

Supporting Information

A. Details about molecular features

Table S1: Atom and bond features

Feature Type	Attribute	Size	Description
Atom Features	Atom type	100	Chemical elements with atomic number ≤ 100
	Degree	6	No. of bonds in which the atom is involved
	Formal charge	5	Electronic charge assigned to an atom
	Chirality	4	Unspecified, tetrahedral CW/CCW, or other types of chirality
	Number of H	5	No. of bonded hydrogen atoms
	Hybridization	5	sp, sp ² , sp ³ , sp ³ d, or sp ³ d ²
	Aromaticity	1	Whether the atom is a component of an aromatic system
	Atomic mass	1	Mass of the atom (divided by 100)
Bond Features	Bond type	4	Single, double, triple, or aromatic
	Conjugated	1	Whether the bond is conjugated
	Ring	1	Whether the bond is in a ring
	Stereo	6	Stereochemistry of bonds (none, any, E/Z or cis/trans)

Table S2: 200 Molecular descriptors generated by RDKit

Module	Descriptor Name			
Graph Descriptors	BalabanJ	BertzCT	Chi0	Chi0n
	Chi0v	Chi1	Chi1n	Chi1v
	Chi2n	Chi2v	Chi3n	Chi3v
	Chi4n	Chi4v	HallKierAlpha	Ipc
	Kappa1	Kappa2	Kappa3	
Descriptors	ExactMolWt	FpDensityMorgan1	FpDensityMorgan2	FpDensityMorgan3
	HeavyAtomMolWt	MaxAbsPartialCharge	MaxPartialCharge	MinAbsPartialCharge
	MinPartialCharge	MolWt	NumRadicalElectrons	NumValenceElectrons
Lipinski	FractionCSP3	HeavyAtomCount	NHOHCount	NOCCount
	NumAliphaticCarbocycles	NumAliphaticHeterocycles	NumAliphaticRings	NumAromaticCarbocycles
	NumAromaticHeterocycles	NumAromaticRings	NumHAcceptors	NumHDonors
	NumHeteroatoms	NumRotatableBonds	NumSaturatedCarbocycles	NumSaturatedHeterocycles
	NumSaturatedRings	RingCount		
EState_VSA	EState_VSA1	EState_VSA10	EState_VSA11	EState_VSA2
	EState_VSA3	EState_VSA4	EState_VSA5	EState_VSA6
	EState_VSA7	EState_VSA8	EState_VSA9	VSA_EState1
	VSA_EState10	VSA_EState2	VSA_EState3	VSA_EState4

	VSA_EState5 VSA_EState9	VSA_EState6	VSA_EState7	VSA_EState8
EState	MaxAbsEStateIndex	MaxEStateIndex	MinAbsEStateIndex	MinEStateIndex
Crippen	MolLogP	MolMR		
	LabuteASA	PEOE_VSA1	PEOE_VSA10	PEOE_VSA11
	PEOE_VSA12	PEOE_VSA13	PEOE_VSA14	PEOE_VSA2
	PEOE_VSA3	PEOE_VSA4	PEOE_VSA5	PEOE_VSA6
	PEOE_VSA7	PEOE_VSA8	PEOE_VSA9	SMR_VSA1
	SMR_VSA10	SMR_VSA2	SMR_VSA3	SMR_VSA4
MolSurf	SMR_VSA5	SMR_VSA6	SMR_VSA7	SMR_VSA8
	SMR_VSA9	SlogP_VSA1	SlogP_VSA10	SlogP_VSA11
	SlogP_VSA12	SlogP_VSA2	SlogP_VSA3	SlogP_VSA4
	SlogP_VSA5	SlogP_VSA6	SlogP_VSA7	SlogP_VSA8
	SlogP_VSA9	TPSA		
	fr_Al_COO	fr_Al_OH	fr_Al_OH_noTert	fr_ArN
	fr_Ar_COO	fr_Ar_N	fr_Ar_NH	fr_Ar_OH
	fr_COO	fr_COO2	fr_C_O	fr_C_O_noCOO
	fr_C_S	fr_HOCCN	fr_Imine	fr_NH0
	fr_NH1	fr_NH2	fr_N_O	fr_Ndealkylation1
	fr_Ndealkylation2	fr_Nhpyrrole	fr_SH	fr_aldehyde
	fr_alkyl_carbamate	fr_alkyl_halide	fr_allylic_oxid	fr_amide
	fr_amidine	fr_aniline	fr_aryl_methyl	fr_azide
	fr_azo	fr_barbitur	fr_benzene	fr_benzodiazepine
	fr_bicyclic	fr_diazo	fr_dihydropyridine	fr_epoxide
	fr_ester	fr_ether	fr_furan	fr_guanido
	fr_halogen	fr_hdrzine	fr_hdrzone	fr_imidazole
	fr_imide	fr_isocyan	fr_isothiocyan	fr_ketone
Fragments	fr_ketone_Topliiss	fr_lactam	fr_lactone	fr_methoxy
	fr_morpholine	fr_nitrile	fr_nitro	fr_nitro_ arom
	fr_nitro_ arom_nonortho	fr_nitroso	fr_oxazole	fr_oxime
	fr_para_hydroxylation	fr_phenol	fr_phenol_noOrthoHbond	fr_phos_acid
	fr_phos_ester	fr_piperdine	fr_piperzine	fr_priamide
	fr_prisulfonamd	fr_pyridine	fr_quatN	fr_sulfide
	fr_sulfonamd	fr_sulfone	fr_term_acetylene	fr_tetrazole
	fr_thiazole	fr_thiocyan	fr_thiophene	fr_unbrch_alkane
	fr_urea			
QED	ged			

B. Details about self-attention mechanisms inside ABT-MPNN

Table S3: Algorithm of Bond Attention

Initialization	
At iteration t , given a molecular graph G with N bonds, the input bond message matrix $H_b = [m_{b_1}^t, \dots, m_{b_i}^t, \dots, m_{b_{2N}}^t]$. $H_b \in \mathbb{R}^{2N \times d}$, where d is the hidden dimension.	
1)	$Q_b = [q_{b_1}, \dots, q_{b_i}, \dots, q_{b_{2N}}] = H_b$ $K_b = [k_{b_1}, \dots, k_{b_i}, \dots, k_{b_{2N}}] = H_b$ $V_b = [v_{b_1}, \dots, v_{b_i}, \dots, v_{b_{2N}}] = H_b$
Bond Attention	
1)	for each bond message b_i :
2)	$\alpha_{b_i} \leftarrow \frac{\exp(q_{b_i} w_q / \sqrt{d})}{\sum_{j=1}^{2N} \exp(q_{b_j} w_q / \sqrt{d})}$
3)	$q_b \leftarrow \sum_{i=1}^{2N} \alpha_{b_i} q_{b_i}$
4)	$p_{b_i} \leftarrow q_b * k_{b_i}$
5)	$\beta_{b_i} \leftarrow \frac{\exp(p_{b_i} w_k / \sqrt{d})}{\sum_{j=1}^{2N} \exp(p_{b_j} w_k / \sqrt{d})}$
6)	$k_b \leftarrow \sum_{i=1}^{2N} \beta_{b_i} k_{b_i}$
7)	$u_{b_i} \leftarrow k_b * v_{b_i}$
8)	$r_{b_i} \leftarrow u_{b_i} w_r + q_{b_i}$
9)	$O_b \leftarrow \text{Layernorm}([r_{b_1}, \dots, r_{b_{2N}}])$

Table S4: Algorithm of Atom Attention

Initialization	
1)	Given a molecular graph G with M atoms, the input atom hidden matrix $H_a = [m_{a_1}, \dots, m_{a_i}, \dots, m_{a_M}]$. $H_a \in \mathbb{R}^{M \times d}$, where d is the hidden dimension. $Q_a = K_a = V_a = H_a$
2)	If $head_1$ or $head_2$: $M_{graph} = \lambda \cdot M_{Adjacency} \in \mathbb{R}^{M \times M}$ If $head_3$ or $head_4$: $M_{graph} = \lambda \cdot M_{Distance} \in \mathbb{R}^{M \times M}$ If $head_5$ or $head_6$: $M_{graph} = \lambda \cdot M_{Coulomb} \in \mathbb{R}^{M \times M}$
Atom Attention	
1)	$A_a \leftarrow \frac{Q_a W_Q (K_a W_K)^T}{\sqrt{d}} + M_{graph}$
2)	$O_a \leftarrow \text{Layernorm}(\text{Softmax}(A_a) V_a W_V)$

C. Details about the ablation study of ABT-MPNN

Fig. S1 Comparison of ablation experiments using 5-fold cross-validation (A) Performance evaluation of each fold for the classification task (ClinTox) measured with AUROC. Experiments settings: #1: baseline; #2: use bond attention (Transformer); #3: use bond attention (Fastformer); #4 use atom attention; #5 use atom attention with inter-atomic matrices #6 use bond attention (Fastformer) and atom attention; #7 use bond attention (Fastformer) and atom attention with inter-atomic matrices (B) Performance evaluation of each fold for the regression task (ESOL) measured by RMSE. The settings of each experiment in the regression task are identical to those in the classification one.

