| Supporting Information | 584 |
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| SI: Supporting Information for "FRETpredict: A Python Package for | 585 |
| FRET efficiency predictions using Rotamer Libraries". | 586 |
| S1 Text: Detailed description of the steps used to create new rotamer | 587 |
| libraries. | 588 |
| 1. Generation of the conformational ensemble of the FRET probe. We | 589 |
| generated conformational ensembles of the FRET probes by performing replica | 590 |
| exchange MD (REMD) simulations, using the force fields developed by Graen et | 591 |
| al. [32] with some minor corrections [52]. From these trajectories, we here saved | 592 |
| and analysed approximately 28,000 frames. | 593 |
| 2. Selection of the peaks of the distributions of dihedral angles in the | 594 |
| linkers. We calculated the distributions of the dihedral angles in the linker using | 595 |
| the conformational ensembles frem REMD as input. Combinations of the dihedral | 596 |
| angles corresponding to peaks in the dihedral distributions were combined to | 597 |
| generate distinct probe conformers corresponding to C1 cluster centers. | 598 |
| 3. First clustering step. Trajectory frames are assigned to the C1 cluster centers | 599 |
| of least-squares deviation of the dihedral angles. | 600 |
| 4. Second clustering step. Averages over the dihedral angles in the trajectory | 601 |
| frames assigned to each cluster center are calculated to generate a new set of $\mathrm{C2}$ | 602 |
| center centers. As the C2 cluster centers do not necessarily represent physical | 603 |
| conformations of the probe, they cannot not be directly used to build the rotamer | 604 |
| library. Instead, the probe conformation with the minimum least-squares | 605 |
| deviation from the C2 cluster center is chosen as the representative conformation | 606 |
| of each center. Moreover, each C2 cluster center is assigned a weight equal to the | 607 |
| number of conformations in the cluster (cluster population). When normalized | 608 |
| over all clusters, this statistical weight approximates the Boltzmann probability of | 609 |

the representative conformation for a free dye in solution, p_i^{int} . These steps are

linkers in many FRET probes, extra steps are needed to decrease the number of

sufficient for short linkers with few dihedral angles. However, for the longer

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rotamers while ensuring a good coverage of the conformational space.

- 5. Filtering based on cluster populations. In most cases, including all the C2 614 cluster centers into the rotamer library (e.g., 8776 conformers for Lumiprobe 615 Cy7.5 L1R) would defeat the purpose of using the RLA as its computational cost 616 would be considerable, albeit much lower than for an MD simulation with explicit 617 probes. Therefore, we implemented a weight-based cutoff to reduce the number of 618 conformations in the library while maintaining a balanced coverage of the 619 conformational space sampled by the probes. Namely, we filtered out C2 clusters 620 with fewer than 10, 20, or 30 members, thus obtaining new sets of C3 clusters, 621 which will be referred in this work as *large*, *medium*, and *small* rotamer libraries, 622 respectively. Since filtering by the assigned weights skews the remaining weights 623 from the underlying Boltzmann distribution, we implemented a third clustering 624 step, in which the conformations previously belonging to a discarded C2 cluster 625 are moved to the C3 cluster of minimum least-squares deviation, and the p_i^{int} 626 values are updated accordingly. 627
- 6. Alignment and writing data to file. The C3 cluster centers are aligned to the plane defined by the C α atom and the C–N peptide bond. The resulting rotamer library is composed of a structure file (PDB format) and a trajectory file (DCD format) for the aligned FRET probe rotamers, and a text file containing the intrinsic Boltzmann weights of each rotamer state p_i^{int} .

S2 Text Detailed description of the rotamer library placement and weighting steps.

Rotamer library placement. The first step in calculating FRET efficiencies is 635 to place the FRET probes from the rotamer library at the protein site to be labeled, 636 following the same procedure introduced in DEER-PREdict [29]. Briefly, the 637 fluorophore library coordinates are translated and rotated based on the positions of the 638 backbone $C\alpha$, amide N, and carbonyl C atoms. This results in a perfect overlap with 639 the N and C α coordinates of the protein backbone and an approximate alignment with 640 the carbonyl C, which ensures that the $C\alpha - C\beta$ vector of the probe has the correct 641 orientation relative to the side chain of the labeled residue. 642

Rotamer library weighting. For each protein conformation, the overall 643 probability of the *i*th rotamer of a probe is estimated by combining the intrinsic and the 644 external Boltzmann probabilities of the inserted probe, independently from the other 645 probe. The intrinsic probabilities, p_i^{in} , are obtained from the clustering procedure 646 performed on the representative dihedral conformations of the free dye in solution and 647 are related to the free energy of the rotamer, ϵ_i^{int} , via Boltzmann inversion. Following 648 the approach of Polyhach et al. [25], we account for the environment surrounding the 649 FRET probe and calculate the probe-protein interaction energy, e_i^{ext} . This is achieved 650 by summing up 12-6 Lennard-Jones pair-wise interaction energies between the heavy 651 atoms of the probe and the surrounding protein within a 1-nm radius. The 652 Lennard-Jones atomic radii (σ) and potential-well depth (ϵ) parameters are obtained 653 from the CHARMM36m force field [53]. The σ parameters can be scaled by a "forgive" 654 factor which is set through the input parameter sigma_scaling and defaults to 0.5. 655 This scaling compensates for inaccuracies in the placement of the bulky FRET probe, 656 which tend to lead to clashes even for conformers with reasonably correct orientations of 657 the probe with respect to the side chain of the labeled residue. The contribution of 658 electrostatic interactions between charged probe and protein atoms is also taken into 659 account using a dielectric constant of 78, and can be turned off by setting the 660 electrostatic input parameter to False. Hence, the overall probability of the *i*th 661

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rotamer state attached to the sth protein conformation is calculated as

$$p_{si} = p_i^{\text{int}} p_{si}^{\text{ext}} = p_i^{\text{int}} \frac{\exp(-e_{si}^{\text{ext}}/kT)}{Z},$$
(10)

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where $Z = \sum_{i} p_{i}^{\text{int}} \exp(-e_{si}^{\text{ext}}/kT)$ is the steric partition function quantifying the fit of 663 the rotamer in the embedding protein conformation. Low Z values result from large 664 probe-protein interaction energies, suggesting tight placement of the probe due to either 665 (i) misplacement of the rotamers or (ii) protein conformations incompatible with the 666 presence of the FRET probe at the labeled site. Therefore, frames with Z < 0.05 are 667 discarded in the FRET efficiency calculation to preclude spurious conformers from 668 contributing to the ensemble average, corresponding to a situation in which all of the 669 rotamers have a positive steric energy. In FRET predict, the default Z cutoff can be 670 conveniently replaced by a user-provided value. This procedure could, in principle, be 671 generalized to account for the effect of the probe on the protein free energy by weighting 672 the protein conformations by the chromophore free energies $-k_{\rm B}T\ln(Z)$ in subsequent 673 analysis, since the effect will differ by conformation even for those with Z above the 674 cut-off. 675



S3 Figure: Structural formulae of the AlexaFluor probes.

Structural formulae of the 13 AlexaFluor probes for which we generated rotamer libraries. Each column corresponds to a different fluorophore (acronym in parentheses). The names of the linkers are reported above each formula.

S4 Figure: Structural formulae of the ATTO probes.



Structural formulae of the 14 ATTO probes for which we generated rotamer libraries. Each column corresponds to a different fluorophore (acronym in parentheses). The names of the linkers are reported above each formula.

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S5 Figure: Structural formulae of the Lumiprobe probes.

Structural formulae of the four Lumiprobe probes for which we generated rotamer libraries. Each column corresponds to a different fluorophore (acronym in parentheses). The names of the linkers are reported above each formula.

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S6 Figure: Scatter plot of Rotamer Libraries central atoms for unfiltered $_{679}$ rotamer libraries (cutoff = 0).



2D projections of the position of the fluorophore with respect to the C α atom for the unfiltered rotamer libraries generated in this work (C2 cluster centers). The projections are obtained as the x and y coordinates of the central atom of the fluorophore (*O91* for AlexaFluor, *C7* for ATTO, and *C10* for Lumiprobe), after placing the C α atom at the origin. Each plot represents a different FRET probe, divided into rows according to linker type (C1R, C2R, C3R, L1R, B1R, from top to bottom), and colored according to the manufacturer (green for AlexaFluor, orange for ATTO, and blue for Lumiprobe).

(cutoff = 20).

S7 Figure: Scatter plot of medium-size rotamer libraries' central atoms



2D projections of the position of the fluorophore with respect to the $C\alpha$ atom for the *medium* rotamer libraries generated in this work. The projections are obtained as the x and y coordinates of the central atom of the fluorophore (*O91* for AlexaFluor, *C7* for ATTO, and *C10* for Lumiprobe), after placing the $C\alpha$ atom at the origin. Each plot represents a different FRET probe, divided into rows according to linker type (C1R, C2R, C3R, L1R, B1R, from top to bottom), and colored according to the manufacturer (green for AlexaFluor, orange for ATTO, and blue for Lumiprobe).

= 30).



S8 Figure: Scatter plot of small-size rotamer libraries central atoms (cutoff 683

2D projections of the position of the fluorophore with respect to the $C\alpha$ atom for the *small* rotamer libraries generated in this work. The projections are obtained as the x and y coordinates of the central atom of the fluorophore (*O91* for AlexaFluor, *C7* for ATTO, and *C10* for Lumiprobe), after placing the $C\alpha$ atom at the origin. Each plot represents a different FRET probe, divided into rows according to linker type (C1R, C2R, C3R, L1R, B1R, from top to bottom), and colored according to the manufacturer (green for AlexaFluor, orange for ATTO, and blue for Lumiprobe).



S9 Figure: Large, medium, and small rotamer libraries populations.

Distribution of the number of conformers across all the *large* (blue), *medium* (orange), and *small* (green) rotamer libraries generated in this work.

| | small | medium | large |
|-------------------|-------|--------|-----------------|
| Donor clusters | 706 | 124 | 32 |
| Acceptor clusters | 574 | 106 | 38 |
| Computation time | 692 s | 120 s | $37 \mathrm{s}$ |

| S10 | Table: | Computational | times | obtained | using | different | cutoffs. |
|-----|--------|---------------|-------|----------|----------|-----------|----------|
| | | 1 | | | <u> </u> | | |

Computational times required to calculate FRET efficiency from a pp11 trajectory of 316 frames (Case study 1) using the *large* (cutoffs = 10), *medium* (cutoff = 20), and *small* rotamer libraries for AlexaFluor 488 - C1R and AlexaFluor 594 - C1R, on a laptop with AMD Ryzen 7 4800h processor with a Radeon graphics card. Compared to the *large* library, the *medium* library has significantly fewer cluster centers and it lowers the computational cost by a factor 6. Instead, choosing the *small* over the *medium* rotamer library results in a gain in computation time of around a factor of 3.

S11 Table: FRETpredict E for Case study 1: pp11 (Fig 3).

| Polyproline 11 (pp11) | | | | | | |
|-----------------------|-------|--------|-------|--|--|--|
| Regime | small | medium | large | | | |
| Static | 0.732 | 0.745 | 0.743 | | | |
| Dynamic | 0.876 | 0.886 | 0.881 | | | |
| Dynamic+ | 0.993 | 0.972 | 0.853 | | | |
| Average | 0.917 | 0.912 | 0.89 | | | |

FRET efficiencies calculated for pp11 using FRETpredict with different rotamer library sizes and three averaging regimes (Static, Dynamic, Dynamic+) as well as the average over those. The reference experimental value is 0.88 whereas the value obtained as the average over the three regimes from MD simulations with explicit FRET probes is 0.83.

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| ACTR | | | | | | |
|-----------------------|--------------|-----------------|--------------|--|--|--|
| Residue pair (Regime) | [Urea] = 0 M | [Urea] = 2.5 M | [Urea] = 5 M | | | |
| 3-61 (Exp) | 0.610 | 0.490 | 0.420 | | | |
| 3-61 (Static) | 0.602 | 0.374 | 0.319 | | | |
| 3-61 (Dynamic) | 0.698 | 0.451 | 0.382 | | | |
| 3-61 (Dynamic+) | 0.763 | 0.513 | 0.431 | | | |
| 3-61 (Average) | 0.688 | 0.446 | 0.377 | | | |
| 3-75 (Exp) | 0.470 | 0.380 | 0.340 | | | |
| 3-75 (Static) | 0.497 | 0.312 | 0.260 | | | |
| 3-75 (Dynamic) | 0.581 | 0.380 | 0.314 | | | |
| 3-75 (Dynamic+) | 0.639 | 0.437 | 0.360 | | | |
| 3-75 (Average) | 0.572 | 0.376 | 0.311 | | | |
| 33-75 (Exp) | 0.610 | 0.510 | 0.460 | | | |
| 33-75 (Static) | 0.476 | 0.474 | 0.450 | | | |
| 33-75 (Dynamic) | 0.574 | 0.567 | 0.539 | | | |
| 33-75 (Dynamic+) | 0.658 | 0.649 | 0.617 | | | |
| 33-75 (Average) | 0.570 | 0.563 | 0.535 | | | |

| S12 Table: | FRET efficiencies | for Cas | e study 2: | ACTR | (Fig 4) |). |
|------------|-------------------|---------|------------|------|---------|----|
|------------|-------------------|---------|------------|------|---------|----|

ACTR FRET efficiencies calculated with FRETpredict for all residue pairs (3-61, 3-75, 33-75) at different urea concentrations (0 M, 2.5 M, and 5 M), for the *medium* rotamer library. The averaging regime is reported in parentheses.

| HiSiaP | | | | | |
|-----------------------------|-------|--------|---------|----------|---------|
| Residue pair (conformation) | Exp | Static | Dynamic | Dynamic+ | Average |
| 58-134 (open) | 0.233 | 0.232 | 0.283 | 0.302 | 0.272 |
| $58-134 \ (closed)$ | 0.321 | 0.284 | 0.364 | 0.379 | 0.342 |
| 55-175 (open) | 0.765 | 0.554 | 0.723 | 0.890 | 0.722 |
| 55-175 (closed) | 0.847 | 0.786 | 0.942 | 0.999 | 0.909 |
| 175-228 (open) | 0.342 | 0.210 | 0.251 | 0.260 | 0.240 |
| $175-228 \ (closed)$ | 0.300 | 0.311 | 0.388 | 0.410 | 0.370 |
| 112-175 (open) | 0.437 | 0.260 | 0.318 | 0.343 | 0.307 |
| 112-175 (closed) | 0.388 | 0.396 | 0.486 | 0.575 | 0.486 |
| | | SBD2 | | | |
| Residue pair (conformation) | Exp | Static | Dynamic | Dynamic+ | Average |
| 319-392 (open) | 0.408 | 0.174 | 0.197 | 0.215 | 0.195 |
| $319-392 \ (closed)$ | 0.661 | 0.614 | 0.792 | 0.920 | 0.775 |
| 369-451 (open) | 0.275 | 0.270 | 0.296 | 0.304 | 0.290 |
| $369-451 \ (closed)$ | 0.469 | 0.477 | 0.587 | 0.627 | 0.564 |
| | | MalE | | | |
| Residue pair (conformation) | Exp | Static | Dynamic | Dynamic+ | Average |
| 87-127 (open) | 0.740 | 0.749 | 0.887 | 0.959 | 0.865 |
| 87-127 (closed) | 0.577 | 0.515 | 0.666 | 0.771 | 0.651 |
| 134-186 (open) | 0.903 | 0.857 | 0.964 | 0.994 | 0.938 |
| 134-186 (closed) | 0.913 | 0.819 | 0.949 | 0.989 | 0.919 |
| 36-352 (open) | 0.401 | 0.411 | 0.491 | 0.530 | 0.477 |
| $36-352 \ (closed)$ | 0.672 | 0.548 | 0.692 | 0.825 | 0.688 |
| 29-352 (open) | 0.219 | 0.177 | 0.217 | 0.237 | 0.210 |
| $29-352 \ (closed)$ | 0.359 | 0.321 | 0.415 | 0.486 | 0.407 |

S13 Table: FRET efficiencies for Case study 3: Single structure proteins (Fig 5)

FRET efficiencies calculated with FRETpredict for the open and closed conformations of all the single-structure proteins (HiSiaP, SBD2, and MalE), for the *large* rotamer library. Every row corresponds to a labeled residue pair, with the protein conformation reported in parentheses. Every column corresponds to an averaging regime or to the experimental value for the specific residue pair and protein conformation.



S14 Figure: Physicochemical parameters affecting FRETpredict

Effects of different physicochemical parameters on FRETpredict calculation (R_0 , probe steric bulk, and electrostatics, in panels A, B, and C, respectively). Calculations were performed on the open structure of MalE with the *large* rotamer library. Reported FRET efficiencies in all panels correspond to the average over the different regimes. In panel A, the R_0 value is changed from the experimental value of 5.1 nm (blue bars) to the actual R_0 of the two FRET probes used in the calculations (AlexaFluor 647 -AlexaFluor 647), i.e., 6.50 nm (orange bars). In panel B, the FRET efficiency was computed by turning electrostatic interactions on (blue bars) or off (orange bars) in the calculation of probe–protein energies. In panel C, the donor FRET probe is AlexaFluor 647 C2R (blue bars), AlexaFluor 647 L1R (orange bars), AlexaFluor 350 C1R (green bars), and AlexaFluor 350 L1R (red bars).