

Supporting Information:

Multiconfiguration Pair-Density Functional Theory for Chromium(IV) Molecular Qubits

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Date of finalization: August 15, 2022

1 Computational details of Kohn-Sham density functional calculations

Kohn-Sham density functional calculations were performed using ORCA^{S1,S2} version 5.0.

For the density functional calculations, we used the B3LYP,^{S3-S6} BP86,^{S3,S7} M06-L,^{S8,S9} M06,^{S9} M06-2X,^{S9} TPSS,^{S10-S12} PBE,^{S13} PBE0,^{S14,S15} and ω B97X^{S16} exchange-correlation functionals to calculate the axial (D) and rhombic (E) zero field splitting parameters (see example input file in Section S1) using the VASP-optimized geometry of complexes **1**, **2**, and

3. The def2-TZVP basis set^{S17} was used on all atoms. For the local exchange-correlation functionals, we used Split-RI-J, which is the default and recommended version of the resolution of identity^{S18-S23} approximation. For the hybrid exchange-correlation functionals, the RIJCOSX^{S19} approximation was used. Tight SCF convergence criteria were applied for all these density functional calculations. The coupled-perturbed method^{S24} was used for the spin-orbit coupling contribution to the D-tensor. Calculations were performed with both spin-orbit coupling and spin-spin coupling and with only spin-orbit coupling (Tables S1-S3 and Figures S1-S2).

1.1 Examples of ORCA input files (excluding coordinates)

Example using the BP86 functional

```
! UKS BP86 def2-TZVP RI def2/J decontractauxj TIGHTSCF
```

```
! SlowConv LargePrint PrintBasis MOREAD
```

```
%moinp "Cr_Toluene_VASP-BP86-DTensor.gbw"
```

```
%pal
```

```
nprocs 16
```

```
end
```

```
%maxcore 3000
```

```
%eprnmr
```

```
DTensor ssandso
```

```
DSOC cp
```

```
DSS uno
```

```
end
```

```
*xyz 0 3
```

Example using the B3LYP functional

```
! UKS B3LYP def2-TZVP RIJCOSX def2/J decontractauxj TIGHTSCF
! SlowConv LargePrint PrintBasis MOREAD
%moinp "Cr_Toluene_VASP-B3LYP-DTensor.gbwn"
```

```
%pal
```

```
nprocs 16
```

```
end
```

```
%maxcore 3000
```

```
%eprnmr
```

```
DTensor ssandso
```

```
DSOC cp
```

```
DSS uno
```

```
end
```

```
*xyz 0 3
```

Example of SA-CASSCF/NEVPT2 calculation

```
! DKH2 DKH-def2-TZVP RIJCOSX def2/j def2-tzvp/c decontractauxj decontractauxc
! LargePrint PrintBasis MOREAD
%moinp "Cr-Toluene-VASP-2in5-NEV_decontractauxc.gbwn"
```

```
%casscf
```

```
nel 2
```

```
norb 5
```

```
mult 3,1
nroots 10,15
printf det
trafostep ri
ptmethod sc_nevpt2
rel
dosoc true
dosscc true
gtensor true
end
end

%pal
nprocs 16
end

%maxcore 3000

*xyz 0 3
```

1.2 Examples of OpenMolcas input files (excluding coordinates)

```
&GATEWAY
RICD
COORD = Cr_Toluene_opt.xyz
group = nosym
basis = Cr.ANO-RCC-VTZP, C.ANO-RCC-VDZ, H.ANO-RCC-VDZ
End of Input
```

&SEWARD

End Of Input

>>COPY \$CurrDir/cas2-5_tol_opt_triplet.RasOrb INPORB

&RASSCF

Lumorb

Symmetry = 1

Spin = 3

NACTEL = 2 0 0

CHARGE = 0

RAS2 = 5

CIRROOT = 10 10 1

ORBListing

ALL

ORBAppear

COMPACT

ITERations = 200 100; CIMX = 500

Sdav = 200; PRWF = 0.01

End of Input

>>COPY \$WorkDir/\$Project.RasOrb \$CurrDir/\$Project.RasOrb

>>COPY \$CurrDir/\$Project.RasOrb INPORB

&MCPDFT

KSDFT = tPBE

NOGRADIENT

&CASPT2

NoMult

MULTistate

10 1 2 3 4 5 6 7 8 9 10

Imag = 0.3

MAXIter = 100

IPEA = 0.25

End Of Input

1.3 Energy gaps by Kohn-Sham density functional theory

Table S1: Calculated triplet-singlet gaps using the optimized **1** structure by Kohn-Sham density functional calculations with various exchange-correlation functionals

	ΔE_{T-S} (eV)	ΔE_{T-S} (cm ⁻¹)*
B3LYP	1.64	13 216.7
BP86	1.46	11 759.7
M06	1.93	15 557.8
M06-2X	1.86	14 993.3
M06-L	1.81	14 578.7
PBE	1.45	11 728.8
PBE0	1.83	14 744.3
TPSS	1.52	12 259.2
ω B97X	1.71	13 792.1
Experiment	1.20	9 678.6

*1 eV = 8 065.54 cm⁻¹.

Table S2: Calculated triplet-singlet gaps using the optimized **2** structure by Kohn–Sham density functional calculations with various exchange-correlation functionals

	ΔE_{T-S} (eV)	ΔE_{T-S} (cm ⁻¹)*
B3LYP	1.73	13 918.2
BP86	1.48	11 955.5
M06	1.93	15 586.1
M06-2X	1.98	15 966.5
M06-L	1.81	14 596.1
PBE	1.48	11 900.0
PBE0	1.92	15 466.8
TPSS	1.56	12 571.7
ω B97X	1.81	14 627.4
Experiment	1.22	9 839.9

*1 eV = 8 065.54 cm⁻¹.

Table S3: Calculated triplet-singlet gaps using the optimized **3** structure by Kohn–Sham density functional calculations with various exchange-correlation functionals

	ΔE_{T-S} (eV)	ΔE_{T-S} (cm ⁻¹)*
B3LYP	1.74	13 999.4
BP86	1.43	11 503.5
M06	1.80	14 553.8
M06-2X	2.01	16 175.7
M06-L	1.79	14 406.3
PBE	1.42	11 423.4
PBE0	1.93	15 565.0
TPSS	1.51	12 216.6
ω B97X	1.84	14 849.7
Experiment	1.20	9 678.6

*1 eV = 8 065.54 cm⁻¹.

1.4 Zero-field splitting parameters by Kohn-Sham density functional theory

Table S4: Calculated absolute values (in GHz) for the axial (D) and rhombic (E) zero-field splitting parameters by Kohn–Sham density functional calculations at the VASP-optimized **1** structure

	D (GHz)	E (GHz)	D (cm ⁻¹)	E (cm ⁻¹)
B3LYP	5.49	0.05	0.183	0.002
BP86	7.03	0.00	0.234	0.000
M06	4.08	0.04	0.136	0.001
M06-2X	4.08	0.07	0.136	0.002
M06-L	2.42	0.00	0.081	0.000
PBE	7.22	0.01	0.241	0.000
PBE0	5.09	0.07	0.170	0.002
TPSS	5.96	0.07	0.199	0.002
ω B97X	5.27	0.50	0.176	0.017
Experiment	3.53	0.00	0.118	0.000

* 1 cm⁻¹ = 29.9792 GHz.

Table S5: Calculated absolute values (in GHz) for the axial (D) and rhombic (E) zero-field splitting parameters by Kohn–Sham density functional calculations at the VASP-optimized **2** structure

	D (GHz)	E (GHz)	D (cm ⁻¹)	E (cm ⁻¹)
B3LYP	3.19	0.52	0.106	0.017
BP86	4.74	0.49	0.158	0.016
M06	2.50	0.13	0.083	0.004
M06-2X	1.88	0.15	0.063	0.005
M06-L	3.36	0.36	0.112	0.012
PBE	4.91	0.39	0.164	0.013
PBE0	2.73	0.49	0.091	0.016
TPSS	4.31	0.38	0.144	0.013
ω B97X	2.24	0.51	0.075	0.017
Experiment	1.92	0.53	0.064	0.018

* 1 cm⁻¹ = 29.9792 GHz.

Table S6: Calculated absolute values (in GHz) for the axial (D) and rhombic (E) zero-field splitting parameters by Kohn–Sham density functional calculations at the VASP-optimized **3** structure

	D (GHz)	E (GHz)	D (cm ⁻¹)	E (cm ⁻¹)
B3LYP	1.14	0.06	0.038	0.002
BP86	2.52	0.09	0.084	0.003
M06	4.11	0.21	0.137	0.007
M06-2X	4.14	0.30	0.138	0.010
M06-L	1.23	0.11	0.041	0.004
PBE	2.38	0.07	0.079	0.002
PBE0	0.73	0.01	0.024	0.000
TPSS	2.30	0.10	0.077	0.003
ω B97X	0.76	0.05	0.025	0.002
Experiment	4.19	0.48	0.140	0.016

* 1 cm⁻¹ = 29.9792 GHz.

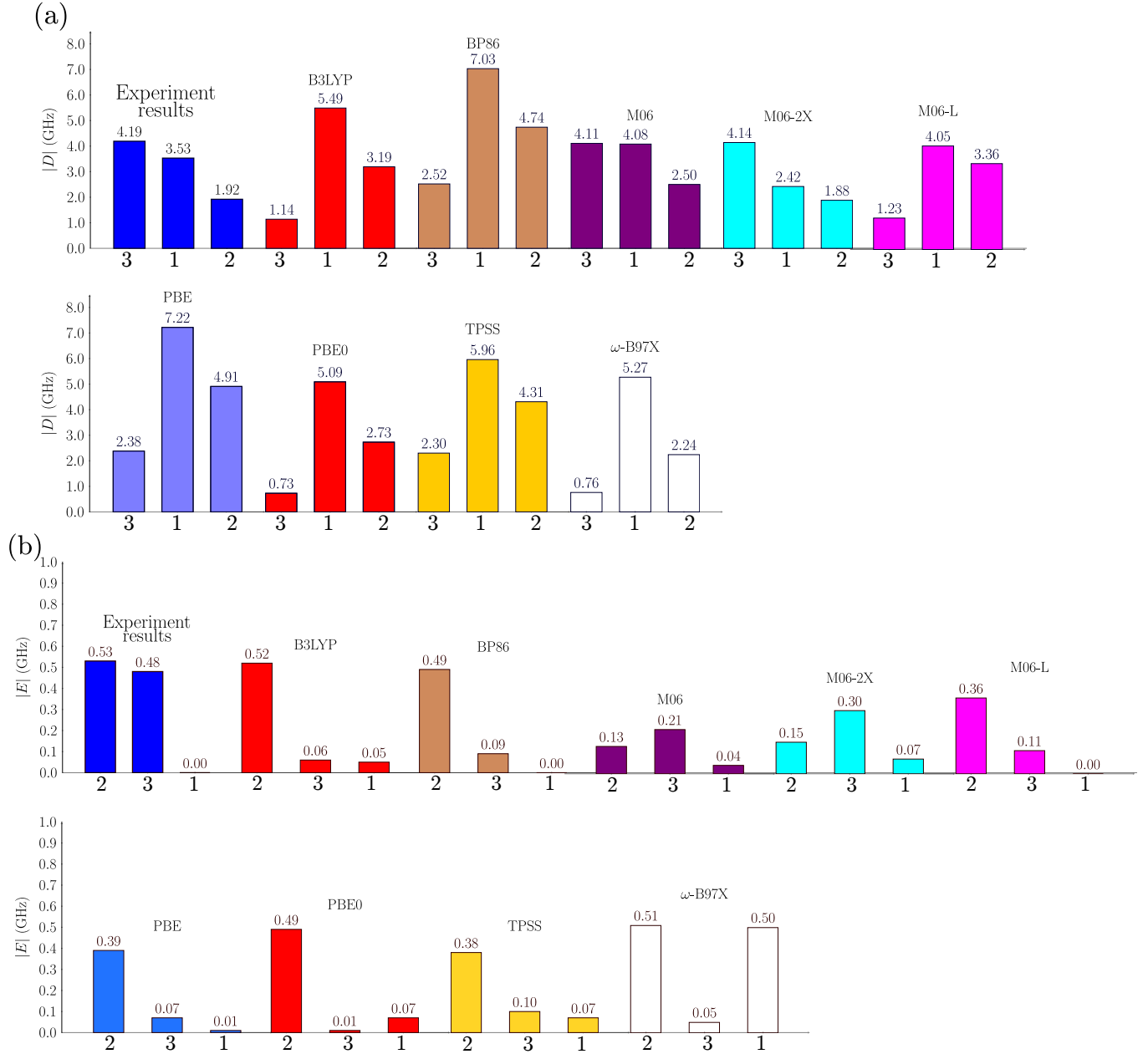


Figure S1: Experimental and calculated values (in GHz) of (a) the axial parameter $|D|$, (b) the rhombic parameter $|E|$. The blue bars are the experimental findings, and the other bars are the computational data using the VASP optimized structure and the B3LYP, BP86, M06, M06-2X, M06-L, PBE, PBE0, TPSS, and ω -B97X exchange-correlation functionals in Kohn-Sham density functional calculations with the def2-TZVP basis set.

1.5 Zero-field splitting by by ORCA SA-CASSCF and NEVPT2 calculations

Table S7: Absolute values (in GHz) for the axial zero-field splitting parameter (D) calculated with SA-CASSCF and NEVPT2, for the experimental and optimized geometries.

Experimental structure					
	SA-CASSCF	SA-CASSCF*	NEVPT2	NEVPT2*	Experiment
1	9.93	10.00	5.37	5.53	3.53
2	2.74	3.14	4.46	4.48	1.92
3	5.12	5.23	1.96	2.11	4.19
VASP optimized structure					
	SA-CASSCF	SA-CASSCF*	NEVPT2	NEVPT2*	Experiment
1	10.65	10.73	3.06	3.18	3.53
2	1.08	1.22	0.48	0.64	1.92
3	4.14	4.23	0.77	0.86	4.19

* Indicates that in addition to spin-orbit coupling, spin-spin coupling was included in the calculation.

Table S8: Absolute values (in GHz) for the rhombic zero-field splitting parameter (E) calculated with SA-CASSCF and NEVPT2, for the experimental and optimized geometries.

Experimental structure					
	SA-CASSCF	SA-CASSCF*	NEVPT2	NEVPT2*	Experiment
1	0.28	0.70	1.43	1.83	0.00
2	0.37	0.46	0.65	0.92	0.53
3	0.82	0.86	0.13	0.16	0.48
VASP optimized structure					
	SA-CASSCF	SA-CASSCF*	NEVPT2	NEVPT2*	Experiment
1	0.01	0.01	0.01	0.01	0.00
2	0.32	0.34	0.13	0.18	0.53
3	1.02	1.06	0.21	0.22	0.48

* Indicates that in addition to spin-orbit coupling, spin-spin coupling was included in the calculation.

SA-CASSCF/NEVPT2 (2e, 5o); 10 Triplets, 15 Singlets

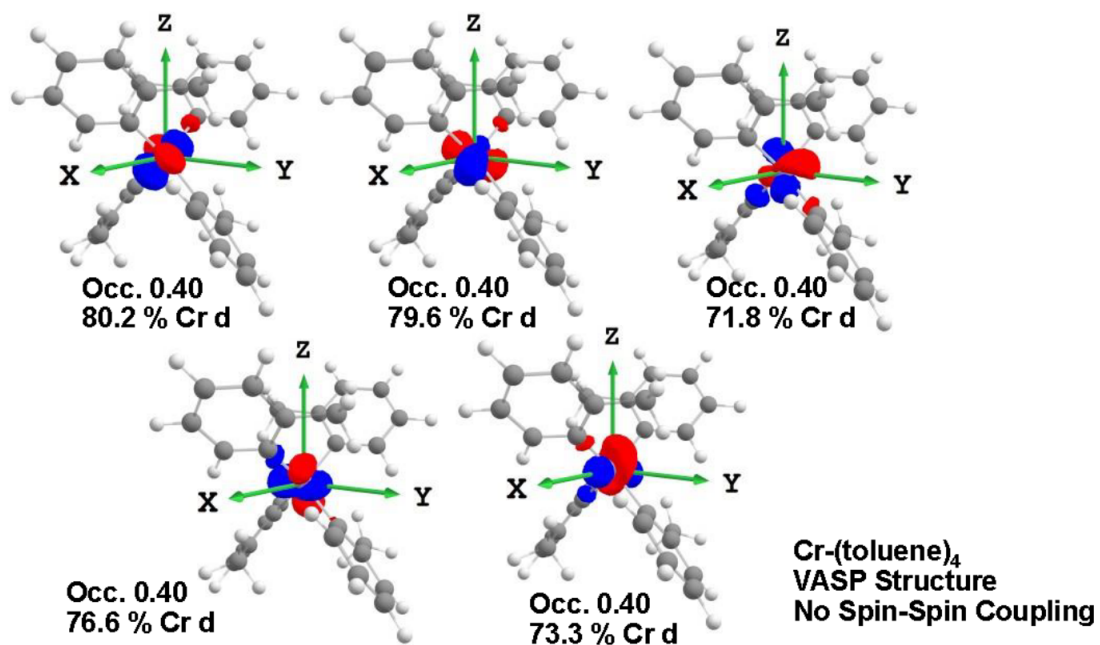


Figure S2: Representative active orbitals used in SA-CASSCF(2,5)/NEVPT2 calculations.

2 Structures

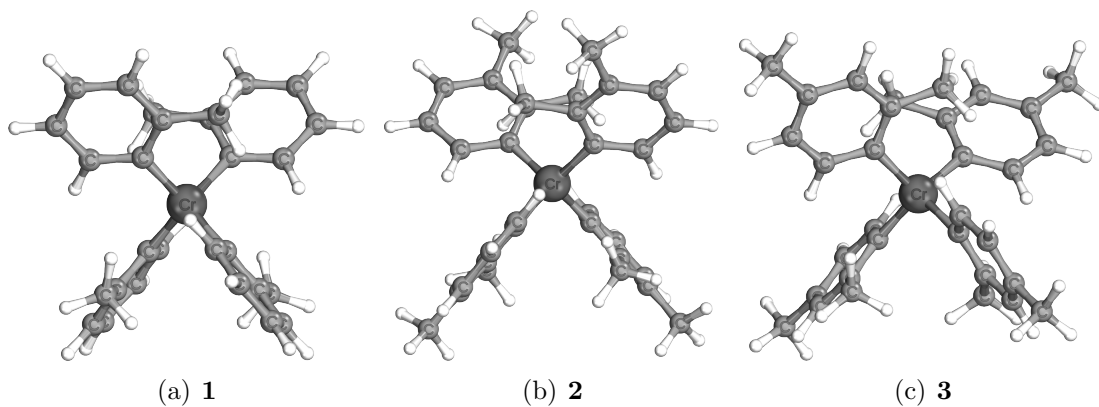
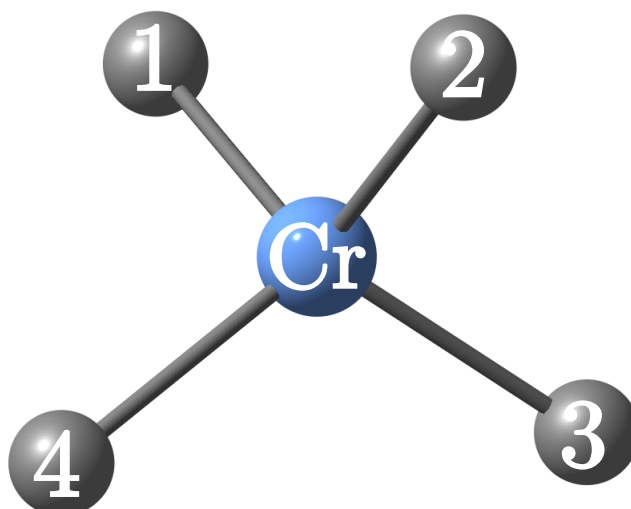
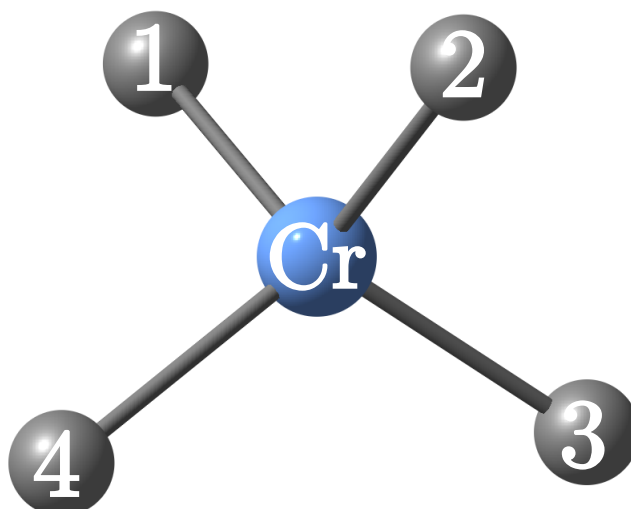


Figure S3: Molecular structures of the optimized Cr(IV) aryl complexes studied in this article.



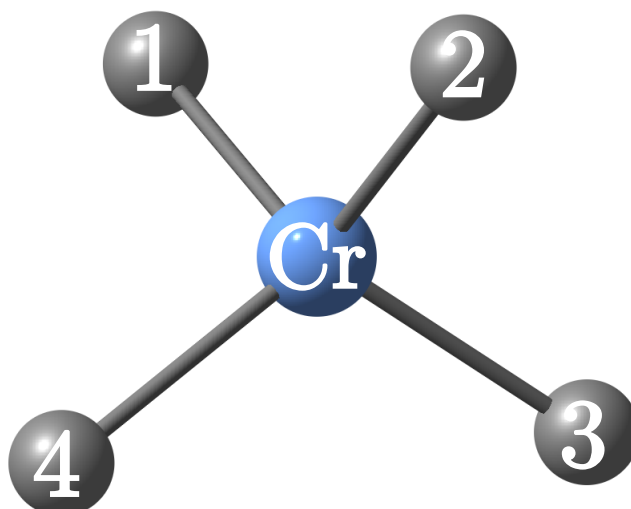
Bond distances					
Atoms	Unit Cell	Opt. Geom. (Å)	Expt. Geom. (Å)	Gas-Phase	Opt. Geom. (Å)
Cr-1		1.97	2.00		1.98
Cr-2		1.97	1.99		1.98
Cr-3		1.97	1.98		1.98
Cr-4		1.97	1.99		1.98
Bond angles					
Atoms	Unit Cell	Opt. Geom. (deg)	Expt. Geom. (deg)	Gas-Phase	Opt. Geom. (deg)
1-Cr-2		102.4	102.4		104.8
1-Cr-3		113.2	113.5		111.8
1-Cr-4		113.2	110.9		111.8
2-Cr-3		113.2	111.9		111.8
2-Cr-4		113.2	113.3		111.9
3-Cr-4		102.3	105.1		104.8

Figure S4: Geometrical data for molecule **1** optimized and experimental structures.



Bond distances					
Atoms	Unit Cell	Opt. Geom. (Å)	Expt. Geom. (Å)	Gas-Phase	Opt. Geom. (Å)
Cr-1		1.98	2.02		1.98
Cr-2		1.98	2.02		1.98
Cr-3		1.98	2.00		1.98
Cr-4		1.98	2.00		1.98
Bond angles					
Atoms	Unit Cell	Opt. Geom. (deg)	Expt. Geom. (deg)	Gas-Phase	Opt. Geom. (deg)
1-Cr-2		107.9	107.8		104.5
1-Cr-3		110.4	110.4		111.9
1-Cr-4		109.5	109.6		112.0
2-Cr-3		109.5	109.6		111.9
2-Cr-4		110.4	110.4		112.0
3-Cr-4		109.2	109.2		104.5

Figure S5: Geometrical data for molecule **2** optimized and experimental structures.



Bond distances					
Atoms	Unit Cell	Opt. Geom. (Å)	Expt. Geom. (Å)	Gas-Phase	Opt. Geom. (Å)
Cr-1		1.98	2.00		1.98
Cr-2		1.98	1.99		1.98
Cr-3		1.97	2.00		1.97
Cr-4		1.97	1.99		1.97
Bond angles					
Atoms	Unit Cell	Opt. Geom. (deg)	Expt. Geom. (deg)	Gas-Phase	Opt. Geom. (deg)
1-Cr-2		109.1	109.3		104.3
1-Cr-3		109.2	109.1		111.8
1-Cr-4		109.7	110.6		112.0
2-Cr-3		111.1	109.7		112.5
2-Cr-4		109.3	109.1		112.3
3-Cr-4		108.5	109.0		104.2

Figure S6: Geometrical data for molecule **3** optimized and experimental structures.

3 Active spaces

In the following figures are shown the molecular orbitals used for each of the complexes in each active space.

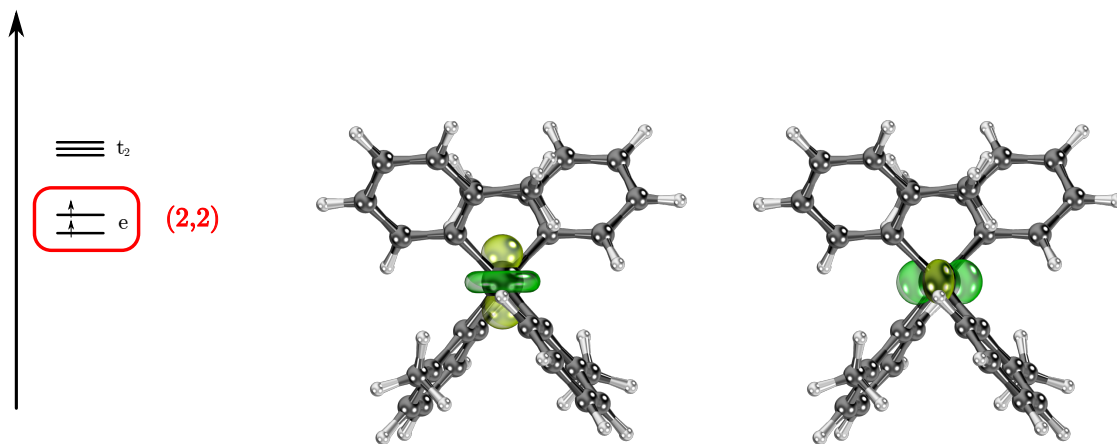


Figure S7: Molecular orbitals in the (2,2) active space of complex **1**.

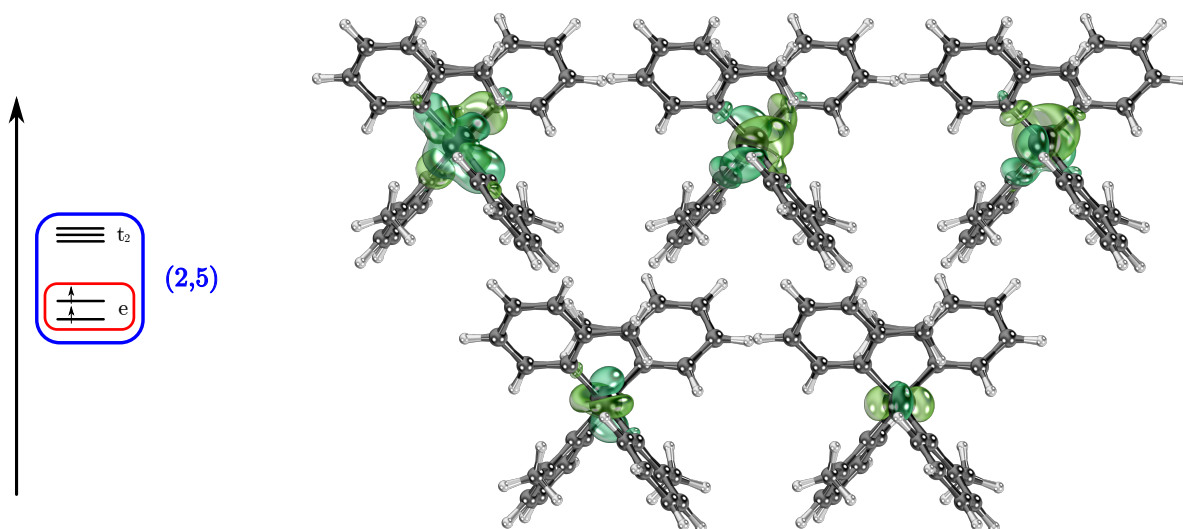


Figure S8: Molecular orbitals in the (2,5) active space of complex **1**.

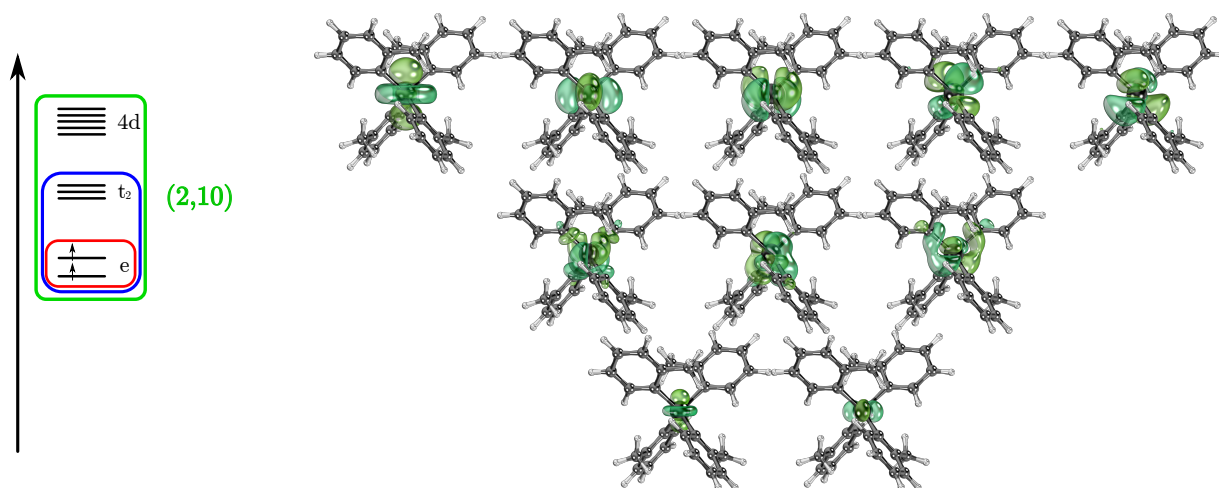


Figure S9: Molecular orbitals in the (2,10) active space of complex **1**.

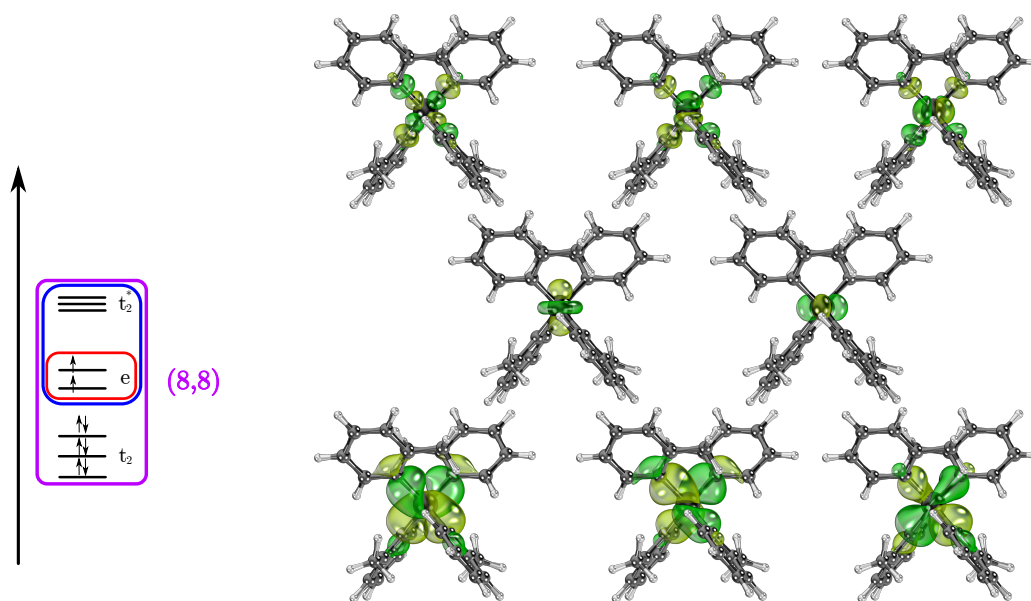


Figure S10: Molecular orbitals in the (8,8) active space of complex **1**.

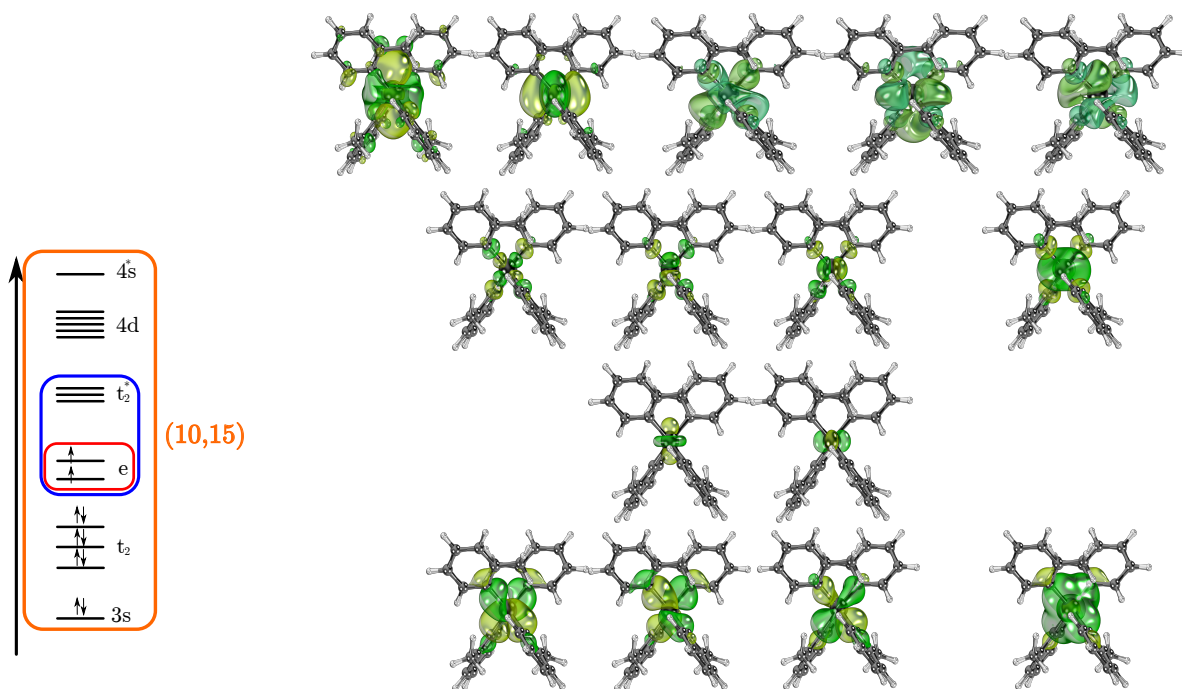


Figure S11: Molecular orbitals in the (10,15) active space of complex **1**.

4 Energy gaps (ΔE_{T-S})

The energy difference between the triplet ground-state and the first excited state (a singlet) for the chromium(IV) complexes using the five active spaces considered in this research are given in the following tables.

Table S9: Calculated triplet-singlet gaps (ΔE_{T-S}) in eV and cm^{-1} inside the parenthesis, using the unit cell optimized triplet structure of molecule **1**, the experimental structure, and gas-phase optimized triplet and singlet structures. The energy gaps were obtained with SA-CASSCF, MS-CASPT2, tPBE and tPBE0 methods.

Periodic optimized geometry					
Active space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2, 2)	1.87(14 254.7)	1.23(9 778.6)	0.55(5 110.2)	0.88(7 396.3)	
(2, 5)	1.89(15 218.6)	0.94(7 606.5)	0.48(3 831.2)	0.83(6 678.1)	
(2, 10)	1.81(14 634.1)	0.98(7 902.4)	0.51(4 096.8)	0.83(6 731.1)	
(8, 8)	1.83(15 561.1)	1.41(11 592.9)	0.94(7 407.4)	1.16(9 445.8)	
(10, 15)	1.66(13 388.8)	1.41(11 353.5)	1.02(8 226.9)	1.18(9 517.3)	1.20(9 678.6)
Experimental geometry					
Active space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2,2)	1.75(14 105.3)	1.20(9 697.0)	0.64(5 201.2)	0.92(7 427.2)	
(2,5)	1.89(15 212.6)	0.92(7 418.6)	0.49(3 927.5)	0.84(6 748.8)	
(2,10)	1.81(14 620.7)	0.97(7 800.1)	0.52(4 174.4)	0.98(7 882.2)	
(8,8)	1.83(14 740.9)	1.43(11 565.9)	0.97(7 792.9)	1.18(9 529.9)	
(10,15)	1.49(12 018.3)	1.51(12 190.5)	1.15(9 315.8)	1.24(9 991.4)	1.20(9 678.6)
Gas-phase optimized geometry					
Active space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2, 2)	1.94(15 656.5)	1.02(8 261.3)	0.41(3 272.9)	0.79(6 368.8)	
(2, 5)	1.90(15 348.3)	0.98(7 905.2)	0.48(3 906.1)	0.84(6 766.6)	
(2, 10)	1.83(14 776.3)	1.01(8 181.1)	0.52(4 174.7)	0.85(6 825.1)	
(8, 8)	1.85(14 952.6)	1.44(11 604.2)	0.94(7 594.5)	1.17(9 434.0)	
(10, 15)	1.68(13 574.4)	1.43(11 532.2)	1.04(8 393.6)	1.20(9 688.8)	1.20(9 678.6)

1 eV = 8 065.54 cm^{-1} .

Table S10: Calculated triplet-singlet gaps (ΔE_{T-S}) in eV and cm^{-1} inside the parenthesis, using the unit cell optimized triplet structure of molecule **2**, the experimental structure, and gas-phase optimized triplet and singlet structures. The energy gaps were obtained with SA-CASSCF, MS-CASPT2, tPBE and tPBE0 methods.

Periodic optimized geometry					
Active Space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2, 2)	1.85(14 940.4)	1.20(9 709.1)	0.59(4 770.7)	0.91(7 313.1)	
(2, 5)	1.93(15 013.7)	1.03(9 834.3)	0.48(4 863.5)	0.84(7 401.0)	
(2, 10)	1.86(14 989.6)	1.06(8 554.8)	0.52(4 200.9)	0.86(6 898.1)	
(8, 8)	1.92(15 466.6)	1.43(11 533.3)	0.93(7 536.7)	1.18(9 519.2)	
(10, 15)	1.74(14 069.0)	1.42(11 419.2)	0.94(7 560.4)	1.14(9 187.6)	1.22(9 840.0)
Experimental geometry					
Active Space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2,2)	1.86(15 140.7)	1.22(9 904.4)	0.60(4 840.3)	0.92(7 415.4)	
(2,5)	1.94(15 550.7)	1.04(8 276.4)	0.49(3 873.9)	0.86(6 793.1)	
(2,10)	1.87(15 081.8)	1.08(8 673.8)	0.53(4 312.0)	0.87(7 004.4)	
(8,8)	1.89(15 283.5)	1.47(11 871.3)	0.96(7 778.5)	1.20(9 654.7)	
(10,15)	1.64(13 244.8)	1.52(12 279.4)	1.13(9 134.9)	1.26(10 162.4)	1.22(9 840.0)
Gas-phase optimized geometry					
Active space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2, 2)	1.94(15 676.7)	1.02(8 216.1)	0.41(3 295.8)	0.79(6 391.1)	
(2, 5)	1.91(15 394.5)	0.98(7 909.3)	0.49(3 923.5)	0.84(6 791.2)	
(2, 10)	1.84(14 820.5)	1.02(8 216.1)	0.52(4 199.9)	0.85(6 855.0)	
(8, 8)	1.86(14 978.7)	1.45(11 681.3)	0.95(7 665.6)	1.18(9 493.9)	
(10, 15)	1.69(13 656.7)	1.44(11 631.1)	1.05(8 471.4)	1.21(9 767.7)	1.22(9 840.0)

1 eV = 8 065.54 cm^{-1} .

Table S11: Calculated triplet-singlet gaps (ΔE_{T-S}) in eV and cm^{-1} inside the parenthesis, using the unit cell optimized triplet structure of molecule **3**, the experimental structure, and gas-phase optimized triplet and singlet structures. The energy gaps were obtained with SA-CASSCF, MS-CASPT2, tPBE and tPBE0 methods.

Periodic optimized geometry					
Active Space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2, 2)	1.87(15 074.6)	1.21(9 755.7)	0.59(4 791.9)	0.91(7 362.6)	
(2, 5)	1.93(15 539.5)	1.07(8 624.7)	0.47(3 798.5)	0.83(6 733.7)	
(2, 10)	1.86(14 991.9)	1.11(8 963.0)	0.51(4 143.3)	0.85(6 855.4)	
(8, 8)	1.89(15 222.7)	1.45(11 676.8)	0.92(7 406.6)	1.16(9 360.7)	
(10, 15)	1.76(14 168.5)	1.35(10 919.3)	0.93(7 514.6)	1.14(9 178.1)	1.20(9 678.6)
Experimental geometry					
Active Space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2,2)	1.88(15 140.7)	1.23(9 904.4)	0.60(4 840.3)	0.92(7 415.4)	
(2,5)	1.94(15 618.6)	1.08(8 728.6)	0.49(3 926.9)	0.85(6 849.8)	
(2,10)	1.87(15 073.7)	1.13(9 132.7)	0.53(4 312.0)	0.86(7 004.4)	
(8,8)	1.90(15 309.9)	1.47(11 839.8)	0.94(7 547.1)	1.18(9 487.8)	
(10,15)	1.56(12 615.7)	1.56(12 613.5)	1.16(9 361.1)	1.26(10 174.8)	1.20(9 678.6)
Gas-phase optimized geometry					
Active space	SA-CASSCF	MS-CASPT2	tPBE	tPBE0	Expt.
(2, 2)	1.93(15 563.6)	0.99(7 973.1)	0.40(3 226.9)	0.78(6 311.0)	
(2, 5)	1.89(15 259.9)	0.96(7 712.9)	0.48(3 868.7)	0.83(6 716.5)	
(2, 10)	1.82(14 681.8)	0.99(7 973.1)	0.51(4 129.5)	0.83(6 767.6)	
(8, 8)	1.84(14 869.9)	1.43(11 507.4)	0.94(7 586.2)	1.17(9 407.2)	
(10, 15)	1.68(13 511.0)	1.42(11 456.1)	1.03(8 333.6)	1.19(9 627.9)	1.20(9 678.6)

1 eV = 8 065.54 cm^{-1} .

5 MS-CASPT2 energy spectra

Calculated energy spectra of complexes **1**, **2**, and **3**, calculated with MS-CASPT2 method. The spectra is calculated for (2,5), (2,10), (8,8) and (10,15) active spaces.

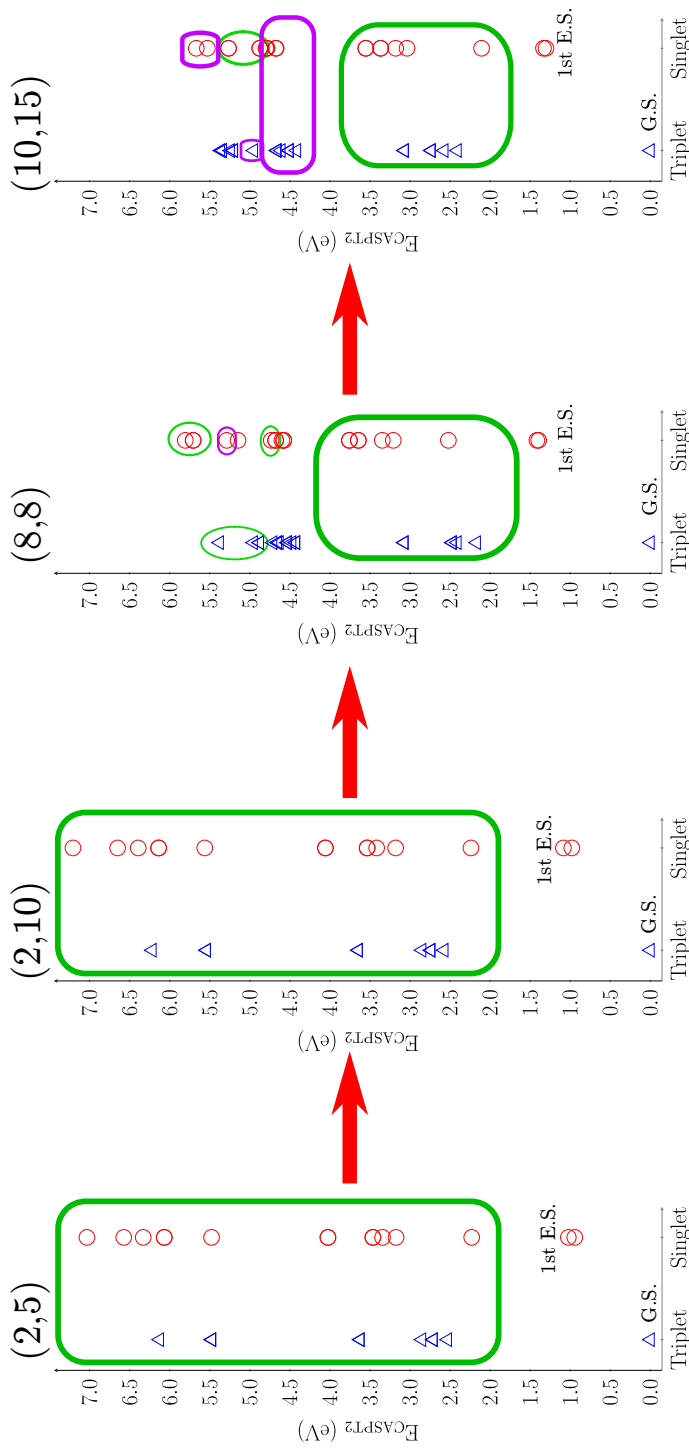


Figure S12: MS-CASPT2 energy plots of the complex **1** periodic optimized geometry. For (2,5) and (2,10) active spaces were computed 10 triplet and 15 singlet states, and 20 lowest-lying triplet and singlet states, each for (8,8), and (10,15) active spaces. The blue triangles correspond to triplet states, and the red circles are for singlet states. In green are highlighted the metal-to-ligand charge transfer states, in purple the ligand-to-metal charge transfer states, and for (8,8) and (10,15), the states without any color box are ligand-to-ligand charge transfer states.

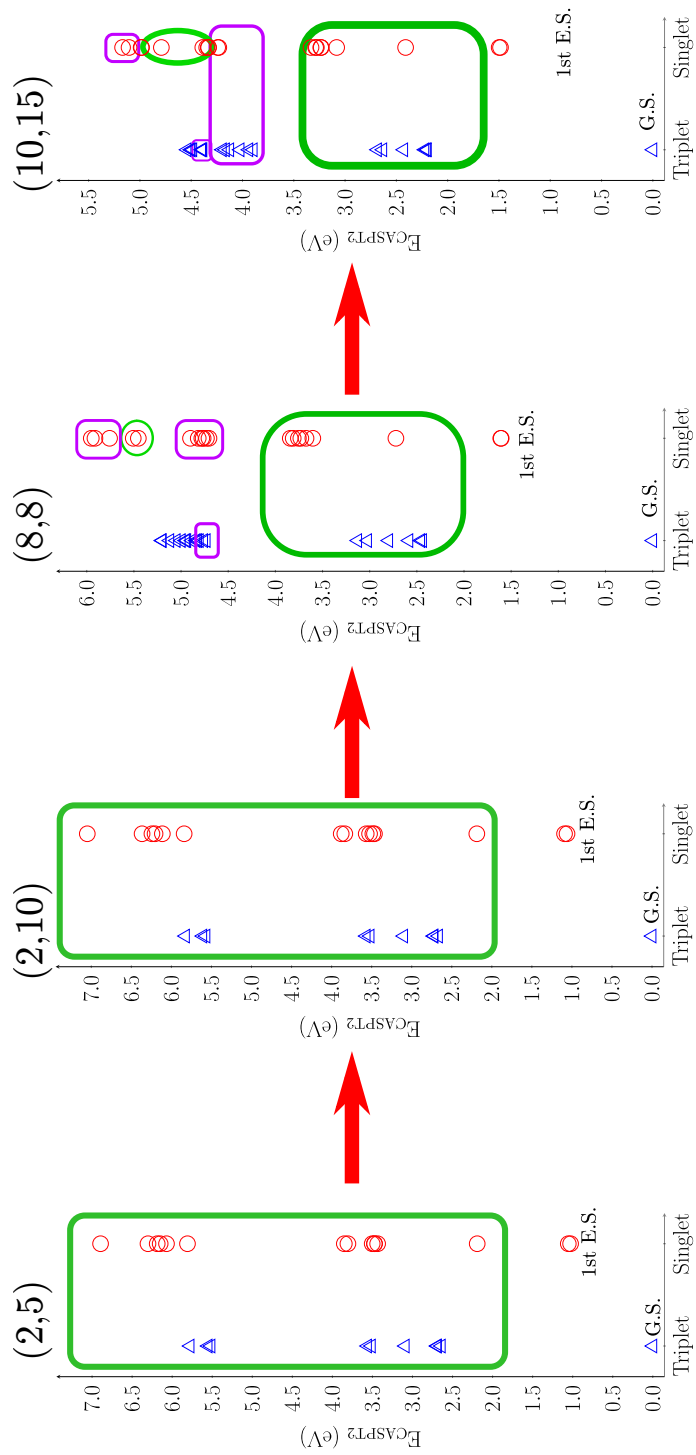


Figure S13: MS-CASPT2 energy plots of the complex **2** periodic optimized geometry. For (2,5) and (2,10) active spaces were computed 10 triplet and 15 singlet states, and 20 lowest-lying triplet and singlet states, each for (8,8), and (10,15) active spaces. The blue triangles correspond to triplet states, and the red circles are for singlet states. In green are highlighted the metal-to-ligand charge transfer states, in purple the ligand-to-metal charge transfer states, and for (8,8) and (10,15), the states without any color box are ligand-to-ligand charge transfer states.

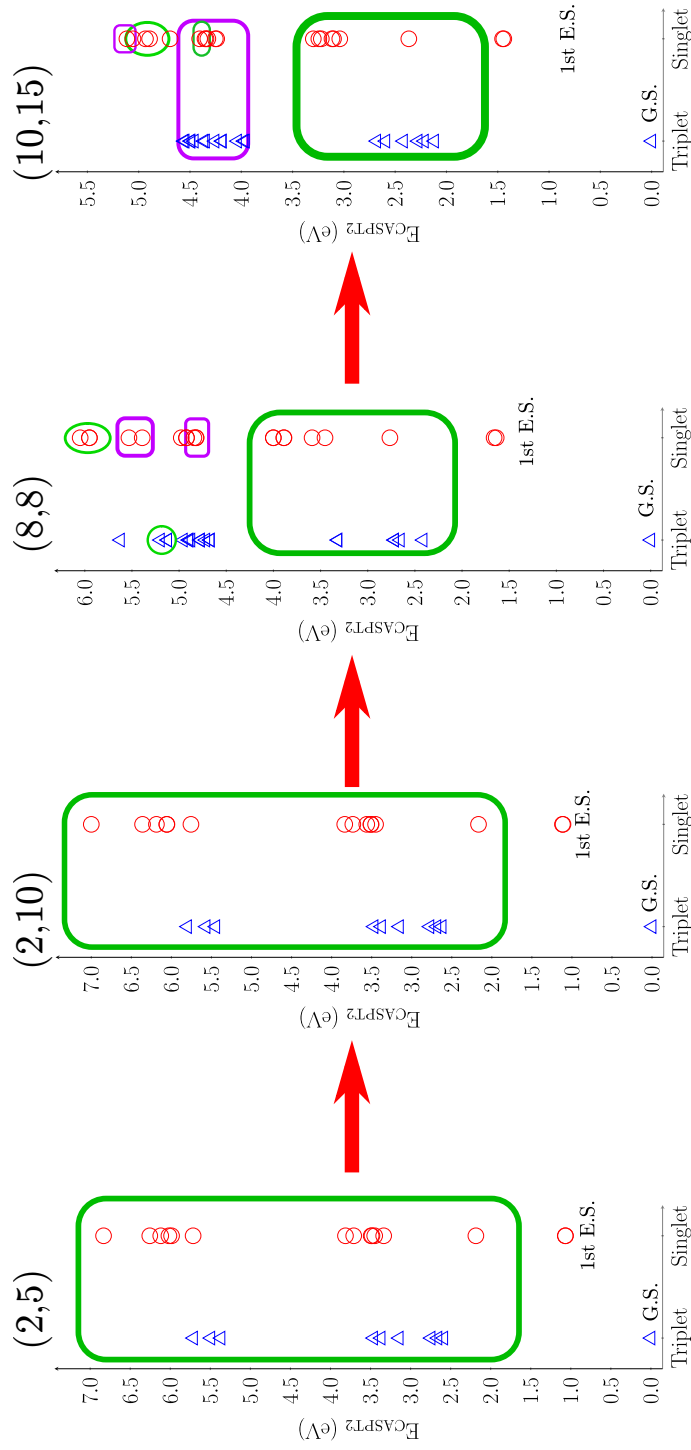


Figure S14: MS-CASPT2 energy plots of the complex **3** periodic optimized geometry. For (2,5) and (2,10) active spaces were computed 10 triplet and 15 singlet states, and 20 lowest-lying triplet and singlet states, each for (8,8), and (10,15) active spaces. The blue triangles correspond to triplet states, and the red circles are for singlet states. In green are highlighted the metal-to-ligand charge transfer states, in purple the ligand-to-metal charge transfer states, and for (8,8) and (10,15), the states without any color box are ligand-to-ligand charge transfer states.

6 HMC-PDFT energy spectra

Calculated energy spectra of complexes **1**, **2**, and **3**, calculated with HMC-PDFT(tPBE0) method. The spectra is calculated for (2,5), (2,10), (8,8) and (10,15) active spaces.

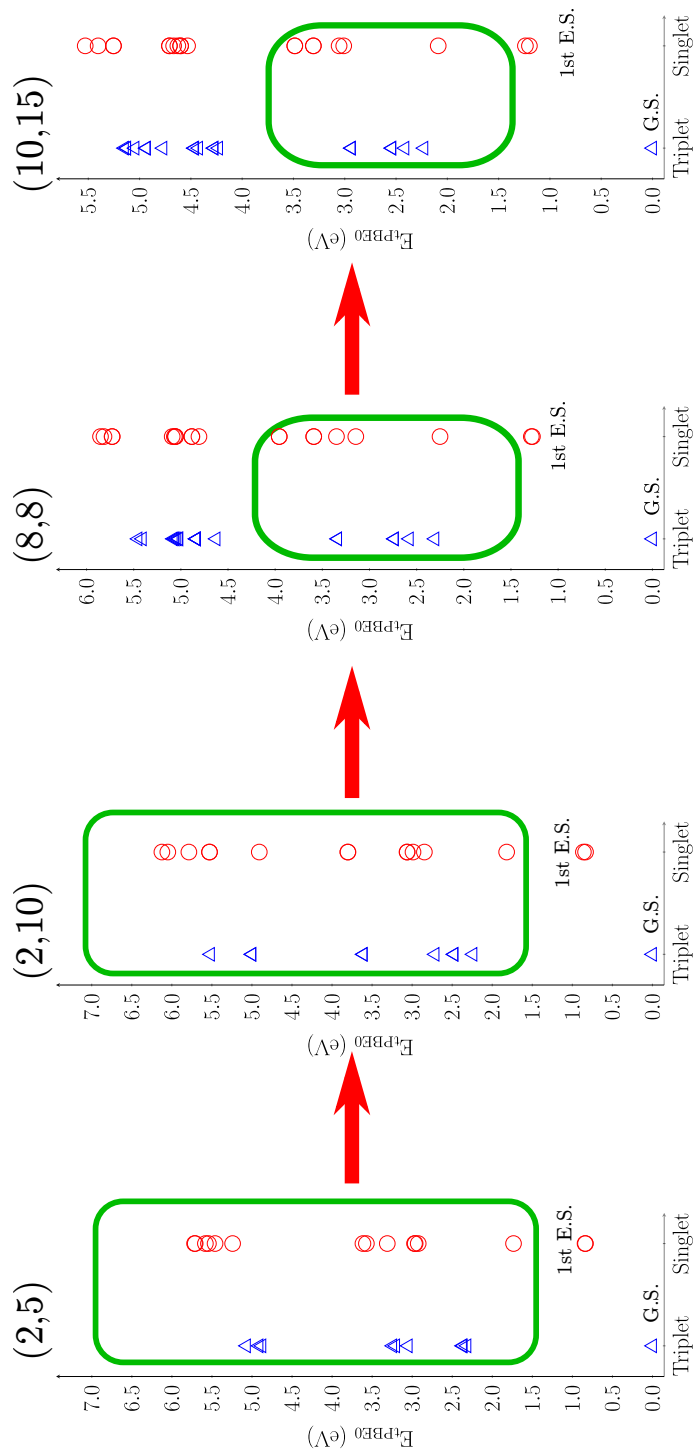


Figure S15: HMC-PDFT(tPBEO) energy plots of the complex **1** periodic optimized geometry. For (2,5) and (2,10) active spaces were computed 10 triplet and 15 singlet states, and 20 lowest-lying triplet and singlet states, each for (8,8), and (10,15) active spaces. The blue triangles correspond to triplet states, and the red circles are for singlet states. In green are highlighted the metal-to-ligand charge transfer states.

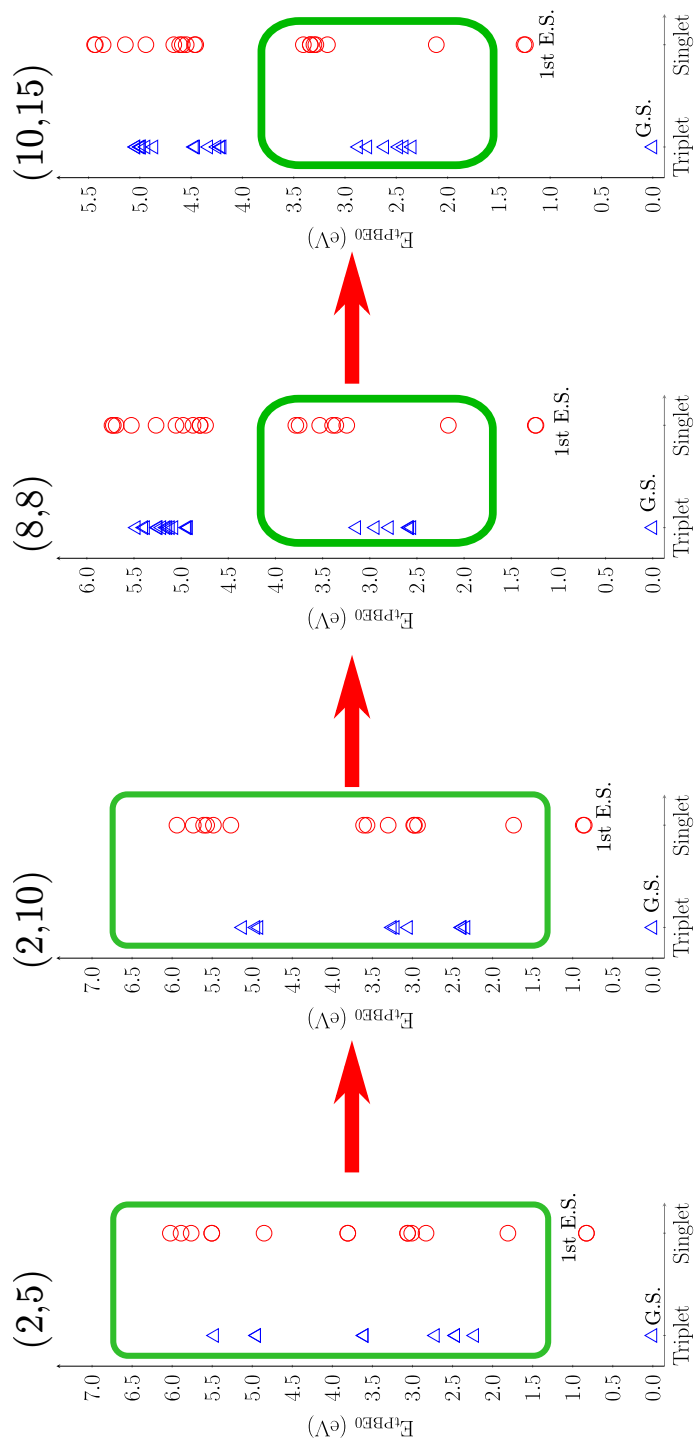


Figure S16: HMC-PDFT(tPBEO) energy plots of the complex **2** periodic optimized geometry. For (2,5) and (2,10) active spaces were computed 10 triplet and 15 singlet states, and 20 lowest-lying triplet and singlet states, each for (8,8), and (10,15) active spaces. The blue triangles correspond to triplet states, and the red circles are for singlet states. In green are highlighted the metal-to-ligand charge transfer states.

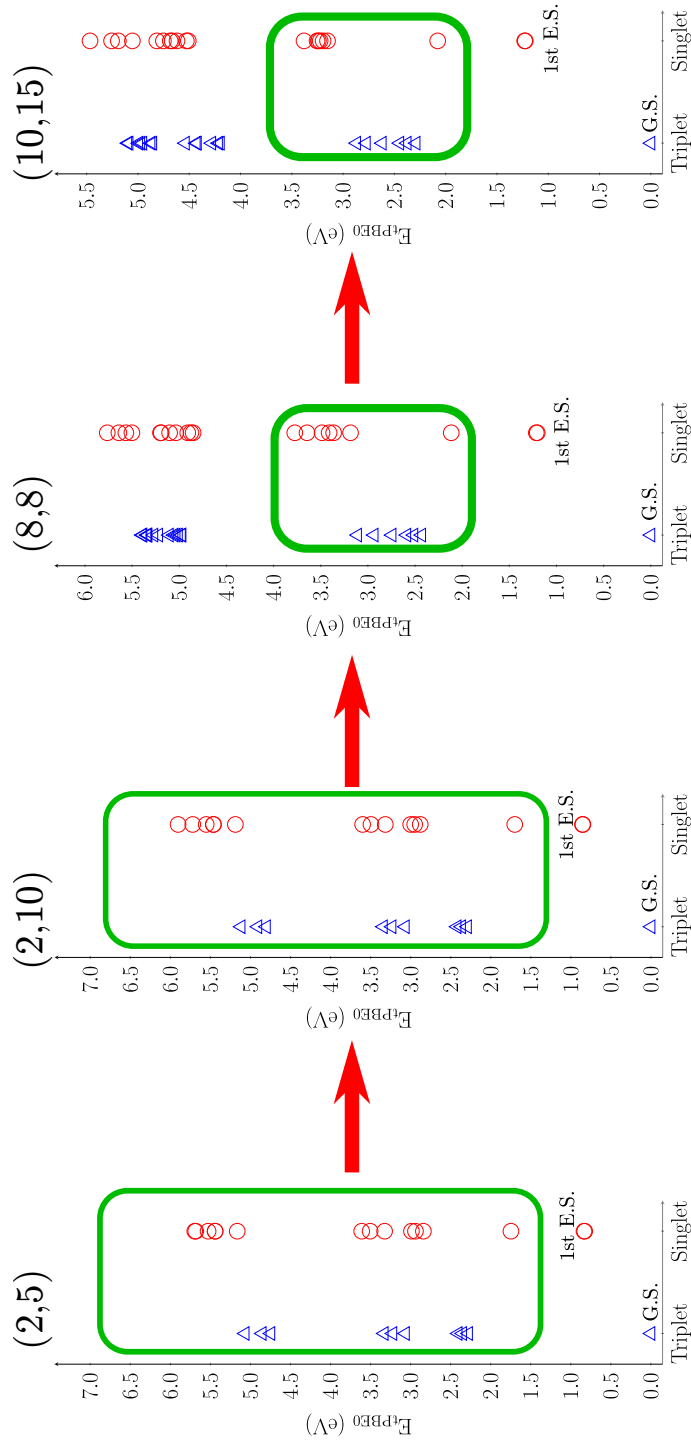


Figure S17: HMC-PDFT(tPBE0) energy plots of the complex **3** periodic optimized geometry. For (2,5) and (2,10) active spaces were computed 10 triplet and 15 singlet states, and 20 lowest-lying triplet and singlet states, each for (8,8), and (10,15) active spaces. The blue triangles correspond to triplet states, and the red circles are for singlet states. In green are highlighted the metal-to-ligand charge transfer states.

7 Zero-field splitting parameters

For complex **1**, the MS-CASPT2 calculation required almost 16 hours to compute the energy of the seven lowest-lying triplet states with (10,15) active space; in comparison the HMC-PDFT calculation required only 1.5 hours—this is a tenfold reduction in compute time as compared to MS-CASPT2.

Table S12: ZFS parameters calculated with the (2,5) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **1**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		10T-15S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	11.27(0.376)	0.00(0.000)	11.33(0.378)	0.00(0.000)	3.53(0.118)	0.00(0.000)
MS-CASPT2	3.53(0.118)	0.01(0.000)	3.66(0.122)	0.01(0.000)		
tPBE	0.98(0.033)	0.00(0.000)	1.12(0.037)	0.00(0.000)		
tPBE0	3.59(0.120)	0.00(0.000)	3.71(0.124)	0.00(0.000)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S13: ZFS parameters calculated with the (2,10) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **1**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		10T-15S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	10.41(0.347)	0.00(0.000)	10.39(0.347)	0.00(0.000)	3.53(0.118)	0.00(0.000)
MS-CASPT2	2.73(0.091)	0.01(0.000)	2.80(0.093)	0.00(0.000)		
tPBE	2.59(0.086)	0.00(0.000)	0.92(0.031)	0.00(0.000)		
tPBE0	4.72(0.157)	0.00(0.000)	3.24(0.108)	0.00(0.000)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S14: ZFS parameters calculated with the (8,8) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **1**. The parameters were computed with SA-CASSCF, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		18T-16S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	6.27(0.209)	0.00(0.000)	5.98(0.199)	0.00(0.000)	3.53(0.118)	0.00(0.000)
MS-CASPT2	3.33(0.111)	0.00(0.000)	2.92(0.097)	0.00(0.000)		
tPBE	3.05(0.102)	0.00(0.000)	2.16(0.072)	0.00(0.000)		
tPBE0	4.26(0.142)	0.00(0.000)	3.49(0.116)	0.00(0.000)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S15: ZFS parameters calculated with the (10,15) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **1**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		13T-16S		16T-15S	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	4.48(0.149)	0.00(0.000)	4.07(0.136)	0.00(0.000)	2.65(0.088)	0.00(0.000)
MS-CASPT2	3.65(0.122)	0.00(0.000)	5.14(0.171)	0.00(0.000)	1.27(0.042)	0.00(0.000)
tPBE	0.73(0.024)	0.00(0.000)	1.21(0.040)	0.00(0.000)	0.32(0.011)	0.00(0.000)
tPBE0	2.07(0.069)	0.00(0.000)	2.28(0.076)	0.00(0.000)	0.78(0.026)	0.00(0.000)

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S16: ZFS parameters calculated with the (2,5) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **2**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		10T-15S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	1.22(0.041)	0.33(0.011)	1.00(0.033)	0.69(0.023)	1.92(0.064)	0.53(0.018)
MS-CASPT2	1.34(0.045)	0.32(0.011)	0.80(0.027)	0.07(0.002)		
tPBE	0.34(0.011)	0.28(0.009)	1.30(0.043)	0.27(0.009)		
tPBE0	0.59(0.020)	0.23(0.008)	0.85(0.028)	0.42(0.014)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S17: ZFS parameters calculated with the (2,10) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **2**. The parameters were computed with SA-CASSCF, CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		10T-15S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	1.24(0.041)	0.19(0.006)	0.97(0.032)	0.53(0.018)	1.92(0.064)	0.53(0.018)
MS-CASPT2	1.16(0.039)	0.20(0.007)	0.72(0.024)	0.10(0.003)		
tPBE	0.31(0.010)	0.25(0.008)	0.98(0.033)	0.26(0.009)		
tPBE0	0.61(0.020)	0.17(0.006)	0.68(0.023)	0.39(0.013)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S18: ZFS parameters calculated with the (8,8) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **2**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		17T-16S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	6.27(0.209)	0.31(0.010)	5.98(0.199)	0.45(0.015)	1.92(0.064)	0.53(0.018)
MS-CASPT2	3.33(0.111)	0.25(0.008)	2.92(0.097)	0.31(0.010)		
tPBE	3.05(0.102)	0.10(0.003)	2.16(0.072)	0.02(0.001)		
tPBE0	4.26(0.142)	0.04(0.001)	3.49(0.116)	0.12(0.004)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S19: ZFS parameters calculated with the (10,15) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **2**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		13T-16S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	1.14(0.038)	0.22(0.007)	2.00(0.067)	0.31(0.010)	1.92(0.064)	0.53(0.018)
MS-CASPT2	1.14(0.038)	0.36(0.012)	2.90(0.097)	0.42(0.014)		
tPBE	1.85(0.062)	0.22(0.007)	0.61(0.020)	0.16(0.005)		
tPBE0	0.81(0.027)	0.19(0.006)	0.82(0.027)	0.19(0.006)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S20: ZFS parameters calculated with the (2,5) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **3**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		10T-15S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	4.45(0.148)	1.15(0.038)	4.52(0.151)	1.20(0.040)	4.19(0.139)	0.48(0.016)
MS-CASPT2	2.72(0.091)	0.82(0.027)	1.65(0.055)	0.21(0.007)		
tPBE	1.30(0.043)	0.30(0.010)	3.55(0.118)	0.38(0.013)		
tPBE0	2.07(0.069)	0.62(0.021)	1.22(0.041)	0.31(0.010)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S21: ZFS parameters calculated with the (2,10) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **3**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		10T-15S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	4.25(0.142)	1.06(0.035)	4.17(0.139)	1.09(0.036)	4.19(0.139)	0.48(0.016)
MS-CASPT2	2.43(0.081)	0.76(0.025)	2.04(0.068)	0.55(0.018)		
tPBE	1.36(0.045)	0.41(0.014)	0.86(0.029)	0.04(0.001)		
tPBE0	2.11(0.070)	0.58(0.019)	1.52(0.051)	0.49(0.016)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S22: ZFS parameters calculated with the (8,8) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **3**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		15T-16S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	2.95(0.098)	0.46(0.015)	3.42(0.114)	0.66(0.022)	4.19(0.139)	0.48(0.016)
MS-CASPT2	2.69(0.090)	0.76(0.025)	2.50(0.083)	1.90(0.063)		
tPBE	1.76(0.059)	0.31(0.010)	3.65(0.122)	0.92(0.031)		
tPBE0	0.93(0.031)	0.20(0.007)	2.89(0.096)	0.94(0.031)		

$$1 \text{ GHz} = 29.9793 \text{ cm}^{-1}.$$

Table S23: ZFS parameters calculated with the (10,15) active space, using different numbers of triplets and singlets at the periodic optimized geometry of complex **3**. The parameters were computed with SA-CASSCF, MS-CASPT2, MS-PDFT(tPBE), and HMS-PDFT(tPBE0). The values are reported in GHz, and cm^{-1} inside the parenthesis.

Method	7T-9S		13T-16S		Experiment	
	$ D $	$ E $	$ D $	$ E $	$ D $	$ E $
SA-CASSCF	2.43(0.081)	0.28(0.009)	3.10(0.103)	0.26(0.009)	4.19(0.139)	0.48(0.016)
MS-CASPT2	2.14(0.071)	0.28(0.009)	3.39(0.113)	0.37(0.012)		
tPBE	0.72(0.024)	0.50(0.017)	3.65(0.122)	0.01(0.000)		
tPBE0	1.08(0.036)	0.22(0.007)	3.47(0.116)	0.09(0.003)		

1 GHz = 29.9793 cm^{-1} .

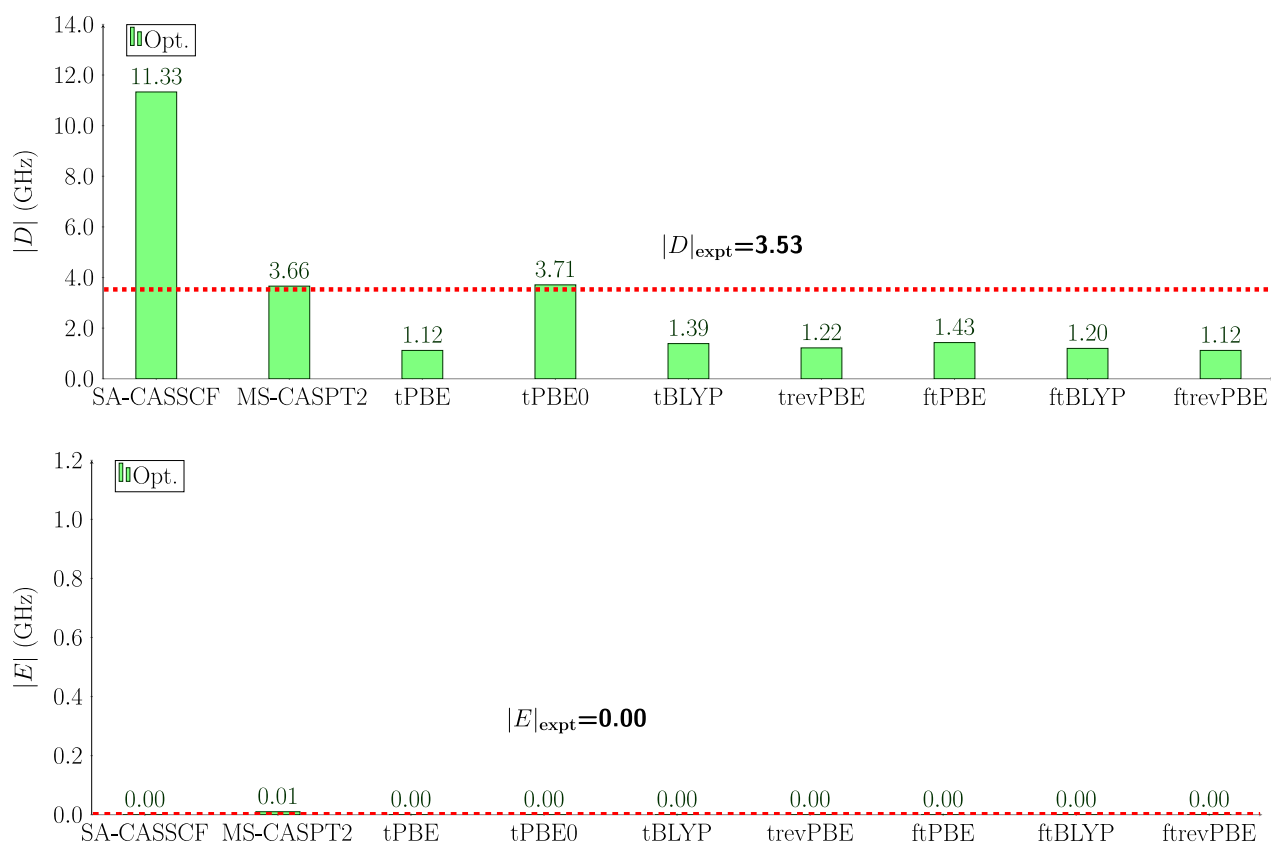


Figure S18: Computed ZFS parameters $|D|$ and $|E|$ of complex **1** with SA-CASSCF, MS-CASPT2, the translated on-top functionals tPBE, tBLYP, and trevPBE, the fully translated on-top functionals ftPBE, ftBLYP, and ftrevPBE, and the hybrid tPBE0 method. The active space is (2,5), and it was used the lowest-lying 10 triplets and 15 singlets states. The horizontal red line represents the experimental values reported in reference.^{S25}

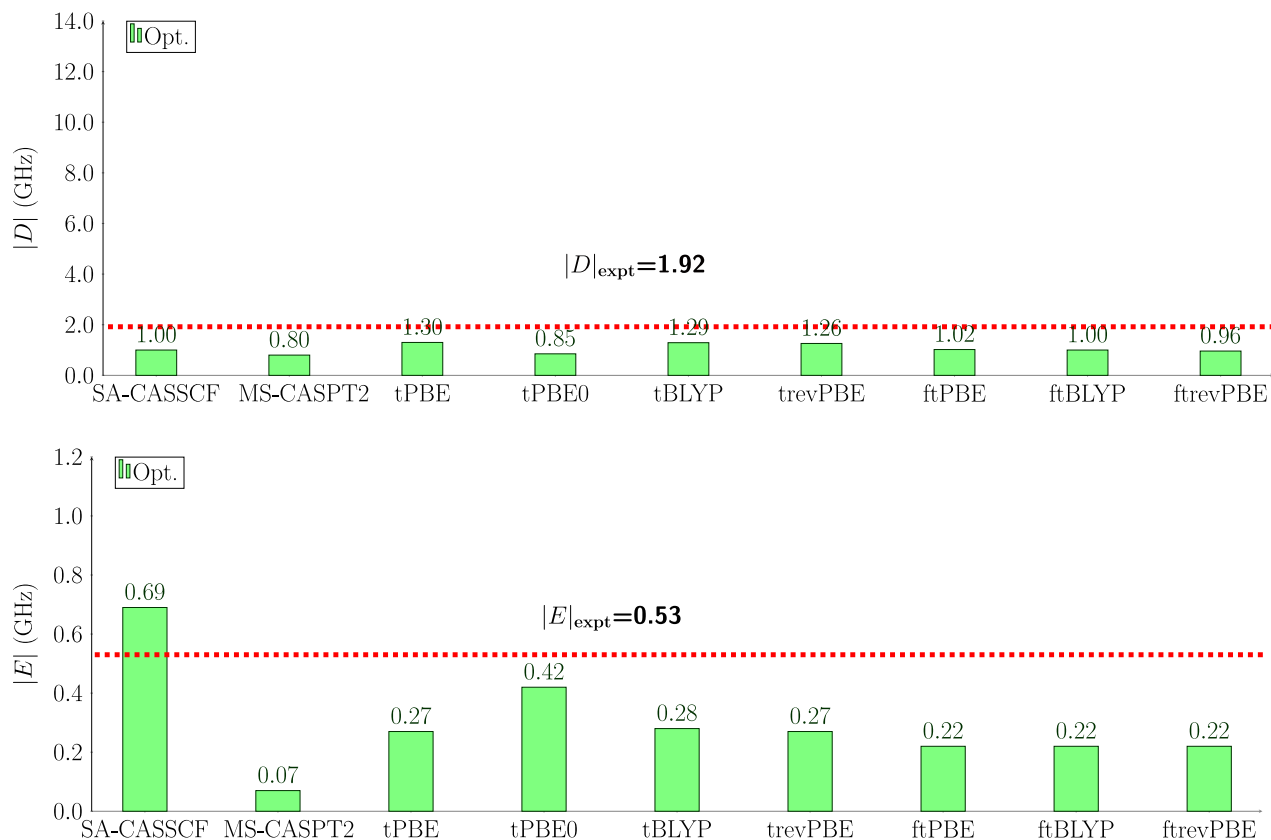


Figure S19: Computed ZFS parameters $|D|$ and $|E|$ of complex **2** with SA-CASSCF, MS-CASPT2, the translated on-top functionals tPBE, tBLYP, and trevPBE, the fully translated on-top functionals ftPBE, ftBLYP, and ftrevPBE, and the hybrid tPBE0 method. The active space is (2,5), and it was used the lowest-lying 10 triplets and 15 singlets states. The horizontal red line represents the experimental values reported in reference.^{S25}

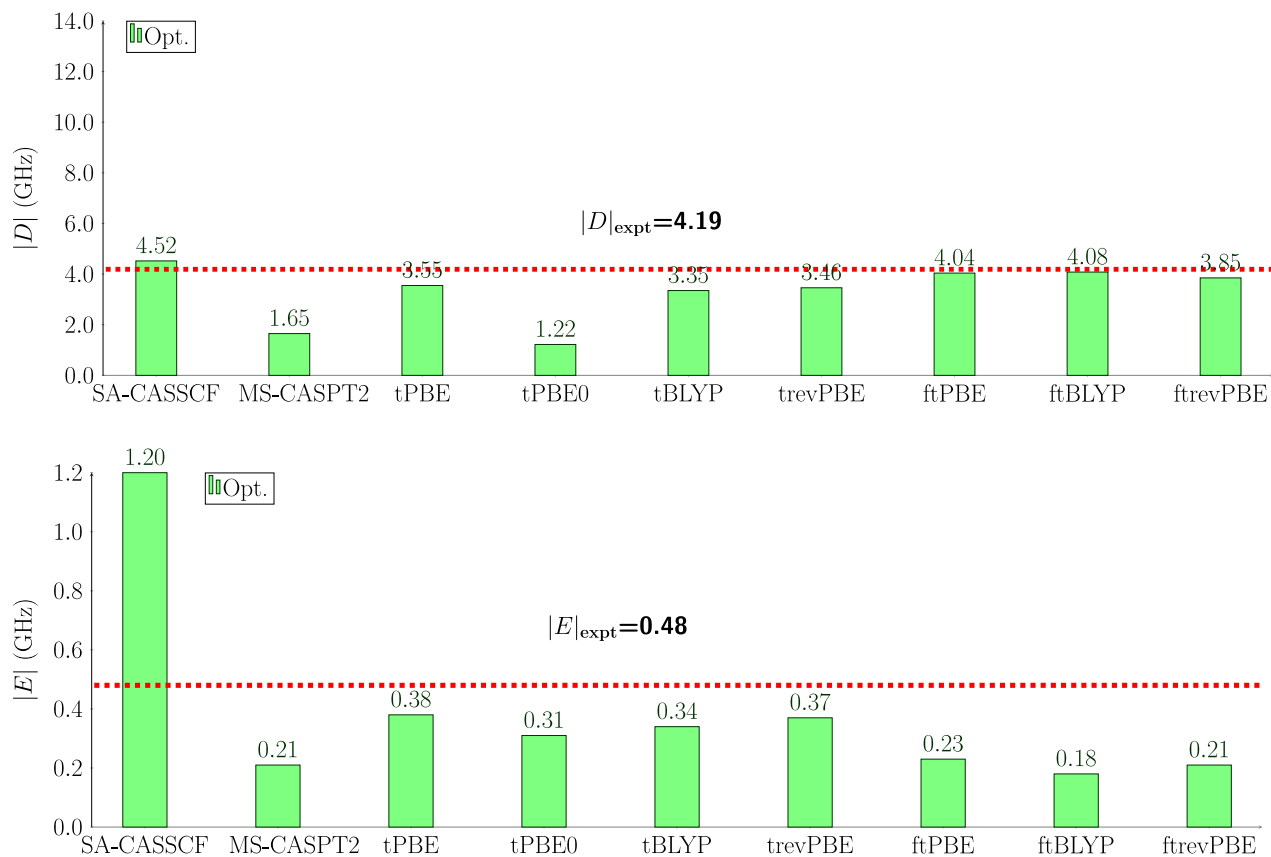


Figure S20: Computed ZFS parameters $|D|$ and $|E|$ of complex **3** with SA-CASSCF, MS-CASPT2, the translated on-top functionals tPBE, tBLYP, and trevPBE, the fully translated on-top functionals ftPBE, ftBLYP, and ftrevPBE, and the hybrid tPBE0 method. The active space is (2,5), and it was used the lowest-lying 10 triplets and 15 singlets states. The horizontal red line represents the experimental values reported in reference.^{S25}

8 Trends using different active spaces

8.1 Structures optimized with periodic calculations

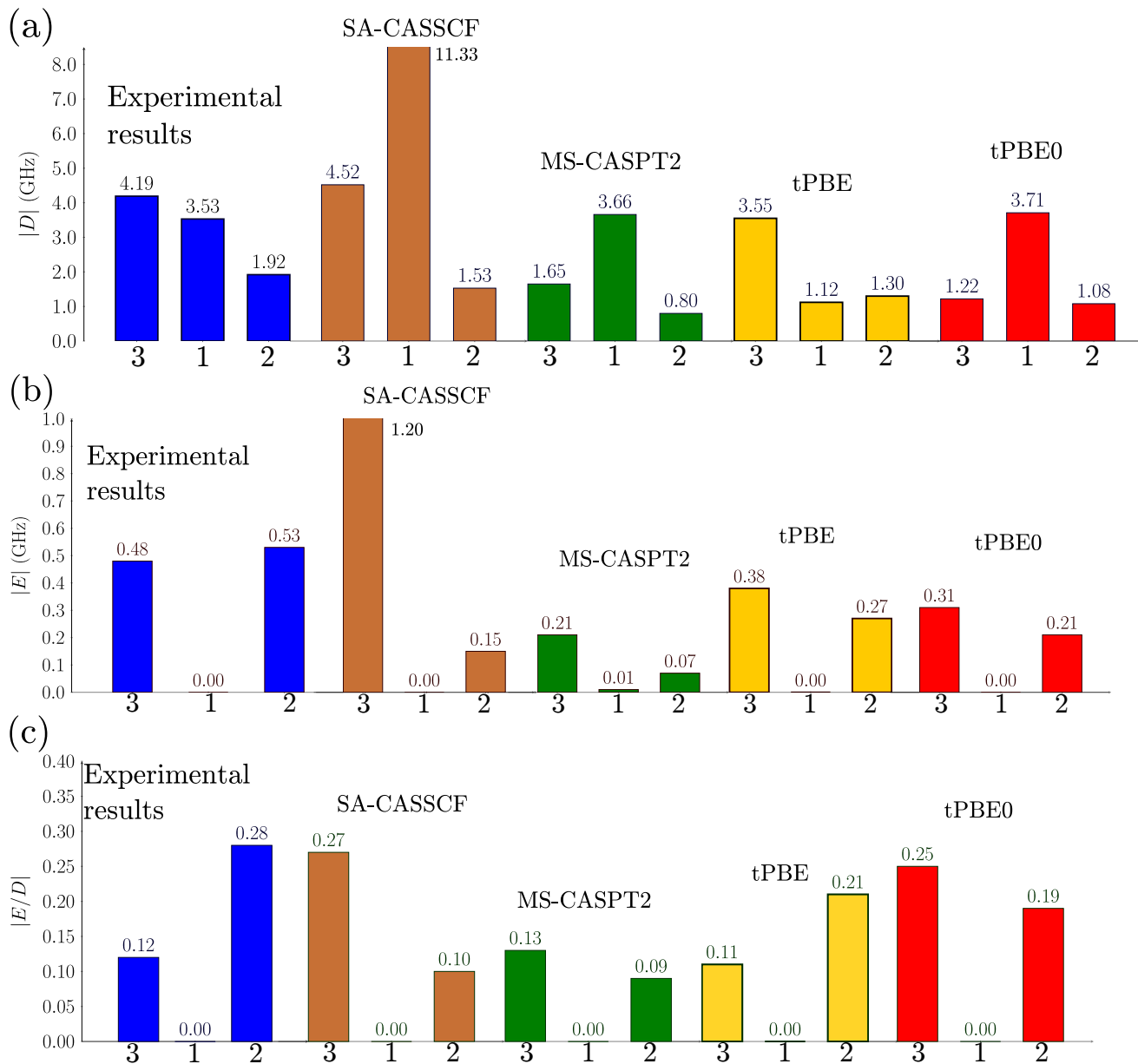


Figure S21: Trends of experimental and calculated values using the (2,5) active space for (a) the axial ZFS parameter $|D|$, (b) the rhombic ZFS parameter $|E|$, and (c) the ratio $|E/D|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

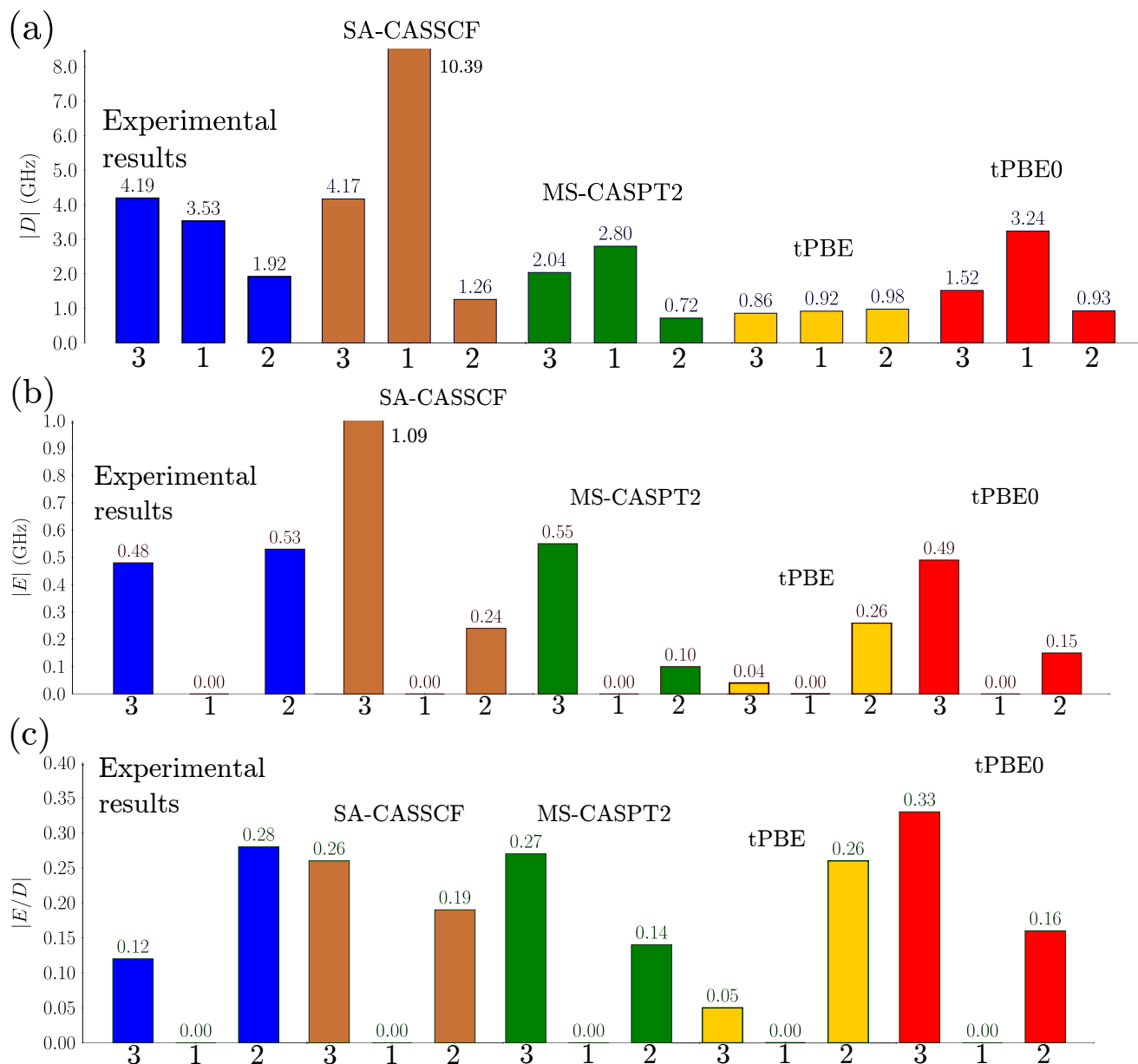


Figure S22: Trends of experimental and calculated values using the (2,10) active space for (a) the axial ZFS parameter $|D|$, (b) the rhombic ZFS parameter $|E|$, and (c) the ratio $|E/D|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

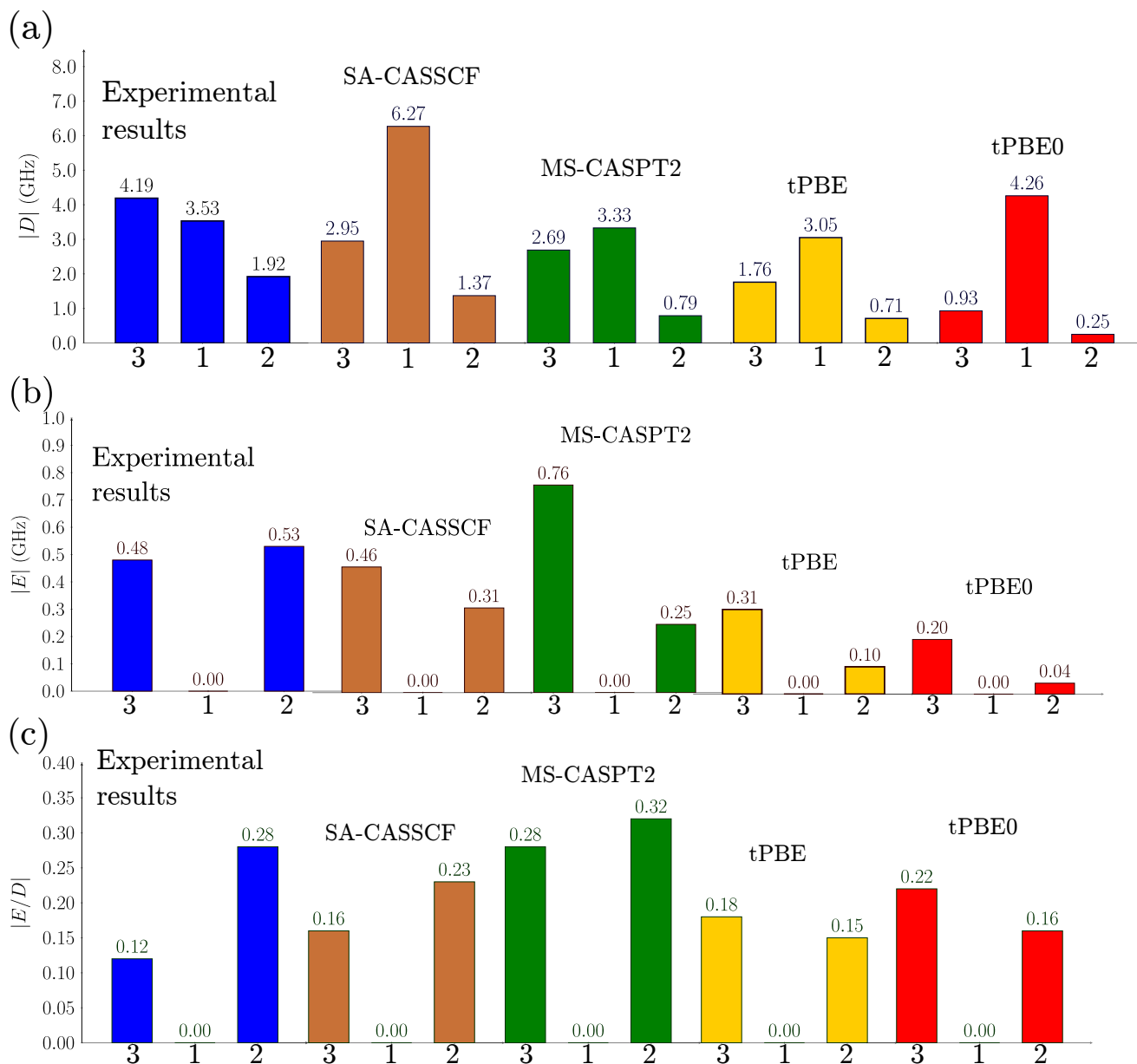


Figure S23: Trends of experimental and calculated values using the (8,8) active space for (a) the axial ZFS parameter $|D|$, (b) the rhombic ZFS parameter $|E|$, and (c) the ratio $|E/D|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

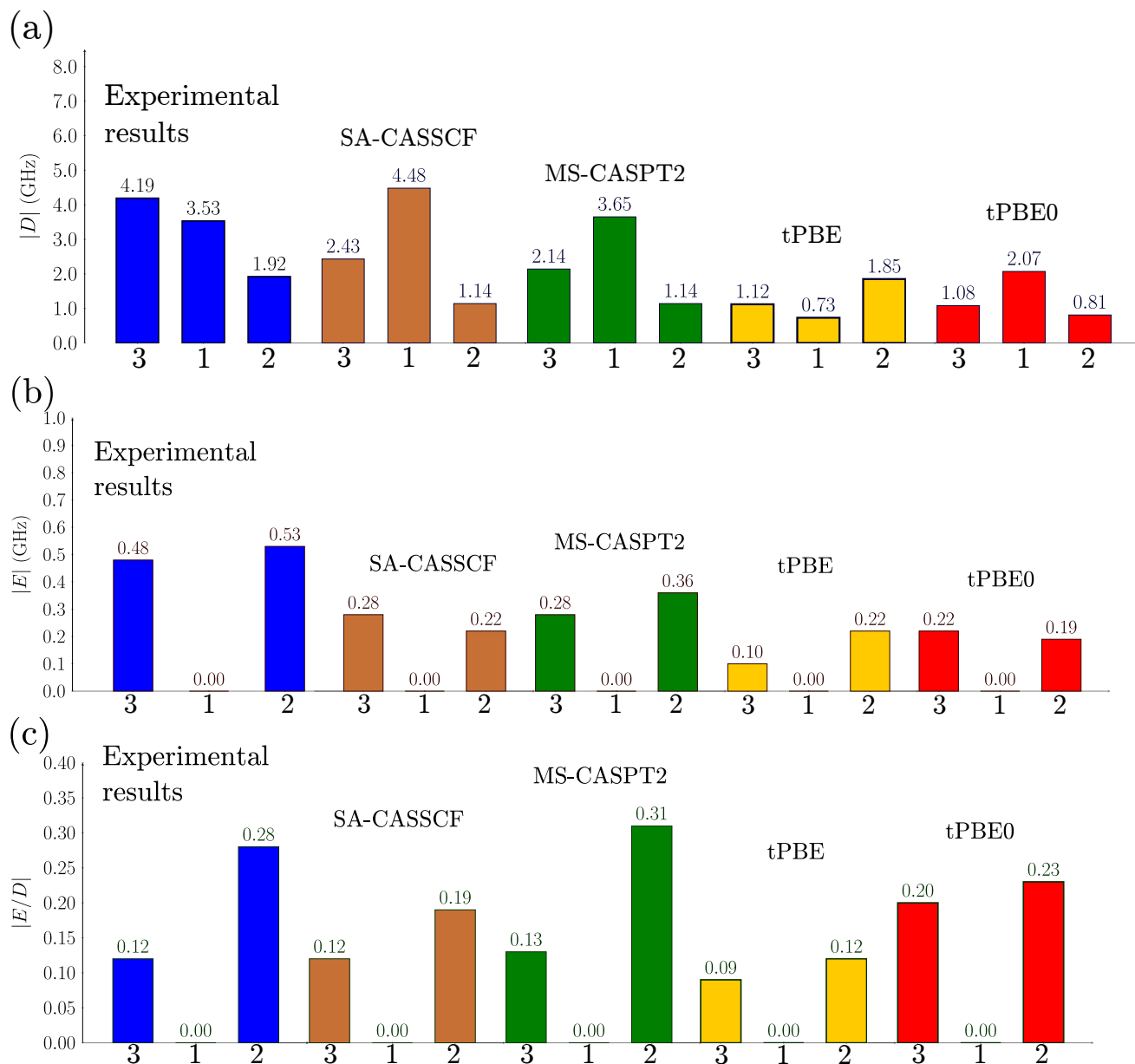


Figure S24: Trends of experimental and calculated values using the (10,15) active space for (a) the axial ZFS parameter $|D|$, (b) the rhombic ZFS parameter $|E|$, and (c) the ratio $|E/D|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

8.2 Structures optimized in gas-phase

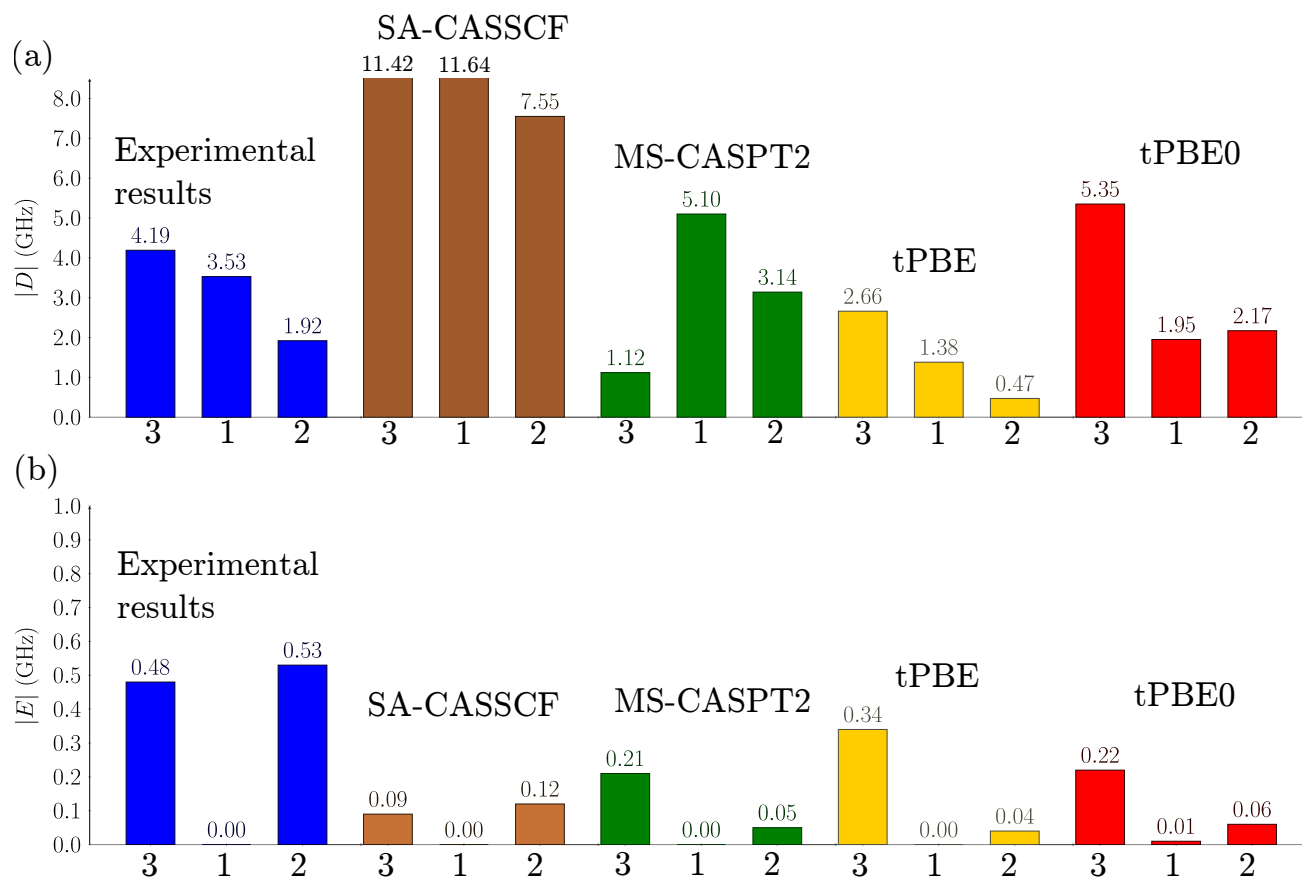


Figure S25: Trends of experimental and calculated values using the (2,5) active space for (a) the axial ZFS parameter $|D|$, and (b) the rhombic ZFS parameter $|E|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

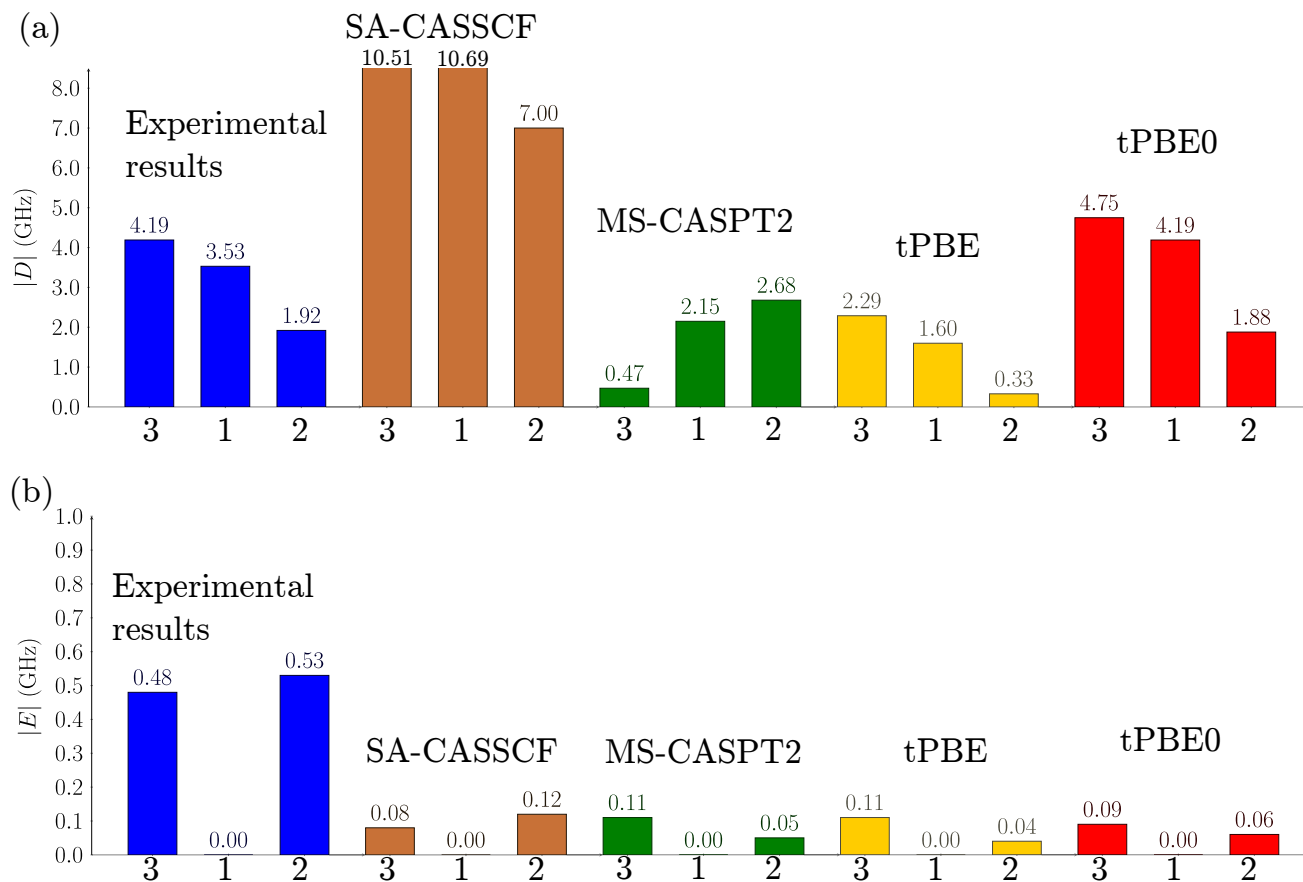


Figure S26: Trends of experimental and calculated values using the (2,10) active space for (a) the axial ZFS parameter $|D|$, and (b) the rhombic ZFS parameter $|E|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

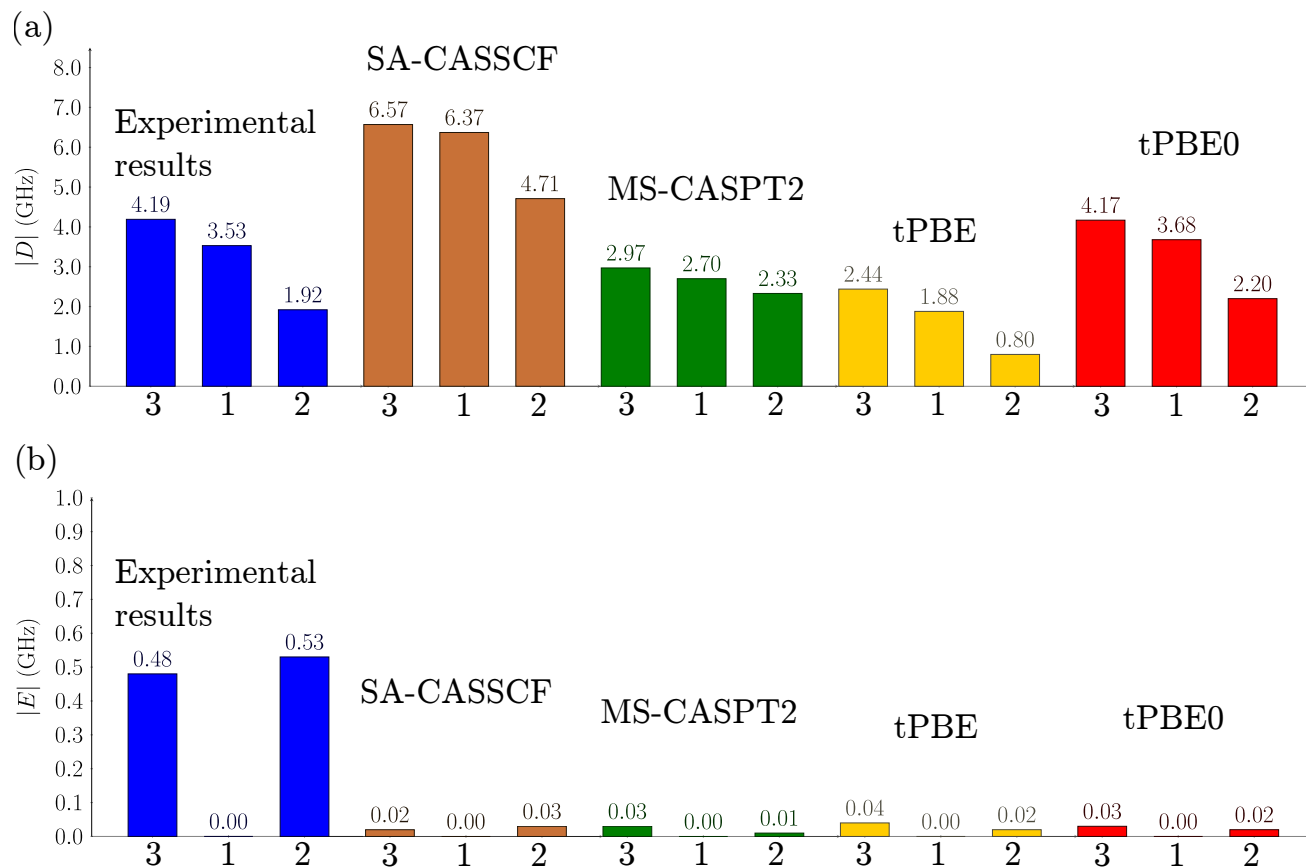


Figure S27: Trends of experimental and calculated values using the (8,8) active space for (a) the axial ZFS parameter $|D|$, and (b) the rhombic ZFS parameter $|E|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

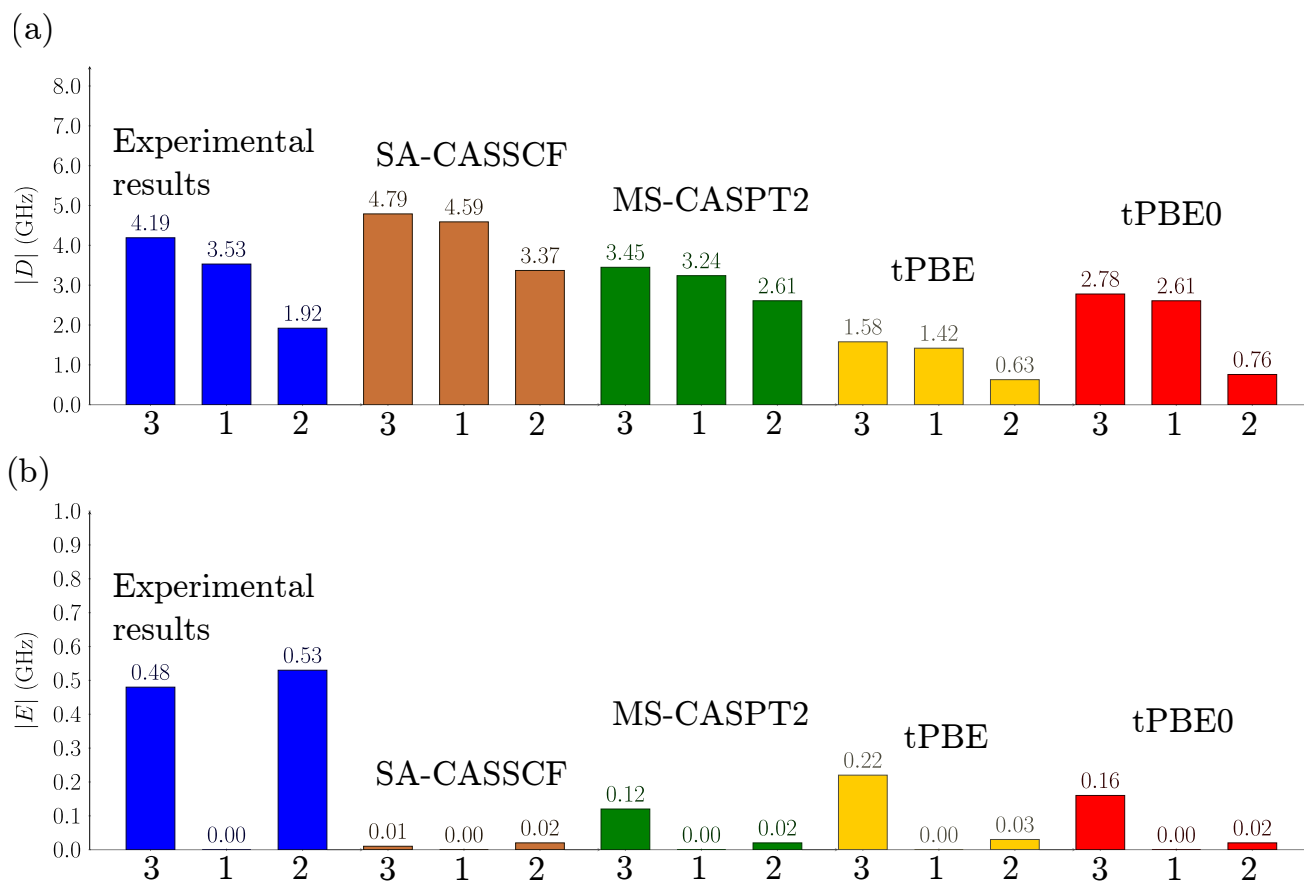


Figure S28: Trends of experimental and calculated values using the (10,15) active space for (a) the axial ZFS parameter $|D|$, and (b) the rhombic ZFS parameter $|E|$. The blue bars correspond to the experimental measurements, and the other bars are for the following electronic structure methods: SA-CASSCF (brown), MS-CASPT2 (green), MS-PDFT(tPBE) (yellow), and HMS-PDFT(tPBE0) (red).

Table S24: Spin-orbit-free energies relative to the ground state of the seven lowest triplet states as calculated with the (2,5) active space at the optimized geometries. The energies were computed with MS-CASPT2 and HMC-PDFT(tPBE0). The values are reported in eV, and cm^{-1} inside the parenthesis.

Method	1			2		
	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0
1	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)
2	2.563(20672.0)	2.277(18365.2)	2.532(20421.9)	2.225(17945.8)	2.641(21301.1)	2.281(18397.5)
3	2.676(21583.4)	2.351(18962.1)	2.709(21849.5)	2.462(19857.4)	2.695(21736.6)	2.326(18760.4)
4	2.729(22010.9)	2.407(19413.8)	2.710(21857.6)	2.462(19857.4)	2.688(21680.2)	2.336(18841.1)
5	3.116(25132.2)	3.065(24720.9)	2.853(23011.0)	2.715(21897.9)	3.091(24930.6)	3.051(24608.0)
6	3.359(27092.1)	3.222(25987.2)	3.622(29213.4)	3.605(29076.3)	3.514(28342.3)	3.197(25785.5)
7	3.463(27931.0)	3.330(26858.2)	3.623(29221.5)	3.605(29076.3)	3.562(28729.5)	3.232(26067.8)

1 eV = 8 065.54 cm^{-1} .

Table S25: Spin-orbit-free energies relative to the ground state of the seven lowest triplet states as calculated with the (2,10) active space at the optimized geometries. The energies were computed with MS-CASPT2 and HMC-PDFT(tPBE0). The values are reported in eV, and cm^{-1} inside the parenthesis.

Method	1			2		
	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0
1	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)
2	2.587(20865.6)	2.292(18486.2)	2.574(20760.7)	2.241(18074.9)	2.666(21502.7)	2.333(18816.9)
3	2.660(21454.3)	2.366(19083.1)	2.738(22083.4)	2.478(19986.4)	2.721(21946.3)	2.379(19187.9)
4	2.745(22139.9)	2.422(19534.7)	2.738(22083.4)	2.478(19986.4)	2.726(21986.7)	2.387(19252.4)
5	3.143(25350.0)	3.068(24745.1)	2.851(22994.9)	2.714(21889.9)	3.101(25011.2)	3.051(24608.0)
6	3.369(27172.8)	3.234(26084.0)	3.644(29390.8)	3.611(29124.7)	3.520(28390.7)	3.216(25938.8)
7	3.463(27931.0)	3.342(26955.0)	3.644(29390.8)	3.611(29124.7)	3.569(28785.9)	3.253(26237.2)

1 eV = 8 065.54 cm^{-1} .

Table S26: Spin-orbit-free energies relative to the ground state of the seven lowest triplet states as calculated with the (8,8) active space at the optimized geometries. The energies were computed with MS-CASPT2 and HMC-PDFT(tPBE0). The values are reported in eV, and cm^{-1} inside the parenthesis.

Method	3		1		2	
	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0
1	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)
2	2.406(19405.7)	2.332(18808.8)	2.319(18704.0)	2.269(18300.7)	2.440(19679.9)	2.404(19389.6)
3	2.525(20365.5)	2.424(19550.9)	2.538(20470.3)	2.594(20922.0)	2.449(19752.5)	2.443(19704.1)
4	2.515(20284.8)	2.482(20018.7)	2.538(20470.3)	2.595(20930.1)	2.485(20042.9)	2.475(19962.2)
5	2.751(22188.3)	2.842(22922.3)	2.554(20599.4)	2.596(20938.1)	2.762(22277.0)	2.837(22881.9)
6	2.970(23954.7)	2.996(24164.4)	3.166(25535.5)	3.259(26285.6)	2.991(24124.0)	3.012(24293.4)
7	3.093(24946.7)	3.085(24882.2)	3.166(25535.5)	3.259(26285.6)	3.031(24446.7)	3.053(24624.1)

1 eV = 8 065.54 cm^{-1} .

Table S27: Spin-orbit-free energies relative to the ground state of the seven lowest states as calculated with the (10,15) active space at the optimized geometries. The energies were computed with MS-CASPT2 and HMC-PDFT(tPBE0). The values are reported in eV, and cm^{-1} inside the parenthesis.

Method	3		1		2	
	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0	MS-CASPT2	tPBE0
1	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)	0.000(0.0)
2	2.406(19405.7)	2.332(18808.8)	2.319(18704.0)	2.269(18300.7)	2.440(19679.9)	2.404(19389.6)
3	2.525(20365.5)	2.424(19550.9)	2.538(20470.3)	2.594(20922.0)	2.449(19752.5)	2.443(19704.1)
4	2.515(20284.8)	2.482(20018.7)	2.538(20470.3)	2.595(20930.1)	2.485(20042.9)	2.475(19962.2)
5	2.751(22188.3)	2.842(22922.3)	2.554(20599.4)	2.596(20938.1)	2.762(22277.0)	2.837(22881.9)
6	2.970(23954.7)	2.996(24164.4)	3.166(25535.5)	3.259(26285.6)	2.991(24124.0)	3.012(24293.4)
7	3.093(24946.7)	3.085(24882.2)	3.166(25535.5)	3.259(26285.6)	3.031(24446.7)	3.053(24624.1)

1 eV = 8 065.54 cm^{-1} .

Optimized Geometries

The following data corresponds to the optimized structures with periodical calculations.

Molecule 1

Cr	0.000000000	0.000000000	0.000000000
C	-1.512325000	0.242037000	1.232610000
C	1.512359000	-0.242037000	1.232614000
C	0.242035000	1.512340000	-1.232644000
C	-0.242008000	-1.512344000	-1.232646000
C	-1.847295000	-0.705409000	2.225921000
C	1.847348000	0.705410000	2.225950000
C	-0.705416000	1.847357000	-2.226000000
C	0.705440000	-1.847374000	-2.226012000
C	-2.871247000	-0.388256000	3.133125000
C	2.871303000	0.388228000	3.133148000
C	-0.388214000	2.871327000	-3.133176000
C	0.388228000	-2.871346000	-3.133183000
C	-2.198202000	1.468925000	1.172491000
C	2.198265000	-1.468936000	1.172517000
C	1.468928000	2.198262000	-1.172562000
C	-1.468906000	-2.198271000	-1.172563000
C	-3.547217000	0.830628000	3.061351000
C	3.547264000	-0.830641000	3.061393000
C	0.830639000	3.547299000	-3.061413000
C	-0.830631000	-3.547308000	-3.061417000
C	-3.217736000	1.763150000	2.075052000

C	3.217779000	-1.763152000	2.075096000
C	1.763132000	3.217796000	-2.075134000
C	-1.763115000	-3.217804000	-2.075134000
C	-1.117588000	-2.017107000	2.355632000
C	1.117618000	2.017100000	2.355634000
C	-2.017108000	1.117620000	-2.355657000
C	2.017133000	-1.117637000	-2.355666000
H	-3.141388000	-1.113549000	3.905304000
H	3.141416000	1.113499000	3.905319000
H	-1.113485000	3.141459000	-3.905325000
H	1.113489000	-3.141476000	-3.905341000
H	-1.927612000	2.201896000	0.411106000
H	1.927666000	-2.201902000	0.411115000
H	2.201893000	1.927648000	-0.411138000
H	-2.201863000	-1.927650000	-0.411131000
H	-4.332739000	1.052059000	3.782093000
H	4.332764000	-1.052075000	3.782121000
H	1.052078000	4.332776000	-3.782129000
H	-1.052076000	-4.332786000	-3.782126000
H	-3.749171000	2.712970000	2.010498000
H	3.749197000	-2.712964000	2.010536000
H	2.712931000	3.749210000	-2.010537000
H	-2.712914000	-3.749201000	-2.010535000
H	-0.656567000	-2.331327000	1.411220000
H	0.656593000	2.331298000	1.411211000
H	-2.331263000	0.656611000	-1.411215000
H	2.331272000	-0.656626000	-1.411222000

H	-1.789644000	-2.817970000	2.690412000
H	1.789646000	2.817970000	2.690408000
H	-2.817972000	1.789638000	-2.690407000
H	2.817997000	-1.789647000	-2.690417000
H	-0.307589000	-1.938919000	3.097397000
H	0.307620000	1.938896000	3.097385000
H	-1.938909000	0.307612000	-3.097383000
H	1.938918000	-0.307629000	-3.097389000

Molecule 2

Cr	0.000000000	0.000000000	0.000000000
C	-2.705519000	-0.434689000	-0.979062000
C	2.705519000	0.434690000	-0.979062000
C	-2.104223000	-2.410950000	-2.877194000
C	2.104223000	2.410951000	-2.877194000
C	-0.859481000	1.351378000	1.166477000
C	0.859481000	-1.351378000	1.166477000
C	-3.421753000	-1.974486000	-2.688826000
C	3.421753000	1.974487000	-2.688826000
C	-0.559014000	2.713926000	0.985864000
C	0.559014000	-2.713925000	0.985864000
C	-1.062452000	-1.835232000	-2.113078000
C	1.062451000	1.835233000	-2.113078000
C	-1.371486000	-0.851753000	-1.148498000
C	1.371487000	0.851754000	-1.148498000
C	-1.754354000	0.954966000	2.183753000

C	1.754353000	-0.954965000	2.183753000
C	-1.810824000	-3.476472000	-3.898184000
C	1.810824000	3.476473000	-3.898184000
C	-2.024628000	-0.495466000	2.476475000
C	2.024628000	0.495467000	2.476475000
C	-3.725498000	-0.989499000	-1.751216000
C	3.725498000	0.989499000	-1.751216000
C	-1.154112000	3.678058000	1.801568000
C	1.154113000	-3.678058000	1.801568000
C	0.351454000	-2.280997000	-2.369014000
C	-0.351454000	2.280998000	-2.369014000
H	-2.949033000	0.337409000	-0.250068000
H	2.949033000	-0.337409000	-0.250068000
H	-4.215610000	-2.401876000	-3.301979000
H	4.215610000	2.401877000	-3.301979000
H	0.147865000	3.025154000	0.215352000
H	-0.147865000	-3.025154000	0.215352000
H	-1.393678000	-4.381131000	-3.428384000
H	1.393678000	4.381131000	-3.428384000
H	-1.070331000	-3.144355000	-4.640623000
H	1.070330000	3.144355000	-4.640623000
H	-2.726935000	-3.756708000	-4.433361000
H	2.726934000	3.756708000	-4.433361000
H	-1.766842000	-1.155257000	1.640778000
H	1.766842000	1.155258000	1.640778000
H	-4.755255000	-0.650897000	-1.629331000
H	4.755255000	0.650897000	-1.629331000

H	-0.936267000	4.735735000	1.661709000
H	0.936267000	-4.735735000	1.661709000
H	0.470463000	-3.364020000	-2.208056000
H	-0.470463000	3.364020000	-2.208056000
H	1.080899000	-1.766091000	-1.734734000
H	-1.080900000	1.766092000	-1.734734000
H	0.639666000	-2.097400000	-3.415866000
H	-0.639667000	2.097401000	-3.415866000
C	-2.370400000	1.936577000	2.994399000
C	2.370399000	-1.936577000	2.994399000
H	-3.072590000	-0.677892000	2.741764000
H	-1.429293000	-0.816654000	3.345601000
H	3.072590000	0.677893000	2.741764000
H	1.429293000	0.816654000	3.345601000
C	-2.043193000	3.284432000	2.798817000
C	2.043194000	-3.284432000	2.798817000
C	-3.357637000	1.553881000	4.059477000
C	3.357637000	-1.553881000	4.059477000
H	-2.494987000	4.030897000	3.453230000
H	2.494987000	-4.030897000	3.453230000
H	-4.215287000	1.012775000	3.631880000
H	-3.739647000	2.438337000	4.581385000
H	-2.913973000	0.882876000	4.808253000
H	2.913973000	-0.882875000	4.808253000
H	3.739647000	-2.438337000	4.581385000
H	4.215286000	-1.012774000	3.631880000

Molecule 3

Cr	0.000000000	0.000000000	0.000000000
C	-1.101538000	1.118807000	-1.191509000
C	0.210792000	-1.794205000	-0.801873000
C	1.750477000	0.878426000	0.244871000
C	-1.690146000	2.347754000	-0.806952000
C	1.040010000	-2.054335000	-1.920561000
C	-0.889700000	-0.178247000	1.758453000
C	1.088468000	-3.356621000	-2.432460000
C	-2.531733000	2.647645000	-3.097646000
C	-2.267456000	-0.470880000	1.908468000
C	-1.258501000	0.673675000	-2.515058000
C	-0.511141000	-2.857522000	-0.234036000
C	-2.390778000	3.083981000	-1.772358000
C	1.847046000	2.237463000	-0.106638000
C	0.363847000	-4.418418000	-1.872264000
C	-0.109938000	0.003851000	2.912655000
C	-2.803122000	-0.566695000	3.200585000
C	2.869932000	0.246064000	0.838242000
C	-0.662228000	-0.097476000	4.189460000
C	-1.600214000	2.868855000	0.602564000
C	-2.023772000	-0.377804000	4.350893000
C	-0.438902000	-4.149479000	-0.758121000
C	-3.176499000	-0.646495000	0.721303000
C	4.105318000	2.370902000	0.773323000
C	2.999586000	2.972931000	0.162867000
C	4.016264000	1.009976000	1.097276000

C	0.463026000	-5.802551000	-2.442457000
C	1.901354000	-0.985955000	-2.537758000
C	2.866701000	-1.220405000	1.172421000
C	5.349971000	3.161740000	1.046537000
C	-2.632826000	-0.440443000	5.721253000
H	-0.827441000	-0.277068000	-2.821179000
H	-1.136361000	-2.682621000	0.640218000
H	-2.827214000	4.043368000	-1.479235000
H	1.012237000	2.733824000	-0.600945000
H	0.952633000	0.227356000	2.824825000
H	-3.866291000	-0.799266000	3.313219000
H	-0.021132000	0.023260000	5.065022000
H	-2.268059000	2.303311000	1.267474000
H	-1.886343000	3.926674000	0.661088000
H	-0.591297000	2.757874000	1.021673000
H	-1.017737000	-4.952085000	-0.295130000
H	-3.519062000	0.328501000	0.342760000
H	-4.065926000	-1.237352000	0.978619000
H	-2.672364000	-1.140345000	-0.118999000
H	3.039907000	4.031458000	-0.098054000
H	4.875745000	0.525090000	1.566504000
H	-0.418284000	-6.397173000	-2.180365000
H	1.343378000	-6.337911000	-2.053548000
H	1.397176000	-0.013355000	-2.601103000
H	2.802408000	-0.819447000	-1.930596000
H	2.064174000	-1.483565000	1.876849000
H	3.817583000	-1.531861000	1.621724000

H	2.702459000	-1.834094000	0.277358000
H	5.883688000	3.394255000	0.112668000
H	6.041704000	2.615498000	1.698565000
H	5.109001000	4.114590000	1.534288000
H	-2.860480000	0.572920000	6.088861000
H	-1.941166000	-0.897426000	6.442209000
H	-3.568526000	-1.014580000	5.722506000
H	1.708460000	-3.551361000	-3.309566000
C	-3.271384000	3.460602000	-4.116230000
C	-1.957062000	1.424241000	-3.458161000
H	0.546352000	-5.784909000	-3.536796000
H	2.234497000	-1.262048000	-3.546693000
H	-4.288077000	3.066296000	-4.256833000
H	-3.359591000	4.509861000	-3.812561000
H	-2.766510000	3.419159000	-5.090749000
H	-2.038256000	1.065234000	-4.486061000

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