Helicate-to-tetrahedron transformation of chiral lanthanide supramolecular complexes induced by ionic radii effect and linker length

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Experimental Procedures

 $(S)-6-((1-phenylethyl) carbamoyl) picolinic acid 1^{S} and (R)-6-((1-phenylethyl) carbamoyl) picolinic acid 1^{R} acid$



This synthesis is reported by our group previously.¹ To a stirred solution of 2,6-pyridinedicarboxylic acid (5 g, 29.90 mmol, 2.50 equiv.) in anhydrous DMF (70 ml) at room temperature, HATU (4.55 g, 11.90 mmol, 1 equiv.) was added in portions over 10 min under nitrogen. After allowing it to stir for 20 min, (S)-(-)-1-phenylethylamine (1.53 ml, 11.97 mmol, 1 equiv.) was added dropwise and the reaction mixture was allowed to stir for 20 min. DIPEA (5.50 ml, 31.60 mmol, 2.60 equiv.) was then added to the reaction mixture over 5 min and the resulting solution was stirred at room temperature for 14 h. The reaction mixture was then diluted with H₂O (100 ml), and extracted with DCM (30 ml x 3), dried with MgSO₄, filtered, and concentrated in vacuo. Then dissolved it in water and extracted with EA to remove excess DMF. The resulting residue was purified by recrystallization in EtOAc solvent to give a white solid. 1^s: (1.46g, 5.42 mmol, 45.39% yield), mp 110.2 - 117.3 °C. ¹H NMR (400 MHz, CDCl₃, 298K, δ): 1.65 (d, 7.0Hz, 3H), 5.37 (p, J=7.1Hz, 1H), 7.20-7.44 (m, 5H), 8.01 (d, J=8.2Hz, 1H), 8.11 (t, J=7.8Hz, 1H), 8.36 (dd, J=7.7, 1.2Hz, 1H), $8.48 (dd, J=7.8, 1.2Hz, 1H).^{13}C NMR (400MHz, CDCl_3, 300K, \delta): 21.50, 49.14, 126.25, 126.72, 126.95, 127.48, 128.67, 139.50, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.14, 120.$ 142.63, 145.37, 149.56, 162.48, 164.67. HRMS (ESI) calcd. for $C_{15}H_{14}N_2O_3Na$ [1^s+Na]⁺: 293.0897, found 293.0895. The enantiomeric purity was determined with HPLC using AS-H column (Hexane/i-propanol: 80/20; flow rate 1.0 ml/min) and compared with a racemic mixture according to the elution orders with the retention times, $t_s = 7.15$ mins and $t_{R} = 9.62$ mins) to be > 99.9% ee. 1^R was isolated, following the procedure for 1^S with the use of (R)-(+)-1-phenylethylamine instead, in 55.10% yield (1.78g, 6.59 mmol): mp 110.3 - 113.9 °C. ¹H NMR (400 MHz, CDCl₃, 298K): δ 1.60 (d, J=6.9Hz, 3H), 5.34 (p, J=7.1Hz, 1H), 7.18-7.41 (m, 5H), 8.06 (t, J=7.8Hz, 1H), 8.29-8.38 (m, 2H), 8.44 (dd, J=7.8, 1.2Hz, 1H). ¹³C NMR (100 MHz, CDCl₃, 300K, \delta): 21.50, 30.94, 49.12, 126.23, 126.69, 126.95, 127.44, 128.63, 139.48, 142.63, 145.41, 149.52, 162.58, 164.80. HRMS (ESI) calcd. for $C_{15}H_{14}N_2O_3Na$ [1^R+Na]⁺: 293.0897, found 293.0896. The enantiomeric purity was determined to be 97.0% ee.

 N^2 , N^2 -(1,4-phenylene)bis(N^6 -((*S*)-1-phenylethyl)pyridine-2,6-dicarboxamide) (L1^{SS}) and N^2 , N^2 '-(1,4-phenylene)bis(N^6 -((*R*)-1-phenylethyl)pyridine-2,6-dicarboxamide) (L1^{RR})



To a stirred solution of 1^R (0.25 g, 0.92 mmol, 2.2 equiv.) in anhydrous DMF (4 mL) at room temperature, HATU (0.765 g, 2.01 mmol, 4.8 equiv.) was added under nitrogen. After allowing it to stir for 20 min, a 4,4'-diamino-p-terphenyl (0.045 g, 0.417 mmol, 1.0 equiv.) was added and the reaction mixture was allowed to stir for 20 min in dark. DIPEA (0.89 mL, 5.1 mmol, 12.5 equiv.) was then added to the reaction mixture and the resulting solution was stirred at room temperature for 14 h. The reaction mixture was then diluted with H₂O (10 mL) and extracted with DCM (5×3 mL). After removing the organic volatile under reduced pressure, the residue was then washed with CH₃CN (10 mL), and fine powder was progressively precipitated out. Then the solid was collected by centrifugation and the desired compound was isolated. (L1^{RR}): (0.20 g, 0.33 mmol, 70% yield), ¹H NMR (400 MHz, (CD₃)₂SO, 299 K, δ): 1.67 (d, J = 8 Hz, 6H), 5.35–5.45 (m, 2H), 7.24 (t, J = 8 Hz, 2H), 7.34 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 2H), 8.35 (d, J = 8 Hz, 2H), 8.39 (d, J = 8 Hz, 2H), 9.27 (d, J = 8 Hz, 2H). ¹³C NMR (100 MHz, (CD₃)₂SO, $300 \text{ K}, \delta): 22.17(\text{CH}_3), 48.81(\text{CH}), 122.36, 125.41, 126.52, 127.28, 128.80, 134.71, 140.20, 144.52, 149.14, 149.42, 162.28, 163.39.$ HRMS (ESI) calcd. for $C_{72}H_{64}N_{12}O_8Na$ [2L1^{RR}+Na]⁺: 1247.4862, found 1247.4850. (L1^{SS}) was synthesized, following the procedure for (L1^{RR}) with the use of 1^S instead, in 60% yield (0.17 g, 0.28 mmol): ¹H NMR (400 MHz, (CD₃)₂SO, 299 K, δ): 1.67 (d, J = 8 Hz, 6H), 5.35–5.45 (m, 2H), 7.24 (t, J = 8 Hz, 2H), 7.34 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.45 (d, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 7.70 (s, 4H), 8.07 (t, J = 8 Hz, 4H), 8.07 (t, J = = 8 Hz, 2H), 8.35 (d, J = 8 Hz, 2H), 8.39 (d, J = 8 Hz, 2H), 9.27 (d, J = 8 Hz, 2H). ¹³C NMR (100 MHz, (CD₃)₂SO, 300 K, δ): 22.15, 48.78, 122.35, 125.39, 125.58, 126.51, 127.26, 128.78, 134.71, 140.19, 144.51, 149.13, 149.41, 162.28, 163.20. HRMS (ESI) calcd. for $C_{72}H_{64}N_{12}O_8Na \ [2L1^{SS}+Na]^+: 1247.4862$, found 1247.4850.

 $N^2, N^2 \cdot ([1,1':4',1''-terphenyl]-4,4''-diyl) bis(N^6 \cdot ((R)-1-phenylethyl) pyridine-2,6-dicarboxamide) (L3^{RR}) and N^2, N^2 \cdot ([1,1':4',1''-terphenyl]-4,4''-diyl) bis(N^6 \cdot ((R)-1-phenylethyl) pyridine-2,6-dicarboxamide) (L3^{RR})$



To a stirred solution of 1^{R} (0.5 g, 1.85 mmol, 2.2 equiv.) in anhydrous DMF (8 mL) at room temperature, HATU (1.65 g, 4.06 mmol, 4.8 equiv.) was added under nitrogen. After allowing it to stir for 20 min, a 4,4°-diamino-p-terphenyl (1.10 g, 4.21 mmol,

1.0 equiv.) was added and the reaction mixture was allowed to stir for 20 min in dark. DIPEA (1.78 mL, 10.2 mmol, 12.5 equiv.) was then added to the reaction mixture and the resulting solution was stirred at room temperature for 14 h. The reaction mixture was then diluted with H2O (20 mL) and extracted with DCM (5 × 6 mL). After removing all of the organic volatile under reduced pressure, the residue was then washed with CH₃CN three times (20 mL x 3), and fine powder was progressively precipitated out. Then the solid was collected by filtration and the desired compound was isolated. (L3^{RR}): (0.62 g, 0.81 mmol, 95.28% yield), ¹H NMR (400 MHz, (CD₃)₂SO, 299 K, δ): 1.69 (d, *J* = 6.96 Hz, 6H), 5.35–5.45 (m, 2H), 7.29 (t, *J* = 2.65 Hz, 2H), 7.39 (t, *J* = 8 Hz, 4H), 7.46 (d, *J* = 8 Hz, 4H), 7.66 (d, *J* = 8 Hz, 8H), 7.78 (d, *J* = 8 Hz, 4H), 8.09 (t, *J* = 8 Hz, 2H), 8.38 (d, *J* = 8 Hz, 2H), 8.44 (d, *J* = 8 Hz, 2H), 8.54 (d, *J* = 8 Hz, 2H), 10.01 (s, 2H). ¹³C NMR (101 MHz, 300 K, δ): ¹³C NMR (101 MHz, (CD₃)₂SO, 300K, δ): 163.11, 162.22, 149.59, 149.14, 144.60, 140.23, 138.74, 137.85, 135.95, 128.83, 127.29, 126.62, 125.66, 125.40, 122.16, 48.68, 22.28. HRMS (ESI) calcd. for C₄₈H₄₀N₆O₄Na [L3^{RR}+Na]⁺: 787.3003, found 787.3038. (L3^{SS)} was synthesized, following the procedure for (L3^{RR}) with the use of 1^S instead, in 80% yield (0.4 g, 0.52 mmol): ¹H NMR (400 MHz, (CD₃)₂SO, 299 K, δ): 1.72 (d, *J* = 8 Hz, 6H), 5.40–5.48 (m, 2H), 7.30 (t, *J* = 8 Hz, 2H), 7.41 (t, *J* = 8 Hz, 4H), 7.49 (d, *J* = 8 Hz, 4H), 7.70 (d, *J* = 8 Hz, 8H), 7.83 (d, *J* = 8 Hz, 4H), 8.13 (t, 2H), 8.40 (d, *J* = 8 Hz, 2H), 8.47 (d, *J* = 8 Hz, 2H), 8.77 (d, *J* = 8 Hz, 2H). ¹³C NMR (100 MHz, (CD₃)₂SO, 300 K, δ): 163.11, 162.22, 149.61, 149.15, 144.60, 140.23, 138.75, 137.86, 135.95, 128.83, 127.29, 126.62, 125.65, 125.40, 122.15, 48.67, 22.28. HRMS (ESI) calcd. for C₄₈H₄₀N₆O₄Na [L3^{RR}+Na]⁺: 787.3003, found 787.3038.

General synthetic procedures of [Ln₂L1₃]



To a white suspension of L1 (10 mg, 0.016 mmol, 1.5 equiv.) in a mixture of 8.49 ml of DCM/MeOH (12:1, v/v), a solution of $Ln(OTf)_3$ (0.011 mmol, 1 equiv.) (Ln = La, Sm, Eu, Gd, Tb and Lu) in 7.83 ml of CH₃CN was added. The solution was changed to homogeneous colorless solution immediately. The solution was then reacted for 16 hrs at room temperature and pressure. After 16 hrs, the solvent was removed under reduced pressure to give desired product.

 $[La_{2}L1^{SS}_{3}]: (12.0 \text{ mg}, 3.99 \text{ x } 10^{-3} \text{ mmol}, 73.3\% \text{ yield}), {}^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): \delta 10.32 (s, 3 \text{ x } 2\text{H}), 9.00 (d,$ *J*= 6.9 Hz, 3 x 2H), 8.56 - 8.35 (m, 3 x 6H), 7.24 - 7.01 (m, 3 x 14H), 5.11 (p,*J*= 7.0 Hz, 3 x 2H), 1.71 (d,*J* $= 7.1 \text{ Hz}, 3 \text{ x } 6\text{H}). {}^{13}\text{C NMR} (100 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 167.57, 166.99, 148.75, 148.51, 143.14, 141.70, 133.52, 128.51, 127.66, 126.60, 126.31, 125.93, 123.56, 52.25, 20.61. \text{ HRMS} (ESI) calcd. for C_{112}H_{96}F_{12}La_{2}N_{18}O_{24}S_{4} [La_{2}(L1^{SS})_{3} + 40\text{Tf}]^{2+}: 1355.6841, \text{ found } 1355.6792. \text{ Elemental analysis calcd. for C}_{114}H_{96}F_{18}La_{2}N_{18}O_{3}O_{6}\cdot 8H_{2}O: C 43.41, \text{H } 3.58, \text{N } 7.99, \text{ found: C } 43.35, \text{H } 3.60, \text{N } 7.92. \text{ } 128.51, 127.66, 126.60, 126.31, 125.93, 128.51, 127.66, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61, 126.61,$

 $[La_{2}L^{1RR}_{3}]: (13.5 \text{ mg}, 4.48 \times 10^{-3} \text{ mmol}, 82.4\% \text{ yield}), {}^{1}\text{H} \text{ NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 10.34 (s, 3 \times 2\text{H}), 9.01 (d,$ *J* $= 7.0 \text{ Hz}, 3 \times 2\text{H}), 8.61 - 8.39 (m, 3 \times 6\text{H}), 7.25 - 6.97 (m, 3 \times 14\text{H}), 5.11 (p,$ *J* $= 7.0 \text{ Hz}, 3 \times 2\text{H}), 1.71 (d,$ *J* $= 7.1 \text{ Hz}, 3 \times 6\text{H}). {}^{13}\text{C} \text{ NMR} (101 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 167.52, 166.92, 148.69, 148.45, 143.05, 141.64, 133.46, 128.44, 127.59, 126.53, 126.25, 125.86, 123.48, 52.21, 20.55. \text{ HRMS} (ESI) calcd. for C_{111}H_{95}F_{9}La_{2}N_{18}O_{21}S_{3} [La_{2}(L1^{RR})_{3} + 30\text{ Tf} - \text{H}^{+}]^{2+}: 1280.7042, \text{ found } 1280.7103. \text{ Elemental analysis calcd. for } C_{114}H_{96}F_{18}La_{2}N_{18}O_{3}O_{6} \cdot 19H_{2}O: C 40.80, \text{H} 4.03, \text{N} 7.52, \text{ found: } C 40.90, \text{H} 3.57, \text{N} 7.30.$

 $[Sm_{2}L1^{SS}_{3}]: (14.5 mg, 4.78 x 10⁻³ mmol, 87.9\% yield), {}^{1}H NMR (400 MHz, CD_{3}CN, 299 K, \delta): 10.40 (s, 3 x 2H), 9.11 (d,$ *J*= 6.8 Hz, 3 x 2H), 8.59 - 8.31 (m, 3 x 6H), 7.18 (dd,*J*= 5.2, 1.9 Hz, 3 x 6H), 7.07 (dd,*J*= 6.8, 2.8 Hz, 3 x 4H), 6.98 (s, 3 x 4H), 5.08 - 4.92 (m, 3 x 2H), 1.66 (d,*J* $= 7.0 Hz, 3 x 6H). {}^{13}C NMR (125 MHz, CD_{3}CN, 300 K, \delta): 169.49, 168.71, 149.49, 149.22, 143.59, 141.77, 133.34, 128.61, 127.66, 125.87, 125.66, 125.32, 123.32, 52.29, 20.63. HRMS (ESI) calcd. for C₁₁₁H₉₆F₉N₁₈O₂₁S₃Sm₂ [Sm₂(L1^{SS})₃ + 3OTf]³⁺: 861.8131, found 861.8192. Elemental analysis calcd. for C₁₁₄H₉₆F₁₈Sm₂N₁₈O₃₀S₆· 18H₂O: C 40.78, H 3.96, N 7.51, found: C 40.80, H 3.53, N 7.42.$

 $[Sm_2 L1^{RR}_3]: (12.1 mg, 3.99 x 10^3 mmol, 73.3\% yield), {}^{1}H NMR (495 MHz, CD_3CN, 299 K, \delta): 10.15 (s, 3 x 2H), 8.89 (s, 3 x 2H), 8.45 - 8.32 (m, 3 x 6H), 7.13 (s, 3 x 6H), 7.03 (s, 3 x 4H), 6.92 (s, 3 x 4H), 5.01 - 4.95 (m, 3 x 2H), 1.72 - 1.50 (m, 3 x 6H). {}^{13}C NMR (125 MHz, CD_3CN, 300 K, \delta): 169.48, 168.71, 149.49, 149.23, 143.59, 141.76, 133.34, 128.61, 127.67, 125.87, 125.66, 125.31, 123.32, 52.28, 20.63. HRMS (ESI) calcd. for C_{111}H_{96}F_{9}N_{18}O_{21}S_{3}Sm_2 [Sm_2(L1^{RR})_3 + 3OTf]^{3+}: 861.8131, found 861.8160. Elemental analysis calcd. for C_{114}H_{96}F_{18}Sm_2N_{18}O_{30}S_6: 18H_2O: C 40.78, H 3.96, N 7.51, found: C 40.80, H 3.36, N 7.35.$

 $[Eu_{2}L1^{SS}_{3}]: (14.1 \text{ mg}, 4.64 \text{ x } 10^{-3} \text{ mmol}, 85.4\% \text{ yield}), ^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 8.12 (s, 3 \text{ x } 4\text{H}), 7.40 (s, 3 \text{ x } 2\text{H}), 7.20 (t,$ *J*= 7.9 Hz, 3 x 2H), 7.05 (d,*J*= 3.9 Hz, 3 x 10H), 6.45 (d,*J*= 8.0 Hz, 3 x 2H), 6.36 (d,*J*= 7.9 Hz, 3 x 2H), 6.14 (s, 3 x 2H), 5.04 (s, 3 x 2H), 2.04 (d,*J* $= 6.0 \text{ Hz}, 3 \text{ x } 6\text{H}). ^{13}\text{C NMR} (125 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 160.24, 155.37, 142.84, 142.47, 141.94, 134.83, 128.50, 127.50, 125.65, 125.29, 91.92, 91.80, 51.70, 21.73. \text{ HRMS} (ESI) calcd. for C_{112}H_{96}Eu_{2}F_{12}N_{18}O_{24}S_4 [Eu_{2}(L1^{SS})_{3} + 40\text{ Tf}]^{2^{+}}: 1369.1985, \text{ found } 1369.1962. \text{ Elemental analysis calcd. for } C_{114}H_{96}F_{18}Eu_{2}N_{18}O_{30}S_{6} \cdot 18H_{2}O: C 40.74, \text{ H } 3.96, \text{ N } 7.50, found: C 40.83, \text{ H } 3.56, \text{ N } 7.44.$

 $[Eu_{2}L^{1RR}_{3}]: (13.6 \text{ mg}, 4.48 \times 10^{-3} \text{ mmol}, 82.3\% \text{ yield}), {}^{1}\text{H} \text{ NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 8.07 (s, 3 \times 4\text{H}), 7.13 (d,$ *J* $= 15.9 \text{ Hz}, 3 \times 4\text{H}), 6.99 (s, 3 \times 10\text{H}), 6.37 (s, 3 \times 2\text{H}), 6.28 (d,$ *J* $= 8.2 \text{ Hz}, 3 \times 2\text{H}), 6.09 (s, 3 \times 2\text{H}), 4.80 (s, 3 \times 2\text{H}), 1.99 (s, 3 \times 6\text{H}). \\ {}^{13}\text{C} \text{ NMR} (125 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 163.43, 160.28, 155.37, 142.83, 142.46, 142.02, 134.81, 128.50, 127.50, 125.66, 125.29, \\ 91.94, 91.80, 51.70, 21.73. \text{ HRMS} (\text{ESI}) \text{ calcd. for } \text{C}_{112}\text{H}_{96}\text{Eu}_{2}\text{F}_{12}\text{N}_{18}\text{O}_{24}\text{S}_{4} [\text{Eu}_{2}(\text{L1}^{\text{RR}})_{3} + 40\text{Tf}^{-2}^{+1}: 1369.1985, \text{ found } 1369.1949. \\ \text{Elemental analysis calcd. for } \text{C}_{114}\text{H}_{96}\text{F}_{18}\text{Eu}_{2}\text{N}_{18}\text{O}_{3}\text{S}_{6}\cdot\text{4H}_{2}\text{O}: C 44.05, \text{H} 3.37, \text{N} 8.11, \text{ found: C } 44.10, \text{H} 3.38, \text{N} 7.99. \\ \end{array}$

 $[Gd_{2}L1^{SS}_{3}]: (12.5 mg, 4.10 x 10^{-3} mmol, 75.4\% yield), HRMS (ESI) calcd. for C_{111}H_{96}F_{9}N_{18}O_{21}S_{3}Gd_{2} [Gd_{2}(L1^{SS})_{3} + 30Tf]^{3+}: 866.4836, found 861.4828. Elemental analysis calcd. for C_{114}H_{96}F_{18}Gd_{2}N_{18}O_{30}S_{6}\cdot 21H_{2}O: C 39.98, H 4.06, N 7.36, found: C 40.01, H 3.54, N 7.30.$

 $[Gd_{2}L1^{RR}_{3}]: (14.3 \text{ mg}, 4.69 \text{ x } 10^{-3} \text{ mmol}, 86.2\% \text{ yield}), \text{HRMS (ESI) calcd. for } C_{111}H_{96}F_{9}N_{18}O_{21}S_{3}Gd_{2} [Gd_{2}(L1^{RR})_{3} + 30Tf]^{3+}: 866.4836, \text{found } 861.4865. \text{ Elemental analysis calcd. for } C_{114}H_{96}F_{18}Gd_{2}N_{18}O_{30}S_{6} \cdot 22H_{2}O: C 39.77, H 4.10, N 7.32, \text{found: } C 39.88, H 3.30, N 7.20.$

 $[Tb_{2}L1^{SS}_{3}]: (14.7 \text{ g}, 4.82 \text{ x} 10^{-3} \text{ mmol}, 88.6\% \text{ yield}), \text{HRMS} (ESI) \text{ calcd. for } C_{109}H_{94}F_{3}N_{18}O_{15}STb_{2} [Tb_{2}(L1^{SS})_{3} + OTf^{-} 2H^{+}]^{3+}: 767.5113, \text{ found } 767.5154. \text{ Elemental analysis calcd. for } C_{114}H_{96}F_{18}Tb_{2}N_{18}O_{30}S_{6} \cdot 16H_{2}O: C 41.01, H 3.86, N 7.55, \text{ found: } C 41.07, H 3.49, N 7.48.$

 $[Tb_{2}L1^{RR}_{3}]: (13.6 \text{ g}, 4.46 \text{ x} 10^{-3} \text{ mmol}, 81.9\% \text{ yield}), \text{HRMS} (ESI) \text{ calcd. for } C_{112}H_{96}Eu_{2}F_{12}N_{18}O_{24}S_{4} [Tb_{2}(L1^{RR})_{3} + 40Tf]^{2+}: 1300.7232, \text{ found } 1300.7169. \text{ Elemental analysis calcd. for } C_{114}H_{96}F_{18}Tb_{2}N_{18}O_{30}S_{6}\cdot 15H_{2}O: C 41.24, H 3.82, N 7.59, \text{ found: } C 41.36, H 3.33, N 7.48.$

 $[Lu_{2}L1^{SS}_{3}]: (14.2 \text{ g}, 4.61 \text{ x } 10^{-3} \text{ mmol}, 84.7\% \text{ yield}), {}^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 10.42 (\text{s}, 3 \text{ x } 2\text{H}), 9.02 (\text{d}, J = 6.8 \text{ Hz}, 3 \text{ x } 2\text{H}), 8.56 - 8.33 (\text{m}, 3 \text{ x } 6\text{H}), 7.17 (\text{ddd}, J = 8.9, 5.5, 3.3 \text{ Hz}, 3 \text{ x } 6\text{H}), 7.02 (\text{d}, J = 5.0 \text{ Hz}, 3 \text{ x } 8\text{H}), 4.97 (\text{p}, J = 6.9 \text{ Hz}, 3 \text{ x } 2\text{H}), 1.75 - 1.58 (\text{m}, 3 \text{ x } 6\text{H}). {}^{13}\text{C NMR} (125 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 166.82, 166.38, 147.04, 146.66, 143.08, 141.74, 133.26, 128.66, 127.61, 126.31, 125.79, 125.69, 123.07, 52.29, 20.77. \text{ HRMS} (\text{ESI}) \text{ calcd. for } C_{111}H_{96}F_{9}Lu_{2}N_{18}O_{21}S_{3} \text{ [Lu}_{2}(L1^{SS})_{3} + 30\text{Tf}]^{3+:} 878.1615, \text{found } 878.1616. \text{ Elemental analysis calcd. for } C_{114}H_{96}F_{18}Lu_{2}N_{18}O_{30}S_{6}\cdot7H_{2}\text{O}: \text{C } 42.68, \text{H } 3.46, \text{N } 7.86, \text{found: C } 42.66, \text{H } 3.39, \text{N } 7.77.$

 $[Lu_2 L1^{RR}_3]: (14.4 \text{ g}, 4.67 \text{ x} 10^{-3} \text{ mmol}, 85.9\% \text{ yield}), {}^{1}\text{H} \text{NMR} (400 \text{ MHz}, \text{CD}_3\text{CN}, 299 \text{ K}, \delta): 10.31 (\text{s}, 3 \text{ x} 2\text{H}), 8.93 (\text{s}, 3 \text{ x} 2\text{H}), 8.38 (\text{s}, 3 \text{ x} 6\text{H}), 7.13 (\text{s}, 3 \text{ x} 6\text{H}), 6.97 (\text{s}, 3 \text{ x} 8\text{H}), 4.92 (\text{d}, J = 7.5 \text{ Hz}, 3 \text{ x} 2\text{H}), 1.61 (\text{d}, J = 7.1 \text{ Hz}, 3 \text{ x} 6\text{H}). {}^{13}\text{C} \text{NMR} (125 \text{ MHz}, \text{CD}_3\text{CN}, 300 \text{ K}, \delta): 166.41, 165.98, 146.63, 146.33, 142.69, 141.32, 128.26, 127.21, 125.87, 125.43, 125.29, 122.64, 51.86, 20.36. \text{HRMS} (\text{ESI}) \text{ calcd. for } \text{C}_{112}\text{H}_{96}\text{F}_{12}\text{Lu}_2\text{N}_{18}\text{O}_{24}\text{S}_4 [Lu_2(L1^{RR})_3 + 4\text{OTf}]^{2+:} 1391.7185, \text{ found } 1391.7209. \text{ Elemental analysis calcd. for } \text{C}_{114}\text{H}_{96}\text{F}_{18}\text{Lu}_2\text{N}_{18}\text{O}_{30}\text{S}_6 \cdot 7\text{H}_2\text{O}: \text{C} 42.68, \text{H} 3.46, \text{N} 7.86, \text{ found}: \text{C} 42.74, \text{H} 3.54, \text{N} 7.84. \text{ } \text{N} 7.84 \text{ } \text{ } \text{N} 7.84 \text{ } \text{ } \text{N} 7.84 \text{ } \text{ } \text{N} 7.84 \text{ } \text{N} 7.84 \text{ } \text{ } \text{N} 7.84 \text{ } \text{ } \text{N} 7.84 \text{ } \text{ } \text{N}$

General synthetic procedures of [Ln₄L1₆]



 Ln_2L1_3 (0.66 mmol) were dissolved in CH₃CN (0.6 ml) and ether was allowed to slowly diffuse into the solution. The solution was decanted, and the crystal was washed with ether and dried under vacuum to obtain the homometallic tetrahedron crystal.

 $[Eu_4L1^{SS}_6]: (1.80 mg, 2.96 x 10^4 mmol, 90.0\% yield), {}^{1}H NMR (495 MHz, CD_3CN, 299 K, \delta): 9.04 (s, 6 x 4H), 7.81 (s, 6 x 2H), 7.31 (s, 6 x 2H), 6.79 (s, 6 x 4H), 6.40 (d,$ *J* $= 31.8 Hz, 6 x 8H), 5.88 (s, 6 x 2H), 5.47 (s, 6 x 2H), 4.09 (s, 6 x 2H), 2.34 (s, 6 x 6H). {}^{13}C NMR (125 MHz, CD_3CN, 300 K, \delta): 161.73, 156.50, 153.58, 142.91, 136.72, 135.57, 133.80, 127.79, 126.76, 125.52, 124.96, 121.93, 119.36, 92.00, 91.32, 52.29, 22.27. HRMS (ESI) calcd. for C₂₂₅H₁₉₂Eu₄F₂₇N₃₆O₅₁S₉ [Eu₄(L1^{SS})₆ + 9 OTf]³⁺: 1875.2490, found 1875.2516. Elemental analysis calcd. for C₂₂₈H₁₉₂Eu₄F₃₆N₃₆O₆₀S₁₂· 11H₂O· C₆H₁₄O: C 44.10, H 3.61, N 7.91, found: C 44.12, H 3.68, N 7.83.$

 $[Eu_4 L^{1RR}_6]: (1.68 mg, 2.77 x 10^{-4} mmol, 83.8\% yield), {}^{1}H NMR (495 MHz, CD_3CN, 299 K, \delta) 9.03 (s, 6 x 4H), 7.80 (s, 6 x 2H), 7.33 (s, 6 x 2H), 6.79 (s, 6 x 4H), 6.40 (d,$ *J* $= 30.9 Hz, 6 x 8H), 5.89 (s, 6 x 2H), 5.47 (s, 6 x 2H), 4.11 (s, 6 x 2H), 2.33 (s, 6 x 6H). {}^{13}C NMR (125 MHz, CD_3CN, 300 K, \delta): 161.81, 156.51, 153.57, 142.91, 136.77, 135.56, 133.85, 128.50, 127.79, 126.76, 125.52, 124.96, 121.96, 119.39, 92.10, 91.38, 52.29, 22.26. HRMS (ESI) calcd. for C₂₂₅H₁₉₂Eu₄F₂₇N₃₆O₅₁S₉ [Eu₄(L1^{RR})₆ + 9 OTf]³⁺: 1875.2490, found 1875.2516. Elemental analysis calcd. for C₂₂₈H₁₉₂Eu₄F₃₆N₃₆O₆₀S₁₂· 14H₂O· 2(C₆H₁₄O): C 44.15, H 3.83, N 7.72, found: C 44.13, H 3.78, N 7.72.$

 $[Sm_4 L1^{SS}_6]: (1.74 mg, 2.87 x 10^{-4} mmol, 86.9\% yield), {}^{1}H NMR (495 MHz, CD_3CN, 299 K, \delta) 9.91 (s, 6 x 2H), 9.20 (s, 6 x 2H), 8.76 (d,$ *J*= 9.6 Hz, 6 x 2H), 8.63 (s, 6 x 2H), 8.54 (d,*J*= 8.6 Hz, 6 x 2H), 7.19 – 6.98 (m, 6 x 10H), 6.14 (s, 6 x 4H), 4.52 (d,*J* $= 8.7 Hz, 6 x 2H), 1.43 (s, 6 x 6H). {}^{13}C NMR (125 MHz, CD_3CN, 300 K, \delta): 170.25, 167.32, 150.56, 148.82, 143.61, 142.40, 132.68, 128.54, 127.64, 126.67, 125.68, 125.39, 122.20, 121.60, 119.64, 52.47, 20.73. HRMS (ESI) calcd. for C₂₂₂H₁₉₁F₁₈N₃₆O₄₂S₆Sm₄ [Sm₄(L1^{SS})₆ + 6 OTf⁺ - H⁺]⁵⁺: 1034.1745, found 1034.1748. Elemental analysis calcd. for C₂₂₈H₁₉₂Sm₄F₃₆N₃₆O₆₀S₁₂: 15H₂O·2(C₆H₁₄O): C 44.07, H 3.85, N 7.71, found: C 43.91, H 3.51, N 7.76.$

 $[Sm_4L1^{RR}_6]: (1.89 g, 3.12 x 10^4 mmol, 94.4\% yield), {}^{1}H NMR (495 MHz, CD_3CN, 299 K, \delta) {}^{1}H NMR (495 MHz, Acetonitrile$ $d_3) \delta 9.93 (s, 6 x 2H), 9.22 (s, 6 x 2H), 8.76 (d,$ *J*= 8.9 Hz, 6 x 2H), 8.74 - 8.59 (m, 6 x 2H), 8.54 (d,*J*= 9.3 Hz, 6 x 2H), 7.07 (dd,*J* $= 29.5, 9.9 Hz, 6 x 10H), 6.13 (s, 6 x 4H), 4.52 (s, 6 x 2H), 1.44 (s, 6 x 6H). {}^{13}C NMR (125 MHz, CD_3CN, 300 K, \delta): 170.26, 167.34, 150.55, 148.83, 143.61, 142.42, 132.68, 128.54, 127.64, 126.67, 125.86, 125.67, 125.41, 122.21, 121.62, 119.64, 52.47, 20.73. HRMS (ESI) calcd. for C₂₂₅H₁₉₂Sm₄F₂₇N₃₆O₅₁S₉ [Sm₄(L1^{RR})₆ + 9 OTf]³⁺: 1873.2460, found 1873.2405. Elemental analysis calcd. for C₂₂₈H₁₉₂Sm₄F₃₆N₃₆O₆₀S₁₂: 12H₂O·C₆H₁₄O: C 44.02, H 3.63, N 7.90, found: C 44.03, H 3.72, N 7.92.$

 $[Gd_4L1^{SS}_6]: (1.45 mg, 2.38 x 10^{-4} mmol, 72.1\% yield), HRMS (ESI) calcd for C_{224}H_{192}F_{24}Gd_4N_{36}O_{48}S_8 [Gd_4(L1^{SS})_6 + 8 OTf]^{4+} is 1374.4520, found 1374.4512. Elemental analysis calcd. for C_{228}H_{192}Gd_4F_{36}N_{36}O_{60}S_{12} \cdot 12H_2O: C 43.40, H 3.45, N 7.99, found: C 43.31, H 3.38, N 7.78.$

 $[Gd_4L1^{RR}_6]: (1.23 mg, 2.02 x 10^4 mmol, 61.2\% yield), HRMS (ESI) calcd for C_{225}H_{192}F_{27}Gd_4N_{36}O_{51}S_9 [Gd_4(L1^{RR})_6 + 9 OTf]^{4+} is 1882.2535 (100\%), found 1882.2499. Elemental analysis calcd. for C_{228}H_{192}Gd_4F_{36}N_{36}O_{60}S_{12}\cdot 13H_2O: C 43.28, H 3.47, N 7.97, found: C 43.22, H 3.58, N 7.85.$

 $[Tb_4L1^{SS}_6]: (1.37 mg, 2.25 x 10^4 mmol, 68.1\% yield), HRMS (ESI) calcd for C_{222}H_{191}F_{18}N_{36}O_{42}S_6Tb_4 [Tb_4(L1^{SS})_6 + 6 OTf - H^+]^{5+} is 1040.9802, found 1040.9800. Elemental analysis calcd. for C_{228}H_{192}Tb_4F_{36}N_{36}O_{60}S_{12} \cdot 12H_2O \cdot C_6H_{14}O: C 43.79, H 3.61, N 7.86, found: C 43.74, H 3.68, N 7.81.$

 $[Tb_4L1^{RR}_6]: (1.66 mg, 2.72 x 10^4 mmol, 82.5\% yield), HRMS (ESI) calcd for C_{222}H_{191}F_{18}N_{36}O_{42}S_6Tb_4 [Tb_4(L1^{SS})_6 + 6 OTf - H^+]^{5+} is 1040.9802, found 1040.9839. Elemental analysis calcd. for C_{228}H_{192}Tb_4F_{36}N_{36}O_{60}S_{12}\cdot 17H_2O\cdot C_6H_{14}O: C 43.18, H 3.72, N 7.75, found: C 43.13, H 3.46, N 7.67.$

 $[Lu_4L1^{SS}_6]: (1.89 mg, 3.07 x 10^4 mmol, 92.9\% yield), {}^{1}H NMR (400 MHz, CD_3CN, 299 K, \delta) 10.20 (s, 6 x 2H), 9.07 (s, 6 x 2H), 8.46 (dd,$ *J*= 10.6, 5.7 Hz, 6 x 6H), 7.05 (dt,*J*= 21.9, 6.3 Hz, 6 x 10H), 6.71 (d,*J*= 4.9 Hz, 6 x 4H), 5.02 (q,*J*= 6.5 Hz, 6 x 2H), 1.65 (t,*J*= 5.9 Hz, 6 x 6H). HRMS (ESI) calcd. for C₂₂₅H₁₉₂Lu₄F₂₇N₃₆O₅₁S₉ [Lu₄(L1^{SS})₆ + 9 OTf]³⁺: 1905.6090, found 1905.6060.

 $[Lu_4L1^{RR}_6]: (1.34 \text{ mg}, 2.17 \text{ x } 10^{-4} \text{ mmol}, 65.9\% \text{ yield}), {}^{1}\text{H NMR} (405 \text{ MHz}, \text{CD}_3\text{CN}, 299 \text{ K}, \delta) 10.22 (s, 6 \text{ x } 2\text{H}), 9.07 (s, 6 \text{ x } 2\text{H}), 8.47 (d,$ *J*= 5.5 Hz, 6 x 6H), 7.21 - 6.91 (m, 6 x 10H), 6.72 (s, 6 x 4H), 5.02 (p,*J*= 7.0 Hz, 6 x 2H), 1.66 (d,*J* $= 7.1 \text{ Hz}, 6 \text{ x } 6\text{H}). \text{HRMS} (\text{ESI}) \text{ calcd. for } \text{C}_{225}\text{H}_{192}\text{Lu}_4\text{F}_{27}\text{N}_{36}\text{O}_{51}\text{S}_9 [\text{Lu}_4(\text{L1}^{\text{RR}})_6 + 9 \text{ OTf}]^{3+}: 1905.6090, \text{ found } 1905.6080.$

General synthetic procedures of [Ln2L3]



To a white suspension of L3 (30 mg, 0.039 mmol, 1.5 equiv.) in a mixture of 2.55 ml of DCM/MeOH (12:1, v/v), a solution of $Ln(OTf)_3$ (0.026 mmol, 1 equiv.) (Ln = La, Sm, Eu, Gd, Tb and Lu) in 2.35 ml of CH₃CN was added. The solution was changed to yellow immediately. The solution was then reacted for 16 hrs at room temperature and pressure. After 16 hrs, the solvent was removed under reduced pressure to give desired product.

 $[La_{2}L3^{85}_{3}]: (39.4 \text{ mg}, 0.114 \text{ mmol}, 86.9\% \text{ yield}), {}^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 10.21 (s, 3 x 2\text{H}), 9.07 (d,$ *J*= 7.1 Hz, 3 x 2H), 8.67 - 8.40 (m, 3 x 6H), 7.88 (d,*J*= 8.3 Hz, 3 x 4H), 7.31 - 7.20 (m, 3 x 6H), 7.14 (s, 3 x 4H), 7.02 (d,*J*= 8.3 Hz, 3 x 4H), 6.95 (s, 3 x 4H), 5.14 - 5.05 (m, 3 x 2H), 1.76 (d,*J* $= 7.1 \text{ Hz}, 3 x 6\text{H}). {}^{13}\text{C NMR} (101 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 168.78, 168.17, 150.80, 150.04, 144.52, 142.98, 139.58, 130.07, 129.10, 128.65, 128.40, 127.82, 127.37, 123.02, 119.33, 118.78, 55.51, 22.11. \text{HRMS} (ESI) calcd. for C_{147}\text{H}_{120}\text{F}_{9}\text{La}_{2}\text{N}_{18}\text{O}_{21}\text{S}_{3} [La_{2}(L3^{88})_{3} + 3 \text{ OTf}]^{3+:} 1006.2012, found 1006.2037. Elemental analysis calcd. for C_{150}\text{H}_{120}\text{F}_{18}\text{N}_{18}\text{O}_{30}\text{S}_{6}\text{La}_{2}\cdot\text{7H}_{2}\text{O}: C 50.14, \text{H } 3.76, \text{N} 7.02, found: C 50.24, \text{H } 4.21, \text{N} 6.71. \text{C} \text{S}_{12} \text{ M}_{12} \text{ M}_{12}\text{ M}_{12$

 $[La_2L3^{RR}_3]: (37.9 \text{ mg}, 0.109 \text{ mmol}, 83.7\% \text{ yield}), {}^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_3\text{CN}, 299 \text{ K}, \delta): 10.21 (s, 3 x 2H), 9.07 (d,$ *J*= 6.6 Hz, 3 x 2H), 8.54 (d,*J*= 21.5 Hz, 3 x 6H), 7.88 (d,*J*= 8.3 Hz, 3 x 4H), 7.25 (s, 3 x 6H), 7.13 (s, 3 x 4H), 7.02 (d,*J*= 8.2 Hz, 3 x 4H), 6.96 (s, 3 x 4H), 5.08 (s, 3 x 2H), 1.76 (d,*J* $= 7.1 \text{ Hz}, 3 x 6H). {}^{13}\text{C NMR} (125 \text{ MHz}, \text{CD}_3\text{CN}, 300 \text{ K}, \delta): 167.40, 166.79, 149.42, 148.66, 143.13, 141.62, 138.50, 138.19, 135.54, 128.70, 127.72, 127.27, 127.02, 126.39, 125.98, 121.64, 52.14, 22.24. \text{ HRMS} (ESI) calcd. for C_{147}H_{120}F_9La_2N_{18}O_{21}S_3 [La_2(L3^{RR})_3 + 3 \text{ OTf}]^{3+}: 1006.2012, found 1006.2037. Elemental analysis calcd. for C_{150}H_{120}F_{18}N_{18}O_{30}S_6La_2 \cdot 6H_2O: C 50.40, \text{H} 3.72, \text{N} 7.05, found: C 50.42, \text{H} 3.95, \text{N} 6.90.$

 $[Sm_{2}L3^{SS}_{3}]: (38.1 mg, 0.0109 mmol, 83.5\% yield), {}^{1}H NMR (400 MHz, CD_{3}CN, 299 K, \delta): 10.15 (s, 3 x 2H), 9.03 (d,$ *J*= 7.0 Hz, 3 x 2H), 8.44 (dq,*J*= 7.3, 4.3, 3.5 Hz, 3 x 6H), 7.89 (d,*J*= 8.3 Hz, 3 x 4H), 7.35 - 7.16 (m, 3 x 6H), 7.10 (dd,*J*= 7.0, 2.5 Hz, 3 x 4H), 6.98 (d,*J*= 8.2 Hz, 3 x 4H), 6.91 (s, 3 x 4H), 5.19 (q,*J*= 7.0 Hz, 3 x 2H), 1.77 (d,*J* $= 6.9 Hz, 3 x 6H). {}^{13}C NMR (101 MHz, CD_{3}CN, 300K, \delta): 169.41, 168.43, 149.63, 148.99, 143.29, 141.71, 138.44, 137.96, 135.57, 128.69, 127.62, 127.20, 126.80, 125.81, 125.20, 121.36, 52.31, 20.90. HRMS (ESI) calcd. for C₁₄₇H₁₂₀F₉Sm₂N₁₈O₂₁S₃ [Sm₂(L3^{SS})₃ + 3 OTf]³⁺: 1013.8759, found 1013.8749. Elemental analysis calcd. for C₁₅₀H₁₂₀F₁₈N₁₈O₃₀S₆Sm₂·8H₂O: C 49.58, H 3.77, N 6.94, found: C 49.59, H 4.07, N 6.81.$

 $[Sm_{2}L3^{RR}_{3}]: (36.5 mg, 0.0104 mmol, 79.9\% yield), {}^{1}H NMR (400 MHz, CD_{3}CN, 299 K, \delta): 10.11 (s, 3 x 2H), 9.00 (d,$ *J*= 7.0 Hz, 3 x 2H), 8.43 (dq,*J*= 7.3, 4.3, 3.5 Hz, 3 x 6H), 7.89 (d,*J*= 8.3 Hz, 3 x 4H), 7.42 - 7.17 (m, 3 x 6H), 7.10 (dd,*J*= 7.0, 2.5 Hz, 3 x 4H), 6.98 (d,*J*= 8.2 Hz, 3 x 4H), 6.91 (s, 3 x 4H), 5.19 (q,*J*= 7.0 Hz, 3 x 2H), 1.78 (d,*J* $= 6.9 Hz, 3 x 6H). {}^{13}C NMR (101 MHz, CD_{3}CN, 300K, \delta): 169.42, 168.46, 149.74, 149.03, 143.40, 141.67, 138.49, 138.02, 135.53, 128.68, 127.62, 127.22, 126.87, 125.80, 125.25, 121.32, 52.25, 20.81. HRMS (ESI) calcd. for C₁₄₄H₁₁₈N₁₈O₁₂Sm₂ [Sm₂(L3^{RR})₃ - 3H⁺]³⁺: 863.9162, found 863.9186. Elemental analysis calcd. for C₁₅₀H₁₂₀F₁₈N₁₈O₃₀S₆Sm₂·17H₂O: C 47.46, H 4.09, N 6.64, found: C 47.34, H 3.96, N 6.48.$

 $[Eu_{2}L3^{SS}_{3}]: (36.4 \text{ mg}, 0.0104 \text{ mmol}, 79.8 \% \text{ yield}), ^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 8.21 - 7.96 (m, 3 x 4\text{H}), 7.42 (s, 3 x 2\text{H}), 7.24 (s, 3 x 4\text{H}), 7.15 (d,$ *J* $= 5.8 \text{ Hz}, 3 x 6\text{H}), 7.08 (s, 3 x 4\text{H}), 6.96 (s, 3 x 4\text{H}), 6.76 (s, 3 x 2\text{H}), 6.58 (s, 3 x 4\text{H}), 5.36 (s, 3 x 2\text{H}), 4.99 (s, 3 x 2\text{H}), 1.76 (s, 3 x 6\text{H}). ^{13}\text{C NMR} (125 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 155.25, 142.22, 138.62, 137.71, 135.36, 128.25, 127.19, 126.81, 126.69, 125.21, 122.15, 92.13, 91.52, 50.88, 21.13. \text{ HRMS} (ESI) calcd. for C_{147}H_{120}Eu_{2}F_{9}N_{18}O_{21}S_{3} [Eu_{2}(L3^{SS})_{3} + 30Tf]^{3+}: 1015.2111, found 1015.2097. Elemental analysis calcd. for C_{150}H_{120}F_{18}N_{18}O_{30}S_{6}Eu_{2}\cdot4H_{2}O: C 50.54, \text{H } 3.62, \text{N } 7.07, found: C 50.55, \text{H } 3.90, \text{N } 6.50.$

 $[Eu_{2}L3^{RR}_{3}]: (37.6 \text{ mg}, 0.0108 \text{ mmol}, 82.3\% \text{ yield}), ^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 8.02 (d,$ *J*= 49.6 Hz, 3 x 4H), 7.47 (d,*J*= 38.6 Hz, 3 x 2H), 7.23 (s, 3 x 4H), 7.16 (d,*J*= 5.2 Hz, 3 x 6H), 7.07 (s, 3 x 4H), 6.97 (s, 3 x 4H), 6.79 (s, 3 x 2H), 6.59 (s, 3 x 4H), 5.36 (s, 3 x 2H), 5.03 (s, 3 x 2H), 1.73 (d,*J* $= 22.2 \text{ Hz}, 3 x 6\text{H}). ^{13}\text{C NMR} (125 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 155.62, 142.66, 138.99, 138.10, 135.80, 128.64, 127.58, 127.20, 127.07, 125.61, 122.56, 92.56, 91.97, 51.29, 21.55. \text{ HRMS} (ESI) calcd. for C_{147}\text{H}_{120}\text{Eu}_{2}\text{F}_{9}\text{N}_{18}\text{O}_{21}\text{S}_{3} [Eu_{2}(L3^{RR})_{3} + 3\text{OTf}]^{3+}: 1015.2111, \text{ found} 1015.2097. Elemental analysis calcd. for C_{150}\text{H}_{120}\text{F}_{18}\text{N}_{18}\text{O}_{30}\text{S}_{6}\text{Eu}_{2}\cdot\text{5H}_{20}\text{C} \text{ C} 50.28, \text{H} 3.66, \text{N} 7.04, \text{ found: C} 50.26, \text{H} 4.03, \text{N} 6.99.$

 $[Gd_{2}L3^{SS_{3}}]: (39.5 mg, 0.0113 mmol, 86.2\% yield), HRMS (ESI) calcd. for C_{144}H_{117}Gd_{2}N_{18}O_{12} [Gd_{2}(L3^{SS})_{3} - 3H^{+}]^{3+}: 868.5869, found 868.5845. Elemental analysis calcd. for C_{150}H_{120}F_{18}N_{18}O_{30}S_{6}Gd_{2}\cdot 18H_{2}O: C 47.07, H 4.11, N 6.59, found: C 46.97, H 3.72, N 6.40.$

 $[Gd_{2}L3^{RR}_{3}]: (37.6 mg, 0.0107 mmol, 82.0\% yield), HRMS (ESI) calcd. for C_{147}H_{120}F_{9}Gd_{2}N_{18}O_{21}S_{3} [Gd_{2}(L3^{RR})_{3} + 3OTf]^{3+}: 1018.5452, found 1018.5465. Elemental analysis calcd. for C_{150}H_{120}F_{18}N_{18}O_{30}S_{6}Gd_{2}\cdot 23H_{2}O: C 45.99, H 4.27, N 6.44, found: C 45.88, H 3.76, N 6.21.$

 $[Tb_{2}L3^{SS}_{3}]: (37.2 \text{ mg}, 0.0106 \text{ mmol}, 81.1\% \text{ yield}), \text{HRMS} (ESI) \text{ calcd. for } C_{147}H_{120}F_{9}Tb_{2}N_{18}O_{21}S_{3} [Tb_{2}(L3^{SS})_{3} + 3OTf]^{3+}: 1019.5472, \text{ found } 1019.5485. \text{ Elemental analysis calcd. for } C_{150}H_{120}F_{18}N_{18}O_{30}S_{6}Tb_{2}\cdot 16H_{2}O: C 47.47, H 4.04, N 6.64, \text{ found: } C 47.58, H 3.87, N 6.56.$

 $[Tb_{2}L3^{RR}_{3}]: (38.6 \text{ g}, 0.0110 \text{ mmol}, 84.1\% \text{ yield}), \text{HRMS} (ESI) \text{ calcd. for } C_{147}H_{120}F_{9}Tb_{2}N_{18}O_{21}S_{3} [Tb_{2}(L3^{RR})_{3} + 30Tf^{}]^{3+}: 1019.5472, \text{ found } 1019.5485. \text{ Elemental analysis calcd. for } C_{150}H_{120}F_{18}N_{18}O_{30}S_{6}Tb_{2} \cdot 18H_{2}O: C 47.03, H 4.10, N 6.58, \text{ found: } C 47.02, H 4.06, N 6.19.$

 $[Lu_{2}L3^{SS}_{3}]: (38.6 mg, 0.0109 mmol, 83.4\% yield), {}^{1}H NMR (400 MHz, CD_{3}CN, 299 K, \delta): 10.13 (s, 3 x 2H), 8.99 (d,$ *J*= 7.0 Hz, 3 x 2H), 8.54 (dd,*J*= 6.0, 2.8 Hz, 3 x 2H), 8.46 (d,*J*= 6.0 Hz, 3 x 4H), 7.83 – 7.66 (m, 3 x 4H), 7.27 (dt,*J*= 5.6, 2.8 Hz, 3 x 6H), 7.12 – 7.00 (m, 3 x 4H), 6.89 (d,*J*= 8.5 Hz, 3 x 4H), 6.83 (s, 3 x 4H), 4.95 (t,*J*= 7.0 Hz, 3 x 2H), 1.69 (d,*J* $= 7.0 Hz, 3 x 6H). {}^{13}C NMR (101 MHz, CD_{3}CN, 300K, \delta): 166.79, 166.00, 147.36, 146.91, 142.84, 141.66, 138.40, 137.88, 135.37, 128.72, 127.58, 127.16, 126.75, 126.06, 125.62, 120.98, 52.16, 20.90. HRMS (ESI) calcd. for C₁₄₅H₁₁₈F₃Lu₂N₁₈O₁₅S [Lu₂(L3^{SS})₃ + OTf - 2H⁺]³⁺: 930.2509, found 930.2584. Elemental analysis calcd. for C₁₅₀H₁₂₀F₁₈N₁₈O₃₀S₆Lu₂· 3H₂O: C 50.14, H 3.53, N 7.02, found: C 50.10, H 3.74, N 6.90.$

 $[Lu_{2}L3^{RR}_{3}]: (39.3 \text{ mg}, 0.0111 \text{ mmol}, 85.0\% \text{ yield}), {}^{1}\text{H NMR} (400 \text{ MHz}, \text{CD}_{3}\text{CN}, 299 \text{ K}, \delta): 10.18 (s, 3 x 2\text{H}), 9.03 (d, J = 7.1 \text{ Hz}, 3 x 2\text{H}), 8.54 (d, J = 6.2 \text{ Hz}, 3 x 2\text{H}), 8.52 - 8.38 (m, 3 x 4\text{H}), 7.76 (d, J = 8.4 \text{ Hz}, 2\text{H}), 7.36 - 7.21 (m, 3 x 4\text{H}), 7.11 - 6.99 (m, 3 x 4\text{H}), 6.89 (d, J = 8.5 \text{ Hz}, 3 x 4\text{H}), 6.83 (s, 3 x 4\text{H}), 4.94 (t, J = 7.0 \text{ Hz}, 3 x 2\text{H}), 1.69 (d, J = 7.0 \text{ Hz}, 3 x 6\text{H}). {}^{13}\text{C NMR} (101 \text{ MHz}, \text{CD}_{3}\text{CN}, 300 \text{ K}, \delta): 166.79, 165.98, 147.36, 146.92, 142.82, 141.67, 138.38, 137.83, 135.37, 128.72, 127.58, 127.14, 126.74, 126.07, 125.63, 120.99, 52.18, 20.92. \text{ HRMS} (ESI) calcd. for C_{147}\text{H}_{120}\text{F}_9\text{L}u_2\text{N}_{18}\text{O}_{21}\text{S}_3 \text{ [Lu}_2(L3^{SS})_3 + 30\text{Tf}^{-3}\text{H}: 1030.2241, found 1030.2292. Elemental analysis calcd. for C_{150}\text{H}_{120}\text{F}_{18}\text{N}_{18}\text{O}_{30}\text{S}_6\text{L}u_2 \cdot 3\text{H}_2\text{O}: \text{C} 50.14, \text{H} 3.53, \text{N} 7.02, found: \text{C} 50.09, \text{H} 3.95, \text{N} 7.00.$



Supplementary Figure 1. UV-Vis titration of **L1** with Eu(OTf)₃.(Upper) Variation in UV-Vis absorption spectra of titrating **L1**^{SS} (2.79 x 10⁻⁴M, in 48:4:48, v/v/v, of CHCl₃/MeOH/CH₃CN) with Eu(OTf)₃ (0.036M in MeOH) at 298K (Eu:**L1**^{SS} = 0.0–2.0). (Bottom)Variation of absorbance at four different wavelengths upon titrating **L1**^{SS} with Eu(OTf)₃.



Supplementary Figure 2. UV-Vis titration of **L3** with Eu(OTf)₃.(Upper) Variation in UV-Vis absorption spectra of titrating $L3^{SS}$ (1.96 x 10⁻⁴M, in 48:4:48, v/v/v, of CHCl₃/MeOH/CH₃CN) with Eu(OTf)₃ (0.014M in MeOH) at 298K (Eu: $L3^{SS} = 0.0-2.0$). (Bottom)Variation of absorbance at four different wavelengths upon titrating $L3^{SS}$ with Eu(OTf)₃.



Supplementary Figure 3. Proton NMR of $[Eu_2L1_3]$ (complexation using DCM/MeCN as solvent).



Supplementary Figure 4. Proton NMR of $[Eu_2L1_3](ClO_4)_6$. Free ligand peaks were observed due to the high water content (50%) in perchlorate solution.



Supplementary Figure 5. Proton NMR of $[Eu_2L1_3]Cl_6$.



Supplementary Figure 6. ESI-HRMS of $[Eu_2L1_3]Cl_6$. Complex is only soluble in MeOH and dissociation of complex was found in ESI-HRMS.



Supprementary Figure 7. ¹HNMR of (A) crude Eu complexes prepared by 0.008M L1 (B) 0.0001M L1 in CDCl₃/MeOD/CD₃CN (12/1/12, v/v/v)



Supplementary Figure 8. Variation in ¹HNMR spectra of L1^{RR} (2.15 x 10⁻³M in 70:5:25, v/v/v of CDCl₃/CD₃OD/CD₃CN) with Eu(OTf)₃ (0.09M in CD₃OD) at 298 K.



Supplementary Figure 9. ¹HNMR spectra of [Eu₂(L1)₃]/[Eu₄(L1)₆] at different ligand concentration in CD₃CN at 298 K.



Supplementary Figure 10. ¹HNMR of (A) crude mixture of $[Sm_2(L1)_3]$ and $[Sm_4(L1)_6]$, (B) pure $[Sm_2(L1)_3]$ and (C) pure $[Sm_4(L1)_6]$ in CD₃CN.



Supplementary Figure 11. ¹HNMR of (A) crude Eu complexes prepared by 0.006M L1 in CD₃CN and (B) subjected to 5-fold dilution and performed ¹HNMR instantaneously.



Supplementary Figure 12. ¹HNMR of (A) crude La complexes prepared by 0.006M L1 in CD₃CN and (B) subjected to 5-fold dilution and performed ¹HNMR instantaneously. We hypothesized that the unknown species was La_4L1_6 . However, the exact structure cannot be confirmed due to the poor stability of the unknown species upon dissolution.



Supplementary Figure 13. ¹HNMR of (A) crude $[Lu_2(L1)_3]$ prepared by 0.008M L1, (B) crude $[Lu_2(L1)_3]$ prepared by 0.001M L1 and (C) pure $[Lu_4(L1)_6]$ in CD₃CN.



Supplementary Figure 14. ESI-HRMS of tetrahedron $[Tb_2L2_3]$. (A) The full spectrum. Simulated m/z for $[Tb_2L3_3 + 20Tf - H^+]^{3+}$ is 893.5292(100%), Experimental found m/z is 893.5298 (100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 15. Paramagnetic shift of $[Eu_2(L1)_3]$ and $[Eu_4(L1)_6]$ in CD₃CN.



Supplementary Figure 16. ESI-HRMS of tetrahedron $[Gd_4L1_6]$ after dissolution in CH₃CN for 14 days. The ESI-HRMS result revealed the supramolecular transformation from $[Gd_4L1_6]$ to $[Gd_2L1_3]$. Simulated m/z for $[Gd_2L1_3 + 3 \text{ OTf}]^{3+}$ is 866.4836 (100%), Experimental found m/z is 866.4835(100%).



Supplementary Figure 17. ESI-HRMS of tetrahedron $[Tb_4L1_6]$ after dissolution in CH₃CN for 14 days. The ESI-HRMS result revealed the supramolecular transformation from $[Tb_4L1_6]$ to $[Tb_2L1_3]$. Simulated m/z for $[Tb_2L1_3 - 3H^+]^{3+}$ is 717.5271 (100%), Experimental found m/z is 717.5247(100%).



Supplementary Figure 18. 1 H NMR of $[Lu_4(L)_6]$ upon dissolution in CD₃CN at different timespan.



Supplementary Figure 19. Expanded ¹H NMR of $[Lu_4(L)_6]$ upon dissolution in CD₃CN at different timespan.



Supplementary Figure 20. ¹H NMR of (A) $[La_2(L1)_3]$ in CD₃CN and (B) the powder left after diffusing ether into a solution containing $[La_2(L1)_3]$.







Supplementary Figure 21. Three sets of Arrhenius plot of Eu tetrahedron-to-helicate transformation.









Supplementary Figure 22. Four sets of Arrhenius plot of Sm tetrahedron-to-helicate transformation.

	E _a (kJmol-1)	Α	ΔH_{298} (kJmol ⁻¹)
Eu_A	90.1	2.93 x 10 ¹³	+87.6
Eu_B	98.8	2.63 x 10 ¹³	+96.3
Eu_C	102.3	1.16 x 10 ¹⁵	+99.8
Average	97.1 (5)	4.05 x 10 ¹⁴	+94.6 (5)

Supplementary Table 1. Kinetic data of Eu tetrahedron-to-helicate transformation.

	E _a (kJmol-1)	А	ΔH_{298} (kJmol ⁻¹)
Sm_A	78.8	2.25 x 10 ¹¹	+76.3
Sm_B	89.5	2.06 x 10 ¹³	+87.0
Sm_C	84.5	4.51 x 10 ¹²	+82.0
Sm_D	88.1	2.17 x 10 ¹³	+85.6
Average	85.2 (4)	1.18 x 10 ¹³	+82.7 (4)

Supplementary Table 2. Kinetic data of Sm tetrahedron-to-helicate transformation.



Supplementary Figure 23. Normalized UV-Vis spectrum of $[Eu_2(L1^{SS})_3](OTf)_6$ and $[Eu_4(L1^{SS})_6](OTf)_{12}$ in CH_3CN .



Supplementary Figure 24. CD spectra of [La₂(L1^{SS})₃](OTf)₆ and [La₂(L1^{RR})₃](OTf)₆ in CH₃CN.



Supplementary Figure 25. CD spectra of [Sm₂(L1^{SS})₃](OTf)₆ and [Sm₂(L1^{RR})₃](OTf)₆ in CH₃CN.



Supplementary Figure 26. CD spectra of $[Eu_2(L1^{SS})_3](OTf)_6$ and $[Eu_2(L1^{RR})_3](OTf)_6$ in CH₃CN.



Supplementary Figure 27. CD spectra of $[Gd_2(L1^{SS})_3](OTf)_6$ and $[Gd_2(L1^{RR})_3](OTf)_6$ in CH_3CN .



 $\label{eq:supplementary Figure 28. CD spectra of $[Tb_2(L1^{SS})_3](OTf)_6$ and $[Tb_2(L1^{RR})_3](OTf)_6$ in CH_3CN.}$



Supplementary Figure 29. CD spectra of [Lu₂(L1^{SS})₃](OTf)₆ and [Eu₂(L1^{RR})₃](OTf)₆ in CH₃CN.



 $\label{eq:supplementary Figure 30. CD spectra of $[Sm_4(L1^{SS})_6](OTf)_{12}$ and $[Sm_4(L1^{RR})_6](OTf)_{12}$ in CH_3CN.}$



 $\label{eq:supplementary Figure 31. CD spectra of [Eu_4(L1^{SS})_6](OTf)_{12} \ \text{and} \ [Eu_4(L1^{RR})_6](OTf)_{12} \ \text{in CH}_3CN.$



 $\label{eq:supplementary Figure 32. CD spectra of [Gd_4(L1^{SS})_6](OTf)_{12} \mbox{ and } [Gd_4(L1^{RR})_6](OTf)_{12} \mbox{ in CH}_3CN.$



Supplementary Figure 33. CD spectra of $[Tb_4(L1^{SS})_6](OTf)_{12}$ and $[Tb_4(L1^{RR})_6](OTf)_{12}$ in CH_3CN .



Supplementary Figure 34. CD spectra of $[Lu_4(L1^{SS})_6](OTf)_{12}$ and $[Lu_4(L1^{RR})_6](OTf)_{12}$ in CH_3CN .



Supplementary Figure 35. CD spectra of [La₂(L3^{SS})₃](OTf)₆ and [La₂(L3^{RR})₃](OTf)₆ in CH₃CN.



Supplementary Figure 36. CD spectra of $[Sm_2(L3^{SS})_3](OTf)_6$ and $[Sm_2(L3^{RR})_3](OTf)_6$ in CH₃CN.



Supplementary Figure 37. CD spectra of [Eu₂(L3^{SS})₃](OTf)₆ and [Eu₂(L3^{RR})₃](OTf)₆ in CH₃CN.



Supplementary Figure 38. CD spectra of $[Gd_2(L3^{SS})_3](OTf)_6$ and $[Gd_2(L3^{RR})_3](OTf)_6$ in CH_3CN .



Supplementary Figure 39. CD spectra of [Tb₂(L3^{SS})₃](OTf)₆ and [Tb₂(L3^{RR})₃](OTf)₆ in CH₃CN.



Supplementary Figure 40. CD spectra of $[Lu_2(L3^{SS})_3](OTf)_6$ and $[Lu_2(L3^{RR})_3](OTf)_6$ in CH_3CN .



Supplementary Figure 41. ¹H NMR of L1^{SS} in (CD₃)₂SO.



Supplementary Figure 42. ¹³C NMR of L1^{ss} in (CD₃)₂SO.



Supplementary Figure 43. ¹H NMR of L3^{RR} in (CD₃)₂SO.



Supplementary Figure 44. ¹³C NMR of L3^{RR} in (CD₃)₂SO.


Supplementary Figure 45. ¹H NMR of [La₂(L1^{ss})₃] in CD₃CN.



Supplementary Figure 46. ¹³C NMR of [La₂(L1^{ss})₃] in CD₃CN.



Supplementary Figure 47. ¹H NMR of $[Sm_2(L1^{RR})_3]$ in CD₃CN.



Supplementary Figure 48. ¹³C NMR of $[Sm_2(L1^{RR})_3]$ in CD₃CN.



Supplementary Figure 49. ¹H NMR of [Eu₂(L1^{ss})₃] in CD₃CN.



Supplementary Figure 50. ¹³C NMR of [Eu₂(L1^{RR})₃] in CD₃CN.



Supplementary Figure 51. ¹H NMR of [Lu₂(L1^{RR})₃] in CD₃CN.



Supplementary Figure 52. ¹³C NMR of [Lu₂(L1^{ss})₃] in CD₃CN.



Supplementary Figure 53. ¹H NMR of [Eu₄(L1^{ss})₆] in CD₃CN.



Supplementary Figure 54. ¹³C NMR of [Eu₄(L1^{SS})₆] in CD₃CN.



Supplementary Figure 55. 1 H NMR of [Sm₄(L1^{SS})₆] in CD₃CN.



Supplementary Figure 56. ¹³C NMR of [Sm₄(L1^{RR})₆] in CD₃CN.



Supplementary Figure 57. ¹H NMR of [Lu₄(L1^{SS})₆] in CD₃CN.



Supplementary Figure 58. 1 H NMR of $[La_{2}(L3^{SS})_{3}]$ in CD₃CN.



Supplementary Figure 59. 13 C NMR of $[La_2(L3^{RR})_3]$ in CD₃CN.



Supplementary Figure 60. ¹H NMR of [Sm₂(L3^{SS})₃] in CD₃CN.



Supplementary Figure 61. ¹³C NMR of [Sm₂(L3^{SS})₃] in CD₃CN.



Supplementary Figure 62. ¹H NMR of [Eu₂(L3^{SS})₃] in CD₃CN.



Supplementary Figure 63. 13 C NMR of $[Eu_2(L3^{RR})_3]$ in CD₃CN.



Supplementary Figure 64. ¹H NMR of [Lu₂(L3^{RR})₃] in CD₃CN.



Supplementary Figure 65. 13 C NMR of [Lu₂(L3^{RR})₃] in CD₃CN.



Supplementary Figure 66. COSY NMR of L1 in (CD₃)₂SO.



Supplementary Figure 67. COSY NMR of L3 in $(CD_3)_2SO$.



Supplementary Figure 68. COSY NMR of [La₂(L1^{RR})₃] in CD₃CN.



Supplementary Figure 69. COSY NMR of [Eu₂(L1^{RR})₃] in CD₃CN.



Supplementary Figure 70. COSY NMR of [Sm₂(L1^{RR})₃] in CD₃CN.



Supplementary Figure 71. COSY NMR of $[Lu_2(L1^{RR})_3]$ in CD₃CN.



Supplementary Figure 72. COSY NMR of [Sm₄(L1^{RR})₆] in CD₃CN.



Supplementary Figure 73. COSY NMR of [Eu₄(L1^{RR})₆] in CD₃CN.



Supplementary Figure 74. COSY NMR of $[Lu_4(L1^{RR})_6]$ in CD₃CN.



Supplementary Figure 75. COSY NMR of [La₂(L3^{RR})₃] in CD₃CN.



Supplementary Figure 76. COSY NMR of [Sm₂(L3^{RR})₃] in CD₃CN.



Supplementary Figure 77. COSY NMR of [Eu₂(L3^{RR})₃] in CD₃CN.



Supplementary Figure 78. COSY NMR of $[Lu_2(L3^{RR})_3]$ in CD₃CN.



Supplementary Figure 79. Chemical shift of $[Sm_2(L1)_3]$ and $[Sm_4(L1)_6]$ in CD_3CN .



Supplementary Figure 80. Chemical shift of $[Lu_2(L1)_3]$ and $[Lu_4(L1)_6]$ in CD_3CN.

ESI-HRMS characterization





Supplementary Figure 81. ESI-HRMS of bimetallic helicate $[La_2L1_3]$. (A) The full spectrum. Simulated m/z for $[La_3L1_3 + 4 \text{ OTf}]^{2+}$ is 1355.6841(100%), Experimental found m/z is 1355.6792(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 82. ESI-HRMS of bimetallic helicate $[Sm_2L1_3]$. (A) The full spectrum. Simulated m/z for $[Sm_2L1_3 + 3 \text{ OTf}]^{3+}$ is 861.8131(100%), Experimental found m/z is 861.8192(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks



Supplementary Figure 83. ESI-HRMS of bimetallic helicate $[Eu_2L1_3]$. (A) The full spectrum. Simulated m/z for $[Eu_3L1_3 + 4 OTf]^{2+}$ is 1369.1985(100%), Experimental found m/z is 1369.1962(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 84. ESI-HRMS of bimetallic helicate $[Gd_2L1_3]$. (A) The full spectrum. Simulated m/z for $[Gd_2L1_3 + 3 OTf]^{3+}$ is 866.4836 (100%), Experimental found m/z is 866.4828(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 85. ESI-HRMS of bimetallic helicate $[Tb_2L1_3]$. (A) The full spectrum. Simulated m/z for $[Tb_2L1_3 + OTf -2H^+]^{3+}$ is 767.5113(100%), Experimental found m/z is 767.5154(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 86. ESI-HRMS of bimetallic helicate $[Lu_2L1_3]$. (A) The full spectrum. Simulated m/z for $[Lu_2L1_3 + 30Tf]^{3+}$ is 878.1615(100%), Experimental found m/z is 878.1616(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 87. ESI-HRMS of tetrahedron $[Eu_4L1_6]$. (A) The full spectrum. Simulated m/z for $[Eu_4L1_6 + 9 \text{ OTf}]^{3+}$ is 1875.2490(100%), Experimental found m/z is 1875.2516(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 88. ESI-HRMS of tetrahedron $[Sm_4L1_6]$. (A) The full spectrum. Simulated m/z for $[Sm_4L_6 + 6 \text{ OTf}^+ + H^+]^{5+}$ is 1034.1745(100%), Experimental found m/z is 1034.1748(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 89. ESI-HRMS of tetrahedron $[Gd_4L1_6]$. (A) The full spectrum. Simulated m/z for $[Gd_4L1_6 + 8 \text{ OTf}]^{4+}$ is 1374.4520 (100%), Experimental found m/z is 1374.4512(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.

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Supplementary Figure 90. ESI-HRMS of tetrahedron $[Tb_4L1_6]$. (A) The full spectrum. Simulated m/z for $[Tb_4L1_6 + 6 \text{ OTf}^{\circ} - H^{\circ}]^{5+}$ is 1040.9802 (100%), Experimental found m/z is 1040.9800(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 91. ESI-HRMS of tetrahedron $[Lu_4L1_6]$. (A) The full spectrum. Simulated m/z for $[Lu_4L1_6 + 90Tf]^{3+}$ is 1905.6090(100%), Experimental found m/z is 1905.6060(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.

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Supplementary Figure 92. ESI-HRMS of bimetallic helicate $[La_2L3_3]$. (A) The full spectrum. Simulated m/z for $[La_2L3_3 + 30Tf]^{3+}$ is 1006.2012(100%), Experimental found m/z is 1006.2037(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 93. ESI-HRMS of bimetallic helicate $[Sm_2L3_3]$. (A) The full spectrum. Simulated m/z for $[Sm_2L3_3 + 30Tf^2]^{3+}$ is 1013.8759(100%), Experimental found m/z is 1013.8749(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 94. ESI-HRMS of bimetallic helicate $[Eu_2L3_3]$. (A) The full spectrum. Simulated m/z for $[Eu_2L3_3 + 30Tf]^{3+}$ is 1015.2111(100%), Experimental found m/z is 1015.2097(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 95. ESI-HRMS of bimetallic helicate $[Gd_2L3_3]$. (A) The full spectrum. Simulated m/z for $[Gd_2L3_3 + 30Tf^3^+$ is 1018.5452(100%), Experimental found m/z is 1018.5452(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.

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Supplementary Figure 96. ESI-HRMS of bimetallic helicate $[Tb_2L3_3]$. (A) The full spectrum. Simulated m/z for $[Tb_2L3_3 + 30Tf]^{3+}$ is 1019.5472(100%), Experimental found m/z is 1019.5485(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.



Supplementary Figure 97. ESI-HRMS of bimetallic helicate [Lu_2L3_3]. (A) The full spectrum. Simulated m/z for [$Lu_2L3_3 + OTf - 2H^+$]³⁺ is 930.2509(100%), Experimental found m/z is 930.2548(100%). Inset showing the experimental (upper) and calculated(lower) isotopic patterns. (B) Expanded region of the mass spectrum to show the possible assignments of the corresponding prominent peaks.

Photophysical studies



Supplementary Figure 98. Luminescent data of $[Eu_2(L1^{SS})_3](OTf)_6$ (1.58 x 10⁻⁶ M in CH₃CN).(A) Excitation spectrum, $\lambda_{em} = 616$ nm, slits = 1.5-1.0, filter 380 nm. (b) Emission spectrum, $\lambda_{ex} = 311$ nm, slits = 1.5-1.0, filter 380 nm. (c) Excited state decay curve, $\lambda_{em} = 616$ nm, slits = 6-5, filter 380 nm.


Supplementary Figure 99. Luminescent data of $[Eu_2(L1^{RR})_3](OTf)_6$ (1.60 x 10⁻⁵ M in CH₃CN).(A) Excitation spectrum, $\lambda_{em} = 616$ nm, slits = 1.5-1.0, filter 380 nm. (b) Emission spectrum, $\lambda_{ex} = 311$ nm, slits = 1.5-1.0, filter 380 nm. (c) Excited state decay curve, $\lambda_{em} = 616$ nm, slits = 6-5, filter 380 nm.



Supplementary Figure 100. Luminescent data of $[Eu_4(L1^{ss})_6](OTf)_{12}$ (2.50 x 10⁻⁶ M in CH₃CN).(A) Excitation spectrum, $\lambda_{em} = 616$ nm, slits = 1.5-1.0, filter 380 nm. (b) Emission spectrum, $\lambda_{ex} = 330$ nm, slits = 1.5-1.0, filter 380 nm. (c) Excited state decay curve, $\lambda_{em} = 616$ nm, slits = 5-3, filter 380 nm.



Supplementary Figure 101. Luminescent data of $[Eu_4(L1^{RR})_6](OTf)_{12}$ (2.41 x 10⁻⁶ M in CH₃CN).(A) Excitation spectrum, $\lambda_{em} = 616$ nm, slits = 1.5-1.0, filter 380 nm. (b) Emission spectrum, $\lambda_{ex} = 330$ nm, slits = 1.5-1.0, filter 380 nm. (c) Excited state decay curve, $\lambda_{em} = 616$ nm, slits = 5-3, filter 380 nm.



Supplementary Figure 102. Luminescent data of $[Gd_2(L1^{RR})_3](OTf)_6$ (6.13 x 10⁻⁶ M in 1:4 of MeOH/EtOH at 77K).(A) Excitation spectrum, $\lambda_{em} = 462$ nm, slits = 1.0-0.5, filter 380 nm. (b) Emission spectrum, $\lambda_{ex} = 315$ nm, slits = 1.0-0.5, filter 380 nm. (c) Excited state decay curve, $\lambda_{em} = 462$ nm, filter 380 nm.



Supplementary Figure 103. Luminescent data of $[Gd_2(L3^{SS})_6](OTf)_{12}$ (2.55 x 10⁻⁵ M in 1:4 of MeOH/EtOH at 77K).(A) Excitation spectrum, $\lambda_{em} = 480$ nm, slits = 2.0-0.5, filter 380 nm. (b) Emission spectrum, $\lambda_{ex} = 345$ nm, slits = 2.0-0.5, filter 380 nm. (c) Excited state decay curve, $\lambda_{em} = 480$ nm, filter 380 nm.



Supplementary Figure 104. Luminescent data of $[Gd_4(L1^{RR})_6](OTf)_{12}$ (9.05 x 10⁻⁶ M in 1:4 of MeOH/EtOH at 77K).(A) Excitation spectrum, $\lambda_{em} = 466$ nm, slits = 2.0-0.5, filter 380 nm. (b) Emission spectrum, $\lambda_{ex} = 330$ nm, slits = 2.0-0.5, filter 380 nm. (c) Excited state decay curve, $\lambda_{em} = 466$ nm, filter 380 nm.

	λ_{abs}^{max} (nm)	$arepsilon^{\max}$ (L·mol ⁻¹ ·cm ⁻¹)	λ_{em}^{max} (nm)	ϕ_x^{b} (%)	τ (ms)
$[La_2(L1^{ss})_3](CF_3SO_3)_6$	311	59052.4	/	/	/
$[La_2(L1^{RR})_3](CF_3SO_3)_6$	311	58787.3	/	/	/
$[Sm_2(L1^{SS})_3](CF_3SO_3)_6$	311	60056.4	/	/	/
$[Sm_2(L1^{RR})_3](CF_3SO_3)_6$	311	62036.6	/	/	/
$[\mathrm{Eu}_2(\mathbf{L1^{ss}})_3](\mathrm{CF}_3\mathrm{SO}_3)_6$	311	62925.5	616	4.07 (0.015)	1.42
$[\mathrm{Eu}_2(\mathbf{L1^{RR}})_3](\mathrm{CF}_3\mathrm{SO}_3)_6$	311	61958.6	616	4.41 (0.005)	1.41
$[Gd_2(L1^{ss})_3](CF_3SO_3)_6$	311	58396.8	462	/	0.0073
$[Gd_2(L1^{RR})_3](CF_3SO_3)_6$	311	59227.0	/	/	/
$[Tb_2(L1^{ss})_3](CF_3SO_3)_6$	311	61469.6	/	/	/
$[\mathrm{Tb}_2(\mathbf{L1^{RR}})_3](\mathrm{CF}_3\mathrm{SO}_3)_6$	311	60113.3	/	/	/
$[Lu_2(L1^{ss})_3](CF_3SO_3)_6$	311	60668.1	/	/	/
$[Lu_2(\mathbf{L1^{RR}})_3](CF_3SO_3)_6$	311	59773.5	/	/	/
$[Sm_4(L1^{SS})_6](CF_3SO_3)_{12}$	330	130019.8	/	/	/
$[Sm_4(L1^{RR})_6](CF_3SO_3)_{12}$	330	139354.6	/	/	/
[Eu ₄ (L1 ^{SS}) ₆](CF ₃ SO ₃) ₁₂	330	123947.0	616	0.81 (0.035)	1.28
$[Eu_4(L1^{RR})_6](CF_3SO_3)_{12}$	330	121335.7	616	0.83 (0.035)	1.27
$[Gd_4(L1^{SS})_6](CF_3SO_3)_{12}$	330	123657.1	/	/	/
$[Gd_4(L1^{RR})_6](CF_3SO_3)_{12}$	330	121829.6	466	/	0.0087°
$[Tb_4(L1^{ss})_6](CF_3SO_3)_{12}$	330	131075.9	/	/	/
[Tb ₄ (L1 ^{RR}) ₆](CF ₃ SO ₃) ₁₂	330	127713.5	/	/	/
$[Lu_4(L1^{ss})_6](CF_3SO_3)_{12}$	330	110557.9	/	/	/
[Lu ₄ (L1 ^{RR}) ₆](CF ₃ SO ₃) ₁₂	330	112691.3	/	/	/

Supplementary Table 3. A summary of selected photophysical properties, UV-Vis absorption and luminescence data of $[Ln_2L1_3]$ and $[Ln_4L1_6]$ complexes in acetonitrile solution^a. ^ausing a 10 mm cuvette and filter 380 nm. ^bThe relative quantum yields were referenced with quinine sulfate in 0.1 M sulfuric acid (φ = 0.577, λ_{ex} = 350nm) with 10 mm cuvette. ^cMeasurement performed at 77K in 1:4 MeOH/EtOH.

	λ_{abs}^{max}	ε^{\max}
	(nm)	$(L \cdot mol^{-1} \cdot cm^{-1})$
[La ₂ (L3 ^{ss}) ₃](CF ₃ SO ₃) ₆	345	125117.0
$[La_2(\mathbf{L3^{RR}})_3](CF_3SO_3)_6$	345	128419.6
[Sm ₂ (L3 ^{SS}) ₃](CF ₃ SO ₃) ₆	345	104030.4
$[Sm_2(\mathbf{L3^{RR}})_3](CF_3SO_3)_6$	345	104038.3
$[\mathrm{Eu}_2(\mathbf{L3^{ss}})_3](\mathrm{CF}_3\mathrm{SO}_3)_6$	345	124128.9
$[Eu_2(\mathbf{L3^{RR}})_3](CF_3SO_3)_6$	345	125331.4
$[Gd_2(\textbf{L3}^{\textbf{ss}})_3](CF_3SO_3)_6$	345	108324.9
$[\mathrm{Gd}_2(\mathbf{L3^{RR}})_3](\mathrm{CF}_3\mathrm{SO}_3)_6$	345	115018.7
$[Tb_2(\mathbf{L3^{SS}})_3](CF_3SO_3)_6$	345	114213.3
$[Tb_2(\mathbf{L3^{RR}})_3](CF_3SO_3)_6$	345	119793.5
[Lu ₂ (L3 ^{SS}) ₃](CF ₃ SO ₃) ₆	345	117521.9
[Lu ₂ (L 3 ^{RR}) ₃](CF ₃ SO ₃) ₆	345	115357.7

Supplementary Table 4. A summary of selected photophysical properties, UV-Vis absorption and luminescence data of $[Ln_2L3_3]$ in acetonitrile solution using a 10 mm cuvette and filter 380 nm.

CPL measurements

	$g_{ m lum}$			
	${}^{5}D_{0} - {}^{7}F_{1}$	${}^{5}D_{0} \rightarrow {}^{7}F_{2}$	${}^{5}D_{0} -> {}^{7}F_{4}$	${}^{5}D_{0} - {}^{7}F_{4}$
	$\Delta J = 1$	$\Delta J = 2$	$\Delta J = 4$	$\Delta J = 4$
Complex	(592.5 nm)	(615 nm)	(695.5 nm)	(704 nm)
$[Eu_2(L1^{ss})_3]$	+0.10	-0.02	—	—
$[Eu_2(L1^{RR})_3]$	- 0.10	+0.02	—	—
$[Eu_4(L1^{ss})_6]$	+0.10	-0.02	-0.05	+0.23
$[Eu_4(L1^{RR})_6]$	- 0.08	+0.02	+0.04	-0.23

*All g_{lum} values have associated nominal assumed instrumental uncertainty of $\pm \ 0.01.$

Supplementary Table 5. g_{lum} values for $[Eu_2(L1^{SS/RR})_3]$ and $[Eu_4(L1^{SS/RR})_6]$ calculated from total intensity and CPL spectra.



Supplementary Figure 105. Normalized CPL spectra and $Eu_2(L1^{SS})_3$ and $Eu_2(L1^{RR})_3$.

X-ray crystallography data

Crystal structure of Tb₂(L2^{SS})₃:

Crystal data for Tb₂(L2^{SS})₃: *formula*, M_r = 2372.04, *crystal system*, space group P 2₁ 2₁ 2, Z = 4, a = 26.075(3) Å, b = 28.363(4)Å, c = 23.396(3)Å, $a = 90^{\circ}$, $\beta = 90^{\circ}$, $\gamma = 90^{\circ}$, V = 17304(4) Å³, μ (Mo_{Ka}) = 0.857 mm⁻¹, $\rho_{calc} = 0.911$ mgm⁻³, T = 296(2) K. The crystallographic data for the structural analyses have been deposited with the Cambridge Crystallographic Data Centre, CCDC No. 1009616, and the data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif.

Information	Identifier from cif file
Empirical formula	$C_{126}H_{96}N_{18}O_{12}Tb_2$
Formula weight	2372.04
Temperature/K	296(2)
Crystal system	orthorhombic
Space group	P2 ₁ 2 ₁ 2
a/Å	26.075(3)
b/Å	28.363(4)
c/Å	23.396(3)
α/°	90
β/°	90
γ/°	90
Volume/Å ³	17304(4)
Z	4
$\rho_{calc}g/cm^3$	0.911
μ/mm ⁻¹	0.857
F(000)	4816.0
Crystal size/mm ³	$0.480 \times 0.320 \times 0.200$
Radiation	MoK α ($\lambda = 0.71073$)
20 range for data collection/°	5.202 to 50.7
Index ranges	$-29 \le h \le 31, -34 \le k \le 29, -28 \le l \le 28$
Reflections collected	210003

Independent reflections	$31661 [R_{int} = 0.0893, R_{sigma} = 0.0808]$
Data/restraints/parameters	31661/17/1363
Goodness-of-fit on F ²	0.941
Final R indexes [I>=2 σ (I)]	$R_1 = 0.0524, wR_2 = 0.1159$
Final R indexes [all data]	$R_1 = 0.0774, wR_2 = 0.1240$
Largest diff. peak/hole / e Å ⁻³	0.59/-0.33
Flack parameter	0.002(5)

Th (1.255)	Shape measure (°)		
$10_2(L2^{55})_3$	Tricapped trigonal prism (D _{3h})	Capped square antiprism (C_{4v})	
Tb1	7.04	10.89	
Tb2	6.77	10.43	

Supplementary Table 6. Results of the Shape Analysis for $Tb_2(L2^{SS})_3$ helix.

The coordination geometry of the ${\rm Tb}_2(L2^{ss})_3$: helix can be best described as tricapped trigonal prism.

Crystal structure of Eu₄(L1^{ss})₆:

The crystallographic data for the structural analyses have been deposited with the Cambridge Crystallographic Data Centre, CCDC No. 2014348.

Information	Identifier from cif file
Empirical formula	$C_{225}H_{192}Eu_4F_{27}N_{36}O_{51}S_9$
Formula weight	5625.51
Temperature/K	220.0
Crystal system	trigonal
Space group	R3
a/Å	29.9510(4)
b/Å	29.9510(4)
c/Å	71.8428(16)
α/°	90
β/°	90
$\gamma^{/\circ}$	120
Volume/Å ³	55813.1(19)
Z	6
$\rho_{calc}g/cm^3$	1.004
μ/mm ⁻¹	5.808
F(000)	17046.0
Crystal size/mm ³	$0.24 \times 0.17 \times 0.14$
Radiation	$CuK\alpha \ (\lambda = 1.54178)$
20 range for data collection/°	5.902 to 100.82
Index ranges	$-28 \le h \le 27, -27 \le k \le 29, -69 \le l \le 71$
Reflections collected	41125
Independent reflections	20620 [$R_{int} = 0.0639, R_{sigma} = 0.0648$]
Data/restraints/parameters	20620/1946/2017
Goodness-of-fit on F ²	1.055

Final R indexes [I>=2 σ (I)]	$R_1 = 0.0553, wR_2 = 0.1497$
Final R indexes [all data]	$R_1 = 0.0685, wR_2 = 0.1594$
Largest diff. peak/hole / e Å ⁻³	0.66/-0.18
Flack parameter	0.030(4)

$Eu_4(L1^{ss})_6$	Shape measure (°)		
	Tricapped trigonal prism (D _{3h})	Capped square antiprism (C_{4v})	
Eu1	6.45	11.13	
Eu2	5.82	10.33	
Eu3	5.94	10.23	
Eu4	6.11	10.93	

Supplementary Table 7. Results of the Shape Analysis for $\operatorname{Eu}_4(L1^{ss})_6$ tetrahedron.

The coordination geometry of the $Eu_4(L1^{SS})_6$ tetrahedron can be best described as tricapped trigonal prism.

Supplementary References

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