

# Supporting information to “Self-Consistent Implementation of Kohn-Sham Adiabatic Connection Models with Improved Treatment of the Strong-Interaction Limit”

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## 1 Summary of the basis sets

- **He, He<sub>2</sub>**: even tempered 20s10p2d basis.
- **Be, Ne, Ne<sub>2</sub>**: uncontracted ROOS-ATZP basis<sup>1</sup>.
- **Mg**: uncontracted aug-cc-pVTZ basis set<sup>2</sup>.
- **Ar**: *s* and *p* basis functions from the uncontracted ROOS-ATZP<sup>1</sup> basis set and *d* and *f* functions from the uncontracted aug-cc-pwCVQZ basis set<sup>3</sup>.
- **HF, CO, H<sub>2</sub>O, H<sub>2</sub>, Cl<sub>2</sub>, N<sub>2</sub>, HCl, NH<sub>3</sub>, C<sub>2</sub>H<sub>6</sub>**: uncontracted cc-pVTZ basis set of Dunning<sup>4</sup>.

## 2 Dissociation of H<sub>2</sub> with SPL functional

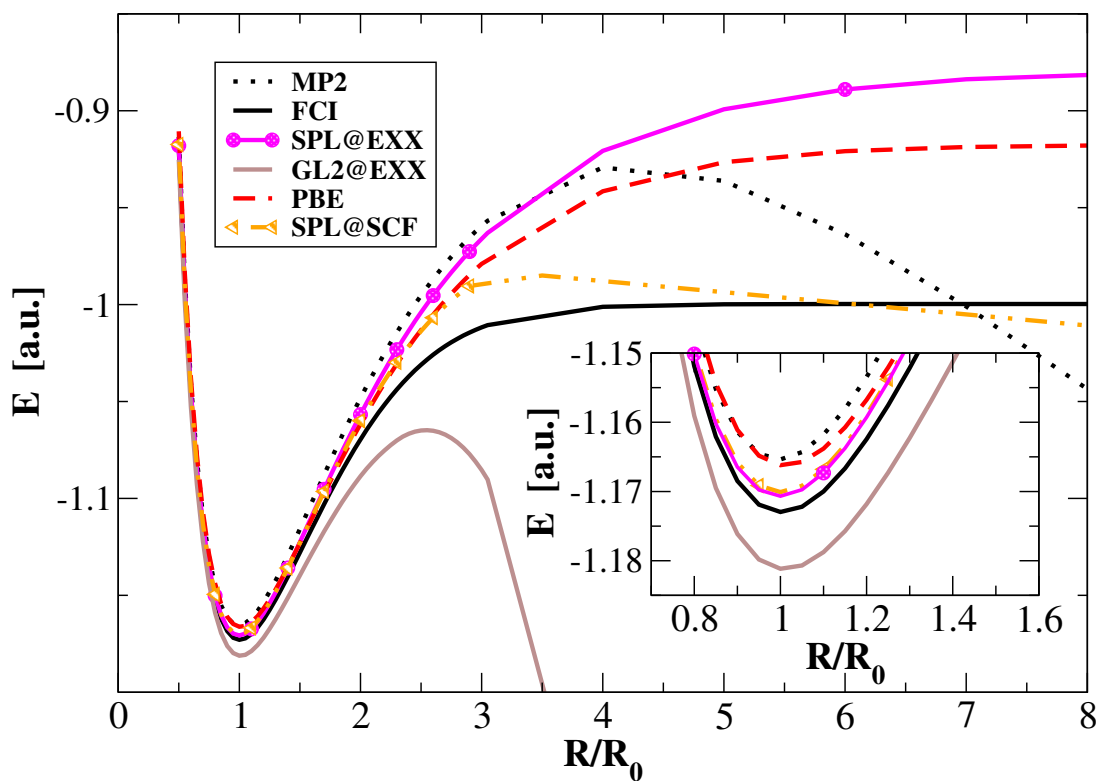


Figure S1: The total energy of the H<sub>2</sub> molecule as it is stretched calculated with the various methods. The inset presents the same data around the equilibrium distance.

### 3 Hookes atom results

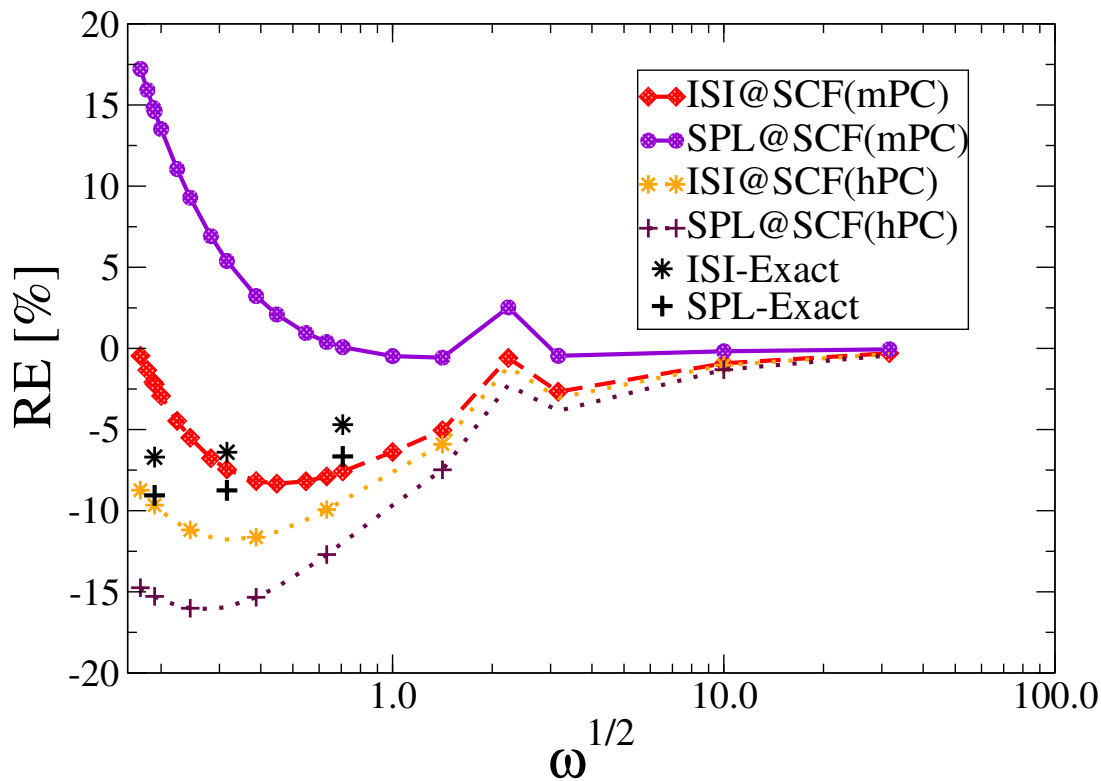


Figure S2: Relative error on correlation energies of harmonium atoms for various values of  $\omega$  computed at @SCF orbitals for ISI and SPL functionals using the hPC and mPC models for the strong-interaction functionals. The errors have been computed with respect FCI data obtained in the same basis set<sup>5</sup>. The exact ISI and SPL values are taken from Ref.<sup>6</sup>, and are obtained by inserting exact densities into the ISI and SPL functionals, including the exact treatment (SCE) of the strong-interaction limit.

## References

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