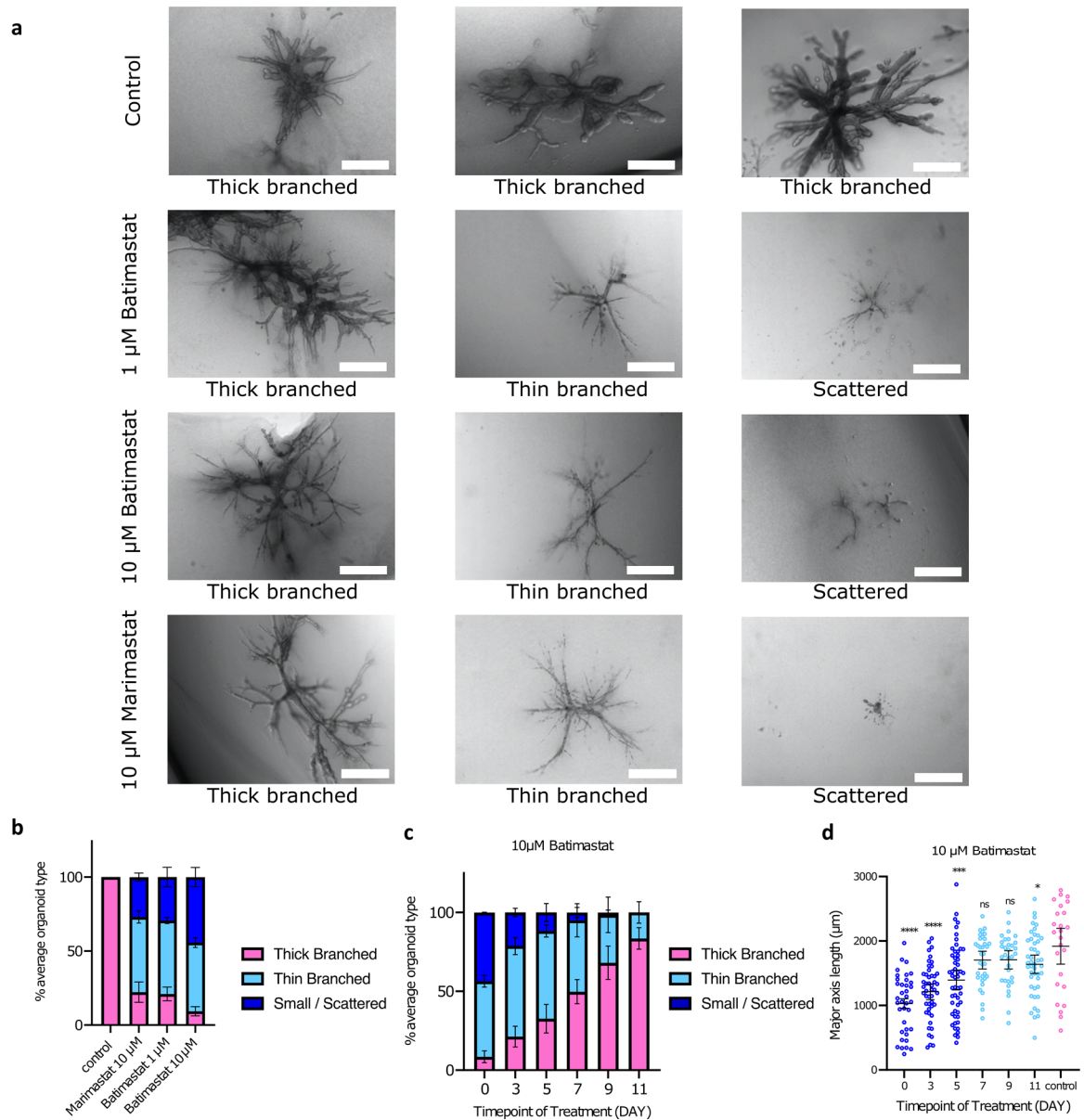
401 (a) Bright field time-lapse of an organoid branch upon addition of $2 \mu\text{g.mL}^{-1}$ of aphidicolin at
 402 D7. Black arrows indicate spots of branch rounding and retraction.

403 (b) Bright field pictures of organoids at D13 in control conditions and upon addition of
 404 forskolin (Fk) at $10 \mu\text{M}$. Forskolin addition triggers the apparition of cystic organoids, with
 405 lumens over-swelling ($n = 3$ individual experiments).

406 (c), (d) Dextran Alexa 488 ((c), 3000 MW, cyan, $200 \mu\text{g.mL}^{-1}$, $n = 3$ replicates) or Dextran
 407 OregonGreen ((d), 10 000 MW, green, $200 \mu\text{g.mL}^{-1}$, $n = 2$ replicates) can be incorporated
 408 inside the lumen upon overnight incubation at D13-14. Confocal slices shown.

409 Scale bars in (a), (c), (d): $100 \mu\text{m}$; in (b): $500 \mu\text{m}$.

410



411

412 **Fig. S4. Effect of MMP inhibition on collagen-grown organoid development.**

413 **(a)** Bright field pictures of organoids at day 13 in control conditions and upon addition of
 414 batimastat at 1 μM or 10 μM , or marimastat at 10 μM (Control: n=156, Marimastat 10 μM :
 415 n=106, Batimastat 1 μM : n=110, Batimastat 10 μM : n=129, organoids). Organoids are labelled
 416 according to their phenotype, in "Thick branched", "Thin branched" and "Scattered"
 417 categories. Scale bars: 500 μm .

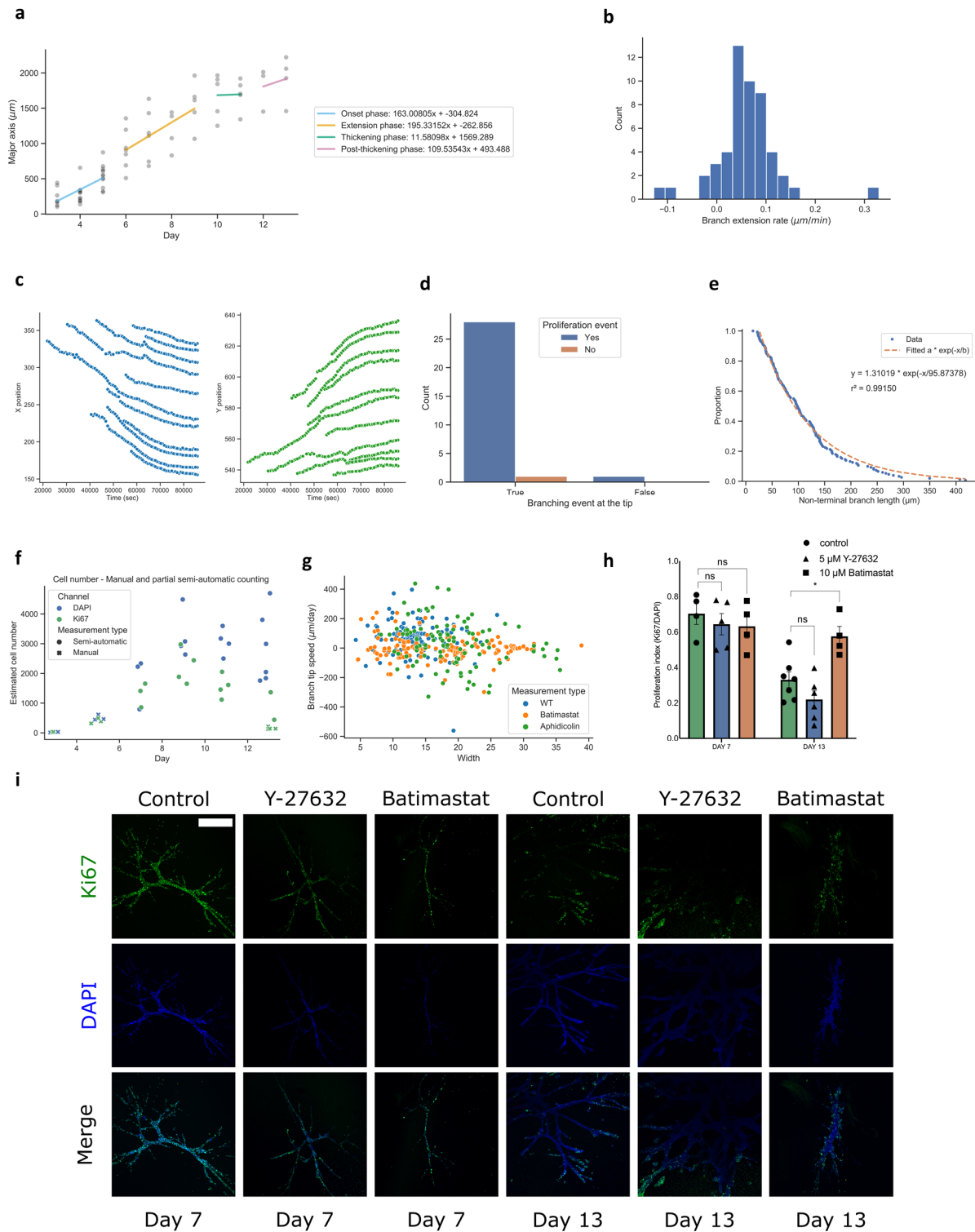
418 **(b)** Distribution of organoid phenotypes at day 13 according to the different MMP-inhibitors
419 used and added at seeding time (Control: n = 156, Marimastat 10 μ M: n = 106, Batimastat
420 1 μ M: n = 110, Batimastat 10 μ M: n = 129, organoids). Bars: mean \pm sem.

421 **(c)** Distribution of organoid phenotypes at day 13 according to the addition day of 10 μ M
422 batimastat. (Control: n = 82, Batimastat: n = 589, organoids). Bars: mean \pm sem.

423 **(d)** Major axis length of organoids at day 13 upon addition of 10 μ M batimastat at different
424 timepoints (n = 275 organoids). Bars: mean \pm sem. Un-paired two tailed parametric t-test; * P
425 = 0.0465, *** P = 0.0006, **** P \leq 0.0001, ns P = 0.131 (batimastat addition at day 7) and P
426 = 0.149 (batimastat addition at day 9).

427 All statistical tests performed against the control population.

428



429

430 **Fig. S5 Quantifications of extension and proliferation dynamics in PDAC organoids.**

431 **(a)** Major axis length evolution of collagen-grown organoids over time with linear fits

432 highlighting the different phases (blue: Onset, orange: Extension, green: Thickening, pink:

433 Post-thickening; $n = 71$ organoids).

434 **(b)** Mean branch extension rate distribution between day 7 and 10 (n = 51 branches).

435 **(c)** X (blue) and Y (green) positions for cells in an extending branch, representative of the
436 dominant extension behavior between day 7 and 10.

437 **(d)** Correlation between branching and proliferation events in the leading 6 cells of a branch
438 tip between day 7 and 10. True-Yes: branching event was preceded by a proliferation event.
439 True-No: branching event occurred without being preceded by a proliferation event. False-
440 Yes: proliferation event occurred but a branching event did not follow (n = 30 events, N = 4
441 organoids).

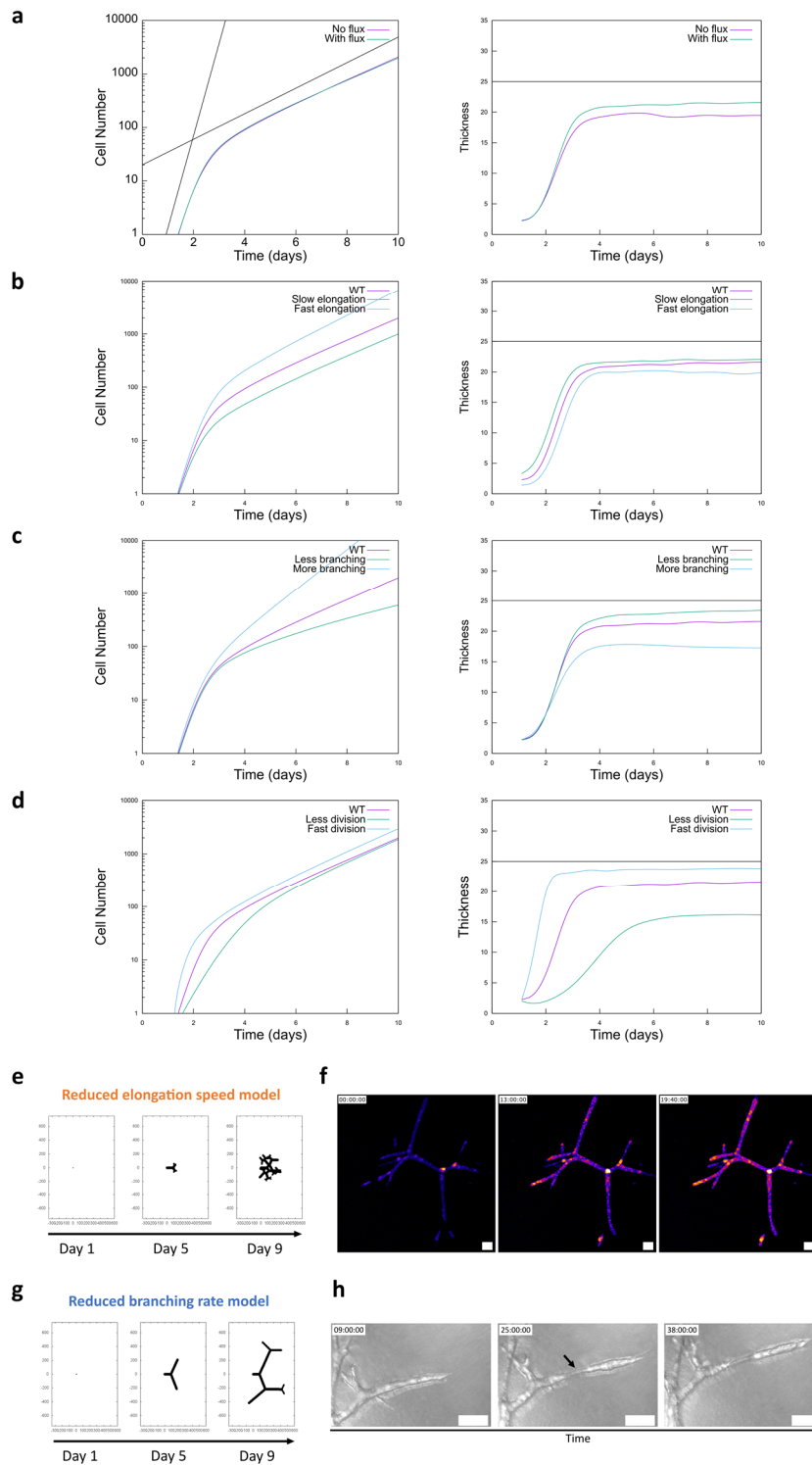
442 **(e)** Complementary empirical cumulative distribution function of non-terminal branch lengths
443 for organoids at day 7-10 (blue dots, n = 151 branches, N = 4 organoids) and fitted curve for
444 an exponential distribution (dashed orange line).

445 **(f)** DAPI (blue) and Ki67-positive (green) cell numbers estimated from maximum projections
446 using manual or semi-automated counting, at day 3, 5, 7, 9, 11, and 13 (n = 24 organoids).

447 **(g)** Instantaneous branch tip speed versus branch width for untreated (WT, blue, n = 103
448 points, N = 3 organoids), batimastat- (orange, n = 142 points, N = 2 organoids), and
449 aphidicolin-treated (green, n = 103 points, N = 3 organoids) organoids at the extension stage.

450 **(h)** Ki67-positive cells over DAPI-positive cells ratio for untreated, Y-27632-treated and
451 batimastat-treated organoids at day 7 and day 13, and representative stainings **(i)**. Bars: mean
452 \pm sem. Un-paired two-tailed parametric t test with Welch's correction; * P = 0.0116, ns P =
453 0.513 (day 7 control versus day 7 addition of Y-27632), P = 0.4632 (day 7 control versus day
454 7 addition of batimastat), P = 0.1201 (day 13 control versus day 13 addition of Y-27632).
455 Scale bar: 100 μ m. Day 7: control n = 4, batimastat n = 4, Y-27632 n = 5 organoids. Day 13:
456 control n = 7, batimastat n = 4, Y-27632 n = 6 organoids.

457



458

459 **Fig. S6. Additional simulations using the minimal biophysical model.**

460 (a-d) Model predictions of cell number evolution (left column) and of mean branch thickness
 461 evolution (right column), under different simulation parameters. Black lines in (a) are shown
 462 as a guide to the eye to indicate the initial exponential growth phase, before the plateauing.

463 Black lines in the right column graphs indicate the maximum width w_0 allowed by the growth
464 feedback, in absence of branching and elongation. Plots are averaged over $n=30$ simulations.

465 **(a)** With/without cell flux between branching point;

466 **(b)** With slower/faster elongation speeds compared to the WT parameters (elongation speed
467 respectively divided by 2 and multiplied by 2);

468 **(c)** With less/more branching comparing to the WT parameters (branching rate respectively
469 divided by 2 and multiplied by 2);

470 **(d)** With less/more division compared to the WT parameters (cell division rate respectively
471 divided by 2 and multiplied by 2).

472 **(e)** Spatial simulation of the branching process over time in pancreatic organoids using a
473 reduced branch elongation speed.

474 **(f)** Local thickness increase visualization in a D8-9 organoid upon addition of 10 μM
475 batimastat. The bright spots indicate areas of increasing thickness. The organoid does not
476 extend in size but thickens, as predicted qualitatively by the model.

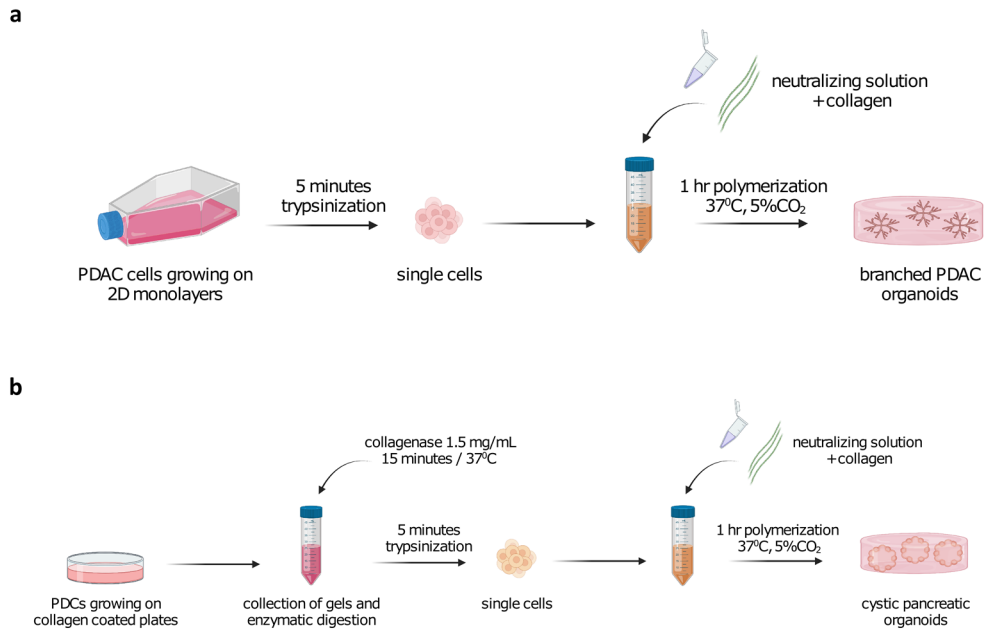
477 **(g)** Spatial simulation of the branching process over time in pancreatic organoids using a
478 reduced branching rate speed.

479 **(h)** Bright field time-lapse of an organoid branch upon addition of 2 $\mu\text{g.mL}^{-1}$ of aphidicolin at
480 D7. Black arrows indicate a spot of local branch thinning due continued cell migration but
481 inhibited proliferation, as predicted qualitatively by the model.

482 Scale bars in (f), (h): 100 μm .

483

484



485

486 **Fig. S7. Culture procedures for PDAC cells and pancreatic ductal cells.**

487 **(a)** Schematic representation of the PDAC culture procedure.

488 **(b)** Schematic representation of the pancreatic ductal cells (PDC) culture procedure.

489 These figures were created with BioRender.com

490

491

PDC Medium composition	Final Concentration	Manufacturer	Cat. Number
DMEM-F12	NA	ThermoFisher Scientific	31330-038
D-Glucose	5mg/mL	Sigma Aldrich	G8270
ITS premix	0.5%	Corning	354350
Dexamethasone	1 μ M	Sigma Aldrich	D1756
Cholera toxin	100 ng/mL	Sigma Aldrich	C8052
Penicillin/Streptomycin	1x	ThermoFisher Scientific	15140-122
Nu Serum	5%	Corning	355500
Bovine Pituitary Extract	25 μ g/mL	ThermoFisher Scientific	13028-014
Primocin	100 μ g/mL	InvivoGen	Ant-pm-1
EGF	20ng EGF	R&D systems	2028-EG
Nicotinamide	10 mM	Sigma Aldrich	N3376

492 **Table S1.** PDC medium composition

Epitope [Clone]	Conjugation	Host	Catalogue number	Supplier	Dilution
Phalloidin	Atto-647		65906	Sigma	1:250
E-cadherin [24E10]	Alexa-488	rabbit mAb (24E10)	3199	Cell Signaling	1:50
N-cadherin [13A9]	-	mouse mAb (13A9)	14215	Cell Signaling	1:100
Krt19	-	rat	Troma III	DSHB	1:100
Ki67	-	rabbit pAb	ab15580	Abcam	1:300
α 6 Integrin [GOH3]	-	rat mAb (GOH3)	Sc-19622	Santa Cruz Biotechnology	1:150
Laminin	-	rabbit pAb	L9393	Sigma	1:100
ZO-1 [ZO1-1A12]	Alexa-594	mouse mAb	339194	Invitrogen	1:100
α SMA [1A4 (asm-1)]	-	mouse mAb	MA5-11547	Thermo Fisher Scientific	1:100
Caspase 3	-	rabbit pAb	9662	Cell Signaling	1:100
Cytokeratin 7	-	rabbit mAb (EPR17078)	ab181598	Abcam	1:100

495 **Table S2.** List of primary antibodies used

Host/Isotype	Species reactivity	Conjugation	Catalogue number	Supplier	Dilution
Goat	Rat	Alexa 594	A11007	Thermo Fisher Scientific	1:250
Donkey	Rabbit	Alexa 546	A10040	Thermo Fisher Scientific	1:250
Goat	Mouse	Alexa 546	A11030	Thermo Fisher Scientific	1:250
Goat	Rabbit	Alexa 488	A11034	Thermo Fisher Scientific	1:250

497 **Table S3.** List of secondary antibodies used

498

499 **References**

- 500 1. Ranft, J. *et al.* Fluidization of tissues by cell division and apoptosis. *Proc. Natl. Acad. Sci.* **107**, 20863–
501 20868 (2010).
- 502 2. Montel, F. *et al.* Stress clamp experiments on multicellular tumor spheroids. *Phys. Rev. Lett.* **107**, 1–4
503 (2011).
- 504 3. Delarue, M. *et al.* Compressive Stress Inhibits Proliferation in Tumor Spheroids through a Volume
505 Limitation. *Biophys. J.* **107**, 1821–1828 (2014).
- 506 4. Delarue, M. *et al.* Self-driven jamming in growing microbial populations. *Nat. Phys.* **12**, 762–766
507 (2016).
- 508 5. Streichan, S. J., Hoerner, C. R., Schneidt, T., Holzer, D. & Hufnagel, L. Spatial constraints control cell
509 proliferation in tissues. *Proc. Natl. Acad. Sci.* **111**, 5586–5591 (2014).
- 510 6. Shraiman, B. I. Mechanical feedback as a possible regulator of tissue growth. *Proc. Natl. Acad. Sci. U. S.*
511 *A.* **102**, 3318–3323 (2005).
- 512 7. Basan, M., Risler, T., Joanny, J. F., Sastre-Garau, X. & Prost, J. Homeostatic competition drives tumor
513 growth and metastasis nucleation. *HFSP J.* **3**, 265–272 (2009).
- 514 8. Hannezo, E. *et al.* A Unifying Theory of Branching Morphogenesis. *Cell* **171**, 242-255.e27 (2017).
- 515 9. Hannezo, E. & Simons, B. D. Multiscale dynamics of branching morphogenesis. *Curr. Opin. Cell Biol.*
516 **60**, 99–105 (2019).
- 517 10. Clément, R., Douady, S. & Mauroy, B. Branching geometry induced by lung self-regulated growth.
518 *Phys. Biol.* **9**, (2012).
- 519 11. Reichert, M. *et al.* Isolation, culture and genetic manipulation of mouse pancreatic ductal cells. *Nat.*
520 *Protoc.* **8**, 1354–1365 (2013).

521