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## **Age-dependent topic modelling of comorbidities in UK Biobank identifies disease subtypes with differential genetic risk**

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Author Contributions

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Competing Interests

G.M. is a director of and shareholder in Genomics PLC, and is a partner in Peptide Groove LLP. The other authors declare no competing financial interests.

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## **Abstract**

The analysis of longitudinal data from electronic health records (EHR) has the potential to improve clinical diagnoses and enable personalized medicine, motivating efforts to identify disease subtypes from patient comorbidity information. Here, we introduce an age-dependent topic modelling (ATM) method that provides a low-rank representation of longitudinal records of hundreds of distinct diseases in large EHR data sets. We applied ATM to 282,957 UK Biobank samples, identifying 52 diseases with heterogeneous comorbidity profiles; analyses of 211,908 All of Us samples produced concordant results. We defined subtypes of the 52 heterogeneous diseases based on their comorbidity profiles and compared genetic risk across disease subtypes using polygenic risk scores (PRS), identifying 18 disease subtypes whose PRS differed significantly from other subtypes of the same disease. We further identified specific genetic variants with subtype-dependent effects on disease risk. In conclusion, ATM identifies disease subtypes with differential genome-wide and locus-specific genetic risk profiles.

## **Introduction**

Longitudinal electronic health record (EHR) data, encompassing diagnoses across hundreds of distinct diseases, offers immense potential to improve clinical diagnoses and enable personalised medicine<sup>1</sup>. Despite intense interest in both the genetic relationships between distinct diseases $2^{-11}$  and the genetic relationships between biological subtypes of disease<sup>12–15</sup>, there has been limited progress on classifying disease phenotypes into groups of diseases with frequent co-occurrences (comorbidities) and leveraging comorbidities to identify disease subtypes. Low-rank modelling has appealing theoretical properties $16,17$ and has produced promising applications<sup>18–24</sup> to infer meaningful representations of highdimensional data. In particular, low-rank representation is an appealing way to summarize data across hundreds of distinct diseases<sup>25–27</sup>, providing the potential to identify patientlevel comorbidity patterns and distinguish disease subtypes. The biological differentiation of disease subtypes inferred from EHR data could be validated by comparing genetic profiles across subtypes, which is possible with emerging data sets that link genetic data with EHR data $28-31$ .

Previous studies have used low-rank representation to identify shared genetic components $25-27$  across multiple distinct diseases, identifying relationships between diseases and generating valuable biological insights. However, age at diagnosis information in longitudinal EHR data has the potential to improve such efforts. For example, a recent study used longitudinal disease trajectories to identify disease pairs with

statistically significant directionality<sup>32</sup>, suggesting that age information could be leveraged to infer comorbidity profiles that capture temporal information. In addition, patient-level comorbidity information could potentially be leveraged to identify biological subtypes of disease, complementing its application to increase power for identifying genetic associations<sup>12</sup> and to cluster disease-associated variants into biological pathways<sup>8</sup>; disease subtypes are fundamental to disease etiology<sup>14,33–36</sup>.

Here, we propose an age-dependent topic modelling (ATM) method to provide a low-rank representation of longitudinal disease records. ATM learns, and assigns to each individual, topic weights for several disease topics, each of which reflects a set of diseases that tend to co-occur within individuals as a function of age. We applied ATM to 1.7 million disease diagnoses spanning 348 diseases in UK Biobank, inferring 10 disease topics; we validated ATM in All of Us. We identified 52 diseases with heterogeneous comorbidity profiles that enabled us to define disease subtypes. We used genetic data to validate the disease subtypes, showing that they exhibit differential genome-wide and locus-specific genetic risk profiles.

## **Results**

#### **Overview of methods**

We propose an age-dependent topic modelling (ATM) model, which provides a low-rank representation of longitudinal records of hundreds of distinct diseases in large EHR data sets (Fig. 1 and Methods). The model assigns to each individual topic weights for several disease topics; each disease topic reflects a set of diseases that tend to co-occur as a function of age, quantified by age-dependent topic loadings for each disease. The model assumes that, for each disease diagnosis, a topic is sampled based on the individual's topic weights (which sum to 1 across topics, for a given individual), and a disease is sampled based on the individual's age and the age-dependent topic loadings (which sum to 1 across diseases, for a given topic at a given age). The model generalizes the latent dirichlet allocation (LDA) model<sup>37,38</sup> by allowing topic loadings for each topic to vary with age (Supplementary Note and Extended Data Fig. 1).

We developed a method to fit this model that addresses several challenges inherent to large EHR data sets; the method estimates topic weights for each individual, topic loadings for each disease, and posterior diagnosis-specific topic probabilities for each disease diagnosis. First, we derived a scalable deterministic method that uses numerical approximation approaches to fit the parameters of the model, addressing the challenge of computational cost. Second, we used the prediction odds ratio $39$  to compare model structures (e.g. number of topics and parametric form of topic loadings as a function of age), addressing the challenge of appropriate model selection; roughly, the prediction odds ratio quantifies the accuracy of correctly predicting disease diagnoses in held-out individuals using comorbidity information, compared to a predictor based only on prevalence (see Methods and Supplementary Table 1). Third, we employed collapsed variational inference<sup>40</sup>, addressing the challenge of sparsity in the data (e.g. in UK Biobank data, the average patient has diagnoses for 6 of 348 diseases analyzed); collapsed variational inference outperformed mean-field variational inference<sup>37</sup> in empirical data. Further details are provided in the

Methods section and Supplementary Note; we have publicly released open-source software implementing the method (see Code Availability).

We applied ATM to longitudinal records of UK Biobank<sup>29</sup> (282,957 individuals with 1,726,144 disease diagnoses spanning 348 diseases; the targeted individuals are those diagnosed with at least two of the 348 diseases studied) and All of  $Us^{30}$  (211,908 individuals with 3,098,771 disease diagnoses spanning 233 of the 348 diseases). Each disease diagnosis has an associated age-at-diagnosis, defined as the earliest age of reported diagnosis of the disease in that individual; we caution that age at diagnosis may differ from age at disease onset (see Discussion). ATM does not use genetic data, but we used genetic data to validate the inferred topics (Methods).

#### **Simulations**

We performed simulations to compare ATM with latent dirichlet allocation  $(LDA)^{37,38}$ , a simpler topic modelling approach that does not model age. Choices of simulation parameters that resemble real data are described in Supplementary Note. We assigned each disease diagnosis to one of two subtypes for the target disease based on age and other subtype differences, considering high, medium, or low age-dependent effects by specifying an average difference of 20, 10, or 5 years respectively in age at diagnosis for the two subtypes. For each level of age-dependent effects, we varied the proportion of diagnoses belonging to the first subtype (i.e. the subtype that has an earlier average age-at-diagnosis) from 10–50%. Our primary metric for evaluating the LDA and ATM methods is the area under the precision-recall curve  $(AUPRC)^{41}$  metric, where precision is defined as the proportion of disease diagnoses that a given method assigned to the first subtype that were assigned correctly, and recall is defined as the proportion of disease diagnoses truly belonging to the first subtype that were assigned correctly. We discretized the subtype assigned to each disease diagnosis by a given method by assigning the subtype with higher inferred probability. We used AUPRC (instead of prediction odds ratio) in our simulations because the underlying truth is known. Further details and justifications of metrics used in this study are provided in the Methods, Supplementary Note, and Supplementary Table 1.

In simulations with high age-dependent effects, ATM attained much higher AUPRC than LDA across all values of subtype sample size proportion (AUPRC difference: 24%–42%), with both methods performing better at more balanced ratios (Fig. 2 and Supplementary Table 2). Accordingly, ATM attained both higher precision and higher recall than LDA (Supplementary Fig. 1). Results were qualitatively similar when using the second subtype as the classification target (Supplementary Fig. 2). In simulations with medium or low agedependent effects, ATM continued to outperform LDA, but with smaller differences between the methods. In simulations without age-dependent effects, ATM slightly underperformed

Code availability

Open-source software implementing the ATM method is available at [https://github.com/Xilin-Jiang/ATM.](https://github.com/Xilin-Jiang/ATM) BOLT-LMM 2.3 is available at <https://alkesgroup.broadinstitute.org/BOLT-LMM/>. Heritability and genetic correlation analysis were performed using LDSC, which is available at <https://github.com/bulik/ldsc>. PLINK v1.9, which was used for  $FST$  and association tests, is available at [https://](https://www.cog-genomics.org/plink/) [www.cog-genomics.org/plink/](https://www.cog-genomics.org/plink/). All code generated in this study is available at<https://zenodo.org/record/8304651> (DOI: 10.5281/ zenodo.8304651).

LDA (Supplementary Fig. 3a). Three secondary analyses are described in the Supplementary Note and Supplementary Figures 3 and 4.

We conclude that ATM (which models age) assigns disease diagnoses to subtypes with higher accuracy than LDA (which does not model age) in simulations with age-dependent effects. We caution that our simulations largely represent a best-case scenario for ATM given that the generative model and inference model are very similar (although there are some differences, e.g. topic loadings were generated using a model different from the inference model), thus it is important to analyze empirical data to validate the method.

#### **Age-dependent comorbidity profiles in the UK Biobank**

We applied ATM to longitudinal hospital records of 282,957 individuals from the UK Biobank with an average record span of 28.6 years<sup>29</sup>. We used Phecode<sup>42</sup> to define 1,726,144 disease diagnoses spanning 348 diseases with at least 1,000 diagnoses each; the average individual had 6.1 disease diagnoses, and the average disease had a standard deviation of 8.5 years in age at diagnosis. The optimal inferred ATM model structure has 10 topics and models age-dependent topic loadings for each disease as a spline function with one knot, based on optimizing prediction odds ratio (see below). We assigned names (and corresponding acronyms) to each of the 10 inferred topics based on the Phecode systems<sup>42</sup> assigned to diseases with high topic loadings (aggregated across ages) for that topic (Table 1 and Supplementary Table 3).

Age-dependent topic loadings across all 10 topics and 348 diseases (stratified into Phecode systems), summarized as averages across age  $< 60$  and age  $< 60$ , are reported in Figure 3, Extended Data Figure 2, and Supplementary Table 4. Some topics such as NRI span diseases across the majority of Phecode systems, while other topics such as ARP are concentrated in a single Phecode system. Conversely, a single Phecode system may be split across multiple topics, e.g. diseases of the digestive system are split across UGI, LGI, and MDS. We note that topic loadings in diseases that span multiple topics are heavily age-dependent. For example, type 2 diabetes patients assigned to the CVD topic are associated with early onset of type 2 diabetes, whereas type 2 diabetes patients assigned to the MGND topic are associated with late onset of type 2 diabetes.

We performed seven secondary analyses to validate the integrity and reproducibility of inferred comorbidity topics. First, we fit ATM models with different model structures using 80% training data, and computed their prediction odds ratios using 20% testing data. The ATM model structure with 10 topics and age-dependent topic loadings modelled as a spline function performed optimally (Supplementary Fig. 5; see Methods). Second, we confirmed that ATM (which models age) attained higher prediction odds ratios than LDA (which does not model age) across different values of the number of topics (Extended Data Fig. 3); for the optimal model with 10 topics, ATM attained an average prediction odds ratio of 1.71, compared to a prediction odds ratio of 1.58 for LDA. Third, we compared the topic loadings by repeating the inference on female-only or male-only populations and observed no major discrepancies, except for genitourinary topics MGND and FGND (topic loading  $R^2$  (female vs. all) = 0.788, topic loading  $R^2$  (male vs. all) = 0.773; Extended Data Fig. 4). Fourth, we verified that BMI, sex, Townsend deprivation index, and birth year explained

very little of the information in the inferred topics (Supplementary Table 3). Three additional secondary analyses are described in the Supplementary Note, Supplementary Figures 6–8, and Supplementary Table 1.

Disease topics capture known biology as well as the age-dependency of comorbidities for the same diseases. For example, early onset of essential hypertension is associated with the CVD topic<sup>43</sup>, which captures the established connection between lipid dysfunction ("hypercholesterolemia") and cardiovascular diseases $44$ , while later onset of essential hypertension is associated with the CER topic, which pertains to type 2 diabetes, obesity and COPD (Fig. 4a). Continuously varying age-dependent topic loadings for all 10 topics, restricted to diseases with high topic loadings, are reported in Supplementary Figure 9 and Supplementary Table 5. We note that most diseases have their topic loadings concentrated into a single topic (Fig. 4b, Supplementary Fig. 10a and Supplementary Table 4), and that most individuals have their topic weights concentrated into  $1-2$  topics (Fig. 4c and Supplementary Fig. 10b). For diseases spanning multiple topics (Extended Data Fig. 2 and Supplementary Table 4), the assignment of type 2 diabetes patients to the CVD topic is consistent with known pathophysiology and epidemiology<sup>45,46</sup> and has been shown in other comorbidity clustering studies, e.g. with the Beta Cell and Lipodystrophy subtypes described in ref. 35 and the severe insulin-deficient diabetes (SIDD) subtype described in ref. 14, which are characterized by early onset of type 2 diabetes and have multiple morbidities including hypercholesterolemia, hyperlipidemia, and cardiovascular diseases $47$ . In addition, early-onset breast cancer and late-onset breast cancer are associated with different topics, e.g. NRI and FGND, consistent with known treatment effects for breast cancer patients that increase susceptibility to infections, especially bacterial pneumonias<sup>48</sup> and hypothyroidism<sup>49</sup>. We conclude that ATM identifies latent disease topics that robustly compress age-dependent comorbidity profiles and capture disease comorbidities both within and across Phecode systems.

#### **Age-dependent comorbidity profiles in All of Us**

To assess the transferability of inferred topics between cohorts, we applied ATM to longitudinal data from 211,908 All of Us samples<sup>30</sup>. We analyzed  $3,098,771$  diagnoses spanning 233 of the 348 diseases analyzed in UK Biobank for which data were available; the average individual had 14.6 disease diagnoses, and an average disease had a standard deviation of 14.0 years in age at diagnosis. The optimal model for All of Us included 13 topics (Supplementary Figs. 11 and 12a,b and Supplementary Table 6); most diseases have their topic loadings concentrated into a single topic, and most individuals have their topic weights concentrated into 1–4 topics (Supplementary Fig. 13).

We assessed the concordance between each UK Biobank topic and each All of Us topic by computing the correlation between the respective topic loadings across the 233 diseases analyzed in both data sets (Fig. 5a,b, Supplementary Fig. 14, and Supplementary Table 7). The median correlation between the ten UK Biobank topics and the most similar All of Us topic was 0.54, confirming qualitative alignment of topic loadings between All of Us and UK Biobank. For example, the topic loadings of CVD and CER topics were qualitatively similar to the most similar All of Us topics (Fig. 5a vs. Fig. 4a), even though

For each of the 233 diseases, we assessed the concordance between UK Biobank and All of Us topic assignments for that disease by computing the correlation between UK Biobank topic assignments and All of Us topic assignments that were mapped to UK Biobank topics (by weighting by correlations between topics; Methods). The average correlation between UK Biobank and All of Us topic assignments for the same disease was 0.70 (vs. average correlation of 0.02 for different diseases) (Fig. 5c, Extended Data Fig. 5, and Supplementary Table 9). We conclude that ATM identifies latent disease topics from the All of Us cohort that align with topics from UK Biobank.

#### **Comorbidity-based subtypes are genetically heterogeneous**

We sought to define disease subtypes in UK Biobank data based on the topic weights of each patient and diagnosis-specific topic probabilities of each disease diagnosis. In some analyses, we used continuous-valued topic weights to model disease subtypes. In analyses that require discrete subtypes, we assigned a discrete topic assignment to each disease diagnosis based on its maximum diagnosis-specific topic probability, and inferred the comorbidity-derived subtype of each disease diagnosis based on the discrete topic assignment; we note that discretizing continuous data loses information (see Discussion). We restricted our disease subtype analyses to 52 diseases with at least 500 diagnoses assigned to each of two discrete subtypes; the average correlation between UK Biobank and All of Us disease subtypes (see above; same metric as Fig. 5c) was 0.64 for the 41 (of 52) diseases that were shared between the two cohorts (Table 2, Methods, Extended Data Fig. 2, Supplementary Fig. 12d, and Supplementary Table 11).

Age-dependent distributions of comorbidity-derived subtypes for four diseases (type 2 diabetes, asthma, hypercholesterolemia, and essential hypertension) are reported in Figure 6a and Supplementary Table 12; results for all 52 diseases are reported in Supplementary Figure 16 and Supplementary Table 12, and age-dependent distributions for the same four diseases in All of Us are reported in Supplementary Figure 17. The number of subtypes can be large, e.g. six subtypes for essential hypertension. Subtypes are often age-dependent, e.g. for the CVD and MGND subtypes of type 2 diabetes<sup>14,35</sup> (discussed above).

ATM and the resulting subtype assignments do not make use of genetic data. However, we used genetic data to assess genetic heterogeneity across inferred subtypes of each disease. We used continuous-valued topic weights in this analysis. We first assessed whether PRS for overall disease risk varied with continuous-valued topic weights for each disease; PRS were computed using BOLT-LMM with five-fold cross validation<sup>50,51</sup> (see Methods and Code Availability). Results for four diseases (from Fig. 6a) are reported in Figure 6b and Supplementary Table 13; results for all 10 well-powered diseases (10 of 52 diseases with highest z-scores for nonzero SNP-heritability) are reported in Extended Data Figure 6 and Supplementary Table 13. We identified 18 disease-topic pairs (of  $10 \times 10 = 100$ )

diabetes, patients assigned to the CVD subtype had significantly higher PRS values than patients assigned to other subtypes. For essential hypertension, patients assigned to the CER subtype had significantly higher PRS values; for type 2 diabetes, patients assigned to the CER subtype had lower PRS values than the CVD subtype, even though the majority of type 2 diabetes diagnoses are assigned to the CER subtype. We further verified that most of the variation in PRS values with disease subtype could not be explained by age<sup>52</sup> or differences in subtype sample size (Supplementary Fig. 18). These associations between subtypes (defined using comorbidity data) and PRS (defined using genetic data) imply that disease subtypes identified through comorbidity are genetically heterogeneous, consistent with phenomenological differences in disease aetiology.

We further investigated whether subtype assignments (defined using comorbidity data) revealed subtype-specific excess genetic correlations. We used discrete subtypes in this analysis. We estimated excess genetic correlations between disease-subtype and subtypesubtype pairs (relative to genetic correlations between the underlying diseases). Excess pairwise genetic correlations for 15 diseases and disease subtypes (spanning 11 diseases and 3 topics: CER, MGND and CVD) are reported in Figure 7a and Supplementary Table 14 (relative to genetic correlations between the underlying diseases; Fig. 7b), and excess pairwise genetic correlations for all 89 well-powered diseases and disease subtypes (89 of 378 diseases and disease subtypes with z-score  $>$  4 for nonzero SNP-heritability; 378 = 348 diseases + 30 disease subtypes) are reported in Supplementary Figure 19 and Supplementary Table 14. Genetic correlations between pairs of subtypes involving the same disease were significantly less than 1 (FDR < 0.1) for hypertension (CER vs. CVD:  $\rho = 0.86 \pm 0.04$ , P = 0.0004; MGND vs. CVD:  $\rho = 0.74 \pm 0.05$ ,  $P = 3 \times 10^{-8}$ ) and type 2 diabetes (CER vs. MGND:  $\rho = 0.64 \pm 0.09$ ,  $P = 8 \times 10^{-5}$ ) (Fig. 7a and Supplementary Table 14). In addition, we observed significant excess genetic correlations (FDR  $< 0.1$ ) for 8 disease-subtype and subtype-subtype pairs involving different diseases (Fig. 7a and Supplementary Table 14). Additional secondary analyses are described in the Supplementary Note, Supplementary Figure 20, and Supplementary Table 15.

Finally, we used the population genetic parameter  $F_{ST}^{53,54}$  to quantify genome-wide differences in allele frequency between two subtypes of the same disease. We used discrete subtypes in this analysis. We wished to avoid inferring genetic differences between subtypes that were due to partitions of the cohort that are unrelated to disease (e.g. we expect a nonzero  $F_{ST}$  between tall vs. short type 2 diabetes cases; see above). Thus, we assessed the statistical significance of nonzero  $F_{ST}$  estimates by comparing the observed  $F_{ST}$  estimates (between two subtypes of the same disease) to the expected  $F_{ST}$  based on matched topic weights (i.e.  $F_{ST}$  estimates between two sets of healthy controls with topic weight distributions matched to the respective disease subtypes) (excess  $F_{ST}$ ; Methods). We determined that 63 of 104 pairs of disease subtypes involving the same disease (spanning 29 of 49 diseases, excluding 3 diseases that did not have enough controls with matched topic weights) had significant excess  $F_{ST}$  estimates (FDR < 0.1) (Extended Data Figure 7 and Supplementary Table 16). For example, the CVD, CER, and MGND subtypes of type 2 diabetes had significant excess  $F_{ST}$  estimates (*F*-statistic = 0.0003, *P* = 0.001 based on 1,000

matched control sets). This provides further evidence that disease subtypes as determined by comorbidity have different molecular and physiological etiologies. We conclude that disease subtypes defined by distinct topics are genetically heterogeneous.

#### **Disease-associated SNPs have subtype-dependent effects**

We hypothesized that disease genes and pathways might differentially impact the disease subtypes identified by ATM. We investigated the genetic heterogeneity between disease subtypes at the level of individual disease-associated variants. We used continuous-valued topic weights in this analysis. We employed a statistical test that tests for  $SNP \times$  topic interaction effects on disease phenotype in the presence of separate SNP and topic effects (Methods). We verified via simulations that this statistical test is well calibrated under a broad range of scenarios with no true interaction, including direct effect of topic on disease, direct effect of disease on topic, pleiotropic SNP effects on disease and topic, and nonlinear effects (Supplementary Fig. 21). We also assessed the power to detect true interactions (Supplementary Fig. 22). To limit the number of hypotheses tested, we applied this test to independent SNPs with genome-wide significant main effects on disease (Methods). We thus performed 2,530 statistical tests spanning 888 disease-associated SNPs, 14 diseases, and 35 disease subtypes (Supplementary Table 17). We assessed statistical significance using global FDR < 0.1 across the 2,530 statistical tests. We also computed main SNP effects specific to each quartile of topic weights across individuals and tested for different odds ratios in top vs. bottom quartiles, as an alternative way to represent  $SNP \times$  topic interactions; the top/bottom quartile test is more intuitive, but less powerful in most cases.

We identified 43 SNP  $\times$  topic interactions at FDR  $< 0.1$  (Extended Data Fig. 8, Supplementary Fig. 23, and Supplementary Tables 18 and 19). Here, we highlight a series of examples. First, the type 2 diabetes-associated SNP rs1042725 in the HMGA2 locus has a higher odds ratio in the top quartile of CVD topic weight  $(1.18 \pm 0.02)$  than in the bottom quartile (1.00  $\pm$  0.02) ( $P = 3 \times 10^{-4}$  for interaction test (FDR = 0.04 < 0.1); P=  $3 \times 10^{-7}$  for top/bottom quartile test (FDR = 0.0002 < 0.1)). *HMGA2* is associated with type 2 diabetes<sup>55</sup> and is reported to have functions in cardiac remodelling<sup>56</sup>, suggesting that shared pathways underlie the observed  $SNP \times$  topic interaction. Second, the asthmaassociated SNP rs1837253 in the TSLP locus has a higher odds ratio in the top quartile of SRD topic weight (1.17  $\pm$  0.02) than in the bottom quartile (1.05  $\pm$  0.02) (P = 6  $\times$ 10<sup>-6</sup> for interaction test (FDR = 0.004 < 0.1);  $P = 1 \times 10^{-3}$  for top/bottom quartile test  $(FDR = 0.08 < 0.1)$ . TSLP plays an important role in promoting Th2 cellular responses and is considered a potential therapeutic target, which is consistent with assignment of asthma and atopic/contact dermatitis<sup>57</sup> to the SRD topic (Supplementary Table 4). Two other examples are described in the Supplementary Note. To verify correct calibration, we performed control  $SNP \times$  topic interaction tests using the same 888 disease-associated SNPs together with random topics that did not correspond to disease subtypes, and confirmed that these control tests were well calibrated (Supplementary Fig. 24b). We conclude that genetic heterogeneity between disease subtypes can be detected at the level of individual disease-associated variants.

## **Discussion**

We have introduced an age-dependent topic modelling (ATM) method to provide a lowrank representation of longitudinal disease records, leveraging age-dependent comorbidity profiles to identify and validate biological subtypes of disease. Our study builds on previous studies on topic modelling<sup>37,38,40,58</sup>, genetic subtype identification<sup>13–15</sup>, and low-rank modelling of multiple diseases to identify shared genetic components<sup>25–27</sup>. We highlight three specific contributions of our study. First, we incorporated age at diagnosis information into our low-rank representation, complementing the use of age information in other contexts<sup>32,52,59</sup>; we showed that age information is highly informative for our inferred comorbidity profiles in both simulated and empirical data, emphasizing the importance of accounting for age in efforts to classify disease diagnoses. Second, we identified 52 diseases with heterogeneous comorbidity profiles that we used to define disease subtypes, many of which had not previously been identified (Supplementary Table 20); comorbidityderived disease subtypes were consistent between UK Biobank and All of Us, despite key differences between these cohorts. Third, we used genetic data (including PRS, genetic correlation and  $F_{ST}$  analyses) to validate these disease subtypes, confirming that the inferred subtypes reflect true differences in disease etiology.

We emphasize three downstream implications of our findings. First, it is of interest to perform disease subtype-specific GWAS on the disease subtypes that we have identified here, analogous to GWAS of previously identified disease subtypes<sup>13-15</sup>. Second, our findings motivate efforts to understand the functional biology underlying the disease subtypes that we identified; the recent availability of functional data that is linked to EHR is likely to aid this endeavor $29,60$ . Third, the efficient inference of ATM permits identifying age-dependent comorbidity profiles and disease subtypes in much larger EHR data sets<sup>61</sup>, though we acknowledge that establishing comprehensive representations of disease topics that are transferable and robust across different healthcare systems and data sources represents a major future challenge.

Our findings reflect a growing understanding of the importance of context, such as age, sex, socioeconomic status and previous medical history, in genetic risk $52,62,63$ . To maximize power and ensure accurate calibration, context information needs to be integrated into clinical risk prediction tools that combine genetic information (such as polygenic risk scores<sup>1,64</sup>) and non-genetic risk factors. Our work focuses on age, but motivates further investigation of other contexts. We note that aspects of context are themselves influenced by genetic risk factors; hence, there is an open and important challenge in determining how best to combine medical history and/or causal biomarker measurements with genetic risk to predict future events<sup>65</sup>.

We note several limitations of our work. First, age at diagnosis information in EHR data may be an imperfect proxy for true age at onset, particularly for less severe diseases that may be detected as secondary diagnoses; although perfectly accurate age at onset information would be ideal, our study shows that that imperfect age at diagnosis information is sufficient to draw meaningful conclusions. Second, raw EHR data may be inaccurate and/or difficult to parse<sup>1</sup>; again, although perfectly accurate EHR data would be ideal, our study shows

that imperfect EHR data is sufficient to draw meaningful conclusions. Third, our ATM approach incurs substantial computational cost (Supplementary Table 21); however, analyses of biobank-scale data sets are computationally tractable, with our main analysis requiring only 4.7 hours of running time. Additional limitations are described in the Supplementary Note. Despite these limitations, ATM is a powerful approach for identifying age-dependent comorbidity profiles and disease subtypes.

#### **Methods**

#### **Ethics statement**

This study analyzed publicly available data sets and hence did not require ethical approval.

#### **Age-dependent topic model (ATM)**

Our age-dependent topic model (ATM) is a Bayesian hierarchical model to infer latent risk profiles for common diseases. The model assumes that each individual possesses several age-evolving disease profiles (topic loadings), which summarize the risk over age for multiple diseases that tend to co-occur within an individual's lifetime, namely the age specific multi-morbidity profiles. At each disease diagnosis, one of the disease profiles is first chosen based on individual weights of profile composition (topic weights); the disease is then sampled from this profile conditional on the age of the incidence.

We constructed a Bayesian hierarchical model to infer  $K$  latent risk profiles for  $D$  distinct common diseases. Each latent risk profile (comorbidity topics) is age-evolving and contains risk trajectories for all D diseases considered. Each individual might have a different number of diseases, while the disease risk is determined by the weighted combination of latent risk topics. We use following indices:

- $s = 1, \ldots, M;$
- $n = 1, \ldots, N_s;$
- $i = 1, \ldots, K$ :
- $j = 1, \ldots, D;$

where *M* is the number of subjects,  $N_s$  is the number of diseases within  $s<sup>th</sup>$  subject, K is the number of topics, and  $D$  is the total number of diseases we are interested in. The plate notation of the generative model is summarized in Extended Data Figure 1:

- $\theta \in R^{M \times K}$  is the topic weight for all subjects (referred to as topic weights), each row of which ( $\in R^{K}$ ) is assumed to be sampled from a Dirichlet distribution with parameter  $\alpha$ .  $\alpha$  is set as a hyper parameter:  $\theta_s \sim Dir(\alpha)$ . We used topic weights to assign continuous values for disease subtypes in PRS and  $SNP \times Topic$  analyses.
- $z \in \{1,2,\ldots,K\}^{\sum_{S}N_S}$  (referred to as diagnosis-specific topic probability) is the topic assignment for each diagnosis  $w \in \{1,2,\ldots,D\}^{\sum_{S}N_S}$ . The total number of diagnoses across all patients are  $\sum_{s} N_s$ . The topic assignment for each

diagnosis is generated from a categorical distribution with parameters equal to  $s^{th}$  individual topic weight:  $z_{sn} \sim Multi(\theta_s)$ . We used diagnosis-specific topic probability to define discrete disease subtypes in excess genetic correlation and excess  $F_{ST}$  analyses.

- $\beta(t) \in F(t)^K \times D$  is the topic loading which is  $K \times D$  functions of age t.  $F(t)$  is the class of functions of t. At each plausible t, the following is satisfied:  $\sum_i \beta_{ij}(t) = 1$ . In practice, we ensure the above is true and add smoothness by constrain  $F(t)$  to be a softmax of spline or polynomial functions:  $\beta_{ij}(t) = \frac{exp(p_{ij}T \phi(t))}{\sum_{i=1}^{n} T_i}$  $\frac{exp(p_{ij} - \phi(i))}{\sum_{j=1}^{D} exp(p_{ij}T \phi(i))}$ , where  $p_{ij}T \phi(i)$  is polynomial and spline functions of t;  $p_{ij} = \{p_{ijd}\}; d = 1,2,\ldots,P; P$  is the degree of freedom that controls the smoothness;  $\phi(t)$  is polynomial and spline basis for age t.
- $w \in \{1,2,\ldots,D\}^{\sum_{S}N_S}$  are observed disease diagnoses. The *n<sup>th</sup>* diagnosis of  $s^{th}$  $th$  and  $th$  a subject  $w_{sn}$  is sampled from the topic  $\beta_{z_{sn}}(t)$  (chosen by  $z_{sn}$ ):  $w_{sn} \sim Multi(\beta_{z_{sn}}(t_{sn}))$ , where  $t_{sn}$  is the the observed age at diagnosis of  $w_{sn}$ .

The variables of interest are disease topics  $\beta(t)$ , individual(patient)-level topic weight  $\theta$ , and diagnosis-specific topic probability z. The innovative element in our model is age-evolving risk profiles, which is achieved by model the comorbidity trajectories  $\beta(t) \in F(t)^K \times D$  as functions of age. We parameterized functionals  $F(t)$  as linear, quadratic, cubic polynomials, and cubic splines with one, two and three knots. We use prediction odds ratio to decide the optimal model structure including the function forms and the number of topics; we use ELBO to choose the optimal inference results (with random parameter initialization) for the same model structure (Supplementary Table 1).

#### **Inference of ATM**

The variables of interest are global topic parameter  $\beta(t)$ , individual (patient) level topic weight  $\theta$ , and diagnosis-specific topic probability z of each diagnosis. We adopt an EM strategy, where in the E-step we estimate posterior distribution of  $\theta$  and z, and then in the M-step we estimate  $\beta$  which maximizes the evidence lower bound (ELBO). For the E-step, we used a collapsed variational inference; for the M-step, we used local variational inference; details are described in the Supplementary Note.

We extract topic weights at patient-level and diagnosis-level from the posterior distribution  $q(z)$ , which is a categorical distribution (equation 8 of Supplementary Note). Our model has the desired property that both patients and diagnoses are assigned to comorbidity topics. We listed following definitions in the paper that are derived from  $q(z)$ :

- **•** Each diagnosis has a diagnosis-specific topic probability, which is computed as  $E_q\{z_n\}$  .
- Each patient has a posterior topic weight θ<sub>s</sub>, which is a dirichlet distribution  $\theta_s \sim Dir(\alpha + \sum_{n=1}^{N_S} E_q\{z_n\})$ . The *topic weights* of each patient is defined as

the mode of this Dirichlet distribution  $\frac{\sum_{n=1}^{N_s} E_q(z_n)}{\sum_{n=1}^{N_s} E_q(z_n)}$  $\sum_{i=1}^{K} \sum_{n=1}^{N_S} E_q\{z_{ni}\}\$ Page 13<br>(we used  $\alpha = 1$ , which<br>weight is the low-rank puts a noninformative prior on the topic weights). Topic weight is the low-rank representation of disease history, which is used in excess PRS and  $SNP \times Topic$ 

- The *average topic assignments* of disease *j* is the mean over all incidences  $\overline{E_{q} \{z_{sn \in \{w_{\text{var}}=J\}\}\}}$ . This metric is used to measure which comorbidity topic a disease is associated with (Fig. 4b), and it is equivalent to a weighted average of topic loadings (Supplementary Note equation 5 shows the link between diagnosisspecific topic probability and topic loading). A disease assigned to multiple topics is considered to have comorbidity subtypes.
- **•** A hard assignment of a patient-diagnosis to a comorbidity-derived subtype is based on the max value of the vector  $E_q\{z_n\}$ . The incident disease is assigned to topic argmax<sub>i</sub>  $(E_{a} \{z_{ni}\})$ .

#### **Metrics for evaluating ATM**

interaction analyses.

ATM is evaluated for different purposes, which requires different metrics (Supplementary Table 1). Here we list the details of the four metrics considered: Prediction odds ratio, Evidence Lower Bound (ELBO), the Area under the Precision-Recall curve (AUPRC)<sup>66</sup>, and Co-occurrence odds ratio.

**Prediction odds ratio.—**We used prediction odds ratio to compare models of different topic numbers and configuration of age profiles. Briefly, prediction odds ratio is defined on 20% held-out test data as the odds that the true diseases are within the top 1% diseases predicted by ATM (trained on 80% of the training set and uses earlier diagnoses as input), divided by the odds that the true diseases are within the top 1% of diseases ranked by prevalence. Details of computing prediction odds ratio for each patient are described in the Supplementary Note.

**Evidence Lower Bound (ELBO).—**ELBO evaluated the accuracy of the variational inference method on a specific data set<sup>39</sup>. The mathematical expression of ELBO for ATM is equation 9 in the Supplementary Note. We computed ELBO when fitting ATM to UK Biobank with 19 choices of the number of topics (5–20, 25, 30, and 50) and 6 choices of age profiles configuration (linear, quadratic polynomial, cubic polynomial, and splines with one, two and three knots). Each model is run for 10 times with random initializations. We choose the model that has the highest ELBO after converging.

**AURPC.—**To evaluate whether a model could capture the comorbidity subtypes in simulation analysis, we compute the precision, recall, and area under precision-recall curve (AUPRC) to correctly assign disease diagnosis to the true topic. The topic of each diagnosis is determined by diagnosis-specific topic probability. Note we could only evaluate AUPRC in simulations where the truth is known.

**Co-occurrence odds ratio.—**To verify that the comorbidity profiles are capturing diseases that are more likely to co-occur within the same individual, we estimate the odds ratio of the disease duo, trio, quartet, and quintet that are captured by the topic versus that of random combinations. Details of computing Co-occurrence odds ratio for each model are described in the Supplementary Note.

#### **Simulations of ATM method**

To test whether the algorithm could assign disease diagnosis to correct comorbidity profiles, we simulated disease using following parameters:

- $M = 10,000$ ;
- $\overline{N_s} = 6.1$ ;
- $N_S \sim exp{\{\overline{N_S}\}};$ •  $\overline{N_s} = 6.1;$ <br>
•  $N_s \sim exp{\{\overline{N_s}\}};$ <br>
•  $D = 20;$ <br>
•  $K = 2;$
- 
- 

•  $N_s \sim exp{\{\overline{N_s}\}};$ <br>
•  $D = 20;$ <br>
•  $K = 2;$ <br>
Here *M* is the number of individuals in the population,  $\overline{N_s}$  is the average number of diseases for each individual,  $D$  is the total number of diseases, and  $K$  is the number of comorbidity topics. The distribution of disease number per-individual  $N<sub>s</sub>$  is sampled from an exponential distribution, which matches those from UK Biobank data (Supplementary Fig. 25). According to equation 3.1 in Ghorbani et al.<sup>67</sup>, whether the topic model could capture the true latent structure is determined by the signal-to-noise ratio and could be evaluated with limits  $M \to \infty$ ;  $D \to \infty$ ;  $\frac{D}{M}$  $\frac{D}{M} \to \delta$ , where  $\delta$  is a constant. Therefore, we choose D and M that make  $\frac{D}{M}$  similar to those of the UK Biobank dataset (samples size = 282,957; distinct disease number  $= 349$ .

Details of topic loadings (Supplementary Fig. 26) and topic weights used in simulations are described in the Supplementary Note.

We simulated diseases with distinct comorbidity subtypes by combining diseases from distinct topics and labelling them as a single disease, using parameters described above. We consider two scenarios: (1) the subtypes of diseases have the same age at diagnosis distribution; (2) the subtypes of disease have distinct age at diagnosis distribution. We first chose one disease (disease A) then sampled a proportion of a second disease (disease B) to label as disease A. The proportion is varied to create a different sample size ratio of the two subtypes. In scenario one, disease B is a disease that has the exact same age distribution as disease A but from the other topic. In scenario two, disease B is from the other topic and has a different age distribution (age at diagnosis moves up for 20 years, 10 years, or 5 years, respectively) than disease A. After changing the labels of disease B to be the same as disease A, we use ATM/LDA to infer diagnosis-specific topic probability to assign diagnoses to the topics.

To evaluate whether a model could capture the comorbidity subtypes, we compute the precision, recall, and area under precision-recall curve (AUPRC) of correctly classifying

incident disease B to be from the correct topic. The topic of each diagnosis is determined by diagnosis-specific topic probability. We use other diseases from the same topic of disease B to benchmark the topic label. Topic modelling on the simulated data is performed with both ATM and LDA (both implemented using collapsed variational inference for fair comparison) to compare the performances.

We evaluate the subtype classification with varying values of four parameters: ratio of sample sizes between the two subtypes, simulated population size, number of distinct diseases, and difference of age distribution; details are described in the Supplementary Note.

#### **UK Biobank comorbidity data**

We analysed comorbidity data from 282,957 UK Biobank samples with diagnoses for at least two of the 348 focal diseases that we studied (see below). We use the hospital episode statistics (HES) data within the UK Biobank dataset, which uses ICD-10/ICD-10CM coding system; the average record span of HES data is 28.6 years. Codes starting with letters from A to N are kept as they correspond to disease codes (as opposed to procedure codes). The disease records were mapped from ICD-10/ICD-10CM codes to Phecodes using a three-step procedure; details are described in the Supplementary Note and the method is implemented in the ATM software.

The mapped Phecodes are filtered to keep only the first diagnosis for the recurrent diseases within a patient. The age at diagnosis for each disease is computed as the difference between month of birth to the episode starting date. We then computed the occurrence of each disease in the UK Biobank and kept 348 that have more than 1,000 occurrences (Supplementary Table 4). Starting with all 488,377 UK Biobank participants (including both European and non-European ancestries), we filtered the patients to keep only those who have at least two distinct diseases from the 348 focal diseases, as we are most interested in the comorbidity information. We treated the death as an additional disease (8,666 records) to evaluate if certain comorbidities are more likely to lead to fatal events. The procedure leaves us 1,726,144 distinct records across 282,957 patients.

To name the topics inferred from the UK Biobank, we take the sum of average topic assignments (section Inference of ATM) over diseases for each Phecode system and extract the three most common Phecode disease systems. Six topics are named using the three most common Phecode disease systems: NRI "neoplasms, respiratory, infectious diseases", CER "cardiovascular, endocrine/metabolic, respiratory", SRD "sense organs, respiratory, dermatologic", FGND "female genitourinary, neoplasms, digestive", MGND "male genitourinary, digestive, neoplasms", and MDS "musculoskeletal, digestive, symptoms". For four topics that are predominantly associated with one system, we name them based on their top associated Phecode system: LGI "lower gastrointestinal", UGI "upper gastrointestinal", CVD "cardiovascular", and ARP "arthropathy".

We present focal diseases by selecting disease with highest average topic loading between age 30 to 81. We chose the top seven diseases for visualization, as we found more diseases would be harder to read on a plot.

To compare the comorbidity heterogeneity between age groups, we group the incidences for each disease to two age groups: young group ( $<60$  years of age) and old group ( $\leq 60$  years of age). We compute the average topic assignment of each group as described in section Inference of ATM. Additionally, we inferred topics for male (984,554 records in 156,366 individuals) and female (741,590 records in 126,591 individuals) populations respectively using ATM with 10 topics and spline function with one knot. We extract the average topic assignment for each disease, and use Pearson's correlation to match the topics for both sexes to the topics inferred on the entire population.

We assigned diagnoses to discrete subtype using max diagnosis-specific topic probability. We focus our genetic heterogeneity analysis on 52 diseases that have at least 500 incidences assigned to a secondary topic.

#### **All of Us comorbidity data**

We analyzed EHR data collected in the EHR domain of All of Us samples, which includes both primary care and secondary care data. The average distance between first and last diagnoses is 7.9 years (vs. 7.0 years in UK Biobank); the average record span period is unknown, but we hypothesized that it is likely to be considerably larger than 7.9 years (vs. 28.6 years in UK Biobank). Disease codes in the All of Us EHR domain are coded in SNOMED CT. Details of mapping from SNOMED CT to Phecode are described in the Supplementary Note and implemented in the ATM software. We kept 233 Phecodes that overlap with the 348 diseases analyzed in the UK Biobank. We kept the first diagnosis for recurrent diseases in each patient. After mapping, we are left with 3,098,771 diagnoses spanning 211,908 All of Us samples. We run ATM with topic number from 5 to 20 and age functions configured as splines with two knots (degree of freedom  $= 5$ ) on the All of Us comorbidity data and computed prediction odds ratio (using five-fold cross validation) and ELBO (on all 211,908 samples).

#### **Comparing disease topics between UK Biobank and All of Us**

We compared the optimal models from UK Biobank (10 topics, degree of freedom = 5) and All of Us (13 topics, degree of freedom  $= 5$ ). We constrained our analyses on 233 of the 348 diseases that are shared between the two data sets. We performed three analyses to compare the comorbidity patterns from the two data sets.

First, we computed the correlation of topic loadings from two data sets. Since the topic loadings are functions of age, we computed their correlations using four different ways to summarize age information: topic loadings averaged across age, and topic loadings at age 50, 60, and 70. For each UK Biobank topic, we found its most similar All of Us topic that has max correlation of topic loadings (averaged across age).

Second, we computed the cross-population prediction odds ratio, using the All of Us topics to predict comorbidity patterns in UK Biobank data. We divided the UK Biobank samples into 10 jackknife blocks and computed prediction odds ratios on each leave-one-out sample.

Third, we compared the correlation of comorbidity profiles (measured by average topic assignments; see Methods for definition) for 233 diseases that are shared between the two

populations. We define correlations between topic assignments as the correlation between UK Biobank average topic assignments and All of Us average topic assignments mapped to UK Biobank topic space; details are described in the Supplementary Note.

#### **UK Biobank genotype data**

For genetic correlation analysis,  $F_{ST}$ , and SNP  $\times$  Topic interaction analyses, we used genetic data from 488,377 UK Biobank participants (prior to restricting to 282,957 samples with at least two of the 348 diseases studied). For PRS and heritability estimation of the 10 topics, we constrained our analysis to 409,694 British Isle ancestry individuals to adjust for population structure. We choose different sets of SNPs that are practical for each method; details are described in the Supplementary Note.

#### **Polygenic risk scores (PRS) analysis**

Although population stratification cannot be excluded<sup>68</sup>, to adjust for and minimize the impact of population stratification, we applied mixed-effect association model to samples of British Isle ancestry group ( $n = 409,694$ ) to compute PRS for 10 heritable diseases that have the highest heritability  $z$ -scores. We used BOLT-LMM to construct genome-wide PRS<sup>50</sup>. Details of creating balanced case-control and SNP selection are described in the Supplementary Note. For each disease, we used 5-fold cross validation to estimate effect sizes using BOLT-LMM and computed the PRS on the held-out testing set. We used linear regression between continuous-valued topic weights and PRS to compute the excess PRS over different topics.

We compute the subtype-specific relative risk for each percentile of PRS using the following formula:

$$
RR_{pt,s} = \frac{n_{pt,s} \times 100}{n_s},
$$

where  $RR_{\mu,s}$  is the relative risk of s subtype for the  $pt^{\text{th}}$  PRS percentile (computed for the entire population);  $n_{\mu,s}$  is the number of cases in s subtype that has PRS within the  $pt^{\text{th}}$ percentile;  $n_s$  is the number of cases in the  $s$  subtype.

#### **Genetic correlation analysis**

We used discrete subtypes in genetic correlation analysis (different from the PRS analysis above). For each disease and disease subtype, we used a case-control matching strategy to construct data to estimate coefficients for genetic correlation analysis. We used a one-to-four case-control ratio, matching sex, BMI, year of birth and 40 genetic principal components. We used PLINK  $1.9<sup>69</sup>$  to perform logistic regression with sex and top 10 principal components as covariates. We used  $LDSC<sup>2</sup>$  and summary statistics from the logistic regression to estimate the heritability for each disease or disease subtype which has more than  $1,000$  incidences (378 = 30 diseases subtypes  $+$  348 diseases). We focus on 71 disease and 18 disease subtypes of the 378 diseases subtypes and diseases that have heritability *z*-score above 4 for genetic correlation analysis.

We used LDSC and summary statistics from the logistic regression to compute genetic correlation for each pair of disease-disease, disease-subtype, and subtype-subtype. We report the estimate of genetic correlation and  $z$ -scores. Additionally, for pairs that involve subtypes (disease-subtype or subtype-subtype), we compute the excess genetic correlation, defined as the difference between the genetic correlation involving subtypes (disease-subtype and subtype-subtype) and the genetic correlation involving all disease diagnoses (diseasedisease). For example, the genetic correlation between T2D-CER and hypertension-CVD is compared to the genetic correlation between all T2D and all hypertension. We note that genetic correlations between subtypes of the same disease are compared to 1. We only reported P-values of excess genetic correlation when both genetic correlation estimation has standard error  $< 0.1$  and at least one of the genetic correlations has  $|z\text{-score}| > 4$ .

To avoid potential collider effects where subtypes are defined by topic components that are independent of the diseases, we performed the same genetic correlation analyses but match cases in each subtype with controls with similar topic loadings; details are described in the Supplementary Note.

#### **FST analysis**

We used discrete subtypes in genetic correlation analysis (same as genetic correlation analysis above; different from the PRS analysis). To evaluate the genetic heterogeneity between disease subtypes, we estimated the  $F_{ST}$  across subtypes for 52 diseases that have at least 500 incidences assigned to a secondary topic. To test the statistical significance of  $F_{ST}$ , we adopted a permutation strategy by sampling controls with matched topic weights and sample size for each disease subtype, and computed  $F_{ST}$  across the subtype-matched control groups; details are described in the Supplementary Note. The  $F_{ST}$ s are computed using PLINK 1.9's weighted mean across all genotyped SNPs.

We obtained 1,000 permutation samples and reported the permutation P-value for each disease. Under the assumption that causal and non-causal variants have similar allele frequency differences across the subtypes,  $F_{ST}$  is a measure of causal genetic effect heterogeneity across subtypes.

#### **SNP × topic interaction test**

We used continuous-valued topic weights in the  $SNP \times$  topic interaction analysis (same as the PRS analysis; different from the genetic correlation and  $F_{ST}$  analyses). We focus on 14 diseases that have heritability z-score above 4. We fit following a logistic regression model:

$$
logit(p) = \beta_0 + \beta_1 * T + \beta_2 * T^2 + \beta_3 * G + \beta_4 * G * T,
$$

where  $T$  is individual topic weights for a specified topic,  $G$  is the genotype, and  $p$  is the  $logit(p) = \beta_0 + \beta_1 * T + \beta_2 * T^2 + \beta_3 * G + \beta_4 * G * T$ ,<br>where *T* is individual topic weights for a specified topic, *G* is the genotype, and *p* is the<br>probability of getting the disease. We computed the test statistics under the n

Simulations (below) showed that the interaction test is underpowered when the variant effects are small; we focused on the set of GWAS SNPs that reaches genome-wide significance level. We used LD-clumping at  $r^2 > 0.6$  to keep moderately independent

variants. We computed the test statistics using the model above (for testing  $\beta_4 = 0$ ) and<br>computed study-wise FDR across 2,530 disease-topic pairs. We used QQ plots to checi-<br>interaction test statistics computed using a computed study-wise FDR across 2,530 disease-topic pairs. We used QQ plots to check that interaction test statistics computed using all non-subtype topics for each disease (which are expected to be null) were well calibrated (Supplementary Fig. 24b).

As an alternative way to verify the interactions, we divided cases into quartiles based on topic weights (which defines disease subtypes continuously) for each disease-topic pair, and randomly sampled two controls that match the topic weights for each case. We estimated the main effect sizes for all GWAS SNPs within each quartile of topic weight and compared the effects between the top and bottom quartiles of topic weights. For visualization, we used GWAS SNPs that have no interaction effect (above,  $P > 0.05$ ) as background SNPs.

#### **Simulations of SNP × topic interaction**

We simulated comorbidity with genetics to test interaction between genetic and comorbidity topics. We simulated 100 independent variants with MAF randomly sampled from the MAF of 888 independent disease-associated SNPs. We assumed an additive model and simulated genotypes for the population using Hardy-Weinberg equilibrium. We simulated three types of genetic effects on topic and diseases, based on the simulation framework described in the Simulations of ATM method section (genetics-topic, genetic-disease-topic, and genetic-topic interaction); details are described in the Supplementary Note.

We simulated with varying disease-topic or topic-disease causal effects with 50 repetitions at each causal effect size. The simulated data are fed to the ATM to infer the topic weights for interaction testing.

## **Extended Data**



Diagnosis-specific topic probability Z



#### **Extended Data Fig. 1. Plate notation of ATM generative model.**

M is the number of subjects;  $N_s$  is the number of records within  $s^{th}$  subject. All plates (circles) are variables in the generative process, where the plates with shade w is the observed variable and plates without shade are unobserved variables to be inferred; is the topic weight;  $z$  is diagnosis-specific topic probability;  $t$  is the age at diagnosis for each diagnosis; is the topic loadings which are functions of age  $t$ , is the (non-informative) hyperparameter of the prior distribution of. The generative process is described in the Methods and Supplementary Note.

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**that have subtypes.** The figure has the same legends as Fig. 3A but focusing on 52 diseases that have a subtype

with at least 500 incidences. Distribution of average topic assignment for these 52 diseases is reported in Supplementary Fig. 15.

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## **Extended Data Fig. 3. Comparison of prediction odds ratio between LDA and ATM.**

Each dot represents results from running either ATM or LDA on the same random training and testing split. The models were run with different topic numbers and we chose a cubic spline with one knot for configuring ATM topic loadings. The prediction odds ratios are computed on the testing data using topic loadings inferred from the training data and topic weights inferred using previous diseases of testing individuals. The odds ratios are between the odds that target diseases are within model-predicted top percentile disease set versus the odds that target diseases are within the prevalence-ordered top percentile disease set. For the optimal model with 10 topics, ATM has an average prediction odds ratio 1.71 (across 10 random training-testing splits); LDA has an average prediction odds ratio 1.58 (across 10 random training-testing splits). Box plots show the distributions of the dots; centre, box bounds, and whisker ends denote median, quartiles, and minima/maxima.



**Extended Data Fig. 4: Posterior topic distributions of female and male populations.** The figure is the same as Fig. 3A but comparing the topics that are inferred from female and male populations separately.



**Extended Data Fig. 5. Subtype correlations between UK Biobank and All of Us for 41 diseases that are presented in both datasets and have subtypes in UK Biobank.**

Each box of the heatmap shows the correlation of average diagnosis-specific topic probability between a disease from All of Us and the other disease from UK Biobank. The diagnosis-specific topic probabilities from All of Us were mapped to UK Biobank based on proportional variance between the two topic spaces (Methods).



#### **Extended Data Fig. 6. Excess PRS analysis for all topics across 10 diseases (selected by heritability z-score).**

The bar plot shows the estimated changes in s.d. of PRS per unit changes in the patient topic weight in disease cases. The PRS is estimated using all the cases in British Isle Ancestry. Error bars denote the 95% confidence interval. The stars show disease-topic pairs that are significant at FDR = 0.05. Numerical results are reported in Supplementary Table 13.





P-values are for testing case- $F_{ST}$  significantly higher than controls of similar topic weight distribution. The permutation controls are sampled for 1,000 times with the same topic weights distribution and sample size to the disease subtypes. We focus on 49 of the 52 diseases which have more than one subgroup of at least 500 cases. Subtypes are defined based on the max value of the diagnosis-specific topic probability. Three diseases ("hypertension", "hypercholesterolemia", and "arthropathy") are excluded as there are not enough controls that match the topic weights of cases. The colour shows the value of  $F_{ST}$ across subtypes. Exact P-values are reported in Supplementary Table 16.



**Extended Data Fig. 8. Examples of SNP × topic interaction effects on disease phenotypes.** For each example, we report main SNP effects (log odds ratios) specific to each quartile of topic weights across individuals, for both the focal SNP (blue dots) and background SNPs for that disease and topic (genome-wide significant main effect ( $P < 5 \times 10-8$ ) but non-significant SNP  $\times$  topic interaction effect (P  $> 0.05$ ); grey dots). Dashed red lines denote aggregate main SNP effects for each focal SNP. Error bars denote 95% confidence intervals. Grey lines denote linear regression of grey dots, with grey shading denoting corresponding 95% confidence intervals. P-values for interaction are for testing the interaction regression coefficients; P-values for top/bottom differences are for two-sided t-test. Numerical results are reported in Supplementary Table 18.

## **Supplementary Material**

Refer to Web version on PubMed Central for supplementary material.

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## **Data availability**

UK Biobank data is publicly available at <https://www.ukbiobank.ac.uk/>(application number 12788); All of Us data is publicly available at [https://allofus.nih.gov](https://allofus.nih.gov/); LD-scores and HAPMAP3 SNP list are available at [https://data.broadinstitute.org/alkesgroup/LDSCORE.](https://data.broadinstitute.org/alkesgroup/LDSCORE)

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**Fig. 1 |. ATM provides an efficient way to represent longitudinal comorbidity data.** Top left: input consists of disease diagnoses as a function of age. Top right: ATM assigns a topic weight to each patient. Bottom: ATM infers age-dependent topic loadings.

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#### **Fig. 2 |. ATM outperforms LDA in simulations with age-dependent effects.**

In simulations at different levels of age-dependent effects (left panels), we report the area under the precision and recall curve (AUPRC) for ATM vs. LDA as a function of subtype sample size proportion (the proportion of diagnoses belonging to the smaller subtype) (right panels). Each dot represents the mean of 100 simulations of 10,000 individuals. Error bars denote 95% confidence intervals. **a**, 20-year difference in age at diagnosis for the two subtypes. **b**, 10-year difference in age at diagnosis for the two subtypes. **c**, 5-year difference

in age at diagnosis for the two subtypes. Numerical results are reported in Supplementary Table 2.



#### **Fig. 3 |. Age-dependent topic loadings of 10 inferred disease topics across 348 diseases in the UK Biobank.**

We report topic loadings averaged across younger ages (age at diagnosis < 60) and older ages (age at diagnosis > 60). Row labels denote disease categories ordered by Phecode systems, with alternating blue and red color for visualization purposes; "Other" is a merge of five Phecode systems: "congenital anomalies", "symptoms", "injuries & poisoning", "other tests", and "death" (which is treated as an additional disease, see Methods). Topics are ordered by the corresponding Phecode system. Further details on the 10 topics are provided in Table 1. Further details on the diseases discussed in the text (type 2 diabetes

and breast cancer) are provided in Extended Data Figure 2. Numerical results are reported in Supplementary Table 4.



#### **Fig. 4 |. Topic loadings in UK Biobank capture age-dependent comorbidities.**

**a**, Age-dependent topic loadings for two representative topics, CER and CVD; for each topic, we include the top seven diseases with highest topic loadings. Results for all 10 topics are reported in Supplementary Figure 9. **b**, Box plot of disease topic loading as a function of rank; disease topic loadings are computed as a weighted average across all values of age at diagnosis. **c**, Box plot of patient topic weight as a function of rank. Centre, box bounds, and whisker ends denote median, quartiles, and minima/maxima. Numerical results are reported in Supplementary Table 5.

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#### **Fig. 5 |. Topic loadings in All of Us capture age-dependent comorbidities that are concordant with UK Biobank.**

**a**, Age-dependent topic loadings for two All of Us topics corresponding to CVD and CER (Fig. 4a); for each topic, we include the top seven diseases with highest topic loadings. Correlations of topic loadings between UK Biobank and All of Us topics were 0.74 for CVD and 0.65 for CER. Numerical results for all 13 topics are reported in Supplementary Table 6. **b**, Topic loading correlations between UK Biobank (UKB) and All of Us (AOU). The <sup>y</sup>-axis reflects the 10 topics from the optimal UK Biobank model; the x-axis reflects the 13 topics from the optimal All of Us model. Numerical results are reported in Supplementary Table 7. **c**, Correlations between UKB and AOU topic assignments were higher for the same diseases (red shading, average  $= 0.70$ ) than for different diseases (grey shading, average  $=$ 0.02). P-value is for two-sided *t*-test; numerical results are reported in Supplementary Table 9.



**Fig. 6 |. Polygenic risk scores vary across disease subtypes defined by distinct topics. a**, Stacked bar plots of age-dependent subtypes (defined by topics) for four representative diseases (type 2 diabetes, asthma, hypercholesterolemia, and essential hypertension); for each disease, we include all subtypes with at least one diagnosis. Results for all 52 diseases are reported in Supplementary Figure 16. **b**, Standardized excess PRS values in disease cases (s.d. increase in PRS per unit increase in patient topic weight) for four representative diseases and four corresponding topics. **c**, Relative risk for cases of type 2 diabetes and hypercholesterolemia of CVD and MGND subtypes (vs. controls) across PRS percentiles. Each point spans 2 PRS percentiles. Lines denote regression on log scale. Error bars denote 95% confidence intervals. Numerical results are reported in Supplementary Tables 11–13.



**Fig. 7 |. Genetic correlations vary across disease subtypes defined by distinct topics.**

**a**, Excess genetic correlations for pairs of 15 disease subtypes or diseases (9 disease subtypes (denoted with asterisks) + 6 diseases without subtypes), relative to genetic correlations between the underlying diseases. Full square with asterisk denotes FDR < 0.1; less than full squares have area proportional to z-scores for difference. Grey squares denote NA (pair of diseases without subtypes or pair of same disease subtype or disease). **b**, Genetic correlations between the underlying diseases. Full circle denotes  $|z\text{-}score| > 4$ for nonzero genetic correlation; less than full circles have area proportional to |z-score|. Numerical results are reported in Supplementary Table 14.

#### **Table 1| Summary of 10 inferred disease topics in the UK Biobank.**

For each topic, we list its 3-letter acronym, disease systems, representative diseases, and number of associated diseases (defined as diseases with average diagnosis-specific topic probability >50% for that topic). Topics are ordered by the Phecode system (see Fig. 3). 316 of 348 diseases analyzed are associated with a topic; the remaining 32 diseases do not have a topic with average diagnosis-specific topic probability >50%. NOS, not otherwise specified.

